

1. What is the value of y after both of the following operations?

```
x = x ^ (~y);  
y = y ^ x;
```

$\sim x$

$y = y \wedge (x \wedge (\sim y)) \rightarrow (y \wedge \sim y) \wedge x \rightarrow 1s \wedge x == \sim x$

After you plug in x, you can use the commutative and associative properties of XOR and do $y \wedge \sim y$ first which results in all 1s. x XORed with 1s flips its bits, thus $\sim x$

Say $x = 0111$ and y is 1010
 $0111 \wedge 0101 = 0010$
 $1010 \wedge 0010 = 1000$ which is $\sim x$

2. Given the following declarations, do the statements below always evaluate to true?

```
int x = foo();  
int y = bar();  
unsigned ux = cookie();
```

a.

$x > ux \implies (\sim x + 1) < 0$

FALSE

Consider $x = -1$.

- The binary is all 1s, thus when you do \sim (all 1s) it becomes all 0s.
 - Adding the 1 makes the value positive.

This is true for all negative x values since the sign bit will always be flipped to 0.

- So the 'it follows' is not true for all $x > ux$.

b.

$ux - 2 \geq -2 \implies ux \leq 1$

TRUE

If ux is 0

- it is comparing the unsigned values of -2 and -2, which are equal.

If ux is 1

- it is comparing the unsigned values of -1 and -2, which are U_{max} vs $U_{max} - 1$. 2,3, etc
 - aren't true and ux can not be a negative value.
- So, it follows that ux must be 0 or 1.

c.

$(x^y)^x == (x+y)^{(x+y)^y}$

TRUE

Notice that both sides are of the form $(A^y)^A$

- For the left hand side, $A = x$
- For the right hand side, $A = x+y$

$(A^y)^A$ is equivalent to y

- Thus, the equivalence simplifies to $y == y$
- Both sides of the equivalence are equal

d.

$(x < 0) \ \&\& \ (y < 0) == (x + y) < 0$

FALSE

Say $x == \text{INTMin}$ and $y == \text{INTMin}$.

- $(x+y)$ would overflow.

3. <code>char** apple[5][9];</code>	360 bytes	$(8 * 5 * 9)$
<code>char* banana[1][9];</code>	72 bytes	$(8 * 1 * 9)$
<code>char strawberry[4][2];</code>	8 bytes	$(1 * 4 * 2)$

How many bytes of space would these declarations require?

4. Consider the following struct:

```
typedef struct {
    char first;
    int second;
    short third;
} stuff;
```

Say we are debugging an application in execution using gdb on a 64-bit, little-endian architecture. The application has a variable called array - defined as:

```
stuff array[2][2];
```

Using gdb we find the following information at a particular stage in the application:

```
[(gdb) p &array
$1 = (stuff (*) [2] [2]) 0x7fffffffef020
```

And:

```
[(gdb) x/48xb 0x7fffffffef020
0x7fffffffef020: 0x61      0x00      0x00      0x00      0x08      0x00      0x00      0x00
0x7fffffffef028: 0x02      0x00      0x00      0x00      0x62      0x00      0x00      0x00
0x7fffffffef030: 0x64      0x00      0x00      0x00      0x04      0x00      0x00      0x00
0x7fffffffef038: 0x63      0x04      0x40      0x00      0xed      0x03      0x00      0x00
0x7fffffffef040: 0xc8      0x00      0xff      0xff      0x64      0x7f      0x00      0x00
0x7fffffffef048: 0x17      0xa6      0x00      0x00      0xe1      0x00      0x00      0x00
```

What is the value of
array[1][0].second

At this particular stage of the application?
i.e. what would be returned from the statement:

```
printf("%d\n", array[1][0].second);
```

1005

Because of alignment, each object of type "stuff" is 12 bytes.

Due to how arrays are stored in memory,

- The array is stored as:
array[0][0], array[0][1], array[1][0], array[1][1]

From the gdb output, we can tell that the array starts at 0x7fffffffef020

- array[1][0] is 0x7fffffffef038 to 0x7fffffffef043
 - Note: this is in hex, so $0x7fffffffef038 + 8 = 0x7fffffffef040$

Second is an integer, and is the 5th to 8th byte of an object of type "stuff"

- These are bytes 0x7fffffffef03c to 0x7fffffffef03f
- They have the values 0xed, 0x03, 0x00, 0x00
- Since this system is little endian, the value is 0x000003ed
 - This is equivalent to 1005

5. The following is part of the result of the command 'objdump -d' on an executable

```

00000000004006dd <IronMan>:
4006dd:    55                push    %rbp
4006de:    48 89 e5          mov     %rsp,%rbp
4006e1:    89 7d ec          mov     %edi,-0x14(%rbp)
4006e4:    8b 45 ec          mov     -0x14(%rbp),%eax
4006e7:    c1 e0 04          shl     $0x4,%eax
4006ea:    89 45 fc          mov     %eax,-0x4(%rbp)
4006ed:    8b 45 fc          mov     -0x4(%rbp),%eax
4006f0:    5d                pop     %rbp
4006f1:    c3                retq

```

Say the declaration for the function IronMan was:

```
int IronMan(int scraps);
```

Given that the integer 23 was passed into the function, what is the return value?

368

After instructions 0x4006e1 and 4006e4, the input (which was stored in %rdi) is now stored in %eax

Instructions 0x4006e7 then shifts %eax to the left by 4

- This is equivalent to multiply by 2^4 , which is 16

$23 * 16 = 368$

6. The following is a continuation from the previous problem:

```
0000000000400721 <Hulk>:
400721: 55                    push    %rbp
400722: 48 89 e5             mov     %rsp,%rbp
400725: 48 83 ec 20          sub     $0x20,%rsp
400729: 48 89 7d e8          mov     %rdi,-0x18(%rbp)
40072d: 48 8b 45 e8          mov     -0x18(%rbp),%rax
400731: 48 89 c7             mov     %rax,%rdi
400734: e8 27 fe ff ff      callq   400560 <atoi@plt>
400739: 89 45 fc             mov     %eax,-0x4(%rbp)
40073c: 8b 45 fc             mov     -0x4(%rbp),%eax
40073f: 89 c7             mov     %eax,%edi
400741: e8 97 ff ff ff      callq   4006dd <IronMan>
400746: 89 45 f8             mov     %eax,-0x8(%rbp)
400749: 81 7d f8 8f 01 00 00  cmpl    $0x18f,-0x8(%rbp)
400750: 7e 10             jle     400762 <Hulk+0x41>
400752: 81 7d f8 f4 01 00 00  cmpl    $0x1f4,-0x8(%rbp)
400759: 7f 07             jg      400762 <Hulk+0x41>
40075b: b8 01 00 00 00      mov     $0x1,%eax
400760: eb 05             jmp     400767 <Hulk+0x46>
400762: b8 00 00 00 00      mov     $0x0,%eax
400767: c9             leaveq  %edi
400768: c3             retq
```

Given that the function returns 1, what do we know about the value of %edi right before instruction 0x400741 is executed?

%edi is between 25 and 31

Since the function returns 1, we know that the jump instructions at 0x400750 and 0x400759 did not jump.

- From instructions 0x400749 and 0x400750
 - we know that we would have jumped if $-0x8(\%rbp)$ was less than or equal to 0x18f
 - Thus we know $-0x8(\%rbp)$ is greater than 0x18f, or 399
- From instructions 0x400752 and 0x400759
 - We know that we would have jumped if $-0x8(\%rbp)$ was greater than 0x1f4
 - Thus we know $-0x8(\%rbp)$ is less than or equal to 0x1f4, or 500
- Thus we know that $-0x8(\%rbp)$ is between 400 and 500, inclusive
 - Thus %eax is between 400 and 500, inclusive

From the previous question, we know that IronMan multiplies inputs by 16

- We also know that the function returns a value between 400 and 500 with input %rdi
- Reversing the function, we know the input must have been between 400/16 and 500/16

Thus we know that %rdi was between 25 and 31 right before the IronMan function call