Course No.:

Algorithm Design & Implementation

Credits: 3-0-0-6

Prerequisites: NIL

#### **Course Objectives:**

- 1. Develop a deeper understanding of the theoretical foundations of algorithm design and analysis, including key concepts such as asymptotic analysis and NP-hardness.
- 2. Learn to apply various algorithmic design paradigms, including backtracking, dynamic programming, and greedy algorithms, to solve a range of real-world problems.
- 3. Understand the basic principles of approximation algorithms and learn to apply them to a variety of optimization problems.
- 4. Gain practical experience in implementing and analyzing algorithms through programming assignments and projects.

#### **Course Outcomes:**

- 1. Students will be able to analyze the complexity of an algorithm and make decisions about which algorithms are best suited for a given problem.
- 2. Students will be able to design algorithms using a variety of techniques, including backtracking, dynamic programming, and greedy algorithms, and apply them to solve problems in various domains.
- 3. Students will be able to apply approximation algorithms to optimization problems, and understand the tradeoffs between approximation quality and runtime.
- 4. Students will be able to implement and analyze algorithms using programming languages such as Python and Java, and use this knowledge to develop and evaluate algorithms for real-world applications.

# **Module 1: Introduction to Algorithms (4 hours)**

- Basic concepts review
- Asymptotic analysis
- Solving recurrence relations: recursion tree and Master Theorem

#### Module 2: Backtracking (4 hours)

- N queens
- Game Trees
- Longest increasing subsequence
- Subset sum
- Optimal binary search trees: analysis

#### **Module 3: Dynamic Programming (6 hours)**

- Principle of dynamic programming: memorization or iteration over subproblems
- Longest increasing subsequence
- Optimal binary search trees
- Shortest paths in a graph
- Negative cycles in a graph

# Module 4: Greedy Algorithms (3 hours)

- Scheduling classes
- Huffman codes
- Stable matching
- The minimum spanning tree problem

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# Module 5: NP-Hardness (6 hours)

- P vs NP, NP-hard, and NP-complete
- Reduction and SAT
- 3 SAT
- Clique and Vertex Cover
- Graph coloring

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#### Module 6: Network Flow (3 hours)

- The maximum flow problem
- Ford-Fulkerson algorithm
- Max flow and Min cut in a Network
- Airline scheduling

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# **Module 7: Approximation Algorithm (6 hours)**

- Introduction to approximation technique
- Deterministic rounding algorithm
- Rounding a dual solution
- Constructing a dual solution-primal dual method
- Randomized rounding algorithm

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# **Module 8: Application of Approximation Algorithm (6 hours)**

- Scheduling jobs with deadlines on a single machine
- The k-center problem
- The traveling salesman problem
- Scheduling jobs on identical parallel machines
- Minimizing the sum of completion times on a single machine

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# Module 9: Randomized Algorithm (3 hours)

- Randomization as Algorithm Design Technique
- Randomized min cut algorithm
- Randomized find
- Birthday paradox

# **TEXTBOOKS:**

- 1. Thomas H Cormen, Charles E Lieserson, Ronald L Rivest and Clifford Stein, Introduction to Algorithms, MIT Press, 2009.
- 2. Jon Kleinberg and Éva Tardos, Algorithm Design, Pearson, 2005.
- 3. David P. Williamson and David B. Shmoys, The Design of Approximation Algorithms, Cambridge University Press, 2010.
- 4. Jeff Erickson, Algorithms, 2019.