Course No.:

Name: Mathematical Foundations for Cloud
Computing

Credits: 3-0-0-6

Prerequisites: YES

COURSE OBJECTIVES:

- 1. Develop an understanding of probability theory, random variables, and processes that are relevant to cloud computing.
- 2. Understand the mathematical concepts that underlie cloud computing systems.
- 3. Learn linear algebra and optimization theory and their application in cloud computing systems.
- 4. Acquire practical skills to apply mathematical concepts in the design and evaluation of cloud computing systems.

COURSE OUTCOMES:

- 1. Explain the concepts of probability theory, random variables, and processes in cloud computing systems.
- 2. Apply linear algebra techniques to solve problems related to cloud computing.
- 3. Apply optimization techniques to formulate and solve problems in cloud computing systems.
- 4. Evaluate and design cloud computing systems using mathematical concepts learned in the course.

Prerequisites:

- 1. Basic understanding of computer science and mathematics
- 2. Familiarity with calculus and linear algebra

Module 1: Introduction to Cloud Computing and Mathematical Foundations (6 hours)

- Introduction to Cloud Computing
- Overview of Mathematical Foundations: Probability theory, Linear Algebra, Optimization Theory

Module 2: Probability Theory and Random Variables for Cloud Computing Systems (18 hours)

- Review of Probability Theory
- Random Variables and Processes for Cloud Computing Systems
- Density Functions and Distribution
- Mean, Variance and Higher Order Moments
- Common Discrete Distributions
- Common Continuous Distributions
- Multivariate Distributions
- Law of Large Numbers (LLN)
- Central Limit Theorem (CLT)

Module 3: Linear Algebra for Cloud Computing Systems (9 hours)

- Vectors and Matrices
- Matrix Operations
- Definition of Eigenvalue and Eigenvector
- Inner Product and Orthogonal Basis

Module 4: Optimization Theory and Its Application for Cloud Computing Systems (12 hours)

- Basics of Optimization Theory
- Classes of Optimization Problems (Linear, Nonlinear, Continuous, Constrained, Unconstrained, Single-Multiple Variables)
- Convex Functions and Its Properties
- Convex Optimization Problem
- Algorithms for Convex Optimization (Steepest Descent and Newton's)

Text/Reference Book:

- 1. Athanasios Papoulis, S. Unnikrishna Pillai, Probability, Random Variables, and Stochastic Processes, Tata McGraw-Hill (2002).
- 2. Alberto Leon-Garcia, Probability and Random Processes for Electrical Engineering, Pearson Education India (1994).
- 3. Stephen Boyd, Stephen P. Boyd, and Lieven Vandenberghe, Convex Optimization,
- 4. Cambridge University Press (2004).
- 5. Suresh Chandra, Jayadeva, and Aparna Mehra, Numerical Optimization with Applications, Alpha Science International (2009).