EAS509 Final Exam

Submit your answers as a single pdf attach all R code. Failure to do so will result in grade reduction.

The exam must be done individually, with no discussion or help with others. Breaking this rule will result in an automatic 0 grade.

Part A (30 points) - each question worth 1 points

Some questions have multiple answers

- 1. Which simple forecasting method says the forecast is equal to the mean of the historical data?
- a. Average Method
- b. Naïve Method
- c. Seasonal Naïve Method
- d. Drift Method

Answer:a. Average Method

- 2. Which simple forecasting method says the forecast is equal to the last observed value?
- a. Average Method
- b. Naïve Method
- c. Seasonal Naïve Method
- d. Drift Method

Answer:b. Naïve Method

- 3. Which simple forecasting method is equivalent to extrapolating a line draw between the first and lost observations?
- a. Average Method
- b. Naïve Method
- c. Seasonal Naïve Method
- d. Drift Method

Answer:d. Drift Method

- 4. Which of the following is an assumption made about forecasting residuals during point forecast?
- a. Residuals are normally distributed
- b. Residuals are uncorrelated
- c. Residuals have constant variance

d. None of the above

Answer: b. Residuals are uncorrelated

- 5. Which of the following is an assumption made about forecasting residuals during interval forecasting? (multiple answers)
- a. Residuals have mean zero
- b. Residuals are normally distributed
- c. Residuals have constant variance
- d. None of the above

Answer:a. Residuals have mean zero,b. Residuals are normally distributed & c. Residuals have constant variance all should present for full score

- 6. What is the consequence of forecasting residuals that are not uncorrelated?
- a. Prediction intervals are difficult to calculate
- b. Information is left in the residuals that should be used
- c. Forecasts are biased
- d. None of the above

Answer: b. Information is left in the residuals that should be used

- 7. What is the consequence of forecasting residuals that don't have mean zero?
- a. Prediction intervals are difficult to calculate
- b. Information is left in the residuals that should be used
- c. Forecasts are biased
- d. None of the above

Answer: c. Forecasts are biased

- 8. Which measure of forecast accuracy is scale independent?
- a. MAE
- b. MSE
- c. RMSE
- d. MAPE

Answer: d. MAPE

- 9. Calculation of forecasts is based on what?
- a. Test set
- b. Training set
- c. Both
- d. Neither

Answer: b. Training set

- 10. Forecast accuracy is based on what?
- a. Test set
- b. Training set
- c. Both
- d. Neeither

Answer: a. Test set

- 11. A series that is influenced by seasonal factors is known as what?
- a. Trend
- b. Seasonal
- c. Cyclical
- d. White Noise

Answer: b. Seasonal

- 12. Data that exhibits rises and falls that are not of a fixed period is known as what?
- a. Trend
- b. Seasonal
- c. Cyclical
- d. White Noise

Answer: a. Trend & c. Cyclicale either or all is ok for full credit

- 13. Data that is uncorrelated over time is known as what?
- a. Trend
- b. Seasonal
- c. Cyclical
- d. White Noise

Answer: d. White Noise

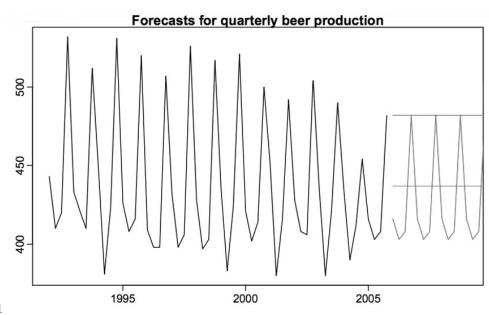
- 14. Which of the following time series decomposition models is appropriate when the magnitude of the seasonal fluctuations are not proportional to the level?
- a. Additive
- b. Multiplicative
- c. Both
- d. Neither

Answer: a. Additive

- 15. Which of the following time series decomposition models is appropriate when the magnitude of the seasonal fluctuations are proportional to the level?
- a. Additive

- b. Multiplicative
- c. Both
- d. Neither

Answer: b. Multiplicative



Line A

Line B (Straight Line)

Line C (Not Straight)

Exhibit 1

- 16. Refer to Exhibit 1. Line A is which simple forecasting method?CHECK
- a. Average Method
- b. Naïve Method
- c. Seasonal Naïve Method
- d. Drift

Answer: b. Naïve Method

- 17. Refer to Exhibit 1. Line B is which simple forecasting method?cHECK
- a. Average Method
- b. Naïve Method
- c. Seasonal Naïve Method
- d. Drift Method

Answer: a. Average Method

- 18. Refer to Exhibit 1. Line C is which simple forecasting method?CHECK
- a. Average Method
- b. Naïve Method
- c. Seasonal Naïve Method
- d. Drift Method

Answer: c. Seasonal Naïve Method

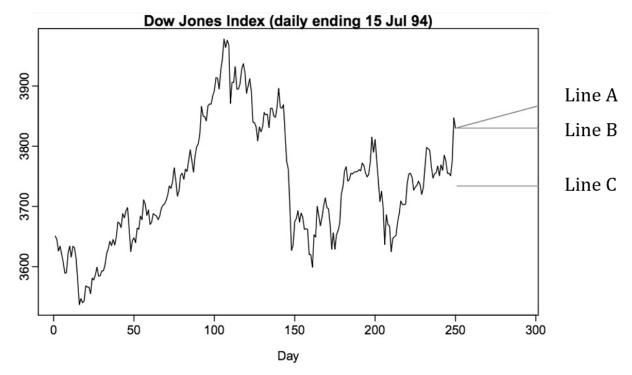


Exhibit 2

- 19. Refer to Exhibit 2. Line A is which simple forecasting method?
- a. Average Method
- b. Naïve Method
- c. Seasonal Naïve Method
- d. Drift Method

Answer: d. Drift Method

- 20. Refer to Exhibit 2. Line B is which simple forecasting method?
- a. Average Method
- b. Naïve Method
- c. Seasonal Naïve Method
- d. Drift Method

Answer: b. Naïve Method

- 21. Refer to Exhibit 2. Line C is which simple forecasting method?
- a. Average Method
- b. Naïve Method
- c. Seasonal Naïve Method
- d. Drift Method

Answer: a. Average Method

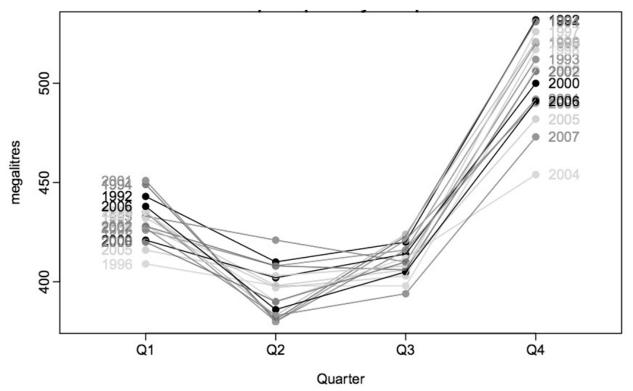


Exhibit 3

- 22. Refer to Exhibit 3. The peaks are in which quarter?
- a. Quarter 1
- b. Quarter 2
- c. Quarter 3
- d. Quarter 4

Answer: d. Quarter 4

- 23. Refer to Exhibit 3. The trough are in which quarter?
- a. Quarter 1
- b. Quarter 2
- c. Quarter 3
- d. Quarter 4

Answer: b. Quarter 2 there are few in Q3 but largly it is Q2

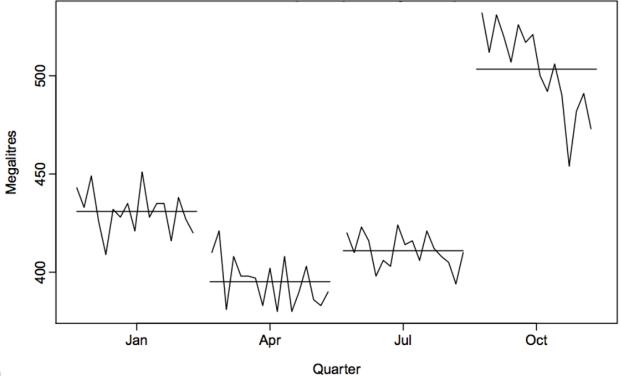


Exhibit 4

- 24. Refer to Exhibit 4. The peaks are in which quarter?
- a. Quarter 1
- b. Quarter 2
- c. Quarter 3
- d. Quarter 4

Answer: d. Quarter 4

- 25. Refer to Exhibit 4. The trough are in which quarter?
- a. Quarter 1
- b. Quarter 2
- c. Quarter 3
- d. Quarter 4

Answer: b. Quarter 2

- 26. Refer to Exhibit 4. In which quarter is there a decline in the seasonal affect?
- a. Quarter 1
- b. Quarter 2
- c. Quarter 3
- d. Quarter 4

Answer: d. Quarter 4

Figure 5

Year 1				Year 2			
Q1	Q2	Q3	Q4	Q1	Q2	Q3	Q4
10	6	8	12	11	7	9	13

- 27. Refer to Figure 5. Using the average method, what is the forecast of Quarter 2 of Year 3? (Don't use a calculator.)
- a. 7
- b. 9.5
- c. 13.85
- d. 13

Answer: b. 9.5

- 28. Refer to Figure 5. Using the naïve method, what is the forecast of Quarter 2 of Year 3? (Don't use a calculator.)
- a. 7
- b. 9.5
- c. 13.85
- d. 13

Answer:d. 13

- 29. Refer to Figure 5. Using the seasonal naïve method, what is the forecast of Quarter 2 of Year 3? (Don't use a calculator.)
- a. 7
- b. 9.5
- c. 13.85
- d. 13
- e. 7 **Answer: a. 7**
- 30. Refer to Figure 5. Using the drift method, what is the forecast of Quarter 2 of Year 3? (Don't use a calculator.)
- a. 7
- b. 9.5
- c. 13.85
- d. 13

Answer: c. 13.85

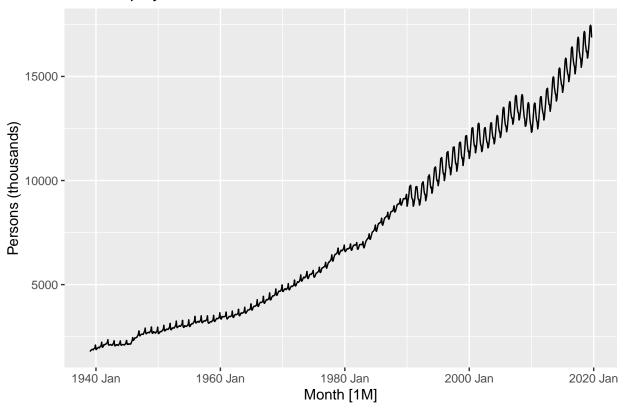
Part B (30 points)

Choose a series from us_employment.cvs, the total employment in leisure and hospitality industry in the United States (see, title column).

a. Produce an STL decomposition of the data and describe the trend and seasonality. (4 points)

```
# I am reading the data of Lesiure and hospitality industry
data <- fread('us_employment.cvs')</pre>
us_employemnt <- data[Title == 'Leisure and Hospitality']</pre>
head(us_employemnt)
##
         Month
                   Series_ID
                                                Title Employed
## 1: 1939 Jan CEU7000000001 Leisure and Hospitality
                                                          1807
## 2: 1939 Feb CEU7000000001 Leisure and Hospitality
                                                          1804
## 3: 1939 Mar CEU7000000001 Leisure and Hospitality
                                                          1834
## 4: 1939 Apr CEU7000000001 Leisure and Hospitality
                                                          1863
## 5: 1939 May CEU7000000001 Leisure and Hospitality
                                                          1882
## 6: 1939 Jun CEU7000000001 Leisure and Hospitality
                                                          1894
#Now lets convert the data into timeseries.
us_employemnt_TS <- us_employemnt %>%
  select(Month, Employed) %>%
  mutate(Month = yearmonth(Month)) %>%
  as_tsibble(index = Month)
head(us_employemnt_TS)
## # A tsibble: 6 x 2 [1M]
##
        Month Employed
##
        <mth>
               <dbl>
## 1 1939 Jan
                  1807
## 2 1939 Feb
                  1804
## 3 1939 Mar
                  1834
## 4 1939 Apr
                  1863
## 5 1939 May
                  1882
## 6 1939 Jun
                  1894
#Before Decomposition Plot
us_employemnt_TS %>%
  autoplot(Employed) +
 labs(
    y = "Persons (thousands)",
    title = "Total employment in US retail"
```

Total employment in US retail



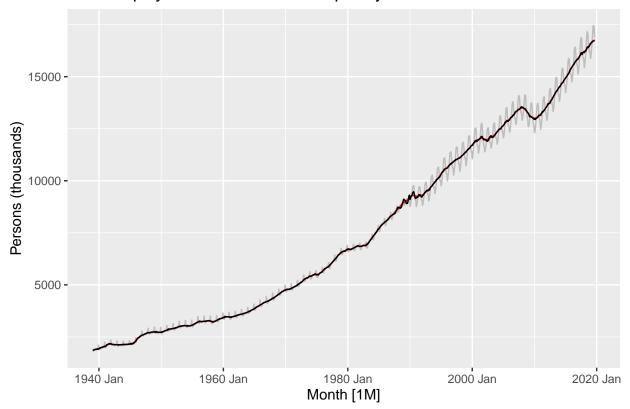
```
#STL Decomposition
us_emp_dcmp <- us_employemnt_TS %>%
  model(stl = STL(Employed))
components(us_emp_dcmp)
```

```
## # A dable: 969 x 7 [1M]
              .model [1]
## # Key:
## # :
              Employed = trend + season_year + remainder
##
      .model
                Month Employed trend season_year remainder season_adjust
##
      <chr>>
                <mth>
                          <dbl> <dbl>
                                            <dbl>
                                                       <dbl>
                                                                      <dbl>
##
    1 stl
             1939 Jan
                           1807 1861.
                                            -49.8
                                                      -4.55
                                                                      1857.
   2 stl
             1939 Feb
                           1804 1868.
                                           -62.8
                                                      -0.973
                                                                      1867.
##
   3 stl
             1939 Mar
                           1834 1874.
                                            -35.5
                                                      -4.77
                                                                      1869.
                           1863 1881.
                                            -17.2
                                                      -0.464
                                                                      1880.
##
   4 stl
             1939 Apr
##
    5 stl
             1939 May
                           1882 1887.
                                           -15.5
                                                      10.3
                                                                      1898.
##
   6 stl
             1939 Jun
                           1894 1894.
                                            -9.18
                                                       9.32
                                                                      1903.
             1939 Jul
                          1873 1900.
                                            -33.9
                                                       6.43
##
   7 stl
                                                                      1907.
                           1868 1907.
                                            -41.4
                                                       2.09
##
   8 stl
             1939 Aug
                                                                      1909.
   9 stl
                           1920 1914.
                                            -2.26
                                                       8.13
                                                                      1922.
##
             1939 Sep
## 10 stl
             1939 Oct
                           1938 1921.
                                            26.6
                                                      -9.60
                                                                      1911.
## # i 959 more rows
```

```
#After Decomposition Plot
us_employemnt_TS %>%
autoplot(Employed, color = "gray") +
```

```
autolayer(components(us_emp_dcmp), trend, color = "red") +
autolayer(components(us_emp_dcmp), season_adjust, color = "black") +
labs(
   y = "Persons (thousands)",
   title = "Total employment in Liesure & Hospitailty"
)
```

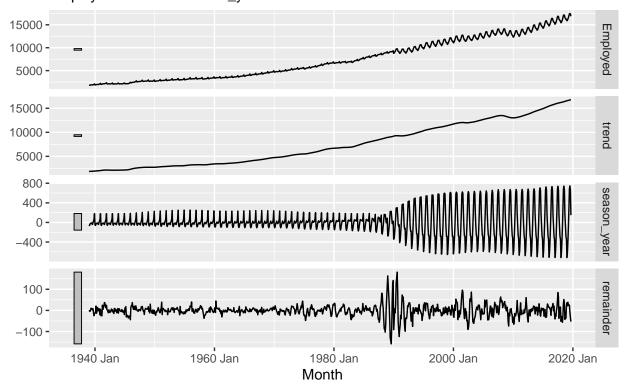
Total employment in Liesure & Hospitailty



components(us_emp_dcmp) %>% autoplot()

STL decomposition

Employed = trend + season_year + remainder

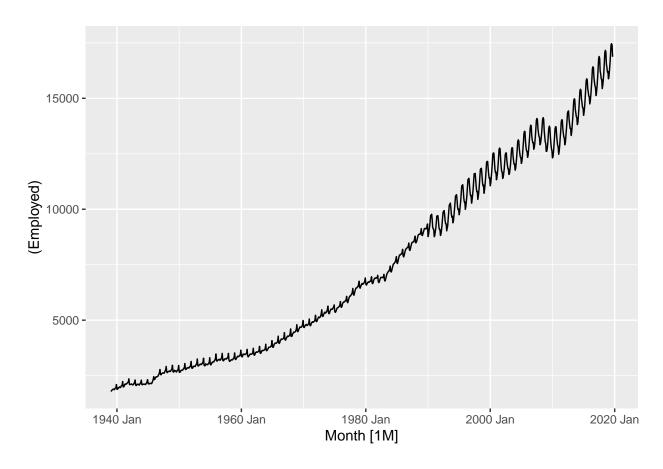


#The trend is increasing over years but we can see some drops in between 2002 and 2010. And in the initial years from 1940 to 1989, we cant see much variations in seasionality, but later especially in 1990 we can see the seasonnality is maximum. b. Do the data need transforming? If so, find a suitable transformation.(4 points)

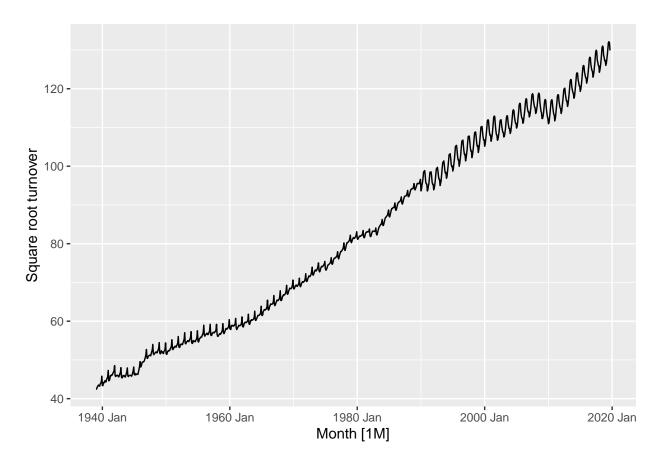
```
us_employemnt_TS %>%
  features(Employed, features = guerrero)

## # A tibble: 1 x 1
## lambda_guerrero
## <dbl>
## 1 -0.216

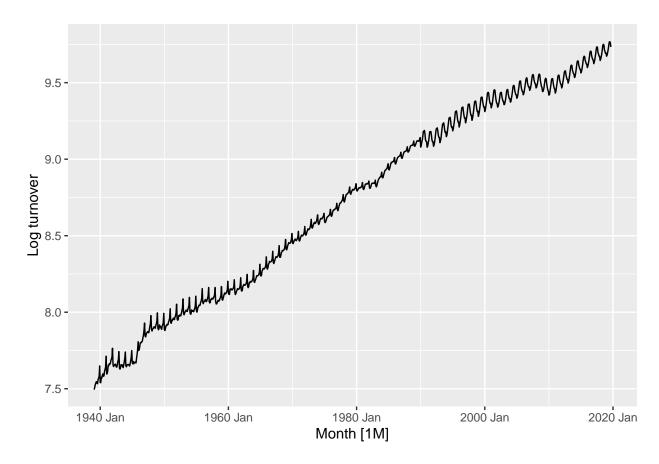
us_employemnt_TS %>% autoplot((Employed))
```



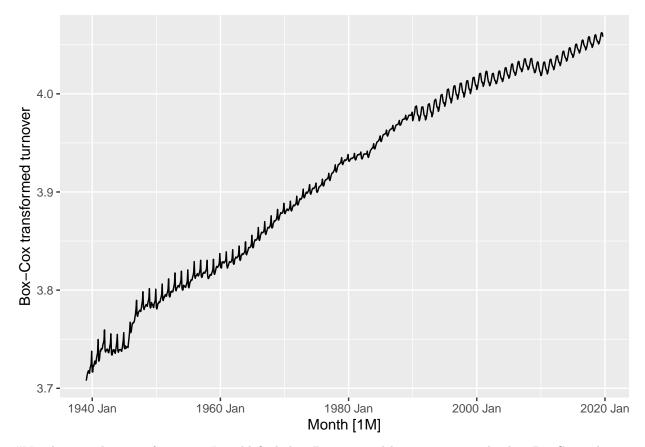
```
us_employemnt_TS %>% autoplot(sqrt(Employed)) +
labs(y = "Square root turnover")
```



```
us_employemnt_TS %>% autoplot(log(Employed)) +
labs(y = "Log turnover")
```



```
us_employemnt_TS %>% autoplot(box_cox(Employed,-0.2164477)) +
labs(y = "Box-Cox transformed turnover")
```



#Yes data needs transaformation.I could find that Box-cox and log are very similar but BoxCox is better, So I transfromed our data and stored into new variable.

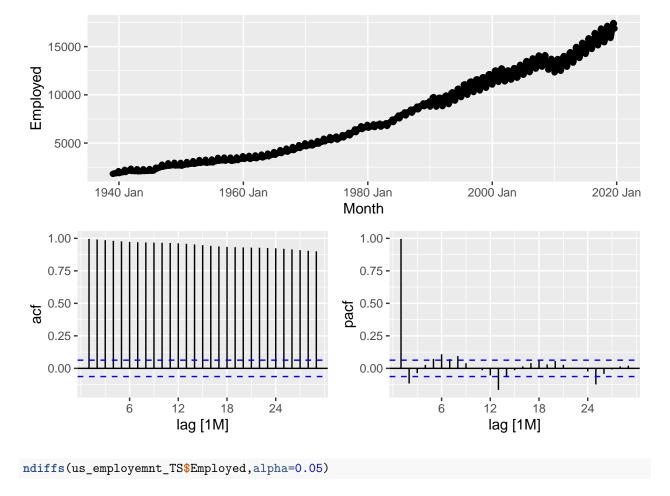
```
us_employemnt_Trans <- us_employemnt_TS %>%
  mutate(Employed = box_cox(Employed, lambda = -0.2164477))
head(us_employemnt_Trans)

## # A tsibble: 6 x 2 [1M]
### # March Fordered
```

```
##
        Month Employed
##
        <mth>
                  <dbl>
                   3.71
## 1 1939 Jan
## 2 1939 Feb
                   3.71
## 3 1939 Mar
                   3.71
## 4 1939 Apr
                   3.71
## 5 1939 May
                   3.72
## 6 1939 Jun
                   3.72
```

c. Are the data stationary? If not, find an appropriate differencing which yields stationary data.(4 points)

```
#ACF & PCF plots
gg_tsdisplay(us_employemnt_TS, Employed, plot_type='partial')
```



[1] 1

As per my observations from PACF and ACF plots, I feel that data is not stationary. Also 1st differencing should be selected.

d. Identify a couple of ARIMA models that might be useful in describing the time series. Which of your models is the best according to their AICc values?(5 points)

```
fit <- us_employemnt_Trans %>%
  model(
    arima_auto = ARIMA(Employed),
    #from ACF&pacf plot
    arima1 = ARIMA(Employed~0+pdq(12,1,0)+PDQ(1,0,0)),
    arima2 = ARIMA(Employed~0+pdq(2,1,2)+PDQ(0,1,2)),
    arima3 = ARIMA(Employed~0+pdq(2,1,0))
  )
accuracy(fit)
## # A tibble: 4 x 10
     .model
                             ME
                                    RMSE
                                             MAE
                                                      MPE
                                                            MAPE MASE RMSSE
                                                                                 ACF1
                .type
```

```
<chr>>
                <chr>
                           <dbl>
                                   <dbl>
                                           <dbl>
                                                     <dbl> <dbl> <dbl> <dbl> <
## 1 arima_auto Train~ -1.56e-5 9.77e-4 5.73e-4 -4.09e-4 0.0148 0.126 0.172 0.0306
                Train~ 9.43e-7 9.12e-4 5.67e-4 3.13e-5 0.0147 0.124 0.161 0.00982
## 2 arima1
                Train~ -1.70e-5 9.92e-4 5.76e-4 -4.45e-4 0.0149 0.126 0.175 0.0246
## 3 arima2
## 4 arima3
                Train~ -1.67e-5 9.87e-4 5.83e-4 -4.37e-4 0.0151 0.128 0.174 0.00330
report(fit[1])
## Series: Employed
## Model: ARIMA(1,1,2)(2,1,1)[12]
##
## Coefficients:
##
            ar1
                     ma1
                              ma2
                                      sar1
                                               sar2
                                                        sma1
##
         0.5861
                 -0.6248
                          0.2476
                                  -1.0777
                                            -0.4674
                                                      0.5957
## s.e. 0.0763
                  0.0755
                          0.0345
                                    0.0668
                                             0.0350
                                                      0.0699
## sigma^2 estimated as 9.746e-07: log likelihood=5362.75
## AIC=-10711.5
                  AICc=-10711.39
                                    BIC=-10677.47
report(fit[2])
## Series: Employed
## Model: ARIMA(12,1,0)(1,0,0)[12]
##
## Coefficients:
##
             ar1
                     ar2
                              ar3
                                      ar4
                                               ar5
                                                         ar6
                                                                 ar7
                                                                         ar8
                                                                                  ar9
##
         -0.0811
                  0.1753
                          0.1469
                                  0.0876
                                           -0.0040
                                                    -0.0313
                                                              0.0020
                                                                      0.0124
                                                                              0.0157
          0.0295
                  0.0295
                          0.0303
                                  0.0306
                                            0.0308
                                                      0.0308 0.0307
                                                                      0.0308 0.0306
## s.e.
##
           ar10
                   ar11
                             ar12
                                     sar1
                                   0.9927
##
         0.0234
                 0.1023
                         -0.4028
                           0.0300 0.0026
## s.e. 0.0303 0.0296
##
## sigma^2 estimated as 8.447e-07:
                                     log likelihood=5387.04
## AIC=-10746.08
                                     BIC=-10677.83
                   AICc=-10745.64
report(fit[3])
## Series: Employed
## Model: ARIMA(2,1,2)(0,1,2)[12]
##
## Coefficients:
            ar1
                     ar2
                               ma1
                                       ma2
                                               sma1
                                                        sma2
##
         0.6914
                 -0.1701
                          -0.7512
                                    0.4173
                                            -0.5077
                                                      0.0668
## s.e. 0.1376
                  0.1253
                            0.1281
                                   0.1107
                                             0.0327
                                                      0.0343
##
## sigma<sup>2</sup> estimated as 1.004e-06:
                                     log likelihood=5345.93
## AIC=-10677.85
                   AICc=-10677.73
                                     BIC=-10643.81
```

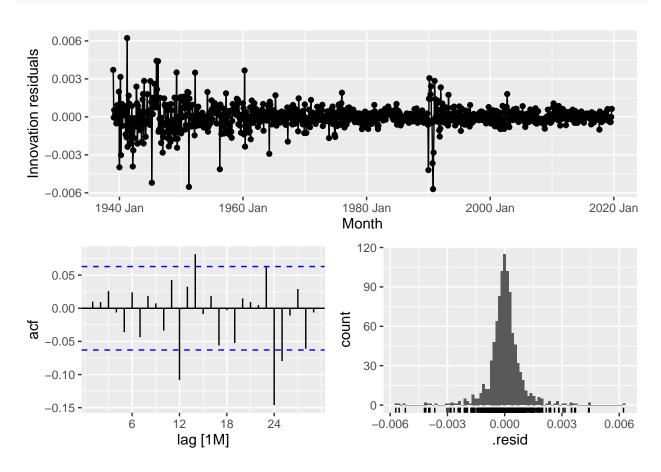
#So Ideally we will conslude that whichever AICc values is lower that should be best model. In our case arimal has AIC (AIC=-10745.64) which is lowest among others, so we will say this model is best.

e. Estimate the parameters of your best model and do diagnostic testing on the residuals. Do the residuals resemble white noise? If not, try to find another ARIMA model which fits better.(5 points)

```
final_model <- fit %>% select(arima1)
report(final_model)
```

```
## Series: Employed
## Model: ARIMA(12,1,0)(1,0,0)[12]
##
##
   Coefficients:
##
             ar1
                      ar2
                               ar3
                                       ar4
                                                 ar5
                                                           ar6
                                                                   ar7
                                                                            ar8
                                                                                    ar9
                   0.1753
##
          -0.0811
                           0.1469
                                    0.0876
                                             -0.0040
                                                      -0.0313
                                                                0.0020
                                                                        0.0124
                                                                                 0.0157
          0.0295
                   0.0295
                           0.0303
                                    0.0306
                                              0.0308
                                                       0.0308
                                                                0.0307
                                                                        0.0308
##
                                                                                 0.0306
##
           ar10
                    ar11
                              ar12
                                      sar1
                                    0.9927
##
         0.0234
                  0.1023
                          -0.4028
## s.e.
         0.0303
                  0.0296
                            0.0300
                                    0.0026
##
## sigma^2 estimated as 8.447e-07:
                                      log likelihood=5387.04
## AIC=-10746.08
                    AICc=-10745.64
                                      BIC=-10677.83
```

gg_tsresiduals(final_model)



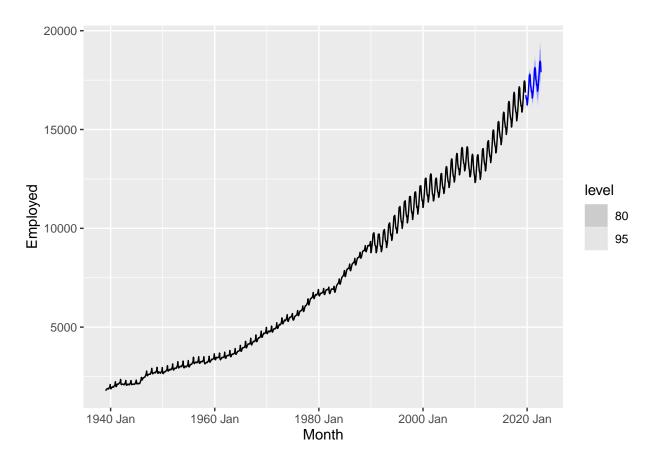
augment(final_model) %>% features(.innov, ljung_box, lag=10, dof=2)

#We found that P values is high than 0.05 so I believe we have white noise and data with white noise is consistent.

f. Forecast the next 3 years of data. Get the latest figures from https://fred.stlouisfed.org/categories/11 to check the accuracy of your forecasts. (5 points)

```
arimafitt <- us_employemnt_TS%>%
model(
arima1 = ARIMA(Employed~0+pdq(12,1,0)+PDQ(1,0,0), stepwise = FALSE,approximation = FALSE)
)

ff <- forecast(arimafitt, h = 36)
ff %>% autoplot(us_employemnt_TS)
```

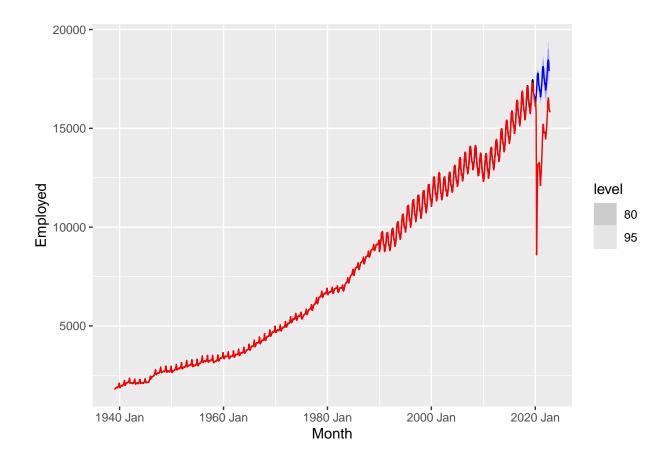


```
#latest data
latest<- fread('CEU7000000001.csv')
head(latest)</pre>
```

DATE CEU700000001

```
## 1: 1939-01-01
                        1807
## 2: 1939-02-01
                         1804
## 3: 1939-03-01
                        1834
## 4: 1939-04-01
                        1863
## 5: 1939-05-01
                         1882
## 6: 1939-06-01
                         1894
latest %>%
 mutate(DATE = yearmonth(DATE)) %>%
 tsibble(index = DATE) -> latestts
latestts
## # A tsibble: 1,007 x 2 [1M]
         DATE CEU7000000001
##
        <mth>
                   <int>
## 1 1939 Jan
                      1807
## 2 1939 Feb
                      1804
## 3 1939 Mar
                       1834
## 4 1939 Apr
                      1863
## 5 1939 May
                       1882
## 6 1939 Jun
                       1894
## 7 1939 Jul
                       1873
## 8 1939 Aug
                      1868
## 9 1939 Sep
                      1920
## 10 1939 Oct
                       1938
## # i 997 more rows
ff %>% autoplot(us_employemnt_TS)+
autolayer(latestts, color = 'red')
```

Plot variable not specified, automatically selected '.vars = CEU7000000001'



g. Eventually, the prediction intervals are so wide that the forecasts are not particularly useful. How many years of forecasts do you think are sufficiently accurate to be usable? (3 points)

#No I don't feel actual and predicted are accurate. It may be because of covid 19 which has impacted the

Part C (8 points)

Consider following transactions:

- 1. Eggs, Bread, Milk, Bananas, Onion, Yogurt
- 2. Dill, Eggs, Bread, Bananas, Onion, Yogurt
- 3. Apple, Eggs, Bread, Milk
- 4. Corn, Bread, Milk, Teddy Bear, Yogurt
- 5. Corn, Eggs, Ice Cream, Bread, Onion
- a) Calculate by hand support, confidence and lift for following rules (without usage of apriory library, show your work)
- {Bananas} -> {Yogurt} (2 points)

N= 5

N_bananas =2

```
N_yogurt = 3
N_bananas_yogurt =2
support = 2/5
confidence = 2/2
support_yogurt = 3/5
lift = 2/2 / 3/5 = 5/3 which is [confidence/support_yogurt]
• {Corn, Bread}->{Onion} (3 points)
N=5
N_0nion = 3
N_{corn} = 2
N_{corn_bread} = 2
N_corn_bread_onion =1
support = 1/5
confidence = 1/2
support onion = 3/5
lift = 1/2 / 3/5 = 3/10 which is [confidence/support_onion]
• {Bread}->{Milk, Yogurt} (3 points)
N=5
N_Bread = 5
N_Milk_Yogurt = 2
N_Bread_Milk_Yogurt = 2
support = 2/5
confidence = 2/5
support_milk_yogurt = 2/5
lift = 2/5 / 2/5 = 1 which is [confidence/support_milk_yogurt]
```

Part D (32 points)

Online_Retail2.csv contains transaction from online store in long format (i.e. single item per line and lines with same InvoiceNo is single transaction).

a) Read data and convert it to transactions (hint: transactions function and format argument). (4 points)

```
order_data <- fread('Online_Retail2.csv')
order_data <- order_data %>%
    select(-CustomerID, -StockCode, -Country, -InvoiceDate)
head(order_data)
```

```
##
      InvoiceNo
                                            Description Quantity UnitPrice
## 1:
         536365 WHITE HANGING HEART T-LIGHT HOLDER
                                                                6
                                                                        2.55
## 2:
         536365
                                  WHITE METAL LANTERN
                                                                6
                                                                        3.39
                       CREAM CUPID HEARTS COAT HANGER
                                                                8
                                                                        2.75
## 3:
         536365
## 4:
         536365 KNITTED UNION FLAG HOT WATER BOTTLE
                                                                6
                                                                        3.39
## 5:
                       RED WOOLLY HOTTIE WHITE HEART.
                                                                6
                                                                        3.39
         536365
## 6:
                         SET 7 BABUSHKA NESTING BOXES
         536365
                                                                        7.65
order_trans <- transactions(order_data, format = 'long')</pre>
order_trans
## transactions in sparse format with
    24446 transactions (rows) and
    4211 items (columns)
head(order trans)
## transactions in sparse format with
## 6 transactions (rows) and
## 4211 items (columns)
  b) Run summary on transactions. How many transactions are there? How many unique items? (4 points)
summary(order trans)
## transactions as itemMatrix in sparse format with
    24446 rows (elements/itemsets/transactions) and
    4211 columns (items) and a density of 0.005143444
##
## most frequent items:
  WHITE HANGING HEART T-LIGHT HOLDER
                                                    REGENCY CAKESTAND 3 TIER
##
                                    2302
                                                                          2169
                                                                PARTY BUNTING
##
               JUMBO BAG RED RETROSPOT
##
                                    2135
                                                                          1706
##
               LUNCH BAG RED RETROSPOT
                                                                       (Other)
##
                                                                        519558
                                    1607
##
  element (itemset/transaction) length distribution:
##
   sizes
            2
                       4
                                  6
                                       7
                                             8
                                                  9
##
      1
                 3
                            5
                                                       10
                                                            11
                                                                 12
                                                                       13
                                                                            14
                                                                                  15
                                                                                       16
##
  4440 1590 1080
                    812
                               671
                                          634
                                                635
                                                     562
                                                           568
                                                                505
                                                                                      557
                          791
                                     654
                                                                      513
                                                                           537
                                                                                 555
##
     17
           18
                19
                     20
                           21
                                22
                                      23
                                           24
                                                 25
                                                      26
                                                            27
                                                                 28
                                                                       29
                                                                            30
                                                                                  31
                                                                                       32
                                     351
                                                                242
##
    468
         444
               491
                    438
                          407
                                349
                                          310
                                                249
                                                     262
                                                           243
                                                                      272
                                                                           226
                                                                                 199
                                                                                       189
##
     33
           34
                35
                     36
                           37
                                38
                                      39
                                           40
                                                 41
                                                       42
                                                            43
                                                                 44
                                                                       45
                                                                            46
                                                                                  47
                                                                                       48
##
    162
         177
               137
                    137
                          131
                                122
                                     139
                                           122
                                                123
                                                      103
                                                            97
                                                                 104
                                                                      100
                                                                             91
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##
     49
          50
                51
                     52
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##
     88
          86
                57
                     65
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                                70
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##
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##
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                                                                            27
                                                                                  15
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```

##

##

```
97
                                         103
##
            98
                  99
                       100
                             101
                                   102
                                                104
                                                      105
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                                                                                     110
                                                                                           111
                                                                                                 112
##
       9
                   5
                              11
                                      3
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     113
           114
                 115
                       116
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                                         119
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                                                                              125
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##
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                   6
                         8
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                 131
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##
    145
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                 163
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##
    363
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##
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##
    420
           428
                 433
                       434
                             438
                                   439
                                         443
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                                                                              463
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##
    487
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                 494
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                             503
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                                         514
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                                                      517
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                                                                        522
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##
    531
           536
                 539
                       541
                             543
                                   552
                                         561
                                                567
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##
    601
           607
                 622
                       629
                             635
                                   645
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                                                                              703
                                                                                     720
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##
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                                                                                       1
##
   1108
##
##
##
       Min. 1st Qu.
                        Median
                                    Mean 3rd Qu.
                                                        Max.
##
       1.00
                 3.00
                          11.00
                                   21.66
                                             24.00 1108.00
##
   includes extended item information - examples:
##
                           labels
        *Boombox Ipod Classic
##
   1
##
   2 *USB Office Mirror Ball
## 3
##
## includes extended transaction information - examples:
      transactionID
## 1
              536365
## 2
              536366
## 3
              536367
#For no of transactions
```

no_trans <- length(order_trans)</pre>

```
#For no of unique values
unique items <- length(itemLabels (order trans))</pre>
cat("No of Transactions:", no_trans, "\n")
## No of Transactions: 24446
cat("Nuo of unique values:", unique_items, "\n")
## Nuo of unique values: 4211
  c) Inspect (with inspect) first three transactions. What items are in basket with transaction id 536366?
     (4 points)
inspect(order_trans[1:3,])
##
       items
                                                transactionID
##
   [1] {CREAM CUPID HEARTS COAT HANGER,
##
        GLASS STAR FROSTED T-LIGHT HOLDER,
        KNITTED UNION FLAG HOT WATER BOTTLE,
##
        RED WOOLLY HOTTIE WHITE HEART.,
##
##
        SET 7 BABUSHKA NESTING BOXES,
        WHITE HANGING HEART T-LIGHT HOLDER,
##
##
        WHITE METAL LANTERN}
                                                        536365
## [2] {HAND WARMER RED POLKA DOT,
##
        HAND WARMER UNION JACK}
                                                        536366
## [3] {ASSORTED COLOUR BIRD ORNAMENT,
##
        BOX OF 6 ASSORTED COLOUR TEASPOONS,
        BOX OF VINTAGE ALPHABET BLOCKS,
##
##
        BOX OF VINTAGE JIGSAW BLOCKS,
##
        DOORMAT NEW ENGLAND,
##
        FELTCRAFT PRINCESS CHARLOTTE DOLL,
##
        HOME BUILDING BLOCK WORD,
##
        IVORY KNITTED MUG COSY,
##
        LOVE BUILDING BLOCK WORD,
##
        POPPY'S PLAYHOUSE BEDROOM,
```

#In the order with transaction id 536366 we have following items HAND WARMER RED POLKA DOT, and HAND WARMER UNION JACK. d) Visualize top 10 frequent items. What is the most frequent? (4 points)

536367

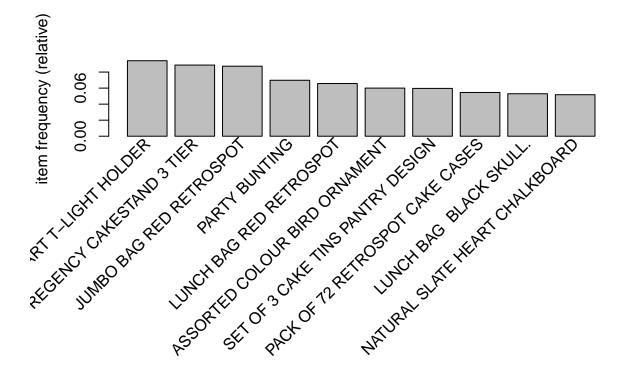
##

##

POPPY'S PLAYHOUSE KITCHEN,

RECIPE BOX WITH METAL HEART}

```
itemFrequencyPlot(order_trans,topN=10)
```



#Most frequent as per plot is WHITE HANGING HEART T-LIGHT HOLDER. e) We want to look at rule which would have at least 100 transactions. What support is corresponding to that? (4 points)

```
temp <- 100/nrow(order_trans)
cat(temp)</pre>
```

0.004090649

f) Calculate rules with a rule. Use previously calculated support, confidence of 0.9 and maxlen of 4 (we are looking into the rules with up to 4 items). (4 points)

```
items <- apriori(order_trans,parameter=list(support=0.0041,confidence=0.9,maxlen =4))</pre>
```

```
## Apriori
##
## Parameter specification:
##
    confidence minval smax arem aval original Support maxtime support minlen
                         1 none FALSE
##
                                                  TRUE
                                                               0.0041
           0.9
                  0.1
##
    maxlen target ext
         4
           rules TRUE
##
##
## Algorithmic control:
##
    filter tree heap memopt load sort verbose
##
       0.1 TRUE TRUE FALSE TRUE
                                          TRUE
##
```

```
## Absolute minimum support count: 100
##
## set item appearances ...[0 item(s)] done [0.00s].
## set transactions ...[4211 item(s), 24446 transaction(s)] done [0.17s].
## sorting and recoding items ... [1558 item(s)] done [0.01s].
## creating transaction tree ... done [0.01s].
## checking subsets of size 1 2 3 4

## Warning in apriori(order_trans, parameter = list(support = 0.0041, confidence = ## 0.9, : Mining stopped (maxlen reached). Only patterns up to a length of 4
## returned!

## done [0.13s].
## writing ... [1216 rule(s)] done [0.00s].
## creating S4 object ... done [0.00s].
```

items

set of 1216 rules

#So we have 1216 rules. g) List top 10 by confidence. What is the sense of confidence (explain on example of the top rule)? (4 points)

inspect(head(sort(items,by='confidence'),n=10))

##		lhs		rhs		support	confidence	coverage
##		{CHRISTMAS TREE HEART DECORATION, SUKI SHOULDER BAG}	=>	{DOTCOM	POSTAGE}	0.004131555	1	0.004131555 3
##		{PIZZA PLATE IN BOX, SUKI SHOULDER BAG} {SKULL SHOULDER BAG,	=>	{DOTCOM	POSTAGE}	0.004417901	1	0.004417901 3
##		URBAN BLACK RIBBONS}	=>	{DOTCOM	POSTAGE}	0.004172462	1	0.004172462 3
	[4]	{RECYCLING BAG RETROSPOT, SET/4 RED MINI ROSE CANDLE IN BOWL}	=>	{DOTCOM	POSTAGE}	0.004295181	1	0.004295181 3
	[5]	{SET/4 RED MINI ROSE CANDLE IN BOWL, SUKI SHOULDER BAG}	=>	{DOTCOM	POSTAGE}	0.004540620	1	0.004540620 3
	[6]	{CHRISTMAS TREE STAR DECORATION, SKULL SHOULDER BAG}				0.004295181		0.004295181 3
##	[7]	{BEADED CRYSTAL HEART GREEN ON STICK,		-	_			
	[8]	VINTAGE PAISLEY STATIONERY SET} {BEADED CRYSTAL HEART GREEN ON STICK,	=>	{DUTCUM	PUSTAGE}	0.004540620	1	0.004540620 3
	[9]	FLORAL FOLK STATIONERY SET} {BEADED CRYSTAL HEART GREEN ON STICK,	=>	{DOTCOM	POSTAGE}	0.004867872	1	0.004867872 3
	[10]	CHARLOTTE BAG SUKI DESIGN} {BEADED CRYSTAL HEART GREEN ON STICK,	=>	{DOTCOM	POSTAGE}	0.004131555	1	0.004131555 3
	[10]		=>	{DOTCOM	POSTAGE}	0.004745153	1	0.004745153 3

From the above data we can say that LHS customer who purchases both {CHRISTMAS TREE HEART DECORATION,SUKI SHOULDER BAG} together also pruchases {DOTCOM POSTAGE} this we can say as the support value is 1. This is the strongest rule in the dataset which we have analysed.

h) List top 10 by lift. What is the sense of lift (explain on example of the top rule)? (4 points)

```
inspect(head(sort(items,by='lift'),n=10))
```

```
##
        lhs
                                         rhs
                                                                          support confidence
                                                                                                 coverage
##
  [1]
        {DOLLY GIRL CHILDRENS CUP,
         SPACEBOY CHILDRENS BOWL,
##
         SPACEBOY CHILDRENS CUP}
                                      => {DOLLY GIRL CHILDRENS BOWL} 0.004254275 0.9811321 0.004336088
##
        {DOLLY GIRL CHILDRENS CUP,
##
         SPACEBOY CHILDRENS BOWL}
                                      => {DOLLY GIRL CHILDRENS BOWL} 0.004826966 0.9593496 0.005031498
##
        {DOLLY GIRL CHILDRENS BOWL,
##
         SPACEBOY CHILDRENS BOWL,
                                      => {DOLLY GIRL CHILDRENS CUP}
##
         SPACEBOY CHILDRENS CUP}
                                                                      0.004254275
                                                                                  0.9541284 0.004458807
        {DOLLY GIRL CHILDRENS BOWL,
##
   [4]
##
         SPACEBOY CHILDRENS CUP}
                                      => {DOLLY GIRL CHILDRENS CUP}
                                                                      0.004581527
                                                                                   0.9411765 0.004867872
##
   [5]
        {DOLLY GIRL CHILDRENS BOWL,
##
         DOLLY GIRL CHILDRENS CUP,
##
         SPACEBOY CHILDRENS CUP}
                                      => {SPACEBOY CHILDRENS BOWL}
                                                                      0.004254275
                                                                                   0.9285714 0.004581527
  [6]
        {DOLLY GIRL CHILDRENS BOWL,
##
##
         SPACEBOY CHILDRENS CUP}
                                      => {SPACEBOY CHILDRENS BOWL}
                                                                      0.004458807
                                                                                   0.9159664 0.004867872
##
  [7]
        {HERB MARKER BASIL,
##
         HERB MARKER CHIVES,
                                      => {HERB MARKER THYME}
##
         HERB MARKER ROSEMARY}
                                                                      0.006913196  0.9825581  0.007035916
##
        {PINK VINTAGE SPOT BEAKER,
##
         RED VINTAGE SPOT BEAKER}
                                      => {BLUE VINTAGE SPOT BEAKER}
                                                                      0.004581527
                                                                                   0.9256198 0.004949685
        {HERB MARKER CHIVES,
##
         HERB MARKER MINT,
                                      => {HERB MARKER PARSLEY}
##
         HERB MARKER ROSEMARY}
                                                                      0.007158635
                                                                                   0.9831461 0.007281355
## [10] {HERB MARKER CHIVES,
         HERB MARKER MINT,
                                                                      0.007117729
##
         HERB MARKER THYME}
                                      => {HERB MARKER PARSLEY}
                                                                                   0.9830508 0.007240448
```

#In the first row we can see lift value as $122.98 \sim 123$ which means that a very strong positive association between the items on LHS and ITEMS AND rhs. This indicates that the probability of purchasing a "DOLLY GIRL CHILDRENS BOWL" in same transACSTIN is increased by 123 times when "SPACEBOY CHILDRENS BOWL" and "DOLLY GIRL CHILDRENS CUP" are there in the transaction, as opposed to when the purchase of the "DOLLY GIRL CHILDRENS BOWL" is made separately from the first two items.

LHS = {DOLLY GIRL CHILDRENS CUP, SPACEBOY CHILDRENS BOWL, SPACEBOY CHILDRENS CUP} RHS= {DOLLY GIRL CHILDRENS BOWL}