

Energy-energy correlators in jets across collision systems

Anjali Nambrath

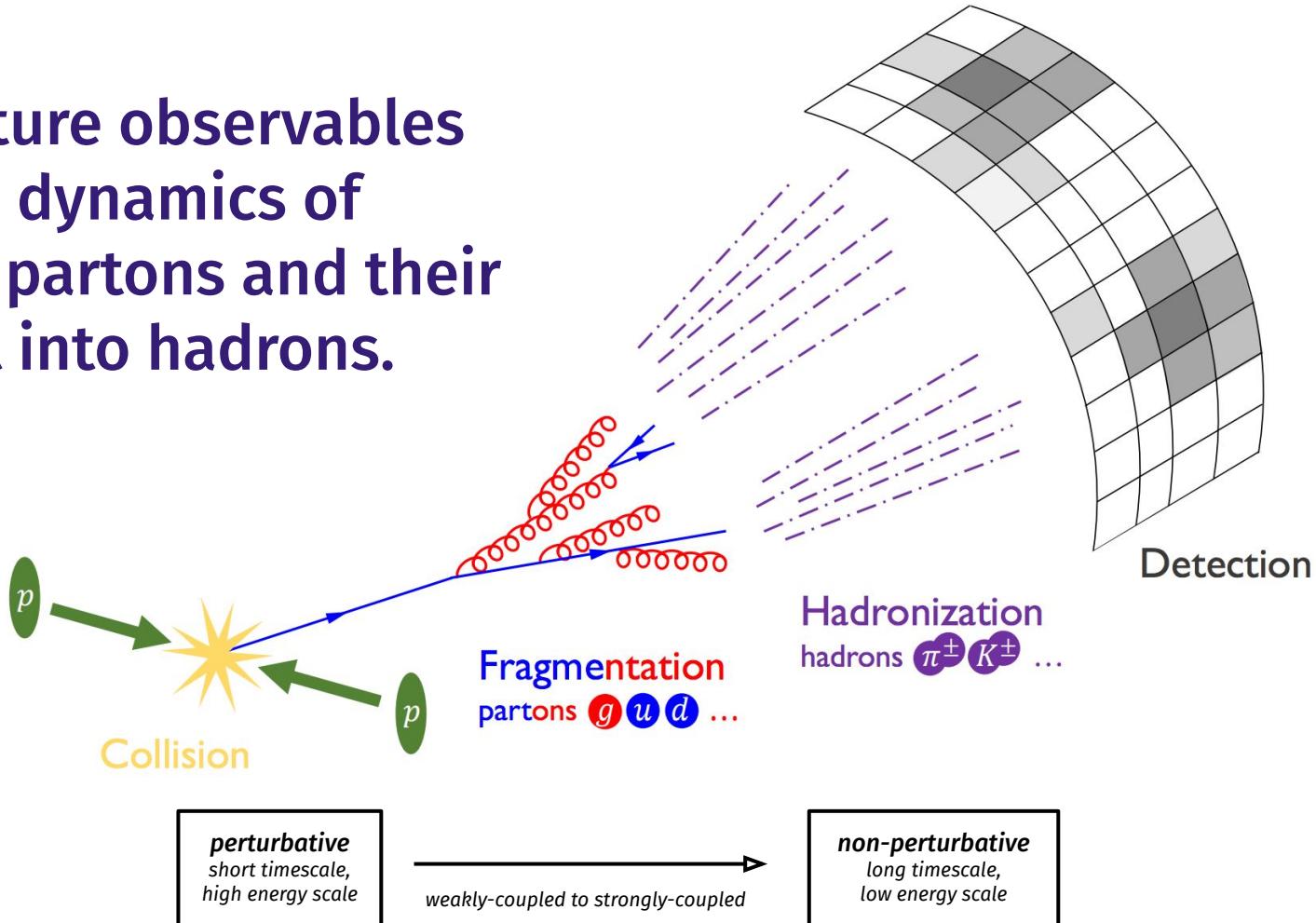
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Jet substructure observables describe the dynamics of high-energy partons and their confinement into hadrons.



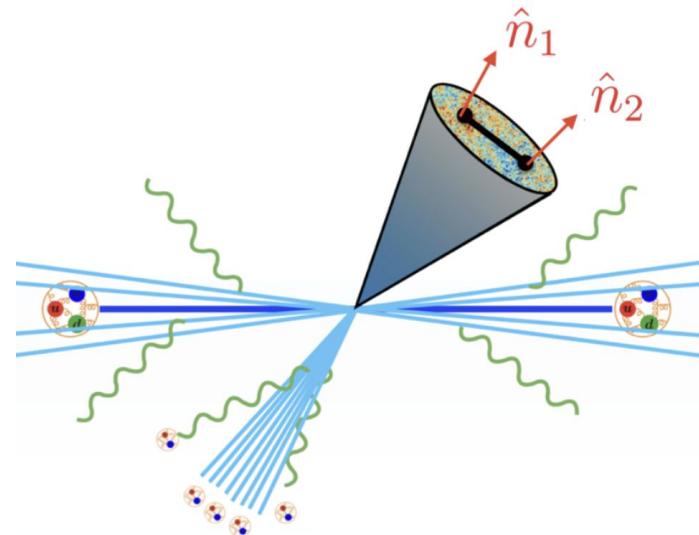
Energy correlators are a novel jet substructure observable.

Energy-energy correlators measure statistical correlations of energy flow within jets.

- correlations of energy flow operators
- IRC-safe and well-defined in QFT!
- no need for declustering or grooming

$$\frac{d\sigma_{EEC}}{dR_L} = \sum_{i,j} \int d\sigma(R'_L) \frac{p_{T,i} p_{T,j}}{p_{T,jet}^2} \delta(R'_L - R_{L,ij})$$

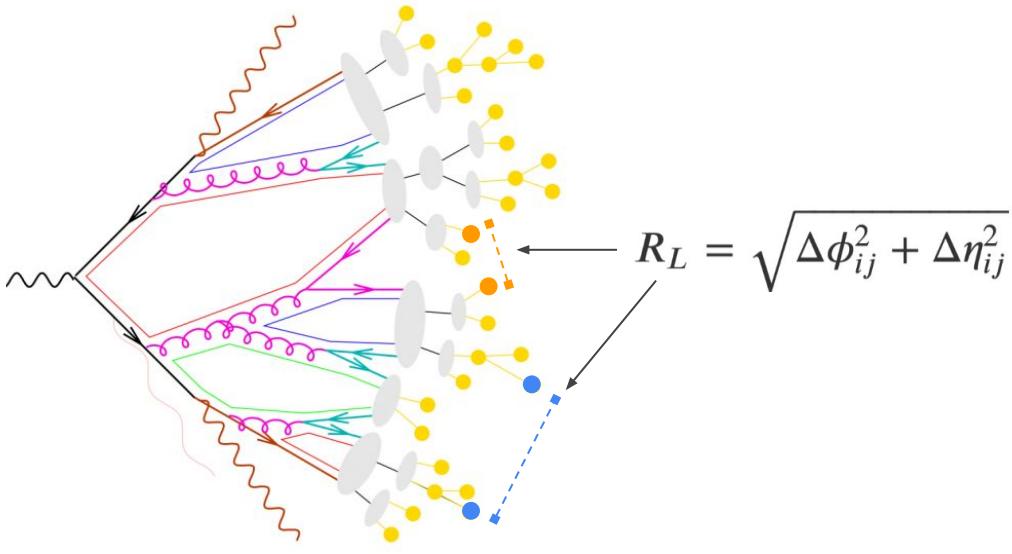
EECs are fundamental theoretical objects
and experimentally measurable!



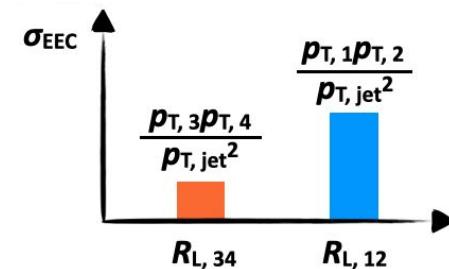
The two-point EEC is calculated from pairs of tracks.

EEC definition:

$$\frac{d\sigma_{EEC}}{dR_L} = \sum_{i,j} \int d\sigma(R'_L) \frac{p_{T,i} p_{T,j}}{p_{T,jet}^2} \delta(R'_L - R_{L,ij})$$

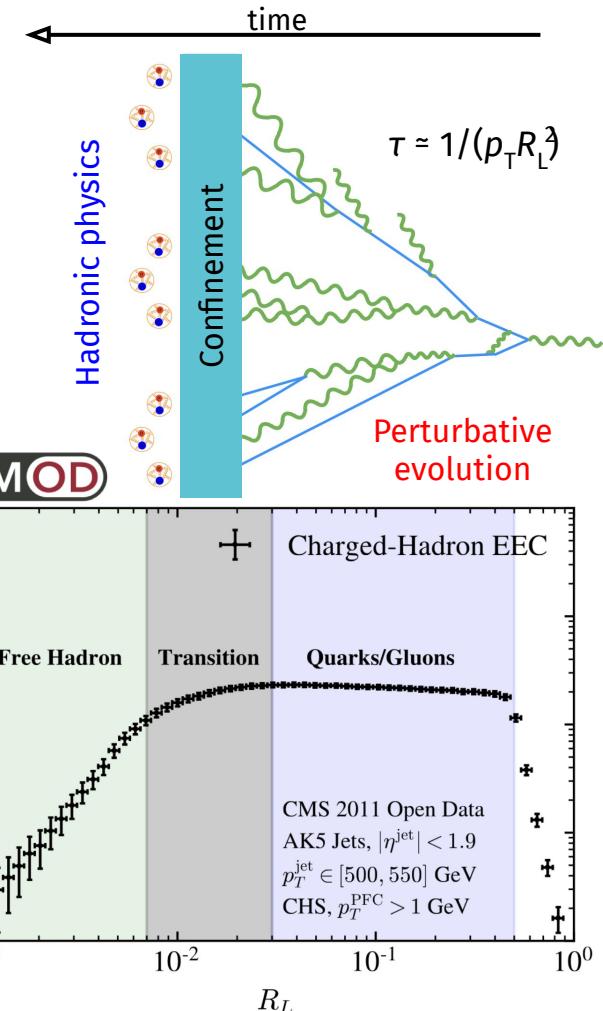


1. For each pair of tracks inside the jet, calculate the **energy weight**.
2. Count the number of weighted track pairs as a function of R_L .



EECs show a clear transition region.

- Transition between **perturbative** (large R_L , partonic) and **non-perturbative** regimes (hadronic, small R_L)
- Time evolution of jet formation is imprinted onto the EEC angular scaling
- EECs let us probe jet formation and confinement!



In this talk: differential measurements of EECs

1. EECs in pp
probing hadronization
2. EECs in D^0 -tagged jets
probing flavor effects
3. EECs in p-Pb
probing jets in higher-multiplicity environments
4. EECs in Pb-Pb
probing jets in the presence of the QGP

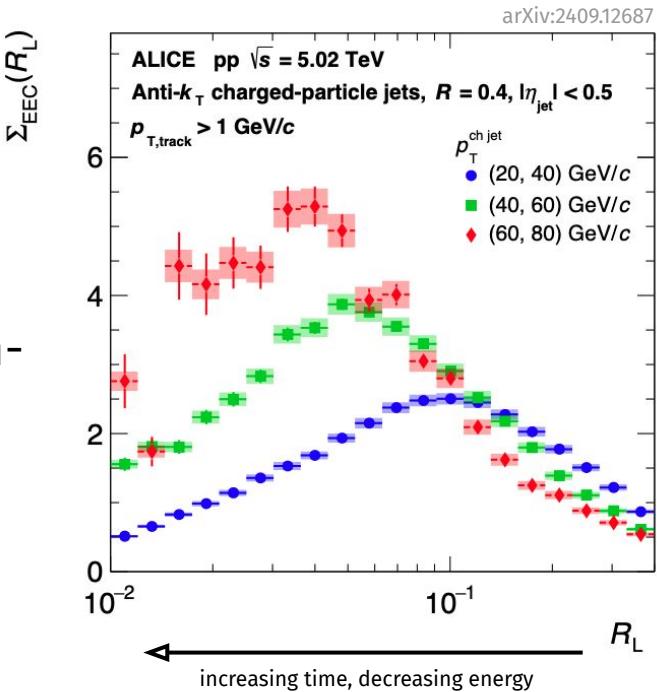
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EECs in pp

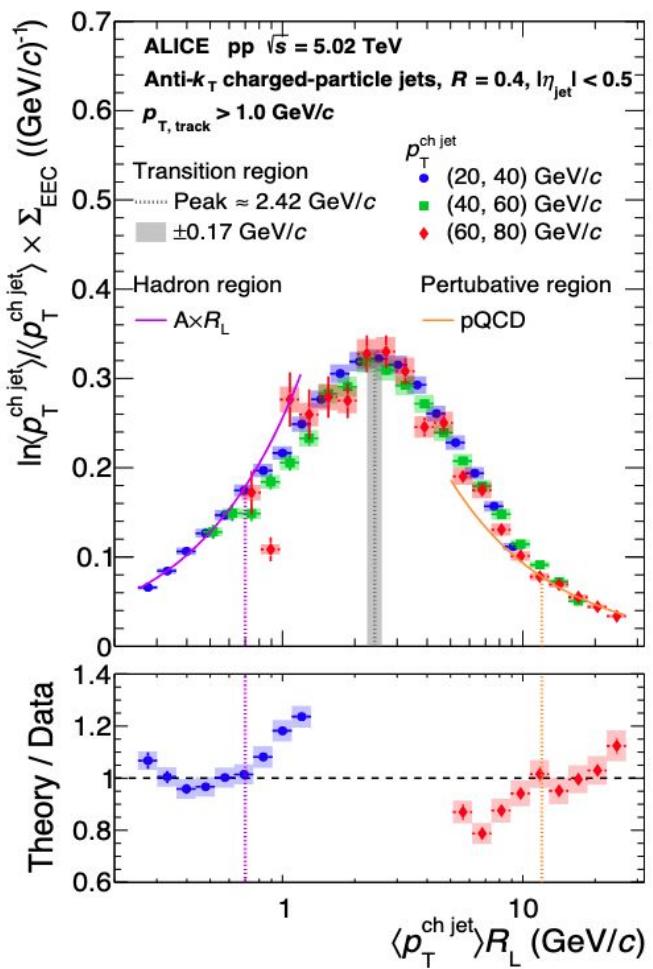
Clear separation of perturbative and non-perturbative regions.

EEC peak is visibly dependent on jet p_T .

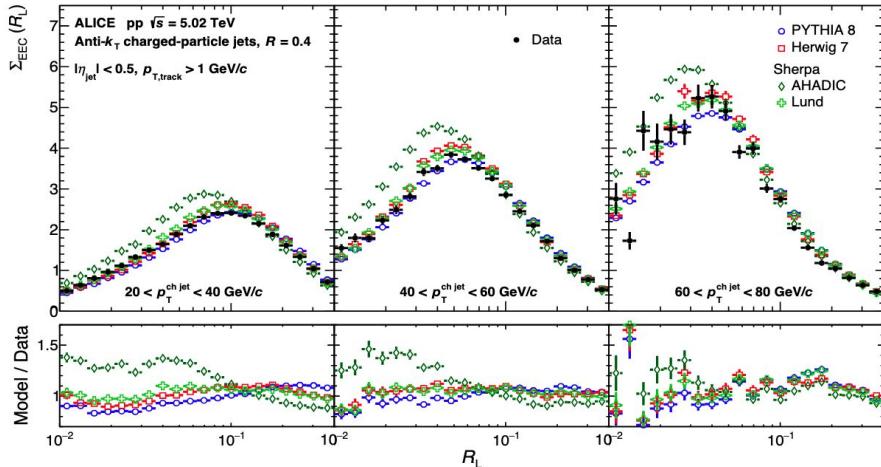


Universal transition region

after rescaling the x-axis to $\langle p_T^{ch\ jet} \rangle R_L$
(common peak position and height).

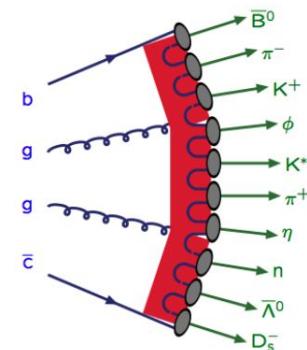


We can probe hadronization with pp EECs...

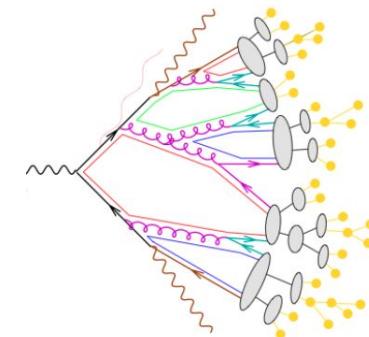


- PYTHIA & Herwig perform well,
Herwig captures peak position
- Sherpa Lund does well, AHADIC does not
- *both cluster models peak at smaller R_L*

Lund string models: PYTHIA 8, Sherpa Lund
Cluster models: Herwig 7, Sherpa AHADIC

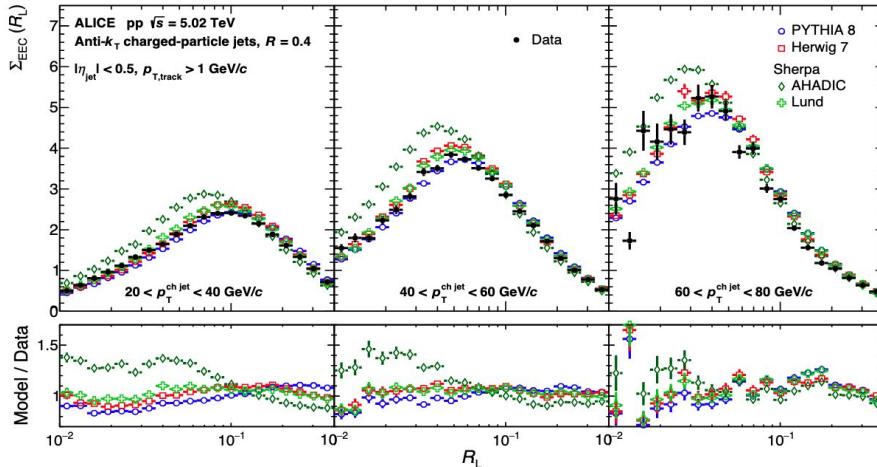


string models



cluster models

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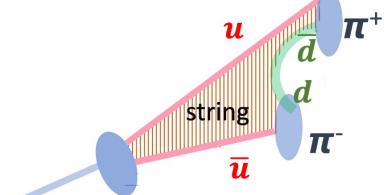


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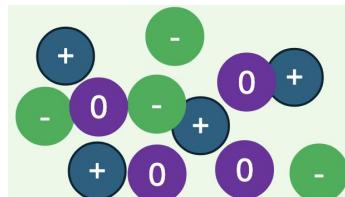
Lund string models: PYTHIA 8, Sherpa Lund
Cluster models: Herwig 7, Sherpa AHADIC

... or with charged energy correlators!

Lund string models: expect correlations between leading di-hadrons in jets



Infinite neutral bath: expect no charge correlations among pairs

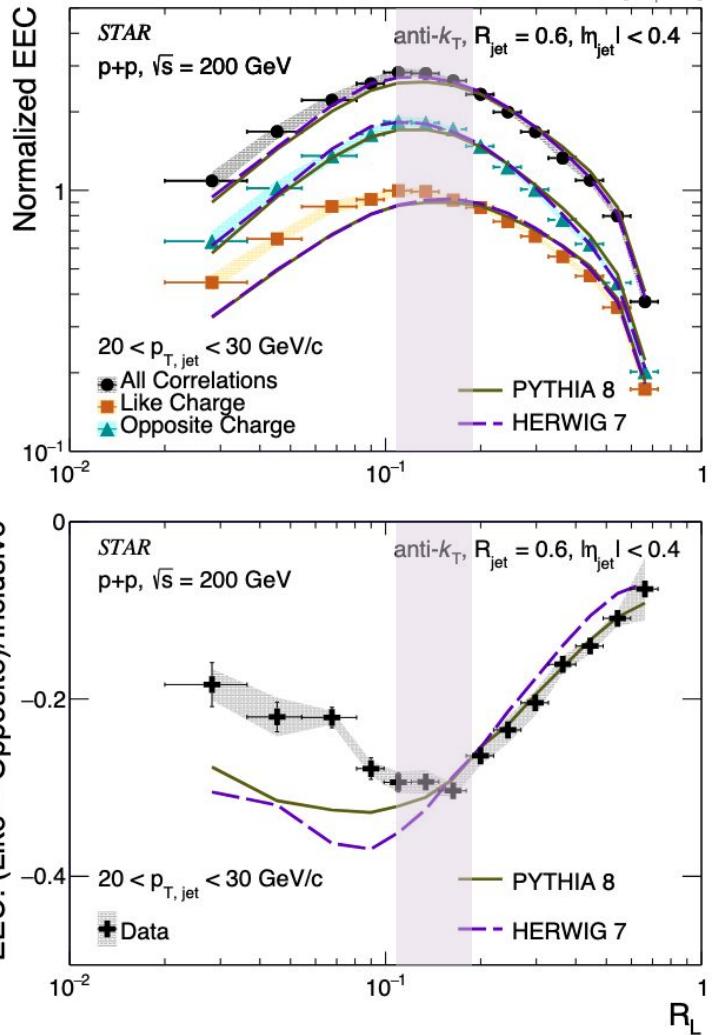


- Are there more unlike-sign or like-sign correlations? $\langle \mathcal{E}_+ \mathcal{E}_- \rangle$ or $\langle \mathcal{E}_+ \mathcal{E}_+ \rangle + \langle \mathcal{E}_- \mathcal{E}_- \rangle$
- Exploring correlations in angle and charge *increases sensitivity to different hadronization mechanisms.*

STAR measured charged correlators.

- The charged EECs align in the perturbative region with MC predictions.
 - MCs underpredict like-sign EEC at small R_L !
 - Cannot resolve the predicted shift in EEC peak

 - Herwig (cluster) and PYTHIA (string) predict similar behavior in the charge-weighted ratio
 - *PYTHIA captures large R_L behavior, but neither model describes small R_L de-correlation!*
 - resembles STAR r_c measurement
- [slides from Youqi Song here]



In this talk: differential measurements of EECs

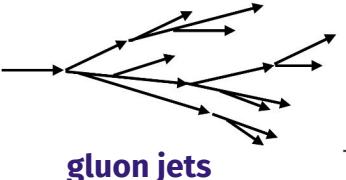
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probing hadronization

- 2. EECs in D^0 -tagged jets
probing flavor effects

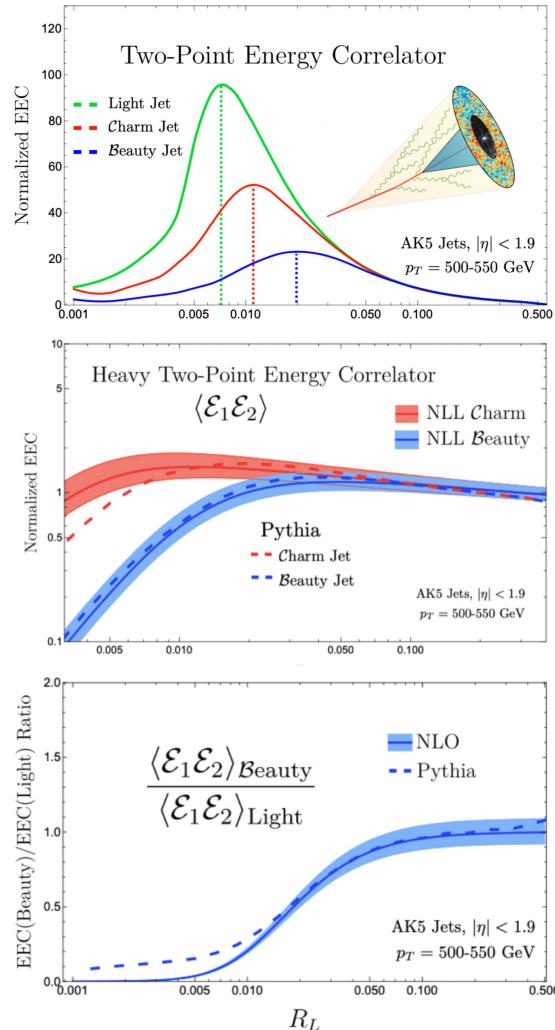
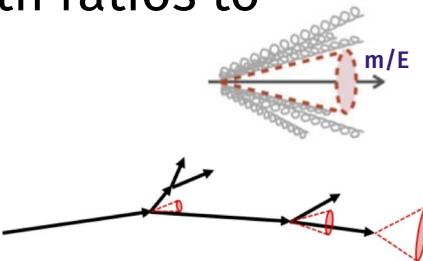
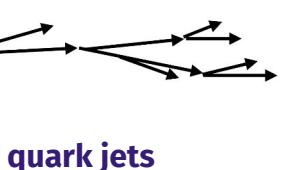
3. EECs in p-Pb
probing jets in higher-multiplicity environments
4. EECs in Pb-Pb
probing jets in the presence of the QGP

How does the shower depend on flavor?

- At the largest R_L , the scaling behavior in heavy-flavor jets is identical to light quark jets.
- *Turnover exhibits a mass dependence!*
- Change of shape at small angles is a consequence of the dead cone.
- Flavor effects can be probed with ratios to inclusive jets.



$$\frac{C_A}{C_F} = \frac{9}{4}$$



Comparing D^0 -tagged jet to inclusive jet EECs

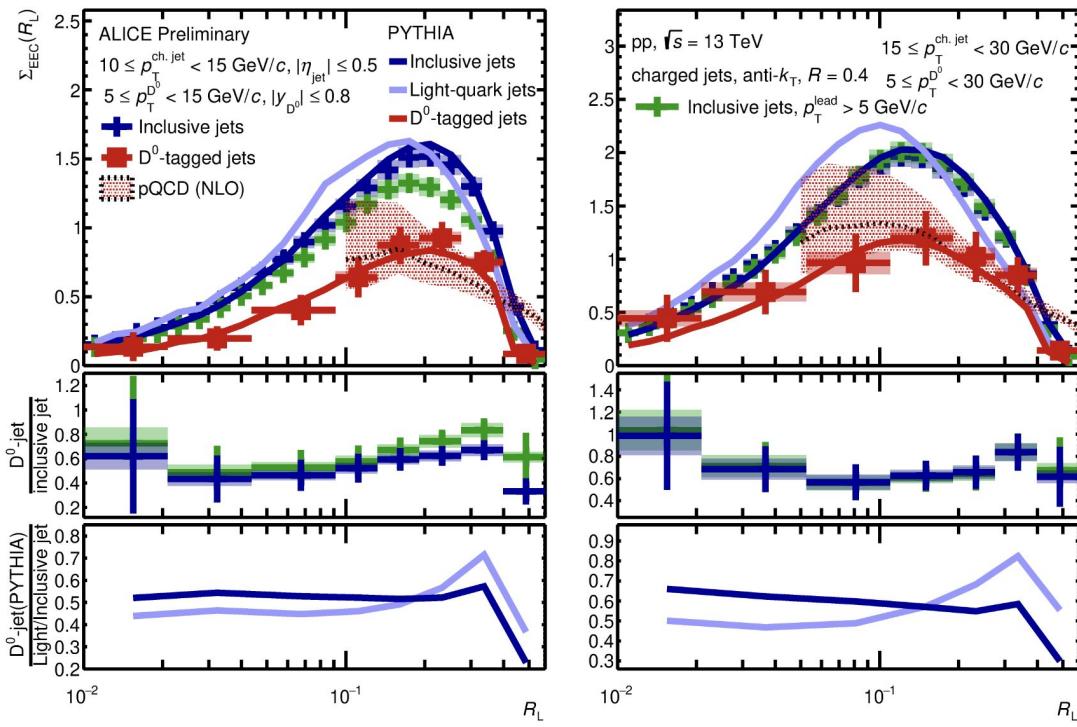
Upper panel:

- p_T cut on leading track in incl. jets to study fragmentation bias
- significant suppression at all R_L , slopes at large R_L seem different
- peak positions are similar due to gluon contribution to inclusive

From the ratios:

- D^0 /inclusive \rightarrow mass + Casimir
- D^0 /LF \rightarrow isolated mass effects

Clear mass effect in D^0 jets!



pQCD calculation from K. Lee

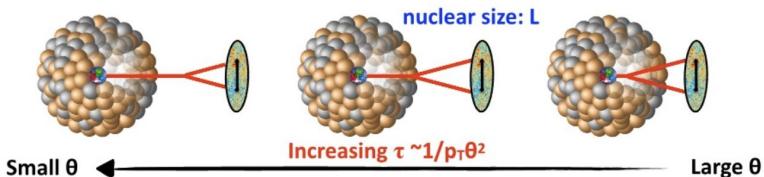
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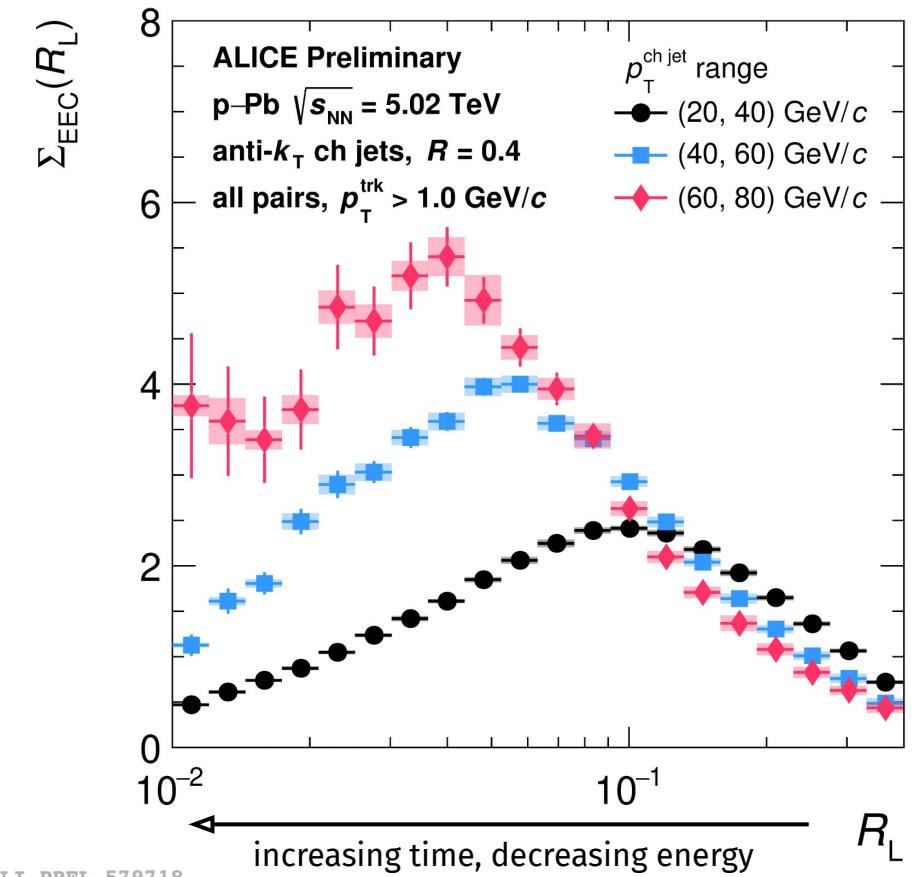
Are EECs modified in p-Pb?

Differences from pp:

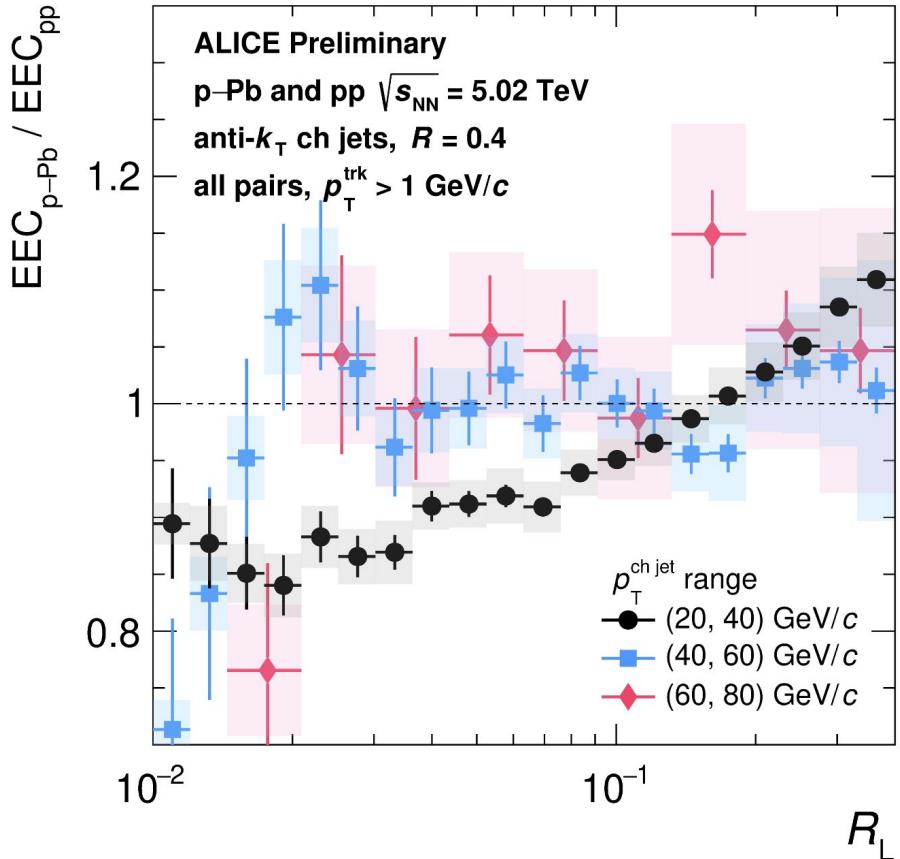
- initial state (nPDF, isospin)
- final-state interactions?
- comovers? collectivity??



EECs in p-Pb are a window into interactions in small systems.



EECs are modified in p-Pb, in the lowest jet p_T range.

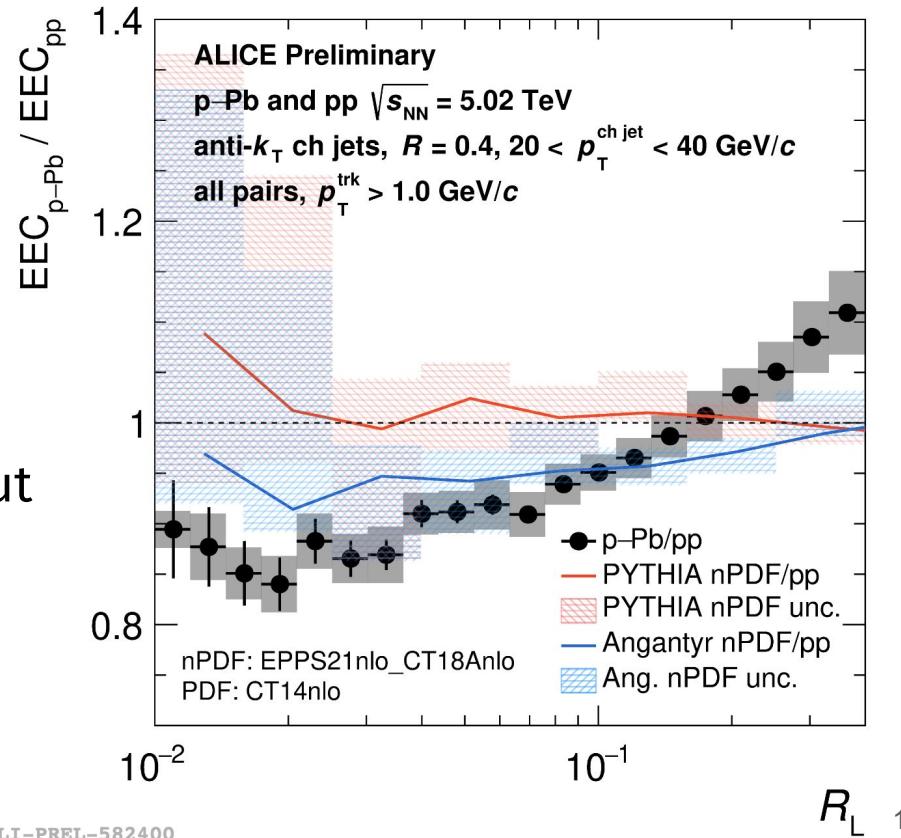


- *Significant difference between EECs in p-Pb compared to pp!*
 - jet structure appears to be altered only in the lowest jet p_T range
- Initial state effect?
 - some models lead to a similar effect
- Final state effect?
 - some calculations reproduce this
- Modification is qualitatively consistent with ALICE measurement* of HM/MB z_{ch} in pp

* arXiv:2311.13322

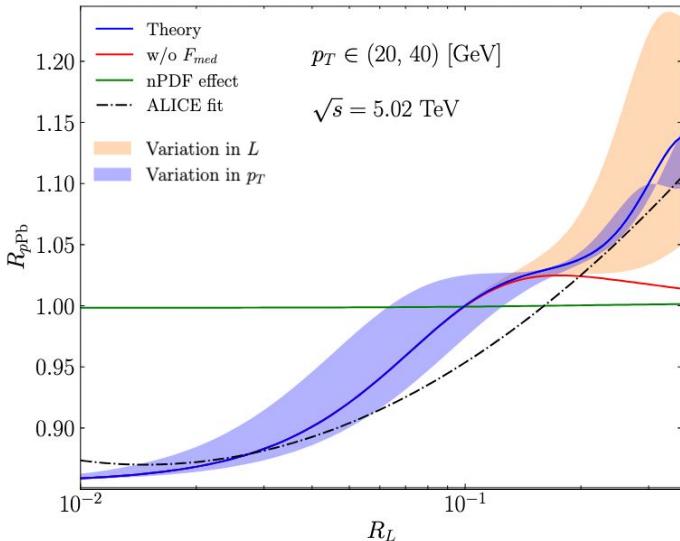
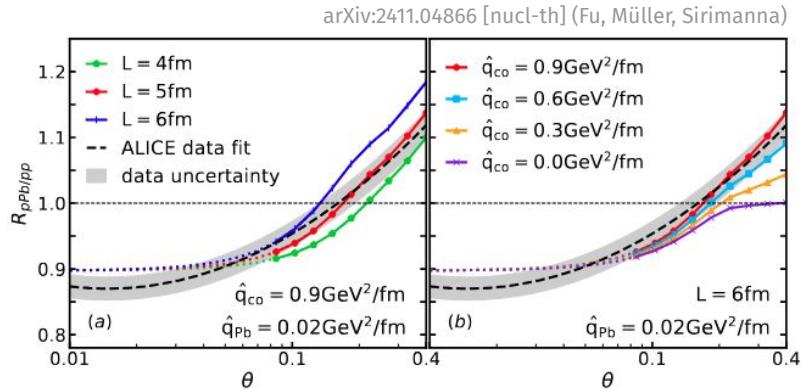
nPDF models do not fully capture the enhancement and suppression seen in data.

- Comparing to PYTHIA with an nPDF turned on, and PYTHIA Angantyr
- PYTHIA results use:
 - nPDF: EPPS21nlo_CT18Anlo
 - PDF: CT14nlo
- nPDFs are within $\sim 1\sigma$ at small R_L – but these are very large uncertainties
- Neither captures the behavior at large R_L .



Some theory models can reproduce the enhancement.

- Fu et al. use a higher-twist model and require comovers to capture the enhancement
 - p_T^{jet} of 30 GeV/c, $R_{p\text{Pb}}$ chosen to be 0.85
- Barata et al. capture the NP region as well with multiple scatterings and transverse momentum broadening
 - HT correction to jet's perturbative evolution
 - p_T broadening in TMD fragmentation function



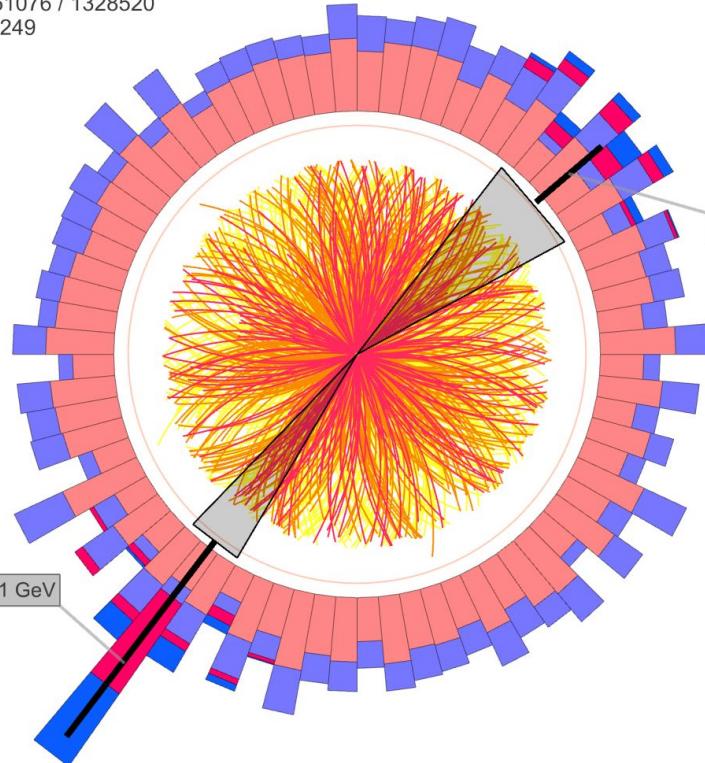
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Jets lose energy as they traverse the quark-gluon plasma.



CMS Experiment at LHC, CERN
Data recorded: Sun Nov 14 19:31:39 2010 CEST
Run/Event: 151076 / 1328520
Lumi section: 249



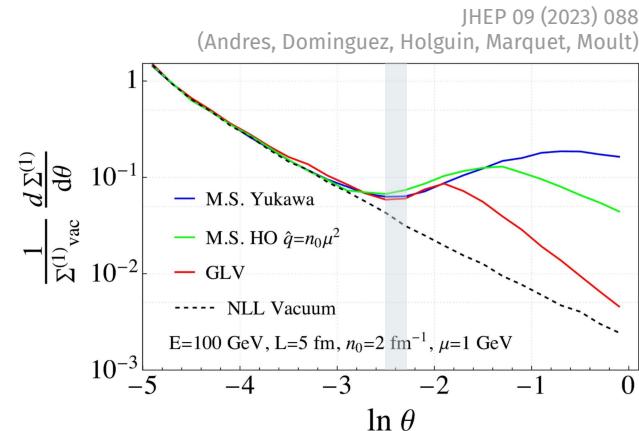
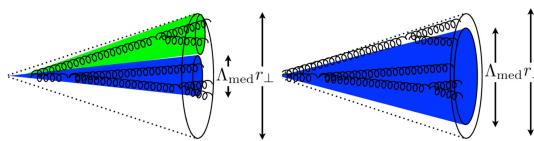
Jet 1, pt: 70.0 GeV

Jet 0, pt: 205.1 GeV

EECs in Pb-Pb can probe various medium effects.

Color coherence

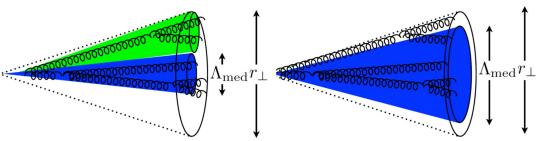
- *large angle emission*: medium resolves emitted gluon as a separate object
- *small angle emission*: gluon and emitter resolved as single object
- *critical angle*: minimum separation to resolve separately



EECs in Pb-Pb can probe various medium effects.

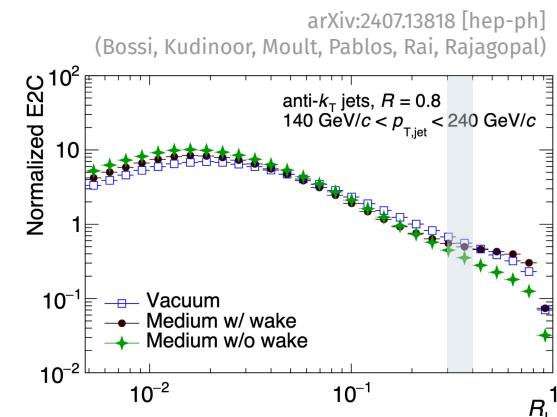
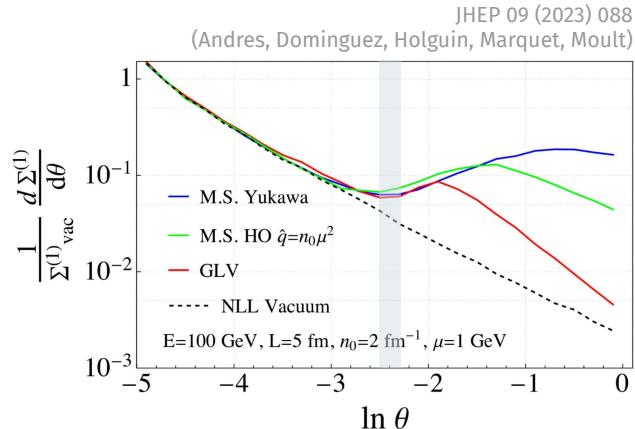
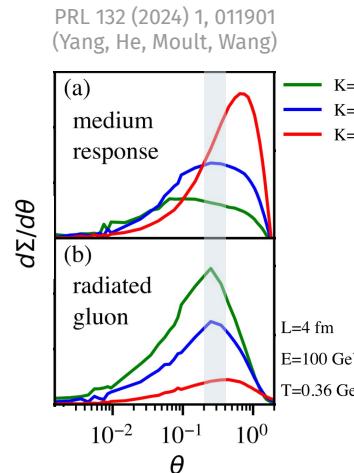
Color coherence

- **large angle emission:** medium resolves emitted gluon as a separate object
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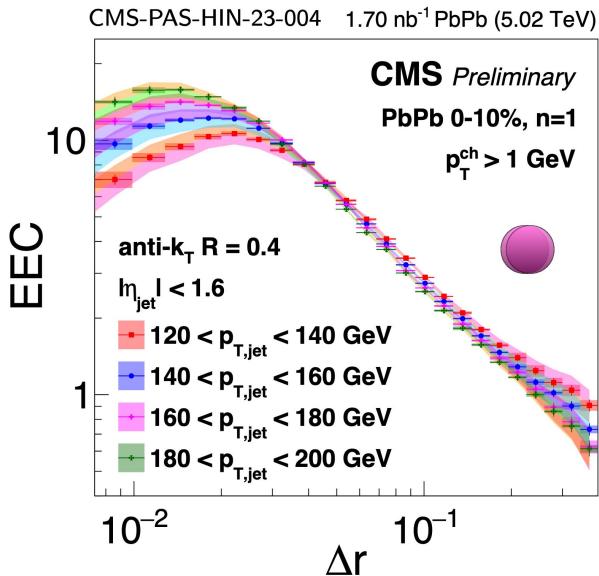


Medium response

- Jets can induce a **medium response** (recoil partons and back-reaction).
- Energetic partons can pull the medium, leaving a depletion called the "**jet wake**".

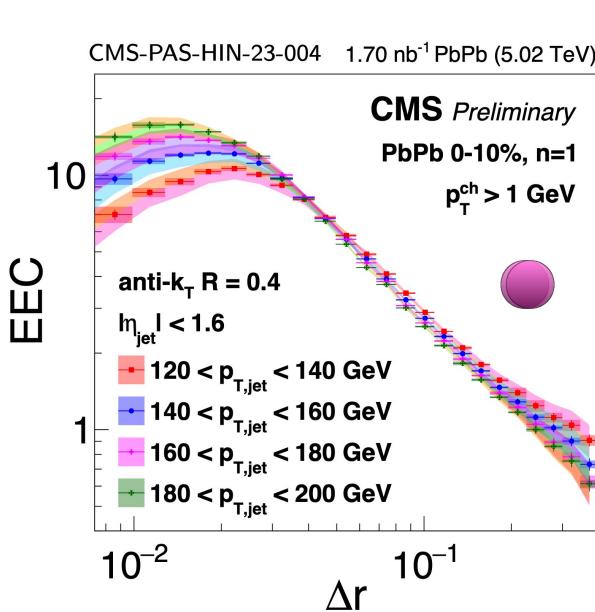


CMS measured EECs in Pb-Pb...

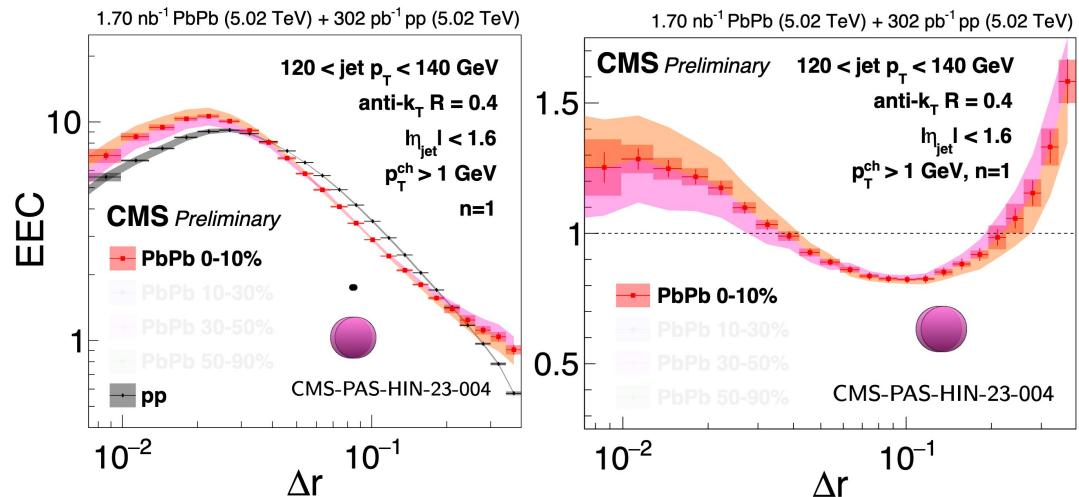


Pb-Pb loosely has the same features as observed in pp.

CMS measured EECs in Pb-Pb... and found differences.



Pb-Pb loosely has the same features as observed in pp.



- *Pb-Pb peaks at smaller R_L than pp*
 - energy loss: Pb-Pb jets have higher initial virtuality
 - flat trend at lowest R_L (free hadron scaling)
- *Pb-Pb EEC has a different shape at large R_L*
 - at $R_L \sim 0.1$, we see another enhancement

How do calculations stack up against this data?

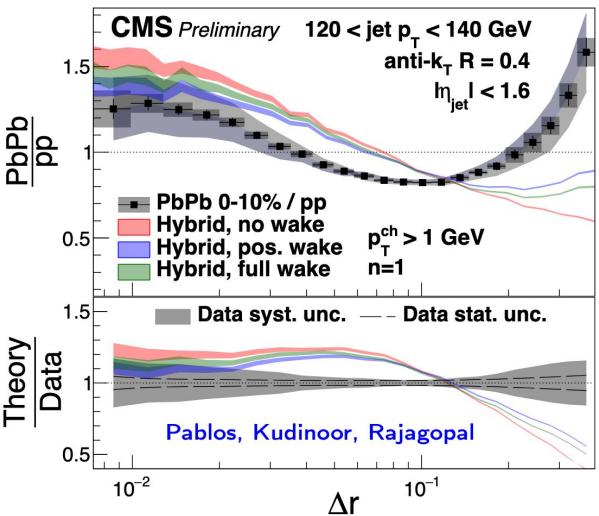
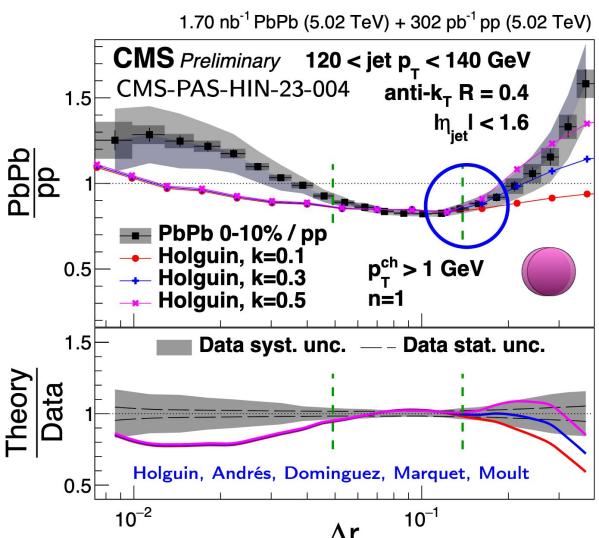
Color coherence

- Holguin et al. calculation* has two free parameters: k and normalization
- Calculation is normalized to data in $0.042 < R_L < 0.126$
- Turn-on angle is similar in data and calculation!

* arXiv:2407.07936 [hep-ph] (Andres, Dominguez, Holguin, Marquet, Moult)

Medium response

- Modeling medium response using jet wake in Hybrid
- Hybrid only predicts the large- R_L enhancement with the wake included
 - does not capture the magnitude or onset of the effect
- JEWEL (not shown) requires recoils for enhancement



Summary and outlook

- Universality of EEC shape and turnover in pp
no very obvious conclusions about hadronization
- EECs are altered in HF jets
dramatic reduction in amplitude – clear mass/flavor effect
- EECs are modified in p-Pb
models with final-state interactions capture large R_L trends
- Energy loss is visible in Pb-Pb EECs
along with some interesting large R_L effects (medium response?)

Not shown here: N -point energy correlators, recent theory developments, and more!

Many more results are coming at QM25 – it's an exciting time in the world of EECs.

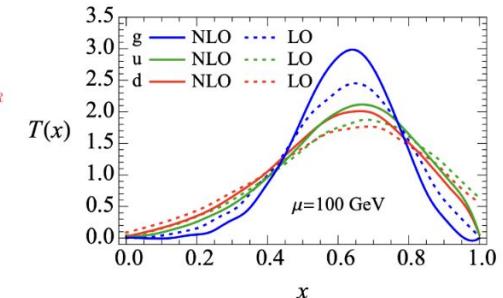
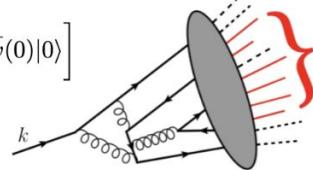
Backup

TRACK FUNCTIONS

Chang, Procura, Thaler, Waalewijn '13
Li, Moult, Waalewijn, Zhu et al '21, 22

- Track functions are **non-perturbative functions** describing the momentum fraction of initial parton converted to hadrons with a particular property **R**.

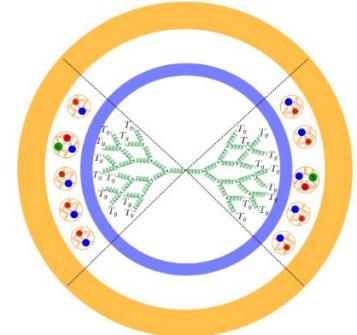
$$T_q(x) = \int dy^+ d^2y_\perp e^{ik^-y^+/2} \frac{1}{2N_c} \sum_X \delta\left(x - \frac{P_R}{k_-}\right) \text{tr} \left[\frac{\gamma^-}{2} \langle 0 | \psi(y^+, 0, y_\perp) | X \rangle \langle X | \bar{\psi}(0) | 0 \rangle \right]$$



- Track functions are technically what is needed for calculating the usual **jet shape observables** on track (jet mass, jet angularities, jet charge, etc...), but is **technically challenging**

$$\delta(e - \hat{e}(\{p_i^\mu \in X_J\})) \rightarrow \delta(e - \hat{e}(\{\textcolor{red}{x_i} p_i^\mu \in X_J\}))$$

requires simultaneous knowledge of all the tracks in jet.

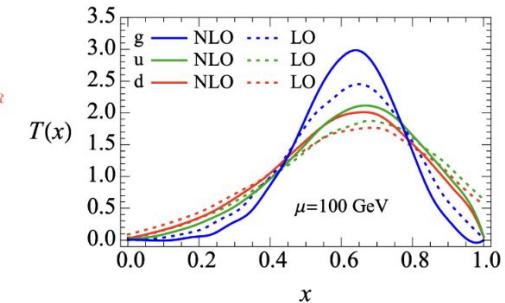
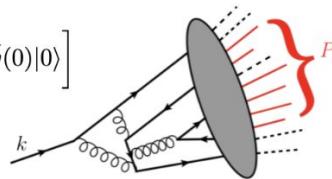


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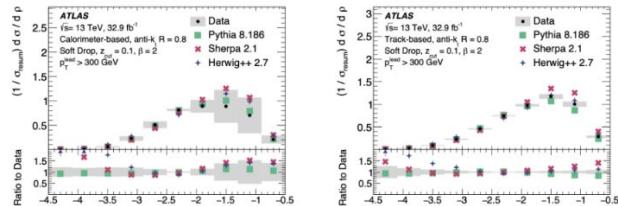
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- Ten years after track function formalism is developed, the computation still remains elusive.

bservables. For all of these observables, the uncertainties for the track-based observables are significantly maller than those for the calorimeter-based observables, particularly for higher values of β , where more oft radiation is included within the jet. However, since no track-based calculations exist at the present me, calorimeter-based measurements are still useful for precision QCD studies. [ATLAS Collaboration, 1912.09837]

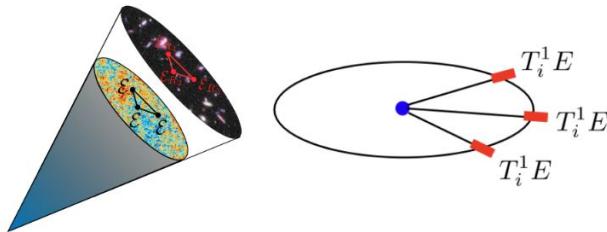
selection of charged particle jets. Note that track-based observables are IRC-unsafe. In general, perturbative track functions can be used to directly compare track-based measurements to analytical ulations [67–69]; however, such an approach has not yet been developed for jet angularities. Two [ALICE Collaboration, 2107.11303]



[ATLAS (2019)]

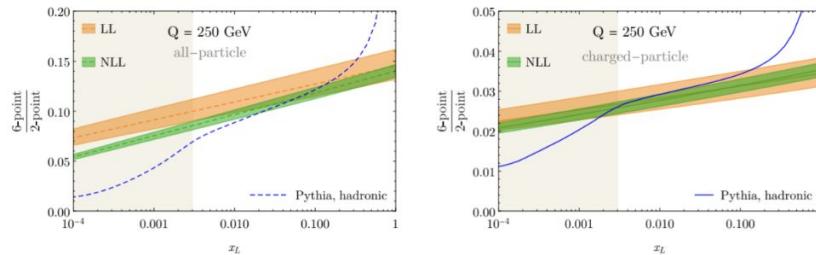
ENERGY CORRELATORS ON TRACK

- From this “detector” as a fundamental operator perspective, track function formalism provides the essential matching between partonic and hadronic detectors.



$$\langle \mathcal{E}_R(\vec{n}_1) \mathcal{E}_R(\vec{n}_2) \cdots \mathcal{E}_R(\vec{n}_k) \rangle = \sum_{i_1, i_2, \dots, i_k} T_{i_1}(1) \cdots T_{i_k}(1) \langle \mathcal{E}_{i_1}(\vec{n}_1) \mathcal{E}_{i_2}(\vec{n}_2) \cdots \mathcal{E}_{i_k}(\vec{n}_k) \rangle + \text{contact terms. Requires up to } k\text{-th moment}$$

- Aside from the fact that this is technically much simpler, it only involves NP numbers, not functions.



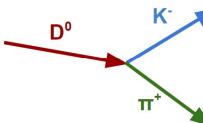
Up to 6 point EEC computed on tracks at NLL!

Jaarsma, Li, Moult, Waalewijn, Zhu '23

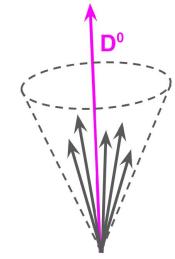
$$\langle \mathcal{E}(n_1) \mathcal{E}(n_2) \cdots \mathcal{E}(n_k) \rangle \rightarrow \langle \mathcal{E}_{\mathbf{R}}(n_1) \mathcal{E}_{\mathbf{R}}(n_2) \cdots \mathcal{E}_{\mathbf{R}}(n_k) \rangle \rightarrow \langle \mathcal{E}_{\mathbf{R}_1}(n_1) \mathcal{E}_{\mathbf{R}_2}(n_2) \cdots \mathcal{E}_{\mathbf{R}_k}(n_k) \rangle$$

D^0 reconstruction steps

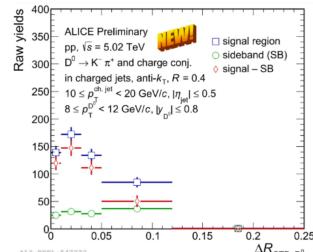
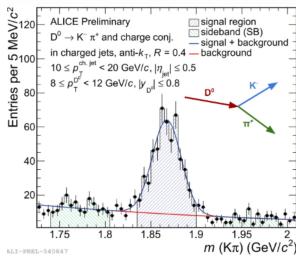
D^0 candidates were reconstructed from daughter tracks using topological and particle identification selections ($D^0 \rightarrow K^- + \pi^+$, and charge conjugates).



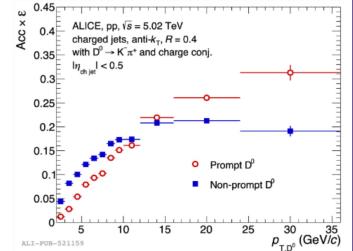
D^0 -tagged charged jets were created using the anti- k_T algorithm ($R=0.4$) for each candidate.



Invariant mass analysis was performed to remove combinatorial $K^-\pi^+$ pairs surviving the D^0 selections.



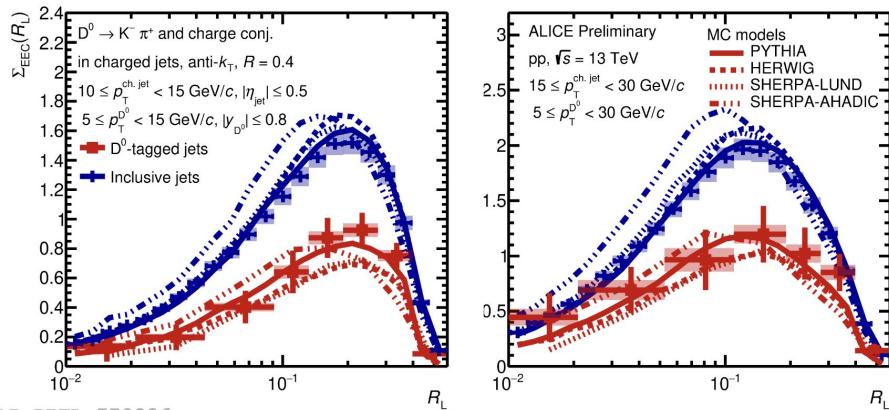
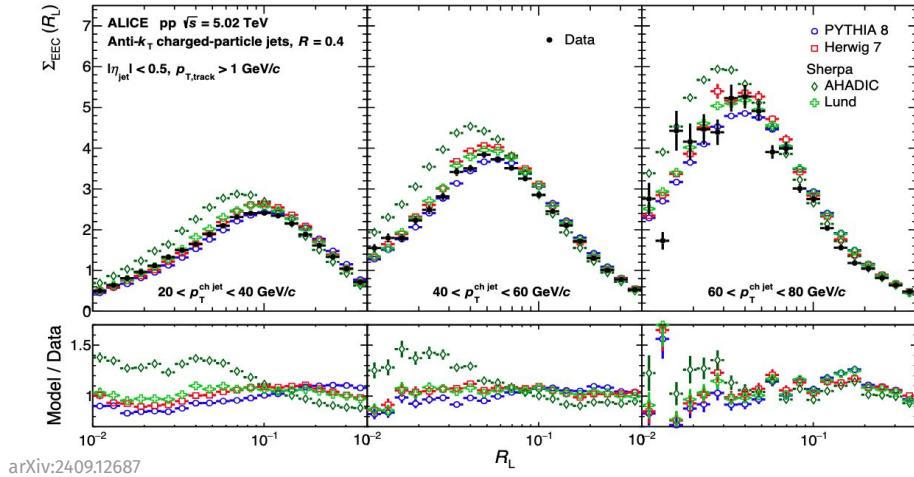
Corrected the EECs for the efficiency of D^0 -tagged jet reconstruction and removed the contribution from beauty decays.



Corrected the EECs for detector effects with a bin-by-bin correction method.

Probing hadronization with pp EECs

Lund string models: PYTHIA 8, Sherpa Lund
 Cluster models: Herwig 7, Sherpa AHADIC



Inclusive jets:

- PYTHIA & Herwig perform well,
Herwig captures peak position
- Sherpa Lund does well, AHADIC does not
- *both cluster models peak at smaller R_L*

Heavy flavor jets:

- *data favors PYTHIA's implementation*
- Herwig overpredicts inclusive jet EECs; underpredicts in HF
- Sherpa Lund underpredicts the data
- AHADIC fails to describe the peak

**Cluster hadronization for higher p_T jets,
 string-breaking models for D^0 jets?**

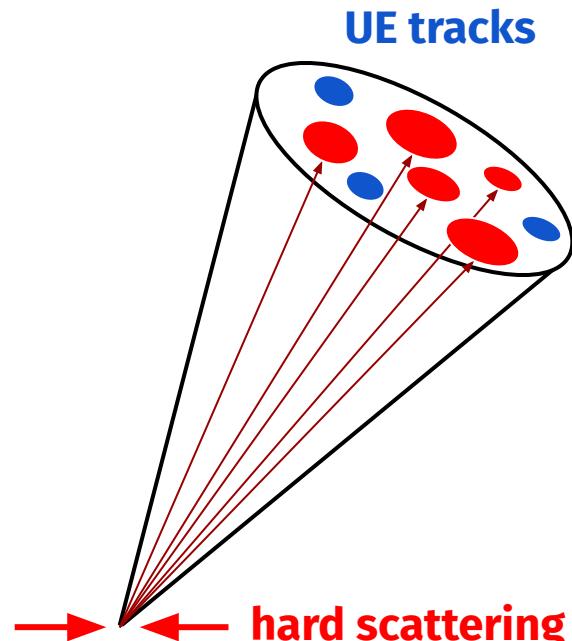
EEC measurements in more complex systems require background subtraction techniques.

1. Subtract UE energy density from the jet p_T :

$$\rho = \text{median} \left\{ \frac{p_{T,\text{jet}}^{k_T}}{A_{\text{jet}}^{k_T}} \right\} \cdot C \quad C = \frac{\sum_j A_j}{A_{\text{acc}}}$$

2. Correct the EEC distribution for combinatorial background:

- **signal-signal** (what we want!)
- **signal-background**
- **background-background**



We use the perpendicular cone to estimate the latter two contributions.

These subtraction steps are also performed for the pp baseline.

Perp. cone for combinatorial EEC background

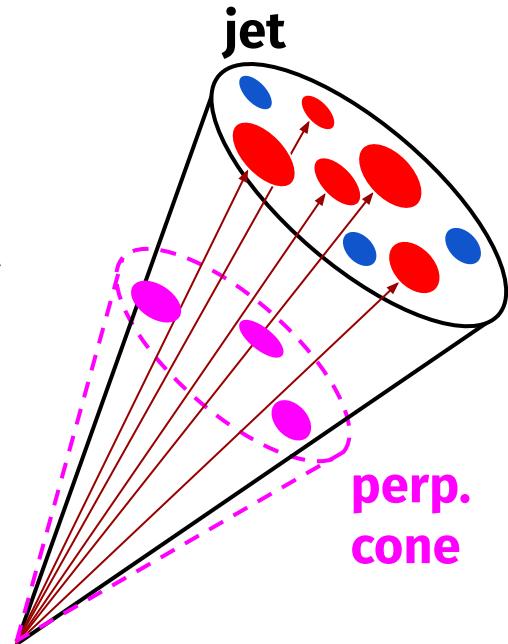
- Particles from jet: $\text{sig} + \text{bkg}$
- Particles from perp cone: bkg'
- Pairs in the combined cone:

$$(\text{sig} + \text{bkg} + \text{bkg}')(\text{sig} + \text{bkg} + \text{bkg}') = \text{sig}^* \text{sig} + 2\text{sig}^* \text{bkg}$$

$$+ \text{bkg}^* \text{bkg} + \boxed{2\text{sig}^* \text{bkg}' + 2\text{bkg}^* \text{bkg}'} + \boxed{\text{bkg}'^* \text{bkg}'}$$

jet-perp

perp-perp



Perp. cone for combinatorial EEC background

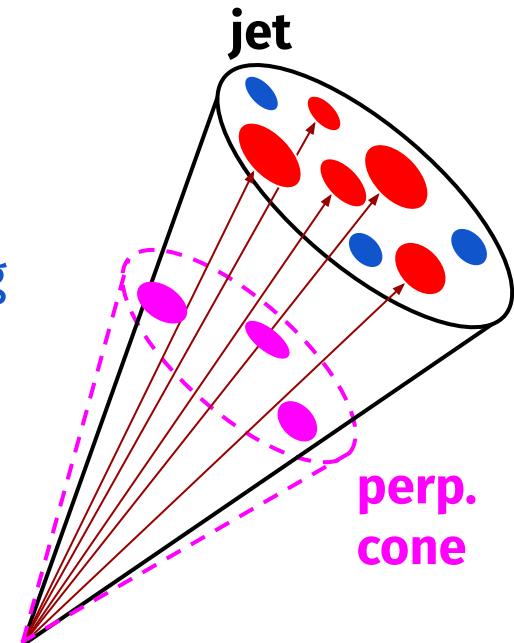
- Particles from jet: sig + bkg
- Particles from perp cone: bkg'
- Pairs in the combined cone:

$$(\text{sig} + \text{bkg} + \text{bkg}')(\text{sig} + \text{bkg} + \text{bkg}') = \text{sig}^* \text{sig} + 2\text{sig}^* \text{bkg}$$

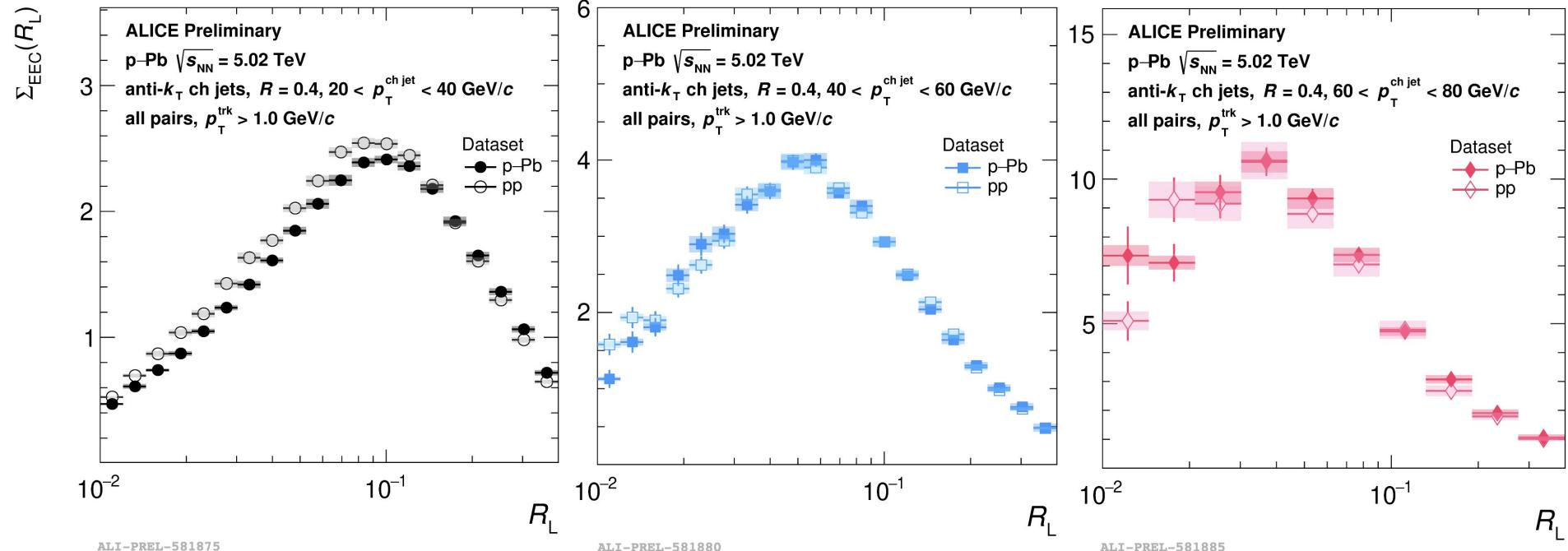
$$+ \text{bkg}^* \text{bkg} + \boxed{2\text{sig}^* \text{bkg}' + 2\text{bkg}^* \text{bkg}'} + \boxed{\text{bkg}'^* \text{bkg}'}$$

jet-perp perp-perp

- Sig-bkg pairs: jet-perp – 2 perp-perp
- Bkg-bkg pairs: perp-perp
- **Total background: jet-perp – perp-perp**

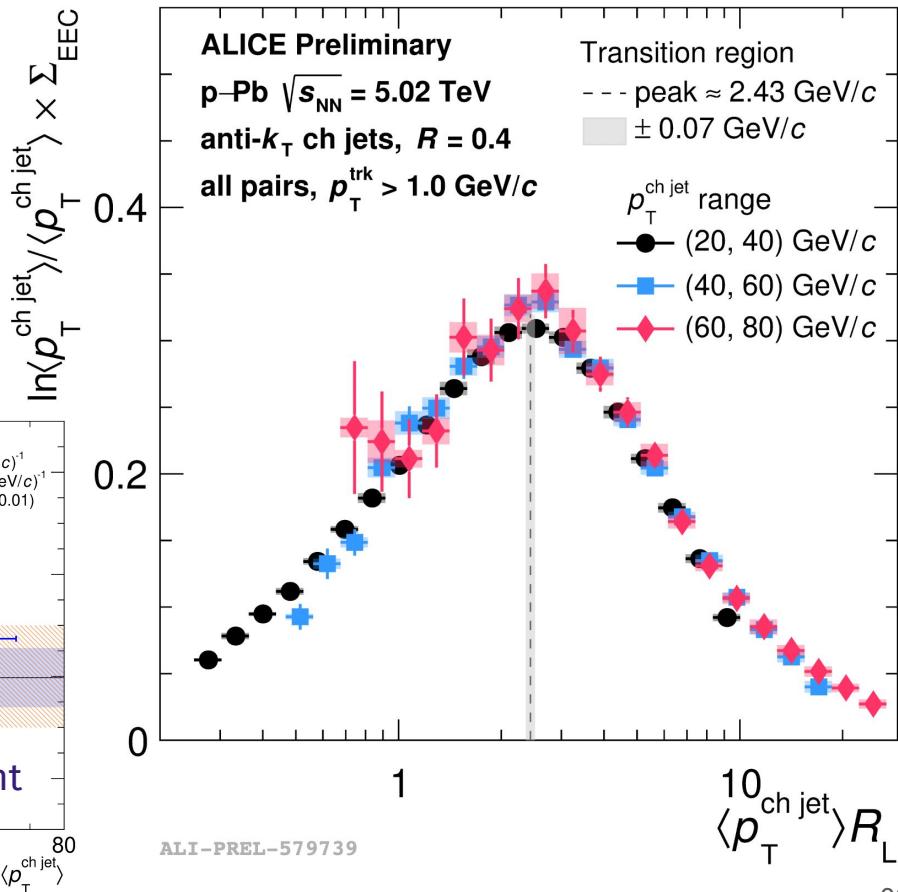
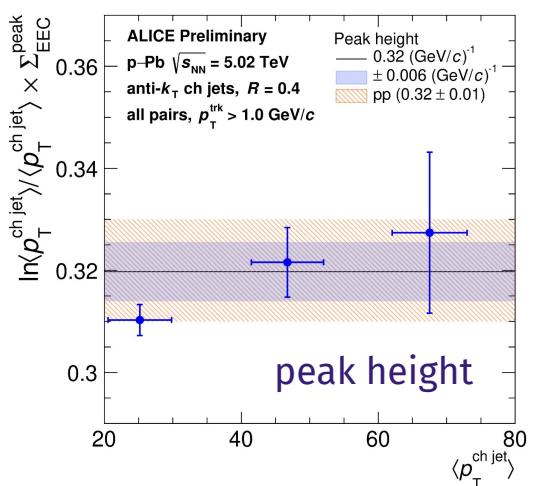
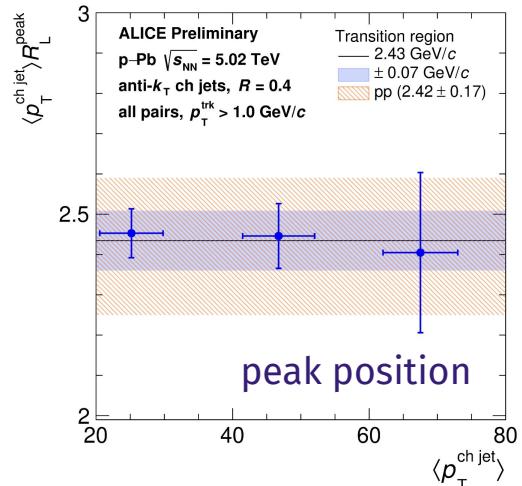


p-Pb and pp comparison

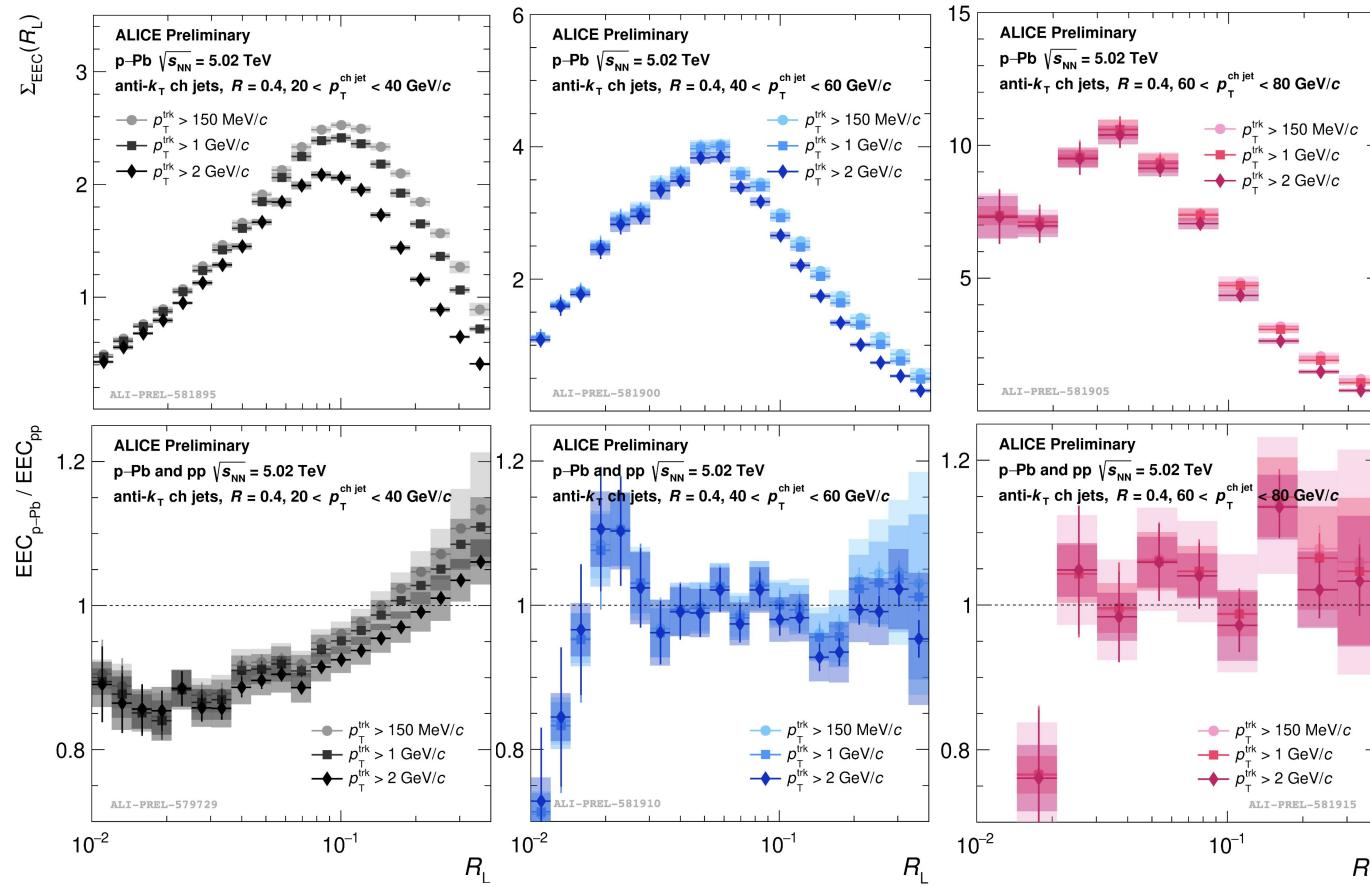


The transition region in p-Pb resembles pp.

- Universality of the EEC peak position across jet p_T and collision system.
- EEC peak height for 20-40 GeV/c jets is slightly lower than for other jets.



Varying the track cut changes the EEC behavior at large R_L .



Strong sensitivity to track p_T cut in low p_T jets!

- non-perturbative effects increase for lower jet p_T

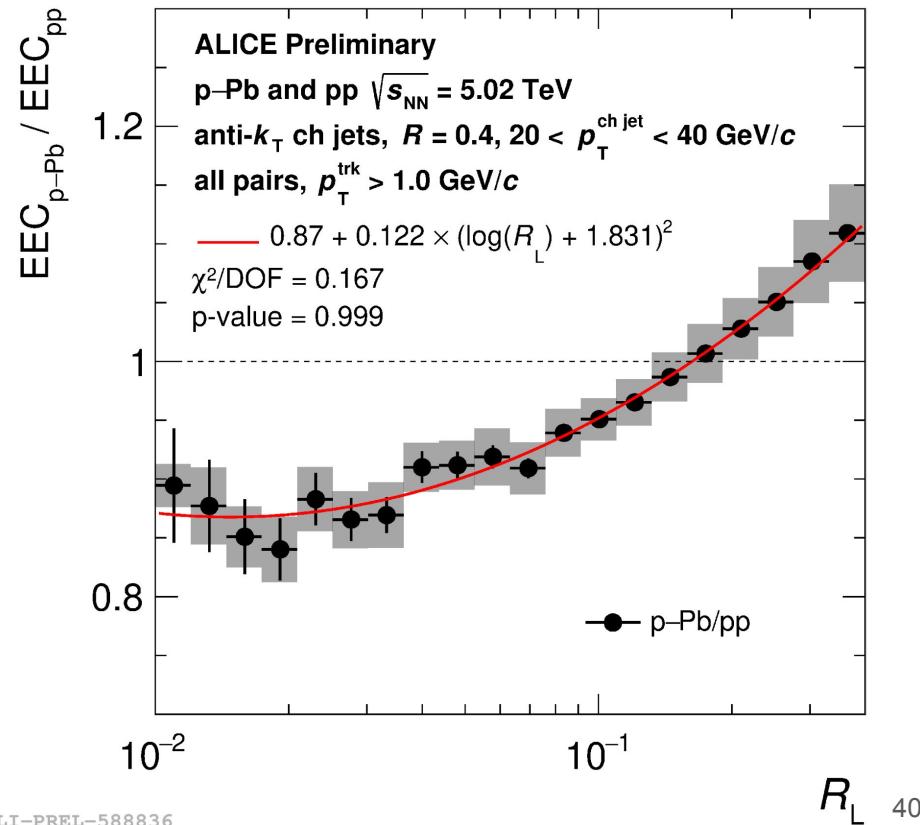
Track cut modifies the enhancement in ratio

- but not the small- R_L suppression

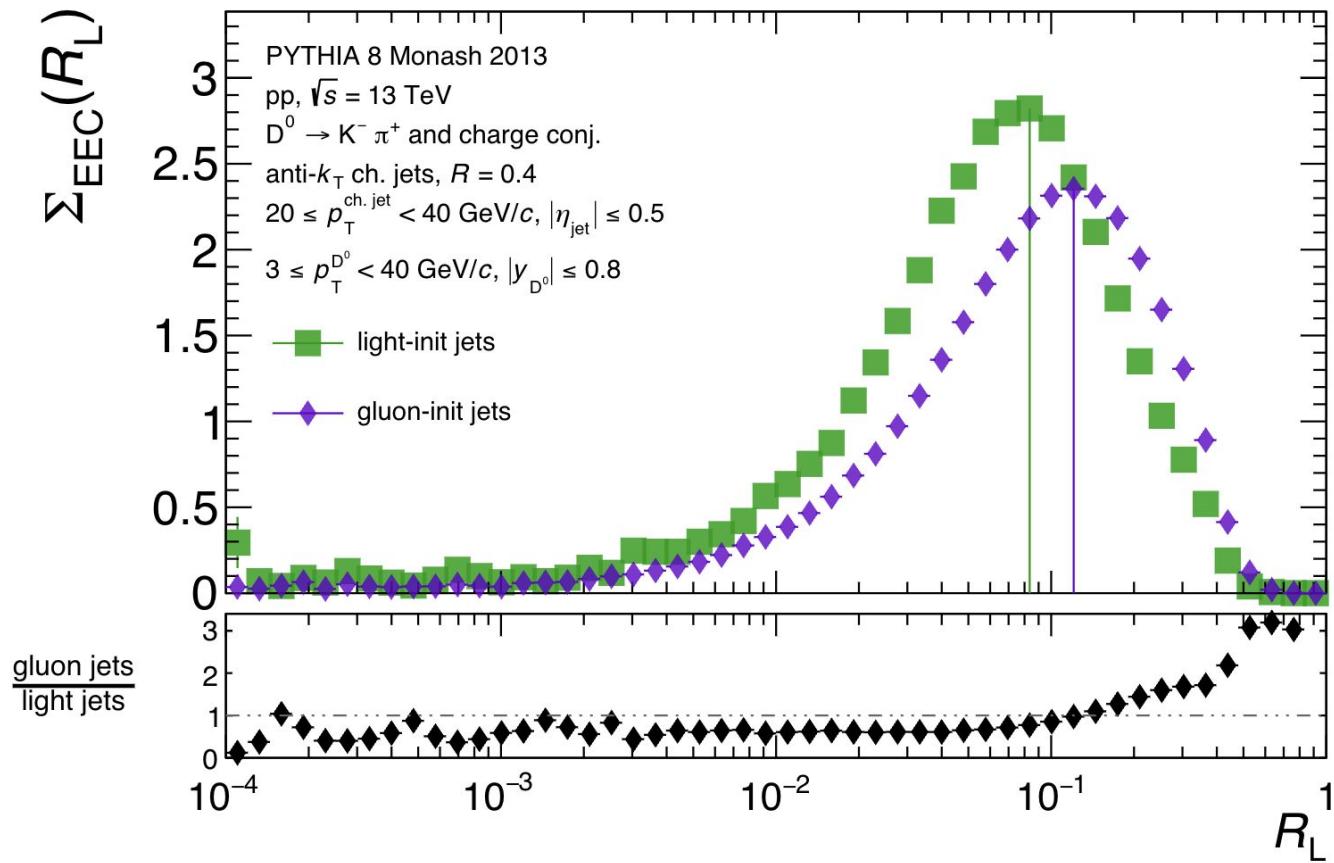
Suggests that the origin of the effect lies in softer interactions at small x!

$\log(R_L)^2$ shape of the p-Pb/pp ratio – why?

- The ratio appears to follow a $\log(R_L)^2$ scaling. Why: change in q/g ratio?



Quark-jet and gluon-jet EECs



Quark-jet and gluon-jet and D⁰-tagged jet EECs

