

Q1

Wednesday, January 27, 2021

12:48 PM

Q1.

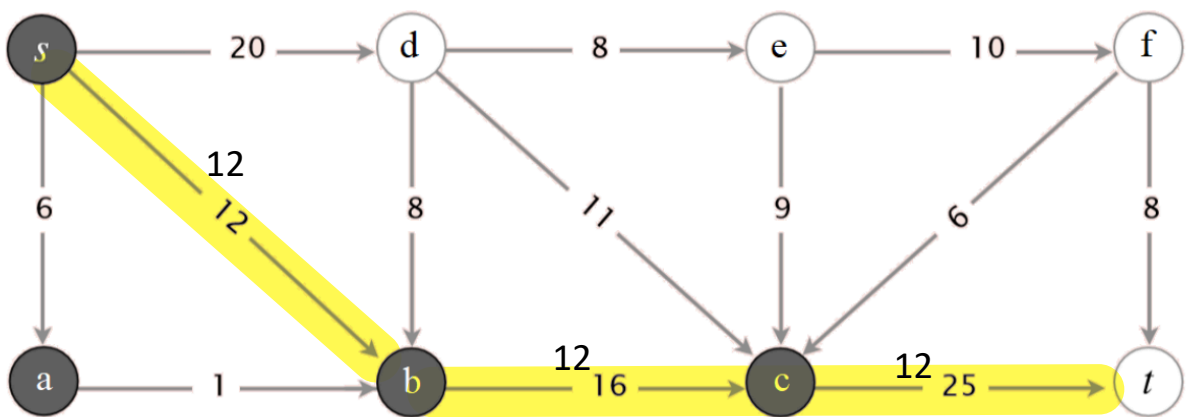
Part 1:

Step 1:

Path: s-b-c-t

Bottle Neck: 12

Max Flow: 12

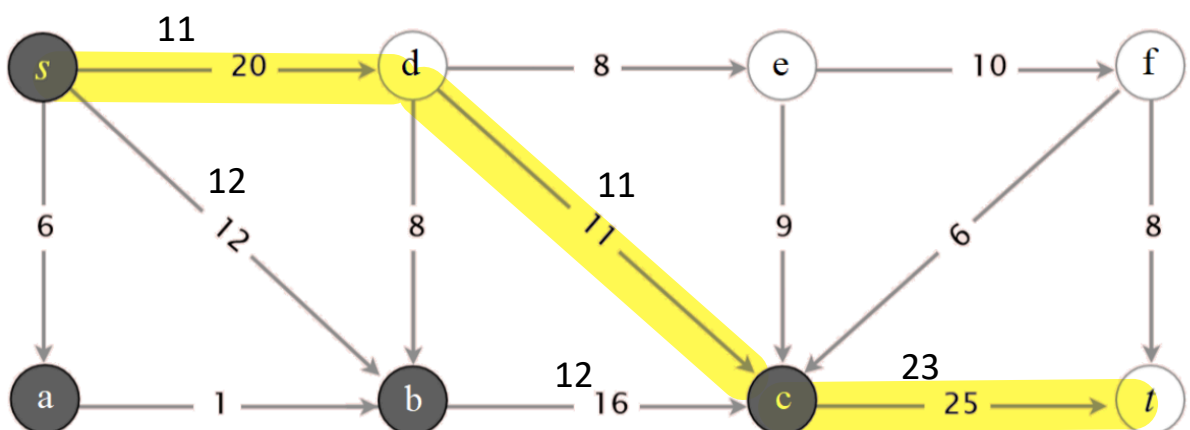


Step 2:

Path: s-d-c-t

Bottle Neck: 11

Max Flow: 23

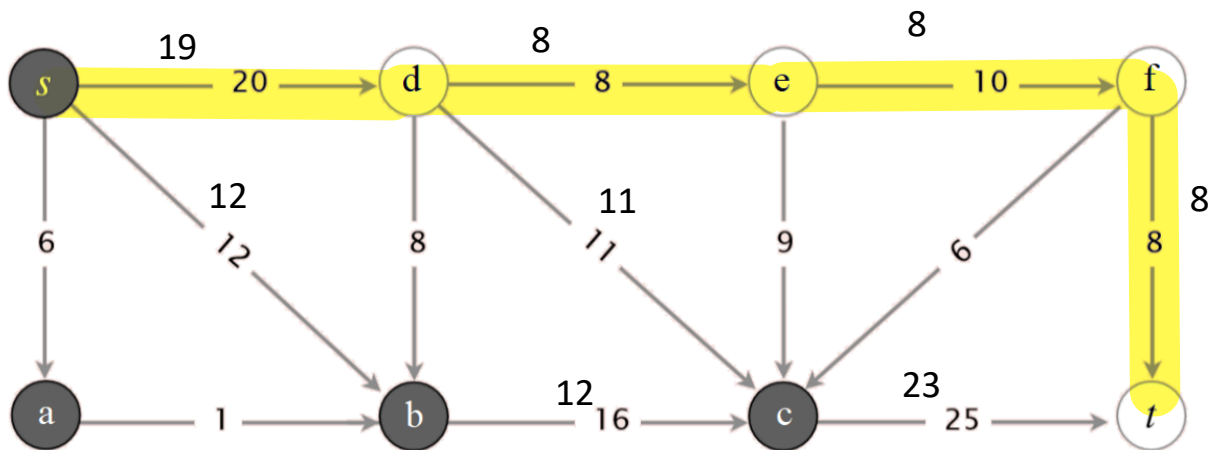


Step 3:

Path: s-d-e-f-t

Bottle Neck: 8

Max Flow: 31

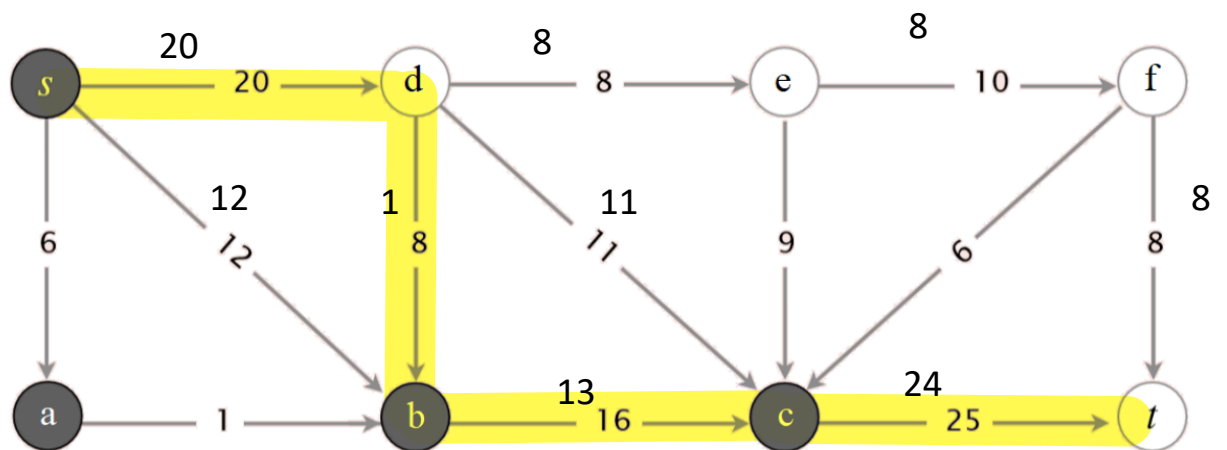


Step 4:

Path: s-d-b-c-t

Bottle Neck: 1

Max Flow: 32

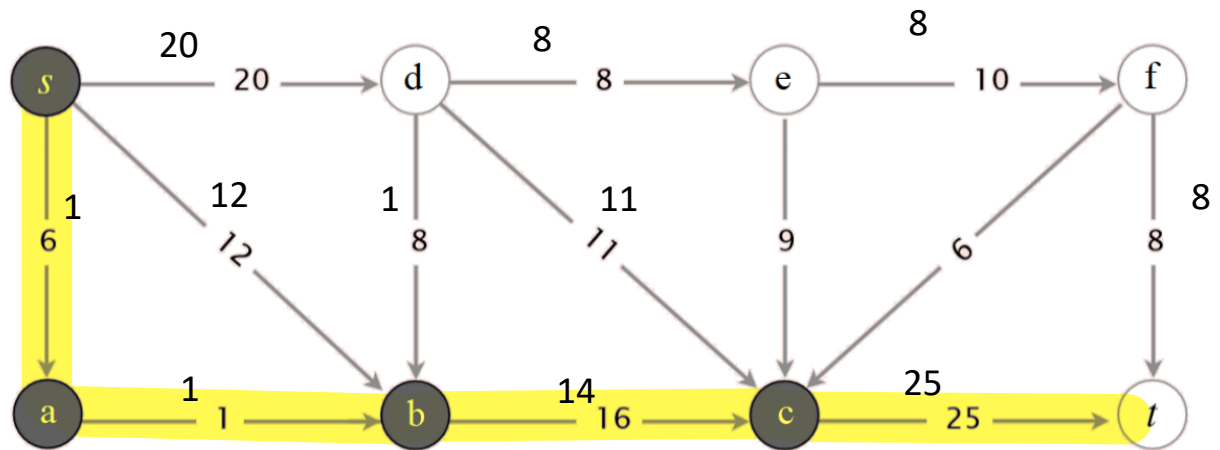


Step 5:

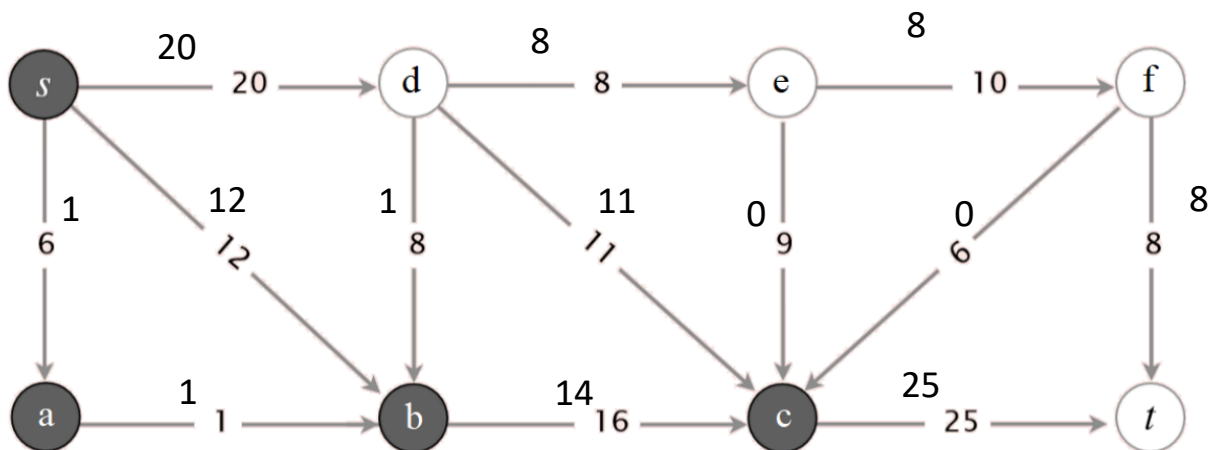
Path: s-a-b-c-t

Bottle Neck: 1

Max Flow: 33



Now I know I'm done since all the edges that go to the sink are full and I can't find any path from S to T on my residual graph, so we have the max flow possible.



Part 2:

No, $\{s, a, b, c\}$ isn't a min-cut since the capacity of the cut is $20+25 = 45$ but the maxflow value is 33 and we know that min cut = max flow.