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ELEMENTS OF CONVERTIBLE BONDS

- Convertible bond represents a combination of a straight bond and a call option on the stock of the same issuer
- Conversion ratio (CR)
 - Number of shares to which a bond can be converted
- Conversion price (CP)
 - At the time of issuance, the issuer has effectively granted the bondholder the right to purchase the common stock at the conversion price
 - Bond's par value divided by the conversion ratio

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CONVERSION PRICE: EXAMPLE 1

Calculate the conversion price of a convertible bond, newly issued at par. The par value is \$1000, the coupon rate is 10% paid semiannually, the maturity is 10 years, and the conversion ratio is 20.

- $\text{Convertible Price} = 1000/20 = \50
- This means that you can effectively buy the issuer's common stock at \$50 per share. You will do that by converting your bond.

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OPTIMAL CONVERSION STRATEGY

- It is almost always optimal to convert the instant prior to the bond's maturity date
- Would you prefer to be holding the bond or the converted shares at the time the bond matures?
 - Convert now
 - What if the stock price falls on the maturity date?
 - What if the stock price rises on the maturity date?
 - Convert at maturity
 - When would an investor convert?

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OPTIMAL CONVERSION STRATEGY

- Consider a zero-coupon convertible bond on a stock that pays no dividend. The bond has a par value of \$1000 and CR of 20.

Stock price at maturity	A's position: converts before maturity	B's position: decides to convert at maturity
\$30	\$600	\$1000
\$40	\$800	\$1000
\$50	\$1000	\$1000
\$60	\$1200	\$1200
\$70	\$1400	\$1400

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OPTIMAL CONVERSION STRATEGY

- Consider the same bond but now it pays a coupon C and the underlying stock pays a dividend D

Stock price at maturity	A's position: converts before maturity	B's position: decides to convert at maturity
\$30	$\$600 + FV(20 \times D)$	$\$1000 + FV(C)$
\$40	$\$800 + FV(20 \times D)$	$\$1000 + FV(C)$
\$50	$\$1000 + FV(20 \times D)$	$\$1000 + FV(C)$
\$60	$\$1200 + FV(20 \times D)$	$\$1200 + FV(C)$
\$70	$\$1400 + FV(20 \times D)$	$\$1400 + FV(C)$

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TRADITIONAL ANALYSIS OF CONVERTIBLES

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TRADITIONAL ANALYSIS

- Minimum value of a convertible
- Conversion premium
- Income differential: difference between the current income of a convertible and that of the common stock
- Downside risk with convertibles

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CONVERSION VALUE AND STRAIGHT VALUE

- Conversion value (CV) of a convertible bond
 - Market value of bond if conversion takes place at the current market price of the stock.
- Straight value (SV) of a convertible bond
 - Market value of a non-convertible bond with the same characteristics as the convertible bond

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CONVERSION VALUE: EXAMPLE 2

Calculate the conversion value of a bond with the following characteristics:

- Current market price of XYZ common stock = \$17
- Dividends per XYZ common stock share = \$1
- Current market price of XYZ bond = \$950
- Par value = \$1,000
- Conversion ratio = 50
- Coupon rate = 10% (annual)
- Maturity = 10 years
- Comparable non-convertible yield = 14%

- Conversion Value = $50 \times 17 = 850$

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STRAIGHT VALUE: EXAMPLE 3

Calculate the straight value of a convertible bond with the following characteristics:

- Current market price of XYZ common stock = \$17
- Dividends per XYZ common stock share = \$1
- Current market price of XYZ bond = \$950
- Par value = \$1,000
- Conversion ratio = 50
- Coupon rate = 10% (semiannual)
- Maturity = 10 years
- Comparable non-convertible yield = 14%

• **Straight Value = $PV(N=20,Y=7,PMT=50,FV=1000) = \788.1197**

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MINIMUM VALUE OF A CONVERTIBLE BOND

- The minimum value of a convertible bond is the higher of its conversion value or its straight value
 - What if the $SV > CV$ and the bond trades at the CV?
E.g. $SV = \$950$ and $CV = \$850$ and the bond trades for \$850
 - What if the $SV < CV$ and the bond trades at the SV?
E.g. $SV = \$750$ and $CV = \$850$ and the bond trades for \$750

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CONVERSION PREMIUM

- The premium effectively paid over the common stock's current market price when purchasing a convertible
 - $CPremium\ per\ share = Market\ Cprice - Common\ Stock\ Price$
- Conversion premium ratio: the conversion premium per share scaled by the common stock's price
 - $CPremium\ ratio = (Market\ CPrice - Common\ Stock\ Price) / Common\ Stock\ Price$

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CONVERSION PREMIUM: EXAMPLE 4

Consider the following convertible bond:

- Current market price of XYZ common stock = \$17
- Dividends per XYZ common stock share = \$1
- Current market price of XYZ bond = \$950
- Par value = \$1,000
- Conversion ratio = 50
- Coupon rate = 10%
- Maturity = 10 years
- Comparable non-convertible yield = 14%

What is the conversion premium ratio for this bond?

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CONVERSION PREMIUM: EXAMPLE 4

What is the conversion premium ratio for this bond?

- Market Cprice = $950/50 = 19$
- Conversion Premium = $19-17 = 2$
- Conversion Premium Ratio = $2/17 = 0.1176 = 11.76\%$

Why would an investor be willing to pay a premium?

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INCOME DIFFERENTIAL

- Conversion premium is offset over time by the difference between the bond's coupon and the stock's dividend
 - Income Diff per share = $(\text{Coupon} - \text{CR} \times \text{Dividend per share}) / \text{CR}$
- Premium payback period (or break-even time): the time it takes to recover the premium per share
 - PPP = $\text{Conversion Premium per share} / \text{Income Diff per share}$

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PREMIUM PAYBACK PERIOD: EXAMPLE 5

- Consider the following convertible bond:
- Current market price of XYZ common stock = \$17
 - Dividends per XYZ common stock share = \$1
 - Current market price of XYZ bond = \$950
 - Par value = \$1,000
 - Conversion ratio = 50
 - Coupon rate = 10%
 - Maturity = 10 years
 - Comparable non-convertible yield = 14%
- What is the premium payback period for the XYZ bond?
- Annual Coupon = 100
 - Income Diff = $100 - 50 \times 1 = 50$
 - Income Diff per share = $50 / 50 = 1$
 - PPP = $2 / 1 = 2$ years

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DOWNSIDE RISK OF A CONVERTIBLE

- SV of a convertible as the floor for its price
- Premium over SV as a measure of downside risk
 - Premium over SV = $(\text{Market Price of bond} - \text{SV}) / \text{SV}$
- How would we evaluate the upside potential of a convertible?

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DOWNSIDE RISK: EXAMPLE 6

- Consider the following convertible bond:
- Current market price of XYZ common stock = \$17
 - Dividends per XYZ common stock share = \$1
 - Current market price of XYZ bond = \$950
 - Par value = \$1,000
 - Conversion ratio = 50
 - Coupon rate = 10%
 - Maturity = 10 years
 - Comparable non-convertible yield = 14%
- What is the premium over SV for this convertible?

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PROFILE/INVESTMENT CHARACTERISTICS
OF CONVERTIBLES

- Profile: what dominates the performance of the convertible
 - Stock price?
 - Interest rates and spreads?
- Types of profiles
 - Busted convertible (or credit sensitive): stock price far below CP
 - Equity sensitive (or equity substitute): stock price above CP
 - Hybrid (or balanced or typical): between the above two cases, displaying characteristics of both a fixed income security and common stock

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PRICING CONVERTIBLES

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PRICING CONVERTIBLE BONDS

- Price of convertible bond = Straight value + Conversion Option
- What are the characteristics/elements of that option?
 - Underlying
 - Exercise Price
 - Expiration
- How does the price of a convertible bond compare to that of a non-convertible bond with the same characteristics as the convertible?
- How does the yield on a convertible bond compare to that on a non-convertible bond with the same characteristics as the convertible?

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PRICING CONVERTIBLE BONDS

- 1. Calculate the straight value of the convertible bond
- 2. Calculate the value of the call option on one share of the common stock (Black-Scholes model)
- 3. Adjust the call option value by the conversion ratio (CR)
- 4. Add together the straight value of the convertible bond and the CR-adjusted call option value

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PRICING CONVERTIBLE BONDS: EXAMPLE 7

- Consider the following information about a convertible bond. Use it to calculate the approximate fair market price for this bond.

Straight Bond Information

Face value: \$1,000
Annual coupon: \$70
Maturity: 3 years
YTM: 12%
Risk free rate: 9%

Stock Information

Stock price: \$40 per share
Standard dev.: 50%
Conversion price: \$50

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PRICING CONVERTIBLE BONDS: EXAMPLE 7 (CONT.)

- 1. Value of bond as a straight debt instrument
Price of Straight bond = $PV(N=3,Y=12,PMT=70,FV=1000)=879.9084$

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PRICING CONVERTIBLE BONDS: EXAMPLE 7
(CONT.)

2. Value of call on one share of stock using Black-Scholes model.

Call = P N(d₁) – X e^{–r t} N(d₂)

where P = price of the underlying security σ = standard deviation of P
X = strike price e = base of natural log
r = risk free interest rate t = time until maturity
N(•) = standard normal cumulative distribution function
 $d_1 = \frac{\ln(\frac{P}{X}) + (r + 0.5\sigma^2)t}{\sigma\sqrt{t}}$ and $d_2 = d_1 - \sigma\sqrt{t}$

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PRICING CONVERTIBLE BONDS: EXAMPLE 7
(CONT.)

2. Value of call on one share of stock using Black-Scholes model.

$d_1 = (\ln(40/50) + (0.09 + 0.5 \cdot 0.5^2) \cdot 3) / (0.5 \cdot 3^{0.5}) = 0.49$
 $d_2 = 0.49 - 0.5 \cdot 3^{0.5} = -0.38$

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Z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7225
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
0.7	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852
0.8	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	0.9772	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9861	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9924	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9958	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9979	0.9980	0.9981
2.9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986



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PRICING CONVERTIBLE BONDS: EXAMPLE 7
(CONT.)

2. Value of call on one share of stock using Black-Scholes model.

$$d_1 = (\ln(40/50) + (0.09 + 0.5 \cdot 0.5^2) \cdot 3) / (0.5 \cdot 3 \cdot 0.5) = 0.49$$
$$d_2 = 0.49 - 0.5 \cdot 3 \cdot 0.5 = -0.38$$

$$N(d_1) = 0.6879$$
$$N(d_2) = 1 - N(0.38) = 1 - 0.6480 = 0.3520$$

$$\text{Call} = 40 \cdot (0.6879) - 50 \cdot (e^{-0.09 \cdot 3} \cdot 0.3520) = 14.0805$$

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PRICING CONVERTIBLE BONDS: EXAMPLE 7
(CONT.)

3. Adjust the call option value by the CR

$$14.0805 \cdot 20 = 281.6104$$

4. Add together the straight value of the convertible bond and the CR-adjusted call option value

$$\text{Price of convertible bond} = 879.9084 + 281.6104 = \$1161.5188$$

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WHY BINOMIAL OPTION PRICING?

- Many convertible bonds are also callable/putable
- B-S does not work well for bond options
 - Remember why?
 - How should we value the convertible?

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PRICING CONVERTIBLE BONDS USING
BINOMIAL PRICING: EXAMPLE 8

Consider a 10% convertible bond that has \$100 face value, 5 years to maturity, CR = 20, and pays interest annually. The market perceives that 5 years from now the shares of the firm are equally likely to be worth \$4 and \$6. The term structure is assumed to be flat at 10%. Assume that investors delay conversion until after they receive their last coupon. What is the fair price for this bond?

If stock price is \$4, $CV = 20 \times 4 = \$80 \rightarrow$ No Convert!
 $\rightarrow Price = PV(N=5, Y=10, PMT=10, FV=100) = \100
If stock price is \$6, $CV = 20 \times 6 = \$120 \rightarrow$ Convert!
 $\rightarrow Price = PV(N=5, Y=10, PMT=10, FV=120) = \112.4184

 $Price\ of\ Convertible = 0.5 \times 100 + 0.5 \times 112.4184 = 106.2091$

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DETERMINANTS OF A CONVERTIBLE'S
PRICE

- The price of the underlying stock
- Expected future volatility of equity returns
- Risk free interest rates
- Issue-specific corporate/Treasury yield spread
- Expected volatility of interest rates and spreads
- Co-movement between the underlying stock price, and interest rates and spreads
- Call provisions

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