

## QUESTION 2

2a) A, C

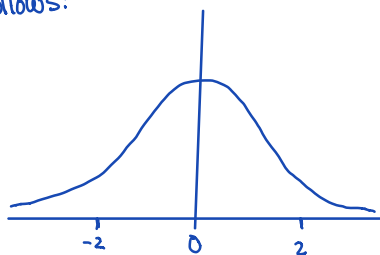
Previously, I thought the answer was only A, the Bonferroni method. This is because Bonferroni controls FWER. We also know  $FDR \leq FWER$ . So FDR is controlled too. What I missed was the LORD algorithm, which controls FDR by definition.

## QUESTION 4

4a) C, D, E

Previously, I had chosen C and D.

What I didn't realize was that E is also capable of generating proposals between -2 and 2. This is because  $\text{Normal}(0,1)$  distribution can be represented as follows:



Hence,  $\text{Normal}(0,1)$  can also generate proposals between -2 and 2.

## QUESTION 5

5b) A

Previously, I chose B. I recognized that  $\frac{a}{a+b}$  should be large because carts are more likely than baskets so the mean of the prior distribution should be large. However what I failed to recognize was that we want carts to be "much more" likely than baskets, which means that we want a much stronger prior.

$$\text{For A: } \frac{a}{a+b} = \frac{30}{30+1} \approx 0.967$$

$$\text{For B: } \frac{a}{a+b} = \frac{3}{3+1} \approx 0.75$$

Therefore, the correct answer is A because the mean of the prior is larger than in B.

5d) Even though I reached the correct answer, I did not set up Bayes' rule in the first step correctly. I should have written:

$$P(\theta_c, \theta_b, \theta_n | x_1, \dots, x_n) \propto P(\theta_c, \theta_b, \theta_n) \left[ \prod_i P(x_i | \theta) \right]$$

Instead, I wrote:

$$P(\theta_c, \theta_b, \theta_n | x_i) \propto P(\theta_c, \theta_b, \theta_n) [P(x_i | \theta)]$$

This was because I forgot to explicitly specify that this relationship was going to hold true for ALL  $x_i$ . This would introduce the multiplication of all  $x_i$  i.e.  $\prod_i P(x_i | \theta)$  instead of  $P(x_i | \theta)$ .

After this, my next steps were correct as follows:

$$\begin{aligned} P(\theta_c, \theta_b, \theta_n | x_1, \dots, x_n) &\propto P(\theta_c, \theta_b, \theta_n) \left[ \prod_i P(x_i | \theta) \right] \\ &\propto \theta_c^{K_c} \theta_b^{K_b} \theta_n^{K_n} [\theta_c^{N_c} \theta_b^{N_b} \theta_n^{N_n}] \\ &\propto \theta_c^{K_c + N_c} \theta_b^{K_b + N_b} \theta_n^{K_n + N_n} \\ &= \text{Dirichlet}(K_c + N_c, K_b + N_b, K_n + N_n) \end{aligned}$$