

# Quiz3

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**Q1 This problem is regarding writing your own code for K nearest neighbor classification.**

##a. Import the training predictors (x), training response (y) and testing (x) data sets provided with this quiz. Merge the testing (x) and training (x) row-wise (using rbind()). The training (x) is a  $100 \times 4$  data frame, the testing (x) is a  $50 \times 4$  data frame, thus the combined data should be  $150 \times 4$  where the first 50 rows are of the testing data.

```
# merge testing (x) and training(x) row-wise
df <- rbind(testX, trainX)
# display df first 6 row
head(df)
```

```
##           V1          V2          V3          V4
## 1 1.145120601 2.2125916 1.8604150 0.8423812
## 2 2.573741105 1.4693364 1.2972234 1.1342930
## 3 1.028673799 2.5158459 0.2376316 2.1784457
## 4 1.170138729 1.4522630 1.7760037 -0.2764890
## 5 2.334068305 0.4221641 1.1313296 -0.3561858
## 6 0.009083285 0.4082762 0.6617695 0.5522097
```

**b. Compute a matrix of distances amongst all observations of the combined data set of part (a). (use the function dist()).**

```
# matrix of distances amongst combined data set
dst <- as.matrix(dist(df, method="euclidean"))
# display dst
head(dst)
```

```
##           1          2          3          4          5          6          7          8
## 1 0.000000 1.730833 2.126974 1.355626 2.566585 2.463145 2.281941 2.426449
## 2 1.730833 0.000000 2.386505 2.046931 1.844739 2.906190 2.153653 2.573264
## 3 2.126974 2.386505 0.000000 3.089420 3.648371 2.882005 2.969498 1.036757
## 4 1.355626 2.046931 3.089420 0.000000 1.684575 2.089550 2.223193 3.619948
## 5 2.566585 1.844739 3.648371 1.684575 0.000000 2.539964 2.280781 4.182943
## 6 2.463145 2.906190 2.882005 2.089550 2.539964 0.000000 1.712394 3.733768
##           9          10          11          12          13          14          15          16
```

|    |   |           |          |          |           |           |          |           |          |
|----|---|-----------|----------|----------|-----------|-----------|----------|-----------|----------|
| ## | 1 | 2.2922620 | 2.627640 | 2.178753 | 3.290777  | 2.794907  | 1.881147 | 3.675566  | 2.345826 |
| ## | 2 | 0.8894629 | 1.961059 | 1.394363 | 3.619482  | 2.688433  | 1.306571 | 4.610634  | 2.327660 |
| ## | 3 | 2.9353992 | 2.433159 | 2.383991 | 4.263445  | 3.719397  | 1.768985 | 2.952590  | 1.553738 |
| ## | 4 | 2.0840846 | 2.481171 | 2.177198 | 2.548598  | 1.708553  | 2.511139 | 4.006641  | 2.679460 |
| ## | 5 | 1.1722028 | 1.973937 | 1.781700 | 2.753380  | 1.334293  | 2.588596 | 4.896067  | 2.881385 |
| ## | 6 | 2.7309901 | 1.770392 | 1.895562 | 1.582449  | 2.203400  | 2.438862 | 2.625906  | 1.634386 |
| ## |   | 17        | 18       | 19       | 20        | 21        | 22       | 23        | 24       |
| ## | 1 | 1.483272  | 2.167165 | 2.821822 | 1.9811497 | 2.604973  | 2.697453 | 2.1933948 | 2.186064 |
| ## | 2 | 2.693671  | 2.977092 | 2.274640 | 2.2355250 | 1.932530  | 2.451753 | 0.9272508 | 1.583028 |
| ## | 3 | 2.385029  | 2.271194 | 2.143689 | 3.7084778 | 3.193763  | 3.079291 | 2.2264516 | 2.622869 |
| ## | 4 | 1.561766  | 2.152941 | 3.522932 | 0.7382091 | 2.131965  | 2.850920 | 2.8247630 | 1.755087 |
| ## | 5 | 2.821944  | 2.996571 | 3.508222 | 1.3463724 | 1.388713  | 2.840136 | 2.6704208 | 1.244956 |
| ## | 6 | 1.369148  | 1.116360 | 3.013701 | 2.4980820 | 1.799241  | 2.189974 | 3.5959982 | 2.050161 |
| ## |   | 25        | 26       | 27       | 28        | 29        | 30       | 31        | 32       |
| ## | 1 | 1.876149  | 3.354727 | 2.492760 | 1.426461  | 4.643174  | 1.398835 | 3.891529  | 2.987553 |
| ## | 2 | 3.112226  | 2.714225 | 2.311210 | 2.138408  | 3.875483  | 1.181838 | 3.271154  | 2.514261 |
| ## | 3 | 2.261735  | 3.867254 | 1.371007 | 2.542518  | 5.547284  | 2.445141 | 4.806031  | 3.943820 |
| ## | 4 | 2.452785  | 4.110499 | 3.519821 | 2.337195  | 5.125360  | 2.197396 | 4.459069  | 3.686712 |
| ## | 5 | 3.704643  | 4.216585 | 3.843147 | 3.205882  | 4.975433  | 2.668305 | 4.453066  | 3.894900 |
| ## | 6 | 3.119291  | 5.457530 | 3.289713 | 2.853993  | 6.458235  | 3.508914 | 5.565268  | 5.033843 |
| ## |   | 33        | 34       | 35       | 36        | 37        | 38       | 39        | 40       |
| ## | 1 | 4.394331  | 3.566810 | 2.102227 | 2.321231  | 1.972278  | 3.192783 | 2.970438  | 3.133886 |
| ## | 2 | 3.632427  | 4.098578 | 2.384772 | 2.544909  | 1.982632  | 3.181072 | 3.161865  | 2.020205 |
| ## | 3 | 4.566768  | 3.639933 | 2.228108 | 1.245968  | 2.421220  | 3.915223 | 3.254486  | 3.244143 |
| ## | 4 | 5.261827  | 4.859587 | 3.373951 | 3.535255  | 2.995238  | 4.190580 | 3.824662  | 3.729229 |
| ## | 5 | 5.230303  | 5.746002 | 4.072308 | 4.163891  | 3.495575  | 4.723014 | 4.340202  | 3.410798 |
| ## | 6 | 6.125418  | 5.602482 | 4.054302 | 3.900335  | 3.465967  | 5.343449 | 3.760452  | 4.059687 |
| ## |   | 41        | 42       | 43       | 44        | 45        | 46       | 47        | 48       |
| ## | 1 | 1.401540  | 1.756784 | 2.674986 | 2.905392  | 3.120653  | 1.690466 | 2.852419  | 4.014796 |
| ## | 2 | 2.032689  | 1.933008 | 3.254645 | 3.110567  | 3.620121  | 2.255608 | 2.420169  | 2.520016 |
| ## | 3 | 2.328702  | 3.197821 | 2.711051 | 2.496208  | 3.844966  | 1.945187 | 3.432396  | 3.545467 |
| ## | 4 | 2.529326  | 2.345774 | 3.590689 | 4.157867  | 4.243948  | 3.010614 | 3.528733  | 4.467609 |
| ## | 5 | 3.369296  | 2.928951 | 4.458392 | 4.782363  | 5.116841  | 3.849776 | 3.769356  | 3.719859 |
| ## | 6 | 3.189759  | 3.364098 | 4.681549 | 4.387954  | 5.442710  | 3.747410 | 4.991023  | 4.550758 |
| ## |   | 49        | 50       | 51       | 52        | 53        | 54       | 55        | 56       |
| ## | 1 | 3.107708  | 3.203587 | 2.637582 | 2.556212  | 2.623490  | 2.870005 | 3.134331  | 2.861687 |
| ## | 2 | 2.666094  | 2.369405 | 2.931333 | 2.924125  | 2.053384  | 2.325459 | 3.049456  | 2.779079 |
| ## | 3 | 3.327190  | 3.480656 | 3.909404 | 3.554717  | 3.284734  | 2.122523 | 3.437111  | 4.399052 |
| ## | 4 | 4.038154  | 4.038371 | 1.485463 | 1.488005  | 2.630346  | 2.942321 | 2.620291  | 2.007600 |
| ## | 5 | 4.238895  | 4.024823 | 1.832792 | 1.853296  | 2.355326  | 2.620659 | 2.566980  | 1.852102 |
| ## | 6 | 4.533295  | 4.898658 | 2.660853 | 1.569717  | 2.453668  | 2.001779 | 3.199602  | 2.651688 |
| ## |   | 57        | 58       | 59       | 60        | 61        | 62       | 63        | 64       |
| ## | 1 | 1.4470252 | 2.359946 | 3.851538 | 1.401567  | 1.1663324 | 1.408707 | 0.9147213 | 3.028771 |
| ## | 2 | 0.8007927 | 2.346070 | 3.030767 | 1.672870  | 1.9812316 | 2.342589 | 1.7995588 | 3.431112 |
| ## | 3 | 1.9129466 | 3.838582 | 3.159103 | 2.082111  | 2.9548380 | 1.945105 | 2.4032188 | 3.621695 |
| ## | 4 | 1.8094205 | 1.362160 | 3.800165 | 2.218416  | 0.8047617 | 2.344371 | 1.9592667 | 2.181237 |
| ## | 5 | 1.9380056 | 1.309825 | 3.095502 | 2.808107  | 1.9995890 | 3.301640 | 2.9216887 | 2.484005 |
| ## | 6 | 2.5941213 | 2.106101 | 2.595905 | 2.430875  | 1.9729955 | 2.281023 | 2.8866359 | 1.430731 |
| ## |   | 65        | 66       | 67       | 68        | 69        | 70       | 71        | 72       |
| ## | 1 | 0.5356456 | 2.608542 | 3.291190 | 2.409469  | 2.2941191 | 3.127014 | 3.075390  | 2.484990 |
| ## | 2 | 1.7357617 | 2.440682 | 3.178609 | 2.772736  | 2.5030031 | 3.978021 | 2.751285  | 2.384549 |
| ## | 3 | 2.3368244 | 4.006758 | 3.511881 | 2.818198  | 3.0135170 | 2.893994 | 4.426821  | 3.138233 |
| ## | 4 | 0.8852928 | 1.418773 | 2.562341 | 2.416704  | 1.6146218 | 3.444706 | 2.168559  | 1.697179 |
| ## | 5 | 2.1877774 | 1.025682 | 2.226005 | 2.851202  | 1.8271469 | 4.270409 | 1.591059  | 1.455529 |

|      |           |          |           |          |           |          |           |          |
|------|-----------|----------|-----------|----------|-----------|----------|-----------|----------|
| ## 6 | 2.2182952 | 2.785463 | 1.566893  | 1.125988 | 0.7417557 | 1.906586 | 2.604666  | 1.244792 |
| ##   | 73        | 74       | 75        | 76       | 77        | 78       | 79        | 80       |
| ## 1 | 3.061190  | 2.508638 | 3.815767  | 1.896446 | 3.416466  | 1.900865 | 3.605274  | 3.046881 |
| ## 2 | 3.859320  | 2.996392 | 2.736775  | 2.342622 | 2.927220  | 2.354570 | 3.419461  | 1.817883 |
| ## 3 | 3.860803  | 3.344532 | 3.073759  | 2.268426 | 5.027584  | 3.527863 | 2.350869  | 3.112717 |
| ## 4 | 3.144956  | 2.821340 | 3.730576  | 2.537409 | 3.204963  | 1.160437 | 3.760161  | 2.749319 |
| ## 5 | 3.952161  | 3.441030 | 2.841948  | 3.165940 | 3.014333  | 1.869034 | 3.722848  | 1.603405 |
| ## 6 | 2.331362  | 2.458845 | 3.229742  | 2.118945 | 4.562430  | 1.936009 | 2.969730  | 2.603233 |
| ##   | 81        | 82       | 83        | 84       | 85        | 86       | 87        | 88       |
| ## 1 | 2.887950  | 1.587398 | 1.4236800 | 2.603696 | 1.402205  | 2.353662 | 2.0345447 | 2.591028 |
| ## 2 | 2.818526  | 1.943492 | 2.6046342 | 1.711038 | 1.641234  | 2.616824 | 2.4779845 | 3.086295 |
| ## 3 | 2.647361  | 1.378807 | 3.4614795 | 3.521932 | 2.089463  | 1.944062 | 2.8787973 | 2.657232 |
| ## 4 | 2.790506  | 1.970500 | 0.9187288 | 2.584870 | 1.773973  | 2.381163 | 1.6999579 | 2.707865 |
| ## 5 | 2.762146  | 2.530465 | 2.4942406 | 2.282789 | 2.284861  | 2.740092 | 2.2410748 | 3.240936 |
| ## 6 | 1.097205  | 1.696711 | 2.6256537 | 4.117844 | 1.653413  | 1.364442 | 0.8027209 | 1.098295 |
| ##   | 89        | 90       | 91        | 92       | 93        | 94       | 95        | 96       |
| ## 1 | 1.9640583 | 2.039755 | 2.928607  | 2.640792 | 2.379452  | 2.701523 | 3.509442  | 4.052405 |
| ## 2 | 2.1687403 | 1.436646 | 2.737614  | 1.829360 | 3.620918  | 2.692772 | 3.527677  | 5.419265 |
| ## 3 | 3.4018582 | 2.049455 | 3.234469  | 2.599492 | 3.428381  | 2.071470 | 3.610119  | 5.155290 |
| ## 4 | 0.7106045 | 2.112384 | 2.241382  | 2.426098 | 1.990828  | 2.694787 | 3.756281  | 3.708963 |
| ## 5 | 1.1694815 | 1.899000 | 1.859304  | 1.752969 | 3.291582  | 2.785246 | 3.910441  | 5.000020 |
| ## 6 | 2.0049451 | 1.764433 | 1.350025  | 1.904549 | 1.663804  | 1.623144 | 2.660169  | 3.298119 |
| ##   | 97        | 98       | 99        | 100      | 101       | 102      | 103       | 104      |
| ## 1 | 2.141781  | 1.956374 | 2.424221  | 2.802349 | 2.816489  | 2.608641 | 2.216702  | 2.602077 |
| ## 2 | 1.039818  | 3.480066 | 1.376567  | 2.818887 | 2.454401  | 2.926719 | 2.381782  | 1.848929 |
| ## 3 | 1.802260  | 3.273997 | 3.650251  | 1.843647 | 2.695539  | 3.245501 | 1.456203  | 3.059175 |
| ## 4 | 2.576806  | 2.225758 | 1.943389  | 2.986477 | 3.869827  | 3.752626 | 3.471507  | 3.441873 |
| ## 5 | 2.340541  | 3.718392 | 1.066276  | 3.137520 | 4.149280  | 4.506457 | 4.070093  | 3.535736 |
| ## 6 | 2.927696  | 2.422876 | 3.228199  | 1.788858 | 4.238976  | 4.910975 | 3.753051  | 4.397424 |
| ##   | 105       | 106      | 107       | 108      | 109       | 110      | 111       | 112      |
| ## 1 | 2.844138  | 2.517072 | 4.543147  | 3.108983 | 2.824147  | 1.878896 | 3.032560  | 3.326799 |
| ## 2 | 2.706081  | 1.823240 | 3.400628  | 2.954860 | 2.570146  | 1.675874 | 2.650445  | 2.973241 |
| ## 3 | 3.102578  | 3.309632 | 4.907248  | 2.923469 | 4.035565  | 3.319648 | 3.598767  | 3.352271 |
| ## 4 | 3.969241  | 3.241915 | 5.051763  | 4.308103 | 3.344996  | 2.227294 | 3.965959  | 4.402030 |
| ## 5 | 4.442739  | 3.358730 | 4.590167  | 4.758680 | 3.603213  | 2.623616 | 4.272386  | 4.735007 |
| ## 6 | 4.917388  | 4.419984 | 5.739748  | 4.987696 | 4.364916  | 3.954899 | 5.122058  | 5.398726 |
| ##   | 113       | 114      | 115       | 116      | 117       | 118      | 119       | 120      |
| ## 1 | 3.440283  | 1.537325 | 2.428781  | 1.592852 | 3.102948  | 3.493665 | 3.600922  | 2.334287 |
| ## 2 | 3.441249  | 2.186351 | 1.935726  | 2.701353 | 3.006699  | 3.660234 | 3.695589  | 1.775265 |
| ## 3 | 2.485161  | 2.386566 | 3.540113  | 3.210708 | 1.849114  | 3.815494 | 3.236064  | 2.490847 |
| ## 4 | 4.707739  | 2.559240 | 3.049824  | 2.524648 | 4.161324  | 4.667571 | 4.827603  | 3.265479 |
| ## 5 | 5.232086  | 3.391682 | 3.252458  | 3.720873 | 4.511015  | 5.327845 | 5.387494  | 3.508458 |
| ## 6 | 5.128013  | 2.982238 | 4.305481  | 3.852721 | 3.745565  | 5.657431 | 5.084769  | 4.304541 |
| ##   | 121       | 122      | 123       | 124      | 125       | 126      | 127       | 128      |
| ## 1 | 4.324586  | 2.243679 | 4.528573  | 3.728667 | 3.031215  | 1.869835 | 2.302035  | 1.099117 |
| ## 2 | 3.823354  | 3.188481 | 3.924748  | 3.970776 | 2.518975  | 2.225962 | 3.100759  | 2.124337 |
| ## 3 | 4.105328  | 3.369485 | 4.726592  | 3.488167 | 1.804422  | 2.768360 | 3.113984  | 1.641883 |
| ## 4 | 5.407843  | 3.322492 | 5.179149  | 4.983656 | 4.085294  | 2.976580 | 3.505381  | 2.336871 |
| ## 5 | 5.596037  | 4.450748 | 5.083864  | 5.695455 | 4.259634  | 3.713403 | 4.533329  | 3.377491 |
| ## 6 | 6.095809  | 4.627110 | 5.288061  | 5.868400 | 4.340878  | 3.917476 | 4.590628  | 3.194140 |
| ##   | 129       | 130      | 131       | 132      | 133       | 134      | 135       | 136      |
| ## 1 | 2.417305  | 3.052088 | 2.820471  | 3.007001 | 2.355224  | 4.124173 | 2.154494  | 2.897326 |
| ## 2 | 2.590498  | 2.452785 | 2.549316  | 3.090025 | 2.301228  | 3.731504 | 1.046293  | 3.541082 |
| ## 3 | 4.002435  | 3.042266 | 3.815664  | 3.380461 | 2.628736  | 4.319236 | 2.292568  | 3.668918 |

```
## 4 2.845892 4.069832 3.601056 4.095856 3.493975 4.945019 2.913326 3.898940
## 5 3.404386 4.243061 3.947079 4.710217 3.998961 5.078160 2.866406 4.782220
## 6 4.092928 4.840101 4.845328 5.321115 4.189919 5.180874 3.600022 4.423808
##      137      138      139      140      141      142      143      144
## 1 2.324116 1.965850 2.373227 1.800320 2.364357 5.051635 2.717067 2.363884
## 2 2.411051 1.604907 1.553853 2.452500 3.509482 4.650804 2.339193 3.259136
## 3 2.690916 2.090005 3.199527 2.543545 2.915966 5.197920 3.608039 2.633863
## 4 3.330852 3.016991 2.957166 3.042447 3.593253 5.959134 3.519752 3.360222
## 5 3.851655 3.360654 2.945417 3.941316 4.829054 6.112277 3.820357 4.336265
## 6 3.661039 3.603016 3.852359 3.902286 4.552650 6.390030 4.795975 3.198627
##      145      146      147      148      149      150
## 1 2.727842 2.869806 1.398305 4.740699 3.315390 1.7069765
## 2 2.533968 3.107744 2.030465 4.066940 3.334460 0.9226643
## 3 2.214275 2.250630 1.793976 4.323557 3.840425 2.4312603
## 4 3.933302 4.045611 2.716841 5.739484 4.362864 2.1408055
## 5 4.355430 4.645344 3.573326 5.741334 4.932964 2.2420634
## 6 4.460037 3.928557 3.479356 6.051147 5.620891 3.3800846
```

c. For each testing data observation find the  $K=15$  nearest training observation. Recall that in the distance matrix of part (b), the first 50 observations (rows) are testing and the remaining are training. To find the  $K$  observations with the least distances, use the following custom function `knearest()`. This will require you to setup a  $50 \times K$  matrix (say `near.neigh`), where each row represents each testing observation and each column has the corresponding  $K$  nearest neighbors. This will require a for loop over the number of testing observations.

```
# split test and train
# first 50 observations are testing
test <- dst[1:50,]
# remaining are training
train <- dst[51:150,]
# function knearest (find smallest among all values of x index)
knearest=function(x,k=15){
  n=length(x)
  ind=c(1:n)
  temp=cbind(ind,x)
  temp.order=temp[order(x),]
  knearest=temp.order[1:k,1]
  return(knearest)
}
# find each testing observation K nearest neighbors (15)
a1 = knearest(test[1,])
a2 = knearest(test[2,])
a3 = knearest(test[3,])
a4 = knearest(test[4,])
a5 = knearest(test[5,])
a6 = knearest(test[6,])
a7 = knearest(test[7,])
a8 = knearest(test[8,])
a9 = knearest(test[9,])
a10 = knearest(test[10,])
```

```

a11 = knearest(test[11,])
a12 = knearest(test[12,])
a13 = knearest(test[13,])
a14 = knearest(test[14,])
a15 = knearest(test[15,])
a16 = knearest(test[16,])
a17 = knearest(test[17,])
a18 = knearest(test[18,])
a19 = knearest(test[19,])
a20 = knearest(test[20,])
a21 = knearest(test[21,])
a22 = knearest(test[22,])
a23 = knearest(test[23,])
a24 = knearest(test[24,])
a25 = knearest(test[25,])
a26 = knearest(test[26,])
a27 = knearest(test[27,])
a28 = knearest(test[28,])
a29 = knearest(test[29,])
a30 = knearest(test[30,])
a31 = knearest(test[31,])
a32 = knearest(test[32,])
a33 = knearest(test[33,])
a34 = knearest(test[34,])
a35 = knearest(test[35,])
a36 = knearest(test[36,])
a37 = knearest(test[37,])
a38 = knearest(test[38,])
a39 = knearest(test[39,])
a40 = knearest(test[40,])
a41 = knearest(test[41,])
a42 = knearest(test[42,])
a43 = knearest(test[43,])
a44 = knearest(test[44,])
a45 = knearest(test[45,])
a46 = knearest(test[46,])
a47 = knearest(test[47,])
a48 = knearest(test[48,])
a49 = knearest(test[49,])
a50 = knearest(test[50,])
# merge all test observations in near.neigh
near.neigh = rbind(a1,a2,a3,a4,a5,a6,a7,a8,a9,a10,
                   a11,a12,a13,a14,a15,a16,a17,a18,a19,a20,a21,a22,
                   a23,a24,a25,a26,a27,a28,a29,a30,a31,a32,a33,a34,a35,
                   a36,a37,a38,a39,a40,a41,a42,a43,a44,a45,a46,a47,a48,a49,a50)
# display near.neigh
near.neigh

```

```

##      1  65  63 128  61   4 147  30  41  60  85  62  83  28  57
## a1   1  65  63 128  61   4 147  30  41  60  85  62  83  28  57
## a2   2  57   9 150  23  97 135  30  14  99  11  90 139  24 138
## a3   3   8  36  27  82 103  16 128  14 147  97 125 100 117  57
## a4   4  89  20  61  65  83  78   1  58  66  51  52  17  69   5

```

```

## a5  5  66  99  89   9  24  58  13  20  21  72  71  80   4  92
## a6  6  69  87  81  88  18  68  72  91  86  17  64  67  52  12
## a7  7  22  53  68  85  87  21  11  76  74  60  90  78  88  14
## a8  8  36 103   3 125  27 145  46 147 113 117  35 138 128  44
## a9  9   2  99  80  11   5  24  57  90  21  92  97 150  10  23
## a10 10  92  90  54  11  80  24  21  16  81  94  91  72  59 100
## a11 11  90  92  10  21  14  85   9  80   7  24  54  53   2  16
## a12 12  87   6  69  68  78  58  71   7  56  72  88  73  21  52
## a13 13  52  51  66  89  72   5  91  24  64  67  69  20   4  55
## a14 14  60  85  11  19  90   2  27 135  76  97 138  57  37  16
## a15 15  70  18  86 100  88  17  94  16   6  93  82  81   3  68
## a16 16 100  54  86  94  82  90  81  10  11  92  85  18  14  88
## a17 17  18  93  87  65   6  82  98  61   1  85  69   4  62  86
## a18 18  86  17   6  82  94  69 100  93  16  87  88  64  81  72
## a19 19  14  27 117  60  76  22  40  37  11 138 146  85 137 101
## a20 20  89   4  66  58  78  61  83   5  51  65  13  52  99  56
## a21 21  11  92  90  10   7  80  72  69   9  53   5  24  58  87
## a22 22   7  53  95  68  76  74  85  11  60  14  87  21  19  88
## a23 23 135   2  97 150 120  57  30 138 104  14   9 106 139 125
## a24 24  92  90  72  10   9  57   5  80  11  91  13  21  89  69
## a25 25 128  65   1  17  82  43  18   3 147  57   4  86  83  36
## a26 26  47 111  32 112 143 106 120 149 132 104  50 105 130 131
## a27 27 117 103  19   8 146  14   3 138 125 101  36  44  37 145
## a28 28 114  41  63  60  62  42  37 137  76 126 140 144  85   1
## a29 29  31  32  33 131 107 143 111  50 115 106  26  38 109 104
## a30 30 150 110 120   2  23 135  57 147 106 138  63   1 128 115
## a31 31   29 131  32 109 115 143 107  50 106  33 111 139  38 104
## a32 32 143 131 106 111 115 104  38  26  50  31 139 105 149 109
## a33 33 121  50 130 111 148 107  31 112 104  49  38 105  32  29
## a34 34 118  45 124 127 102 108 119 105  44  35 140 149  38 141
## a35 35  46 133 140 147 126 145 103 138 105 108  44  37  41 102
## a36 36   8 103 125   3  46 147 145 113 128  35  27 138 120  44
## a37 37 137  41 138 114 133 126 101  28  60  35 140  49  63  42
## a38 38 111 131 118 105 149 102 143  45  32 133 126 112 132 108
## a39 39 137  37 144 114 136 146  28  76  49  74 101  41 134  60
## a40 40 139  49 135 101  50  48 104 138  37  19  14 106 137 107
## a41 41 114  28  63  37 126 140  60 137 147  46  42  62 138  35
## a42 42 129  63  28  41 109 114 126 139  37 115  60 137 116 140
## a43 43 128  36  25 141  47 147 132 120  46  30 122 150   8 124
## a44 44 146 119  35 101 103 133 145 108 137  37  46 117 140 138
## a45 45 102 118 127 149  38 122 132  34 105 140 111 126 141 124
## a46 46 147  35 140 103 126  41 133 128 138 127 145  36  37 102
## a47 47  26 120 110 132  30 150  84 106 112 143 111 149  32  23
## a48 48  40 135  23  19  50 107  14  97 139 104   2 138 101 130
## a49 49 101 133 137  37  50 134 130  40 104 138 139 108 126 105
## a50 50 104 130 106 111 143  49  33  32 105 131 139 115 133 101

```

d. Compute the posterior probability for each testing observation. For each testing observation, recover the training class corresponding to its K nearest neighbors and compute the mean.

```
# all training class corresponding to Knn and compute the mean
pr = c()
pr[1] = mean(train[near.neigh[1,]])
pr[2] = mean(train[near.neigh[2,]])
pr[3] = mean(train[near.neigh[3,]])
pr[4] = mean(train[near.neigh[4,]])
pr[5] = mean(train[near.neigh[5,]])
pr[6] = mean(train[near.neigh[6,]])
pr[7] = mean(train[near.neigh[7,]])
pr[8] = mean(train[near.neigh[8,]])
pr[9] = mean(train[near.neigh[9,]])
pr[10] = mean(train[near.neigh[10,]])
pr[11] = mean(train[near.neigh[11,]])
pr[12] = mean(train[near.neigh[12,]])
pr[13] = mean(train[near.neigh[13,]])
pr[14] = mean(train[near.neigh[14,]])
pr[15] = mean(train[near.neigh[15,]])
pr[16] = mean(train[near.neigh[16,]])
pr[17] = mean(train[near.neigh[17,]])
pr[18] = mean(train[near.neigh[18,]])
pr[19] = mean(train[near.neigh[19,]])
pr[20] = mean(train[near.neigh[20,]])
pr[21] = mean(train[near.neigh[21,]])
pr[22] = mean(train[near.neigh[22,]])
pr[23] = mean(train[near.neigh[23,]])
pr[24] = mean(train[near.neigh[24,]])
pr[25] = mean(train[near.neigh[25,]])
pr[26] = mean(train[near.neigh[26,]])
pr[27] = mean(train[near.neigh[27,]])
pr[28] = mean(train[near.neigh[28,]])
pr[29] = mean(train[near.neigh[29,]])
pr[30] = mean(train[near.neigh[30,]])
pr[31] = mean(train[near.neigh[31,]])
pr[32] = mean(train[near.neigh[32,]])
pr[33] = mean(train[near.neigh[33,]])
pr[34] = mean(train[near.neigh[34,]])
pr[35] = mean(train[near.neigh[35,]])
pr[36] = mean(train[near.neigh[36,]])
pr[37] = mean(train[near.neigh[37,]])
pr[38] = mean(train[near.neigh[38,]])
pr[39] = mean(train[near.neigh[39,]])
pr[40] = mean(train[near.neigh[40,]])
pr[41] = mean(train[near.neigh[41,]])
pr[42] = mean(train[near.neigh[42,]])
pr[43] = mean(train[near.neigh[43,]])
pr[44] = mean(train[near.neigh[44,]])
pr[45] = mean(train[near.neigh[45,]])
pr[46] = mean(train[near.neigh[46,]])
pr[47] = mean(train[near.neigh[47,]])
```

```

pr[48] = mean(train[near.neigh[48,]])
pr[49] = mean(train[near.neigh[49,]])
pr[50] = mean(train[near.neigh[50,]])
# merge all posterior for testing observation in pr
pr = rbind(pr[1],pr[2],pr[3],pr[4],pr[5],pr[6],pr[7],pr[8],pr[9],pr[10],
           pr[11],pr[12],pr[13],pr[14],pr[15],pr[16],pr[17],pr[18],pr[19],
           pr[20],pr[21],pr[22],pr[23],pr[24],pr[25],pr[26],pr[27],pr[28],
           pr[29],pr[30],pr[31],pr[32],pr[33],pr[34],pr[35],pr[36],pr[37],
           pr[38],pr[39],pr[40],pr[41],pr[42],pr[43],pr[44],pr[45],pr[46],
           pr[47],pr[48],pr[49],pr[50])
# display pr
pr

```

```

##           [,1]
## [1,] 2.662567
## [2,] 2.666125
## [3,] 2.560631
## [4,] 2.671795
## [5,] 2.969605
## [6,] 2.595357
## [7,] 2.248945
## [8,] 2.579092
## [9,] 2.848998
## [10,] 2.506007
## [11,] 2.568089
## [12,] 2.707201
## [13,] 2.509286
## [14,] 2.365167
## [15,] 2.509103
## [16,] 2.465648
## [17,] 2.953313
## [18,] 2.557034
## [19,] 2.630779
## [20,] 2.486294
## [21,] 2.665551
## [22,] 2.390446
## [23,] 2.868036
## [24,] 2.738793
## [25,] 2.733766
## [26,] 2.430746
## [27,] 2.916391
## [28,] 2.479589
## [29,] 2.392444
## [30,] 2.692789
## [31,] 2.410597
## [32,] 2.443445
## [33,] 2.391377
## [34,] 2.525182
## [35,] 2.502001
## [36,] 2.632386
## [37,] 2.464069
## [38,] 2.520722
## [39,] 2.667335

```



```
## [40,] 2.319404
## [41,] 2.494658
## [42,] 2.487184
## [43,] 2.693549
## [44,] 2.783705
## [45,] 2.505121
## [46,] 2.471228
## [47,] 2.558101
## [48,] 2.260587
## [49,] 2.410826
## [50,] 2.404711
```

e. Create a prediction variable `pred` with values 0, 1. Compare this prediction vector to the `ytest` variable to compute the total error in your classification.

```
# create prediction variable
pred <- rep(0, length(pr))
pred[pr > 2.5] <- 1
# display pred
pred
```

```
## [1] 1 1 1 1 1 1 0 1 1 1 1 1 1 0 1 0 1 1 1 0 1 0 1 1 1 0 1 0 0 1 0 0 0 1 1 1 0 1
## [39] 1 0 0 0 1 1 1 0 1 0 0 0
```

[illegible]

```
## ytest
##    0    1
## 50  50
```

```
# K = 3
# predictions data in the knn
pred.knn = knn(test, train, pred, k = 3)
# confusing matrix
table(pred.knn, ytest)
```

```
##          ytest
## pred.knn  0  1
##          0 11 24
##          1 39 26
```

```
# fraction of days for which the prediction was correct
mean(pred.knn == ytest)
```

```
## [1] 0.37
```

```
# training error rate
mean(pred.knn != ytest)
```

```
## [1] 0.63
```

Percentage of current KNN [k = 3] predictions

Training correct prediction:

$\frac{(11+26)}{(11+24+39+26)} = 0.37$ ; **37.00 %**

Training error rate:

$1 - 0.37 = 0.63$ ; **63.00 %**

```
# K = 7
# predictions data in the knn
pred.knn = knn(test, train, pred, k = 7)
# confusing matrix
table(pred.knn, ytest)
```

```
##          ytest
## pred.knn  0  1
##          0  5 27
##          1 45 23
```

```
# fraction of days for which the prediction was correct
mean(pred.knn == ytest)
```

```
## [1] 0.28
```

```
# training error rate
mean(pred.knn != ytest)
```

```
## [1] 0.72
```

Percentage of current KNN [k = 7] predictions

Training correct prediction:

$\frac{(4+19)}{(4+31+46+19)} = 0.23$ ; **23.00 %**

Training error rate:

$1 - 0.23 = 0.77$ ; **77.00 %**

```
# K = 10
# predictions data in the knn
pred.knn = knn(test, train, pred, k = 10)
# confusing matrix
table(pred.knn, ytest)
```

```
##          ytest
## pred.knn  0  1
##          0  5 29
##          1 45 21
```

```
# fraction of days for which the prediction was correct  
mean(pred.knn == ytest)
```

```
## [1] 0.26
```

```
# training error rate  
mean(pred.knn != ytest)
```

```
## [1] 0.74
```

Percentage of current KNN [k = 10] predictions

Training correct prediction:

$\frac{(6+21)}{(6+29+44+21)} = 0.27$ ; **27.00 %**

Training error rate:

$1 - 0.27 = 0.73$ ; **73.00 %**

Since the test error rate is high, this classifier is judged to be not suitable for the model.