

### A. Mth Method

*Mth* treats each sample as a capture (or recapture). It predicts the total number of bugs based on Equation 1, 2 [1]. Table I shows the meaning of each variable, how to compute its value based on the bug arrival lookup table in Table II.

$$N = \frac{D}{C} + \frac{f_1}{C} \gamma^2, C = 1 - \frac{f_1}{\sum_{k=1}^t k f_k} \quad (1)$$

$$\gamma^2 = \max\left\{\frac{\frac{D}{C} \sum_k k(k-1) f_k}{2 \sum_{j < k} n_j n_k} - 1, 0\right\} \quad (2)$$

TABLE I: Example of bug arrival lookup table

	#1	#2	#3	#4	#5	#6	#7	#8	#9	#10	#11	#12	...
Sample #1	1	1	1	0	0	0	0	0	0	0	0	0	
Sample #2	0	0	1	1	0	0	0	0	0	0	0	0	
Sample #3	0	0	1	0	1	0	0	0	0	0	0	0	
Sample #4	0	0	0	1	1	1	1	1	0	0	0	0	
Sample #5	0	0	1	1	0	0	0	1	1	1	1	0	
Sample #6	1	0	1	0	1	0	0	0	0	0	0	1	
Sample #7	...												

TABLE II: Variables meaning and computation

Var.	Meaning	Computation based on bug arrival lookup table	Example value
N	Predicted total number of bugs		predicted value: 24
D	Actual number of bugs captured so far	Number of columns	12
t	Number of captures	Number of rows	6
$n_j$	Number of bugs detected in each capture	Number of cells with 1 in row $j$	3, 2, 2, 5, 6, 4
$f_k$	Number of bugs captured exactly $k$ times in all captures, i.e., $\sum f_i = D$	Count the number of cells with 1 in each column, and denote as $r_i$ ; $f_k$ is the number of $r_i$ with value $k$	1=7, 2=2, 3=2, 5=1
$Z_i$	Number of bugs detected only in the $i_{th}$ capture, i.e., $\sum Z_i = f_1$	For row $i$ , count the number of column which only have 1 in row $i$	1=1, 2=0, 3=0, 4=2, 5=3, 6=1
$n_1$	Number of bugs in the capture (e.g., 1-3 sample)	For row 1 to 3, count the number of columns with 1	5
$n_2$	Number of bugs in the recapture (e.g., 4-6 sample)	For row 4 to 6, count the number of columns with 1	11
$m$	Number of bugs contained in both captures	The number of columns which have 1 in both row 1-3 and row 4-5	4

### B. MhJK Method

*MhJK* method is similar with *Mth* method, except its equation for estimating the total number of bugs in Equation 3 [2] (with the value assignments in Table II).

$$N = D + \frac{t-1}{t} f_1 \quad (3)$$

Note that, the *MhJK* estimation has three other expressions. We use all four expressions, and choose the right estimator through hypothesis testing as suggested in [2]. Please refer to [2] for more details.

### C. MhCH Method

*MhCH* method is similar with *Mth* method, except its equation for estimating the total number of bugs in Equation 4, 5 [3] (with the value assignments in Table II).

$$N = D + \frac{f_1^2}{2f_2} \quad (4)$$

or

$$N = D + \frac{\left[\frac{f_1^2}{2f_2}\right] \left[1 - \frac{2f_2}{tf_1}\right]}{1 - \frac{3f_3}{tf_2}}, \text{ if } tf_1 > 2f_2, tf_2 > 3f_3, 3f_1f_2 > 2f_2^2 \quad (5)$$

### D. MtCH Method

*MtCH* method is also similar with *Mth* method, except its equation for estimating the total number of bugs in Equation 6 [4] (with the value assignments in Table II).

$$N = D + \frac{\sum_{i=1}^t \sum_{j=i+1}^t Z_i Z_j}{f_2 + 1} \quad (6)$$

### E. M0 Method

Method *M0* treats the first half samples as the capture, and treats the second half samples as the recapture. The total number of bugs is estimated as Equation 7 [5] (with the value assignments in Table II). Note that, we simply treat  $n_1 \times n_2$  as the total number when  $m$  is 0.

$$N = \frac{n_1 \times n_2}{m} \quad (7)$$

## REFERENCES

- [1] S.-M. Lee, "Estimating population size for capture-recapture data when capture probabilities vary by time, behavior and individual animal," *Communications in Statistics-Simulation and Computation*, vol. 25, no. 2, pp. 431–457, 1996.
- [2] K. P. Burnham and W. S. Overton, "Estimation of the size of a closed population when capture probabilities vary among animals," *Biometrika*, vol. 65, no. 3, pp. 625–633, 1978.
- [3] A. Chao, "Estimating animal abundance with capture frequency data," *The Journal of Wildlife Management*, pp. 295–300, 1988.
- [4] —, "Estimating the population size for capture-recapture data with unequal catchability," *Biometrics*, pp. 783–791, 1987.
- [5] P. S. Laplace, "Sur les naissances, les mariages et les morts," *Histoire de l'Academie Royale des Sciences*, p. 693, 1783.