Active Accuracy Estimation on Large Datasets

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- Setup
 - A classifier $C(\mathbf{x})$ deployed on
 - A large unlabeled dataset D
- Estimate true accuracy μ of $C(\mathbf{x})$ on D
- Given
 - A labeled set L : small or unrepresentative of D
 - ullet Measured accuracy on labeled set eq True accuracy on data
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 - existing work assumes that $C(\mathbf{x})$ is probabilistic and can output well-calibrated $\Pr(y|\mathbf{x})$ values.
- Provide interactive speed to user in loop even when D is very large
 - even a single sequential scan on D may not be practical.
 - D can be accessed only via an index.
- Require user to label as few additional instances as possible
 - Similar to active learning but different ...
 - Active learning usually used in the context of learning classifiers
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Outline

Problem setup

The problem has two aspects

- Accuracy estimation (What this talk is about)
 - Given a fixed L what is the best estimator of μ ?
 - How to do this scalably on large D?
- 2 Instance selection (Not covered in this talk, details in paper)
 - Selecting instances from D to be labeled by a human and adding to L. Performed in a loop.

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- A classical solution : stratified estimate
 - Stratify L and D into B buckets $(L_1, D_1), \ldots, (L_B, D_B)$
 - Measure accuracy $\hat{\mu}_b$ of L_b in each bucket b
 - Estimate weight w_b as fraction of D instances in bucket $b = \frac{|D_b|}{|D|}$
 - Stratified estimate $\hat{\mu}_S = \sum_b w_b \hat{\mu}_b$

- Selecting a stratification strategy that puts instances with same
- **2** Finding w_b scalably when D is large \Rightarrow cannot stratify whole of D.

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Two challenges

- Selecting a stratification strategy that puts instances with same error in the same bucket
- **2** Finding w_b scalably when D is large \Rightarrow cannot stratify whole of D.

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 - Bennett and Carvalho & Druck and McCallum
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- Our Proposal:
 - F(x, C): A feature representation of the input x and the result of deploying C on x
 - Learn a hash function h on features using the labeled data L
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- Our approach: Learn one hyperplane at a time

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 - Distinct hyperplanes: Re-weight instances as in boosting

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- Proposal sampling : $\hat{\mu}_{S_q} = \frac{1}{N} \left(\frac{1}{m} \sum_{i \in Q} \frac{\hat{\mu}_{h(\mathbf{f}_i)}}{q(i)} \right)$
- Optimal $q(i) \propto \hat{\mu}_{h(\mathbf{f}_i)}$: impossible without assigning each $i \in D$
- Allowed q(i) are the ones which assign same probability to all
- Claim : Under above restriction, $q_u \propto \sqrt{\sum_b \hat{\mu}_b^2 p(b|u)}$ where p(b|u) is the fraction of $i \in D_u$ with $h(\mathbf{f}_i) = b$
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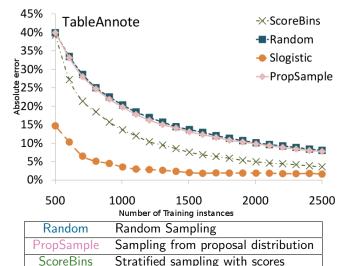
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Summary of datasets used

- TableAnnote: Annotate columns of Web tables to type nodes of an ontology
- **Spam** : Classifying web-pages as spam or not
- **DNA**: Binary DNA classification task
- HomeGround, HomePredicted: Dataset of (entity, web-page) instances and decide if web-page was a homepage for the entity

| Dataset | # | Size | | Accuracy (%) | |
|---------------|----------|---------|-----------------|--------------|---------|
| | Features | Seed(L) | Unlabeled (D) | Seed(L) | True(D) |
| TableAnnote | 42 | 541 | 11,954,983 | 56.4 | 16.5 |
| Spam | 1000 | 5000 | 350,000 | 86.4 | 93.2 |
| DNA | 800 | 100,000 | 50,000,000 | 72.2 | 77.9 |
| HomeGround | 66 | 514 | 1060 | 50.4 | 32.8 |
| HomePredicted | 66 | 8658 | 13,951,053 | 83.2 | 93.9 |

Comparison of estimation strategies on the TableAnnote dataset



Comparison of estimation strategies on remaining datasets

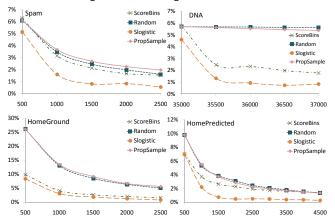
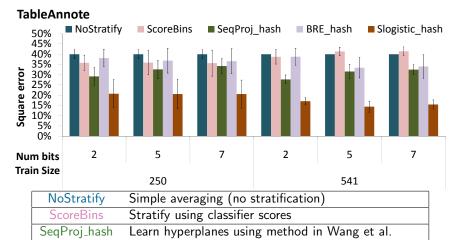


Figure: Absolute error (on the Y axis) of different estimation algorithms against increasing number of labeled instances (on the X axis)

Learn hyperplanes using method in Kulis and Darrell

Results

Comparison of different stratification methods on the TableAnnote dataset



BRE_hash

Comparison of different stratification methods on remaining datasets

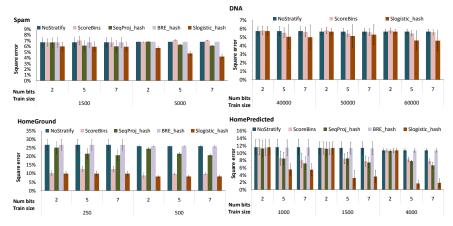


Figure: Error of different stratification methods against increasing training sizes and for different number of bits

Comparison of methods of sampling from indexed data for estimating bucket weights

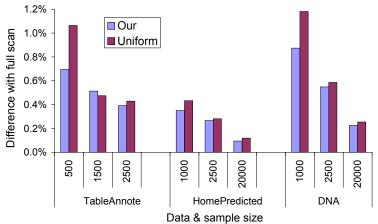


Figure: Comparing methods of sampling from indexed data for estimating bucket weights

- Addressed the challenge of calibrating a classifier's accuracy on large unlabeled datasets given small amounts of labeled data and a human labeler
- Proposed a stratified sampling-based method for accuracy estimation that provides better estimates than simple averaging & better selection of instances for labeling than random sampling
- 3 Between 15% and 62% relative reduction in error achieved compared to existing approaches
- Algorithm made scalable by proposing optimal sampling strategies for accessing indexed unlabeled data directly
- **6** Close to optimal performance while reading three orders of magnitude fewer instances on large datasets

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