Active Accuracy Estimation on Large Datasets

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- Setup
 - A classifier $C(\mathbf{x})$ deployed on
 - A large unlabeled dataset D
- Estimate true accuracy μ of $C(\mathbf{x})$ on D
- Given
 - A labeled set L : small or unrepresentative of D
 - ullet Measured accuracy on labeled set eq True accuracy on data
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 - existing work assumes that $C(\mathbf{x})$ is probabilistic and can output well-calibrated $\Pr(y|\mathbf{x})$ values.
- Provide interactive speed to user in loop even when D is very large
 - even a single sequential scan on D may not be practical.
 - D can be accessed only via an index.
- Require user to label as few additional instances as possible
 - Similar to active learning but different ...
 - Active learning usually used in the context of learning classifiers
 - Task of learning classifiers different from evaluating given classifier

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Outline

Problem setup

The problem has two aspects

- Accuracy estimation (What this talk is about)
 - Given a fixed L what is the best estimator of μ ?
 - How to do this scalably on large D?
- 2 Instance selection (Not covered in this talk, details in paper)
 - Selecting instances from D to be labeled by a human and adding to L. Performed in a loop.

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- A classical solution : stratified estimate
 - Stratify L and D into B buckets $(L_1, D_1), \ldots, (L_B, D_B)$
 - Measure accuracy $\hat{\mu}_b$ of L_b in each bucket b
 - Estimate weight w_b as fraction of D instances in bucket $b = \frac{|D_b|}{|D|}$
 - Stratified estimate $\hat{\mu}_S = \sum_b w_b \hat{\mu}_b$

- Selecting a stratification strategy that puts instances with same
- **2** Finding w_b scalably when D is large \Rightarrow cannot stratify whole of D.

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Two challenges

- Selecting a stratification strategy that puts instances with same error in the same bucket
- **2** Finding w_b scalably when D is large \Rightarrow cannot stratify whole of D.

Stratification strategy (h)

- **Existing approach** : Bin $Pr(y|\mathbf{x})$ values assumed to be provided by a classifier
 - Bennett and Carvalho and Druck and McCallum
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- Our Proposal:
 - F(x, C): A feature representation of the input x and the result of deploying C on x
 - Learn a hash function h on features using the labeled data L
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 - Kulis and Darrell specify hash function in kernel form & params are
 - Wang et al. propose to sequentially update one hyperplane at a
- Our approach: Learn one hyperplane at a time

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 - Distinct hyperplanes: Re-weight instances as in boosting

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- Proposal sampling : $\hat{\mu}_{S_q} = \frac{1}{N} \left(\frac{1}{m} \sum_{i \in Q} \frac{\hat{\mu}_{h(\mathbf{f}_i)}}{q(i)} \right)$
- Optimal $q(i) \propto \hat{\mu}_{h(\mathbf{f}_i)}$: impossible without assigning each $i \in D$
- Allowed q(i) are the ones which assign same probability to all
- Claim : Under above restriction, $q_u \propto \sqrt{\sum_b \hat{\mu}_b^2 p(b|u)}$ where p(b|u) is the fraction of $i \in D_u$ with $h(\mathbf{f}_i) = b$
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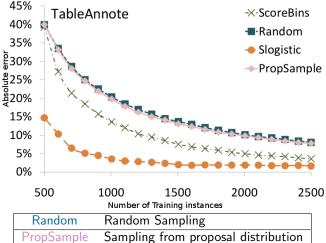
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Summary of datasets used

- TableAnnote: Annotate columns of Web tables to type nodes of an ontology
- **Spam**: Classifying web-pages as spam or not
- **DNA**: Binary DNA classification task
- HomeGround, HomePredicted : Dataset of (entity, web-page) instances and decide if web-page was a homepage for the entity

Dataset	#	Size		Accuracy (%)	
	Features	Seed(L)	Unlabeled (D)	Seed(L)	True(D)
TableAnnote	42	541	11,954,983	56.4	16.5
Spam	1000	5000	350,000	86.4	93.2
DNA	800	100,000	50,000,000	72.2	77.9
HomeGround	66	514	1060	50.4	32.8
HomePredicted	66	8658	13,951,053	83.2	93.9

Comparison of estimation strategies on the TableAnnote dataset



Comparison of estimation strategies on remaining datasets

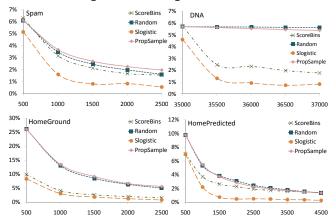
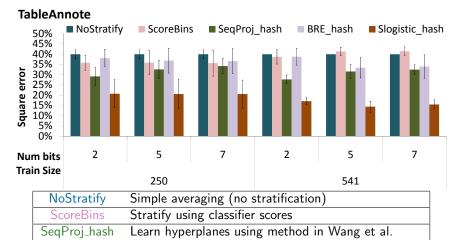


Figure: Absolute error (on the Y axis) of different estimation algorithms against increasing number of labeled instances (on the X axis)

Learn hyperplanes using method in Kulis and Darrell

Results

Comparison of different stratification methods on the TableAnnote dataset



BRE_hash

Comparison of different stratification methods on remaining datasets

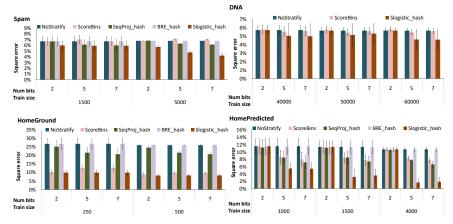


Figure: Error of different stratification methods against increasing training sizes and for different number of bits

Comparison of methods of sampling from indexed data for estimating bucket weights

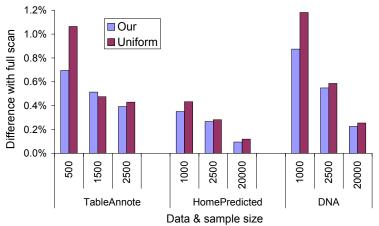


Figure: Comparing methods of sampling from indexed data for estimating bucket weights

- Addressed the challenge of calibrating a classifier's accuracy on large unlabeled datasets given small amounts of labeled data and a human labeler
- Proposed a stratified sampling-based method for accuracy estimation that provides better estimates than simple averaging & better selection of instances for labeling than random sampling
- 3 Between 15% and 62% relative reduction in error achieved compared to existing approaches
- Algorithm made scalable by proposing optimal sampling strategies for accessing indexed unlabeled data directly
- **6** Close to optimal performance while reading three orders of magnitude fewer instances on large datasets

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