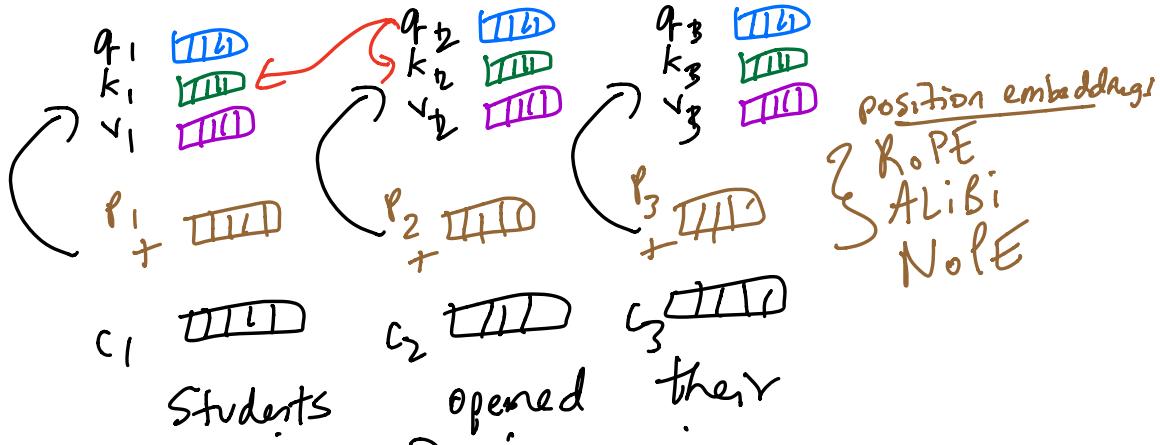


$$\begin{bmatrix} 0.3 \\ 0.7 \end{bmatrix} \begin{bmatrix} f_2 k_1 \\ q_2 k_2 \end{bmatrix}$$

$$h_2 = 0.3 v_1 + 0.7 v_2$$

$$\text{attn: } \text{softmax}(c_{q_2 k_1, q_2 k_2})$$



$$q_1 = f(W_q [c_1 + p_1])$$

→ no dependencies between  $h_1, h_2, h_3$

↳ parallelize

↳ reduce bottleneck

how to parallelize a self-attn computation?

$$\begin{array}{ll} q_1 & \text{█} \\ q_2 & \text{█} \\ q_3 & \text{█} \end{array} \quad \begin{array}{ll} k_1 & \text{█} \\ k_2 & \text{█} \\ k_3 & \text{█} \end{array}$$

attn vectors

$$\begin{aligned} a_1 &:= \langle \underline{q_1}, \underline{k_1} \rangle \\ a_2 &:= \langle \underline{q_2}, \underline{k_1}, \underline{q_2}, \underline{k_2} \rangle \\ a_3 &:= \langle \underline{q_3}, \underline{k_1}, \underline{q_3}, \underline{k_2}, \underline{q_3}, \underline{k_3} \rangle \end{aligned}$$

Step 1:  $\uparrow$

$$\begin{array}{c} \text{Step 1:} \\ \begin{array}{c} q_1 \\ q_2 \\ q_3 \end{array} \times \begin{array}{c} k_1 \\ k_2 \\ k_3 \end{array} \end{array} = \begin{array}{c} \begin{array}{c} k_1 \\ k_2 \\ k_3 \end{array} \\ \begin{array}{c} q_1 \\ q_2 \\ q_3 \end{array} \end{array}$$

these cells have info about the future, need to mask!

Step 2:  $\downarrow$

Softmax

$$\begin{array}{c} \text{Step 2:} \\ \text{Softmax} \end{array} = \begin{array}{c} \begin{array}{c} k_1 \\ k_2 \\ k_3 \end{array} \\ \begin{array}{c} q_1 \\ q_2 \\ q_3 \end{array} \end{array}$$

mask matrix

Step 3:  $\downarrow$

attn scores

$$\begin{array}{c} \text{Step 3:} \\ \text{attn scores} \end{array} = \begin{array}{c} \begin{array}{c} k_1 \\ k_2 \\ k_3 \end{array} \\ \begin{array}{c} q_1 \\ q_2 \\ q_3 \end{array} \end{array} \times \begin{array}{c} \begin{array}{c} v_1 \\ v_2 \\ v_3 \end{array} \\ \begin{array}{c} h_1 \\ h_2 \\ h_3 \end{array} \end{array}$$

## Self-attention :

- ↳ training time : parallelizable
  - ↳ test-time : sequentially
- ⇒ we can only parallelize computations of hidden states when we know the full sequence ahead of time

## test-time

$q_1, k_1, v_1$        $q_2, k_2, v_2$   
↑                      ↑  
Students      opened      ?

$\text{softmax}(q_1 k_1, q_2 k_2)$

*multiply  
by  
value  
vecs*

↳  $h_2$  → softmax layer  $\begin{matrix} a & b & c \\ \hline 0 & 1 & 2 \end{matrix}$   
↑  
Sample "laptops"

$q_1, k_1, v_1$       . . .  
↑  
Students      opened      laptops      ?

## KV cache

- ↳ storing prev. computed keys/values so you don't have to recompute every time step

## Transformer

↳ neural LM built on

multi-head self-attn

↳ "deep", stacked layers (or "blocks")  
of MH self-attn

↳ Vaswani et al - 2017

→ intuition:

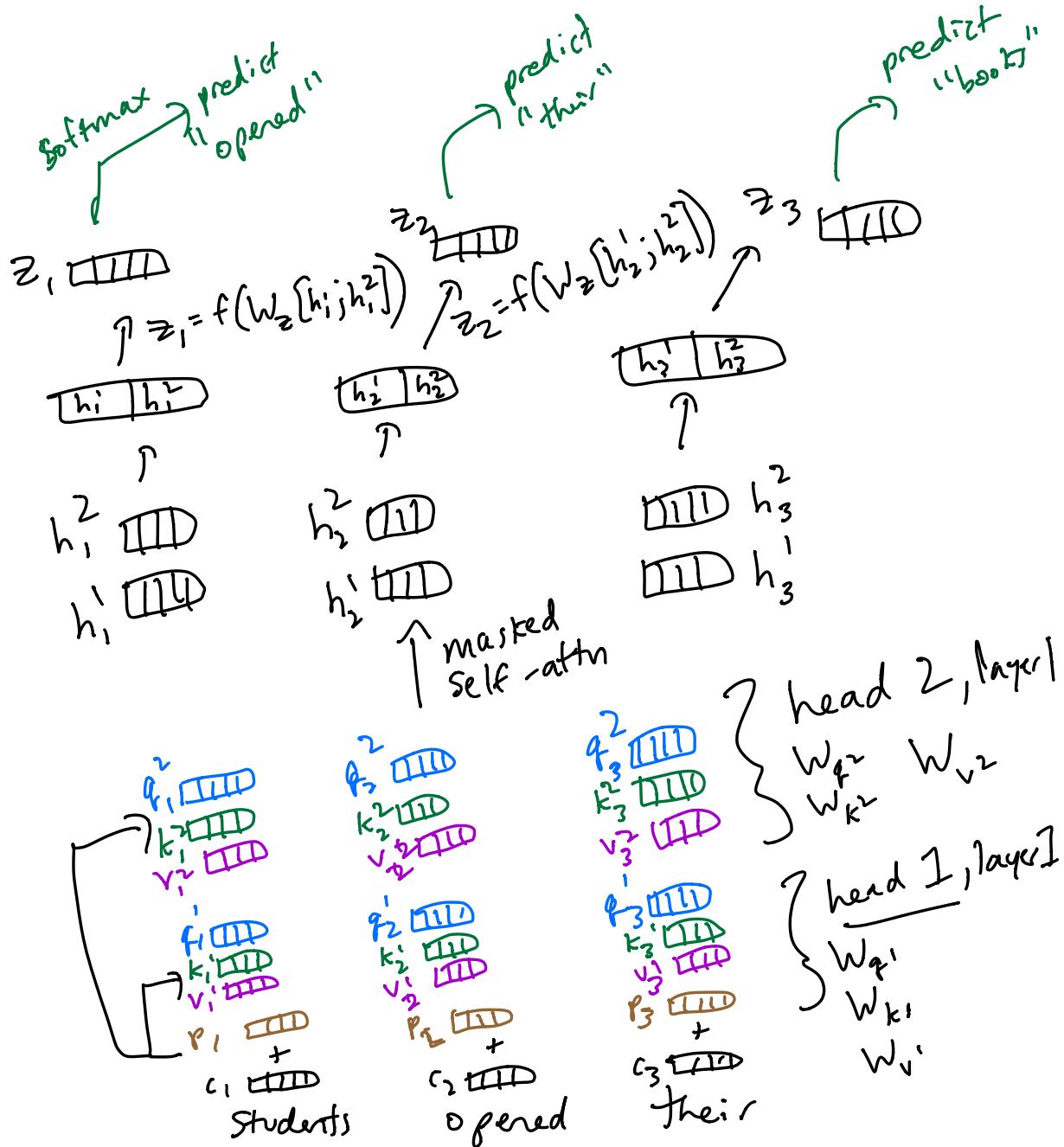
→ let's have multiple sets of  $q, k, v$   
vectors for each token,

then each "head" can focus on  
a specific linguistic property

↳ syntax (e.g. all verbs in prefix)

↳ activate on specific words/phrases

↳ entities / dates



Adding depth:

