

Chinchilla scaling "law":

$L = \text{test loss}$

$\hookrightarrow$  avg. neg. log likelihood of test set

$D = \text{dataset size}$

$\hookrightarrow$  # of tokens

$N = \# \text{ model params}$

$\hookrightarrow$  embeddings,  $W_q, W_k, W_v, W_z, W_{\text{softmax}}$   
 $\underbrace{\quad}_{\propto \text{num layers}}$

$C = \text{compute budget}$

$\text{FLOPS}(D, N) \hookrightarrow$  deterministic fn  
of model / data size

$\hookrightarrow$  floating point operations

goal: given a fixed FLOPS budget  $C$

find

$$\underset{N, D}{\operatorname{argmin}} \quad L(N, D)$$

$$N, D \text{ s.t } \text{FLOPS}(N, D) = C$$

$$L(N, D) = \frac{A}{N^\alpha} + \frac{B}{D^\beta} + E$$

N <sup>$\alpha$</sup>      
 ↓  
 contribution  
of model  
size
 D <sup>$\beta$</sup>      
 ↓  
 contribution  
of data
 E     
 ↓  
 loss of a  
perfect LM

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trained two models w/ same compute C

↳ Gopher : 280B params, 300B tokens

↳ Chinchilla : 70B params, 1.4T tokens

$$L(\text{Gopher}) = 1.993$$

$$L(\text{Chinchilla}) = 1.936$$

Difference between RL and SFT:

In RL, we are maximizing expected reward

$$\max E(R(y|x)) \text{ where } y \text{ is sampled from the model given prompt } x$$

In SFT, we are minimizing loss of ground truth  $y$  that is given to us

$$\min -\log(p(y|x)) \text{ where } y \text{ is given to us}$$

these are actually very similar!

given prompt  $x$ , I sample outputs  $y_L$  and  $y_W$  from the current model

$$R(y_L|x) = 0$$

$$R(y_W|x) = 1$$

What if I do SFT over  $(x, y_W)$

$$L(\theta) = -\log p(y_W|x)$$

$$\frac{dL}{d\theta} = - \underbrace{\frac{d}{d\theta} \log p(y_w|x)}$$

if I instead do RL, via REINFORCE  
(Williams, 1992)

$$\begin{aligned} \frac{dL}{d\theta} E[R(y|x)] &= \\ &\cancel{0 \cdot \frac{d}{d\theta} \log p(y_L|x)} + \\ &1 \cdot \frac{d}{d\theta} \log p(y_w|x) \\ &= \frac{d}{d\theta} \log p(y_w|x) \end{aligned}$$

$$RL: \theta_{new} = \theta_{old} + n \frac{d}{d\theta} \log p(y_w|x)$$

$$SFT: \theta_{new} = \theta_{old} - n \cdot \left[ - \frac{d}{d\theta} \log p(y_w|x) \right]$$

↳ both methods increase  $p(y_w|x)$  "on-policy"

↳ RL samples  $y$  from current model,  
while SFT generally uses  $y_w$   
from an existing dataset ↳ "off. policy"