

# ML Toolbox

## Additional Tools with ML

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# Introduction

Improving prediction performance

- **Stacking** methods
  - Find optimal combination of lower-level models
  - Utilize different types of methods to build ensemble
- Classification with class imbalance
  - Threshold optimization
  - Cost-sensitive training/ case weights
  - **Over- and under-sampling**

# Stacking

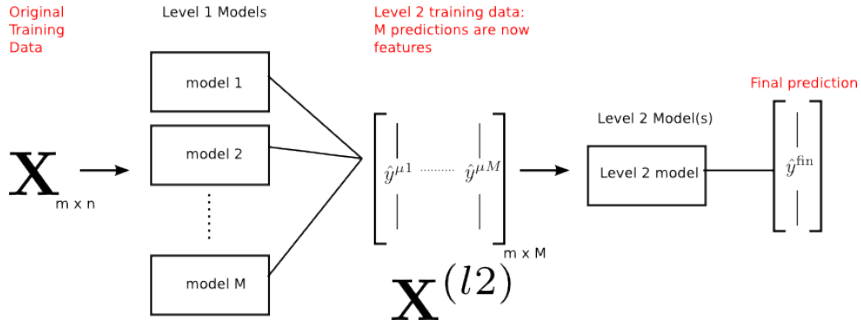
## Combining prediction models

- Do we have to select one ML method to build the final model?
  - Performances might differ between regions of the data
- General idea: Combine multiple models' predictions with a **meta-model**
- Utilize diverse lower-level models that “span the space”
- Draw on advantages of different model types

→ Wolpert 1992, Breiman 1996

# Stacking

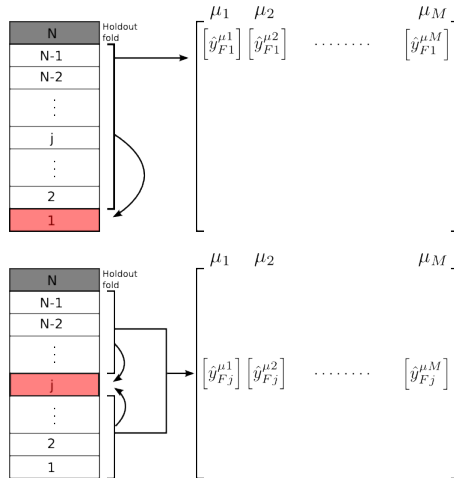
Figure: Stacking process<sup>1</sup>



<sup>1</sup><https://burakhimmetoglu.com/2016/12/01/stacking-models-for-improved-predictions/>

# Second level data

Figure: Create second level training data<sup>2</sup>



<sup>2</sup><https://burakhimmetoglu.com/2016/12/01/stacking-models-for-improved-predictions/>

## Second level model

Input: Cross-validated predictions  $\hat{f}_m^{-i}(x)$

Estimate stacking weights via linear regression...

$$\hat{w}^{st} = \underset{w}{\operatorname{argmin}} \sum_{i=1}^N \left[ y_i - \sum_{m=1}^M w_m \hat{f}_m^{-i}(x_i) \right]^2$$

...or logistic regression for classification problems.

Final prediction

$$\sum_m \hat{w}_m^{st} \hat{f}_m(x)$$

→ Super learner will perform asymptotically as well as the best base learner (van der Laan et al. 2007)

# Stacking process

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## Algorithm 1: Stacking

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**Parameter** :  $V$  folds,  $M$  base learner  $\psi_m$ , metalearning method  $\phi$

**Initialization:** Partition training data into  $V$  folds

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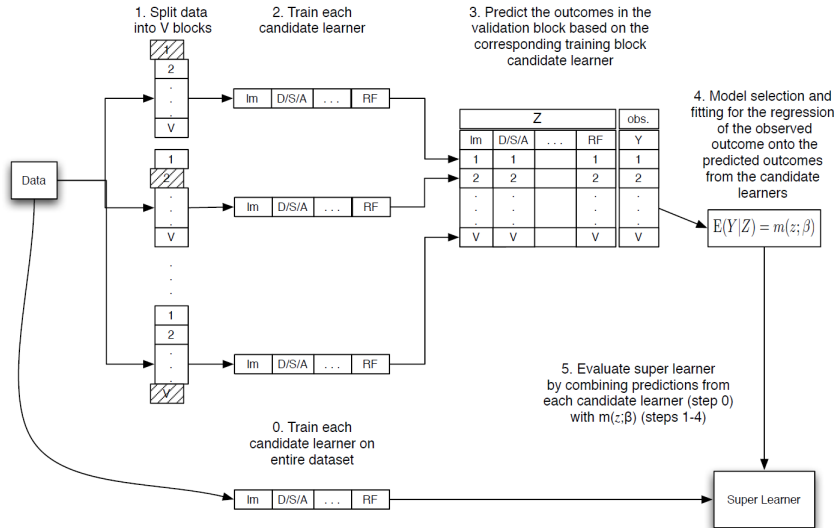
1 for  $v = 1$  to  $V$  do
2   | for  $m = 1$  to  $M$  do
3   |   | Obtain cross-validated predictions  $\hat{\psi}_m^{-v}$  ;
4   | end
5 end
6 Fit meta model  $\hat{\phi}$  using  $\hat{\psi}_m^{-v}$  as inputs ;
7 Fit  $M$  base models with full training data and save with  $\hat{\phi}$  for prediction ;

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# Super Learner

Figure: Super Learner<sup>3</sup>



<sup>3</sup>van der Laan et al. (2007)



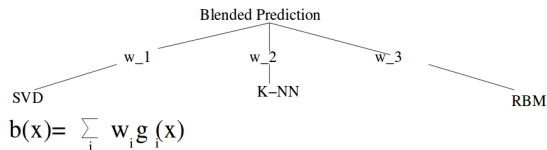
# Extensions

- Blending
  - Throw predictions from various models into one hold-out set
  - Train meta model only on this hold-out set
- Subsemble (Sapp et al. 2014)
  - Introduce additional subset partitions for base learner training
- Feature-Weighted Linear Stacking (Sill et al. 2009)
  - Combines model predictions with meta-features
  - Uses prediction-feature products as meta-model inputs

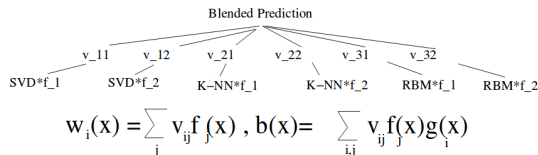
# Feature-Weighted Linear Stacking

Figure: Comparison of SLS and FWLS<sup>4</sup>

## Standard Linear Stacking



## Feature-Weighted Linear Stacking



<sup>4</sup>Sill et al. (2009)