CPSC532W: Probabilistic Programming, Homework 6

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Code for this assignment can be found here: https://github.com/namratadeka/cpsc532W/tree/main/CS532-HW6.

Figure 1: SMC: Address checks and weight updates.

```
def resample_particles(particles, log_weights):
    #TODO
    new_particles = []

weights = torch.exp(torch.FloatTensor(log_weights))
    normalized_weights = weights + le-5 / (weights + le-5).sum()
    logZ = torch.log(weights.mean())

particle_indices = torch.multinomial(normalized_weights, len(particles), True)
    for idx in particle_indices:
        new_particles.append(particles[idx])

return logZ, new_particles
```

Figure 2: Resample particles function.

```
if op == 'sample':
   alpha = evaluate(args[0], env=env)
   d = evaluate(args[1], env=env)
   s = d.sample()
   k = evaluate(args[2], env=env)
   #TODO: put any other stuff you need here
   return k, [s], sigma
elif op == 'observe':
   alpha = evaluate(args[0], env=env)
   d = evaluate(args[1], env=env)
   c = evaluate(args[2], env=env)
   k = evaluate(args[3], env=env)
   sigma = {'type' : 'observe',
            #TODO: put any other stuff you need here
            'logW' : d.log_prob(c),
            'addr': alpha
   return k, [c], sigma
```

Figure 3: Sample and Observe cases in the evaluator.

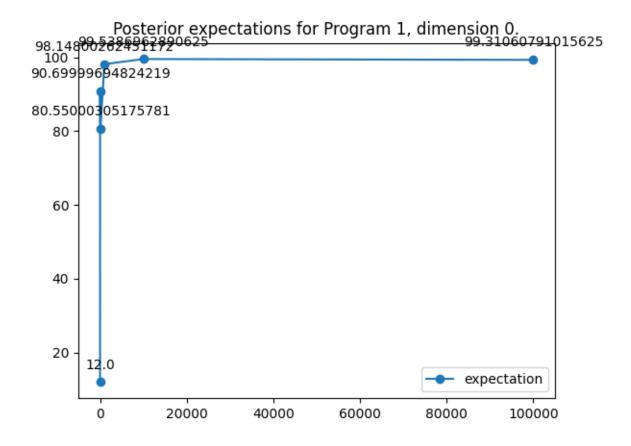


Figure 4: Posterior Means vs number of particles

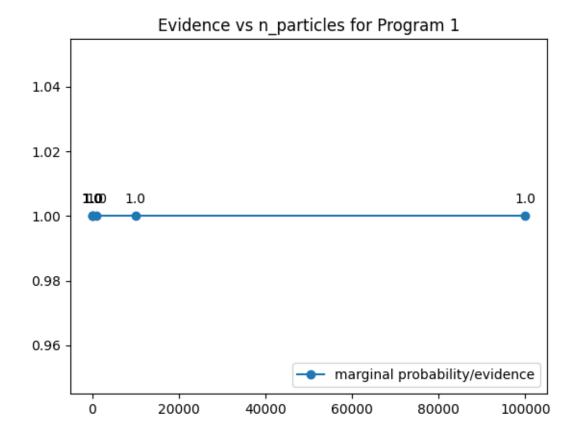


Figure 5: Marginal probability vs number of particles

Program 1, Particles = 1, dimension: 0

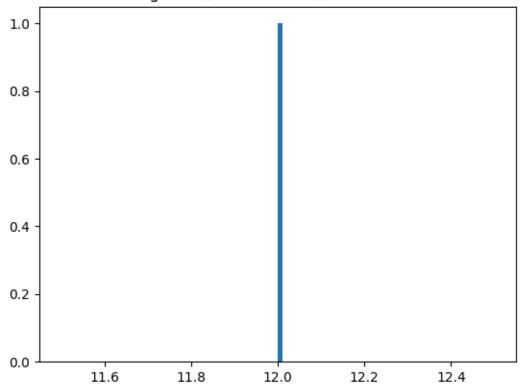


Figure 6: P1 Histogram: 1 particles

Program 1, Particles = 10, dimension: 0

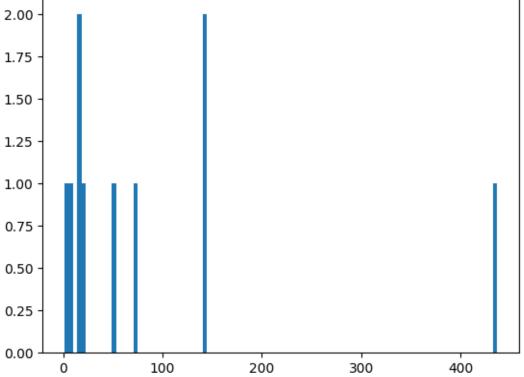


Figure 7: P1 Histogram: 10 particles

Program 1, Particles = 100, dimension: 0

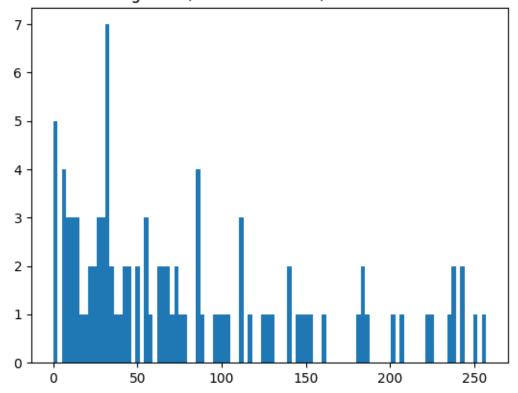


Figure 8: P1 Histogram: 100 particles

Program 1, Particles = 1000, dimension: 0

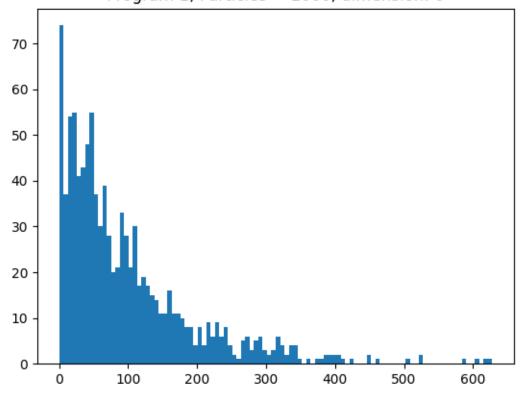


Figure 9: P1 Histogram: 1000 particles

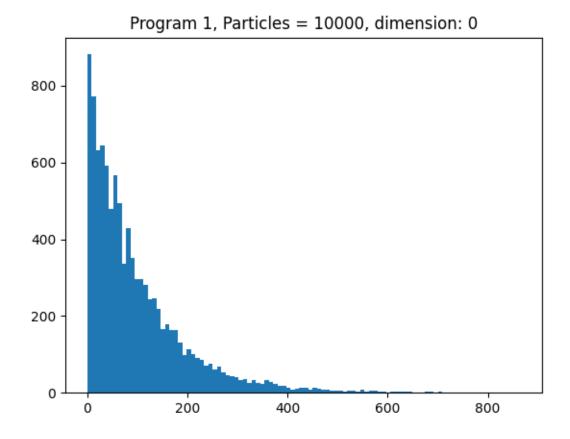


Figure 10: P1 Histogram: 10000 particles

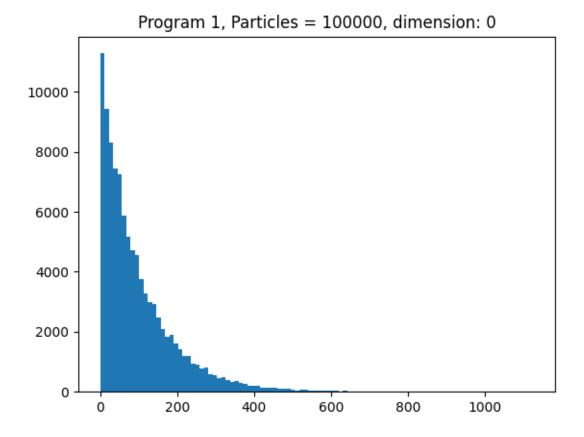


Figure 11: P1 Histogram: 100000 particles

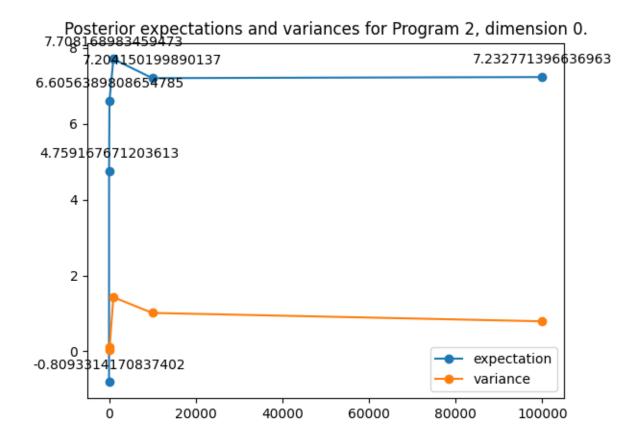


Figure 12: Posterior Means and Variances vs number of particles

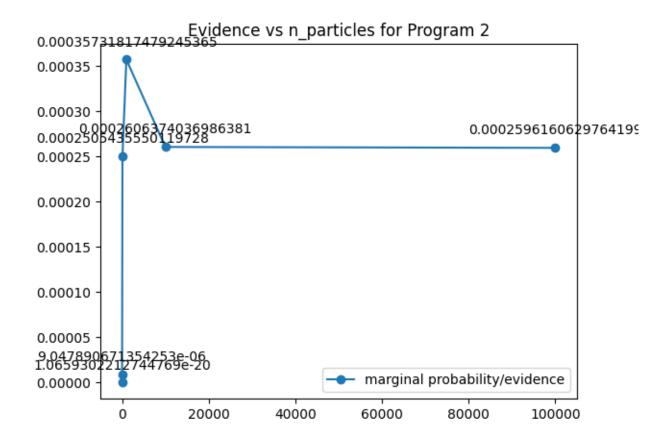


Figure 13: Marginal probability vs number of particles

Program 2, Particles = 1, dimension: 0 1.0 0.8 0.6 0.4 0.2 -

Figure 14: P2 Histogram: 1 particles

-0.8

-0.6

-0.4

-1.0

-1.2

0.0

Program 2, Particles = 10, dimension: 0

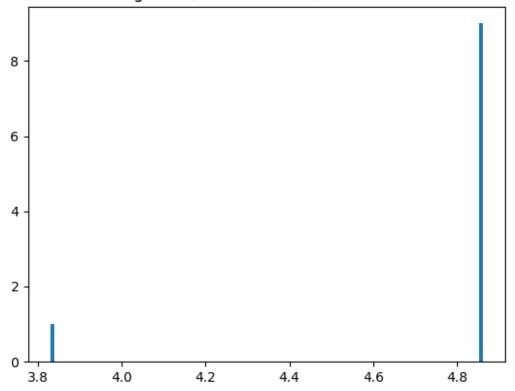


Figure 15: P2 Histogram: 10 particles

Program 2, Particles = 100, dimension: 0 50 40 30 20 10 6.0 6.2 6.4

Figure 16: P2 Histogram: 100 particles

6.6

Program 2, Particles = 1000, dimension: 0

Figure 17: P2 Histogram: 1000 particles

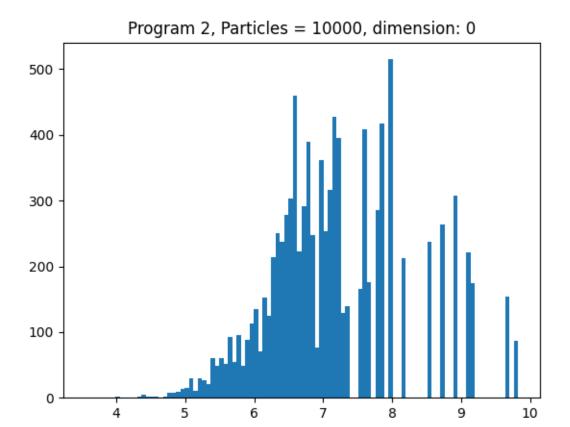


Figure 18: P2 Histogram: 10000 particles

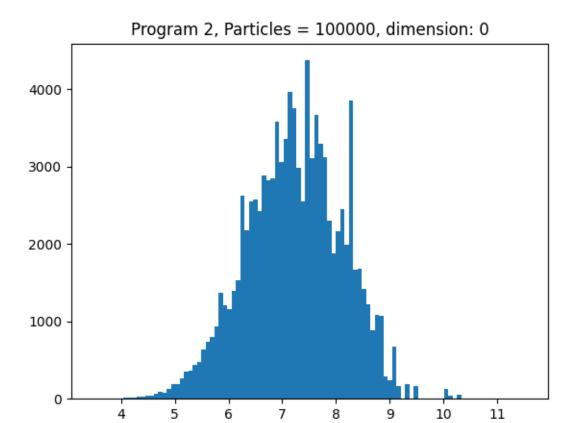


Figure 19: P2 Histogram: 100000 particles

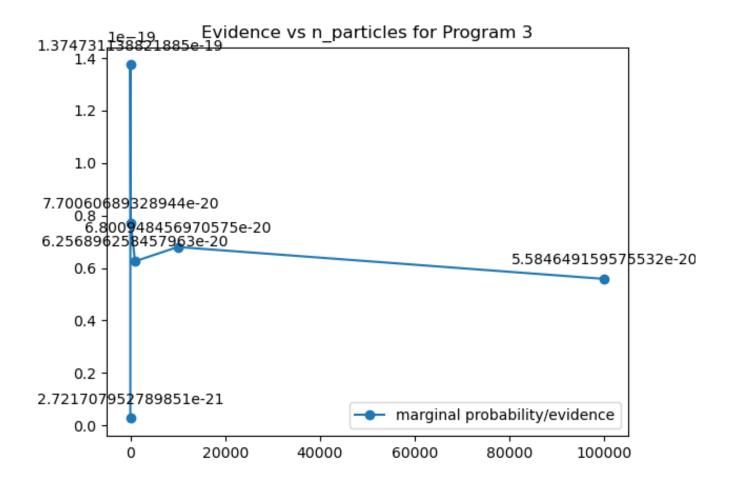


Figure 20: Program 3: Marginal Probability vs number of particles

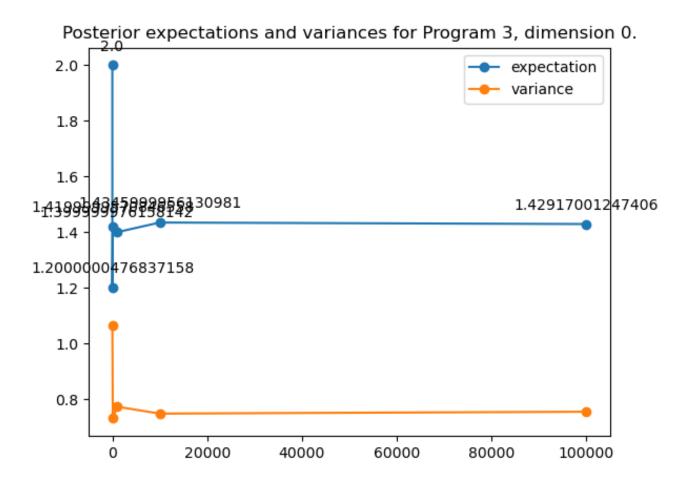


Figure 21: Program 3: Posterior Means and Variances vs number of particles, Dim 0

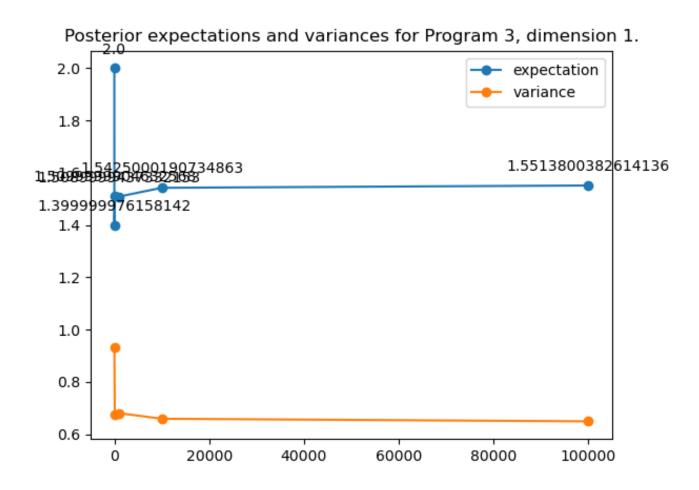


Figure 22: Program 3: Posterior Means and Variances vs number of particles, Dim 1

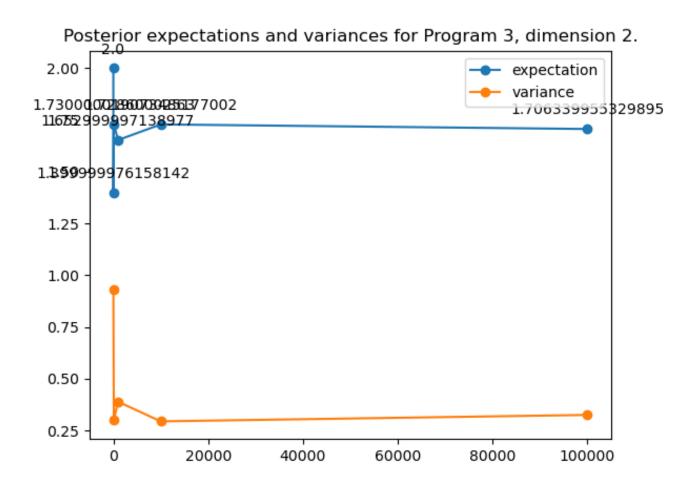


Figure 23: Program 3: Posterior Means and Variances vs number of particles, Dim 2

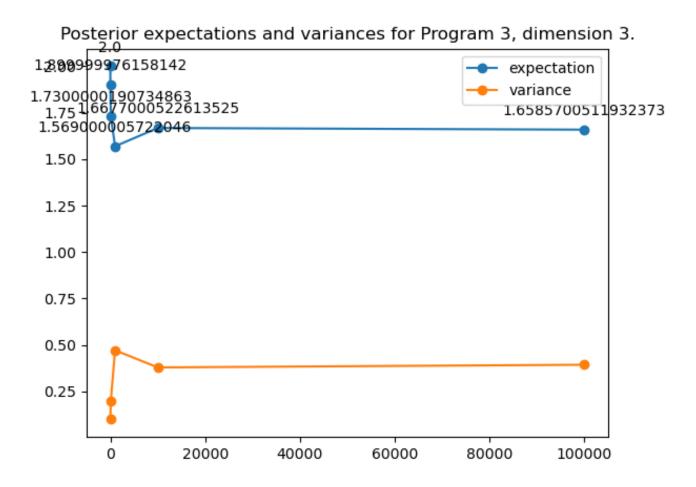


Figure 24: Program 3: Posterior Means and Variances vs number of particles, Dim 3

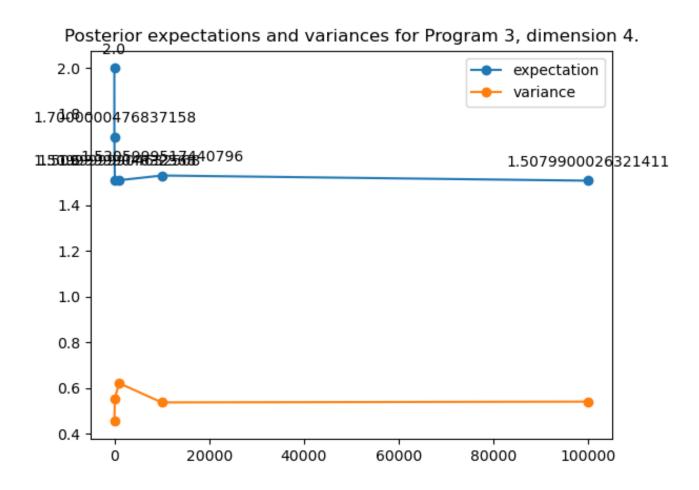


Figure 25: Program 3: Posterior Means and Variances vs number of particles, Dim 4

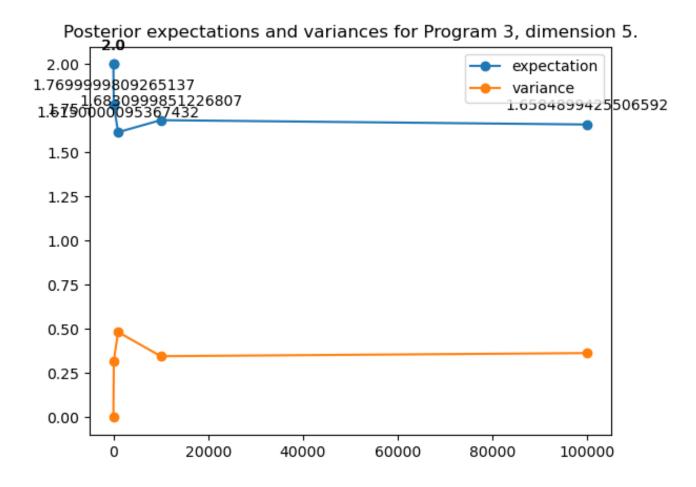


Figure 26: Program 3: Posterior Means and Variances vs number of particles, Dim 5

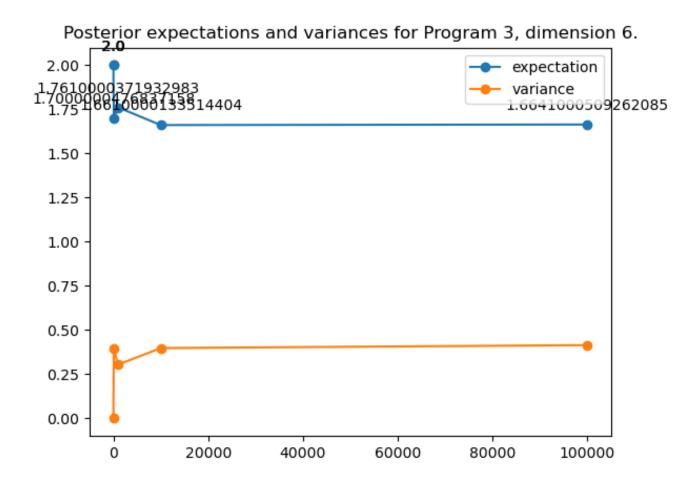


Figure 27: Program 3: Posterior Means and Variances vs number of particles, Dim 6

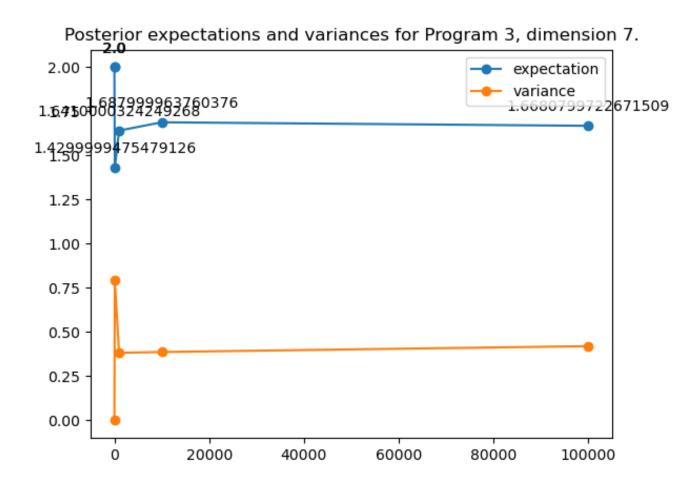


Figure 28: Program 3: Posterior Means and Variances vs number of particles, Dim 7

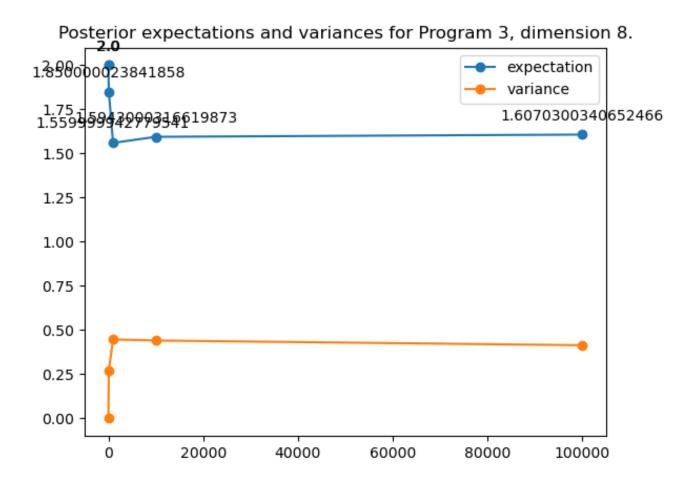


Figure 29: Program 3: Posterior Means and Variances vs number of particles, Dim 8

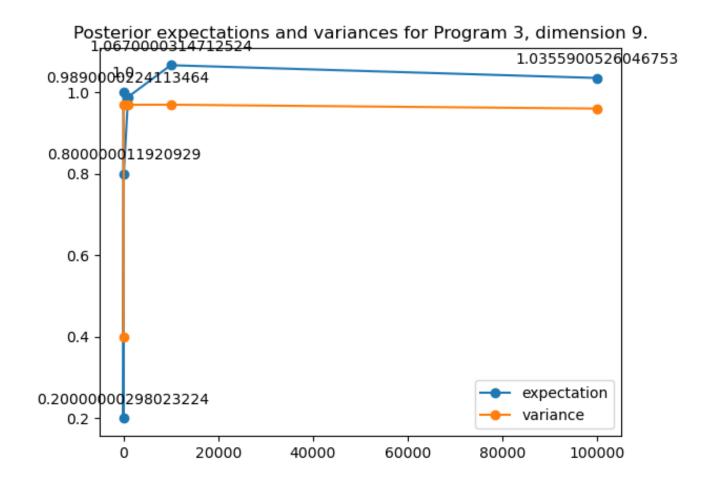


Figure 30: Program 3: Posterior Means and Variances vs number of particles, Dim 9

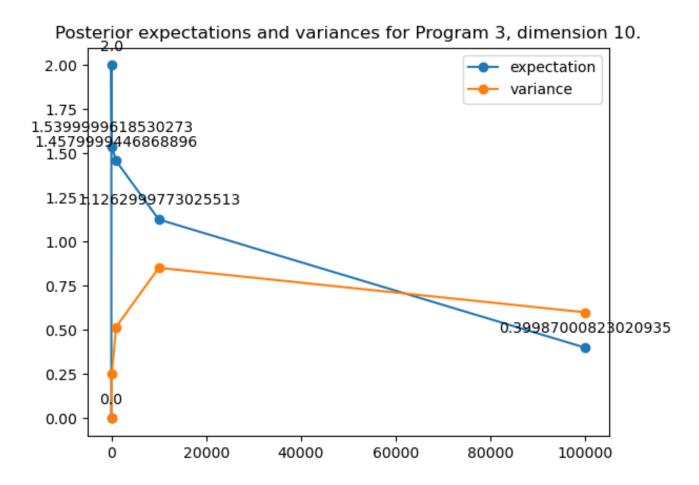


Figure 31: Program 3: Posterior Means and Variances vs number of particles, Dim 10

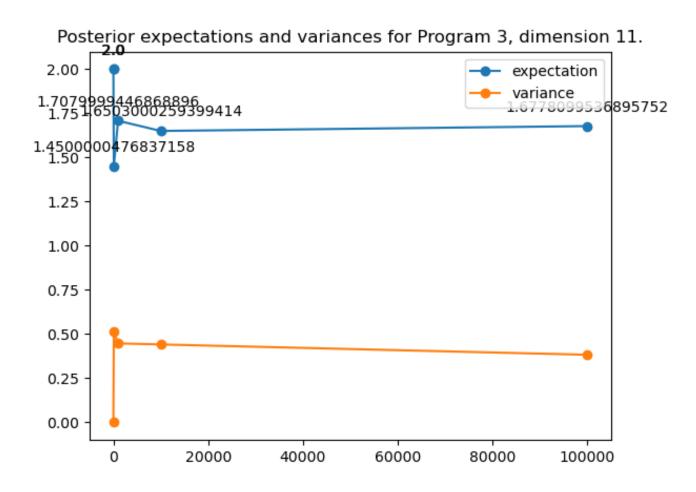


Figure 32: Program 3: Posterior Means and Variances vs number of particles, Dim 11

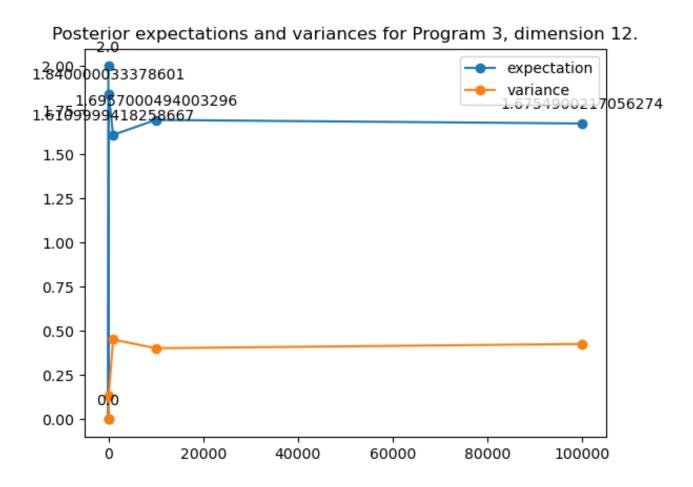


Figure 33: Program 3: Posterior Means and Variances vs number of particles, Dim 12

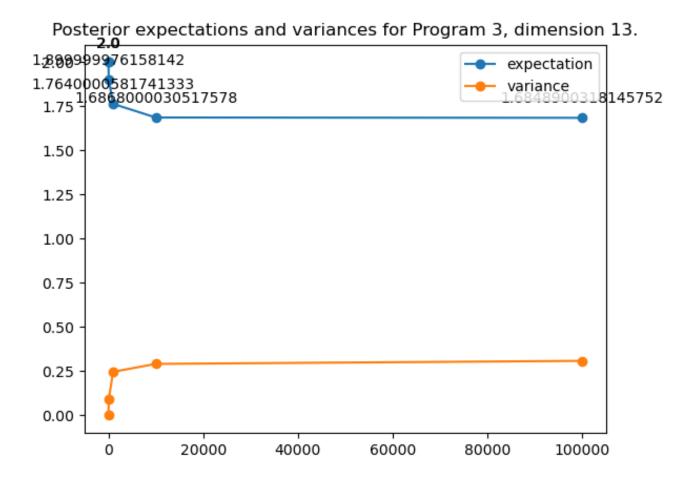


Figure 34: Program 3: Posterior Means and Variances vs number of particles, Dim 13

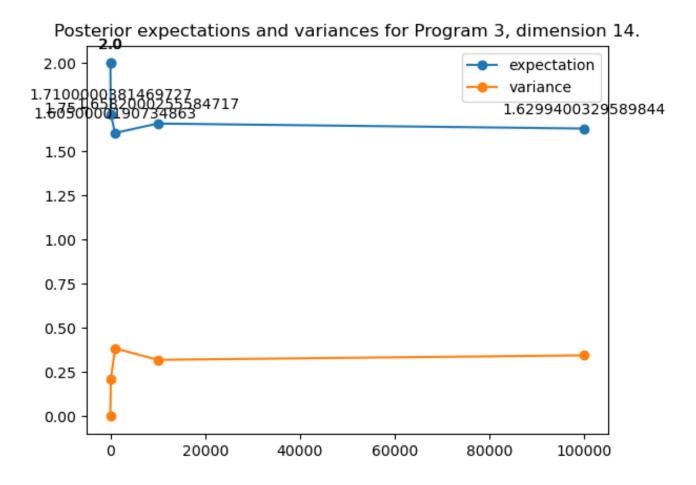


Figure 35: Program 3: Posterior Means and Variances vs number of particles, Dim 14

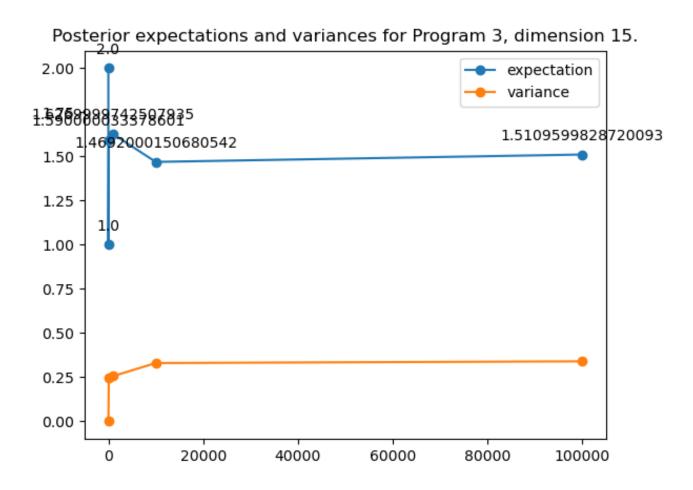


Figure 36: Program 3: Posterior Means and Variances vs number of particles, Dim 15

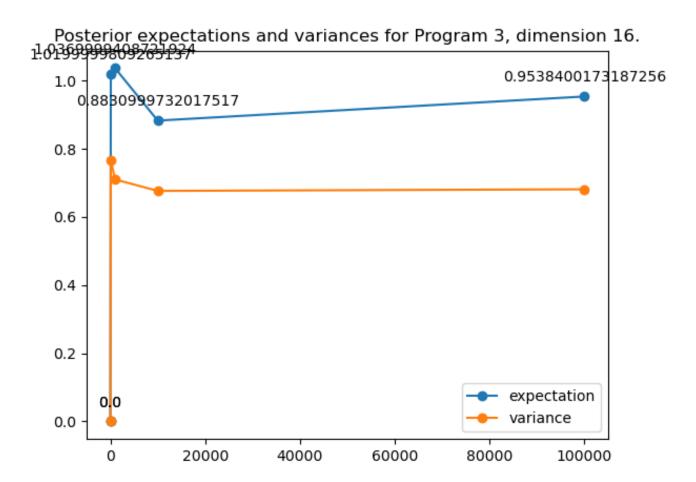


Figure 37: Program 3: Posterior Means and Variances vs number of particles, Dim 16

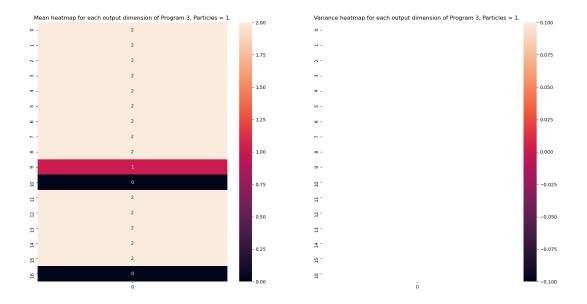


Figure 38: Program 3: Posterior Mean and Variance heatmaps with 1 Particle

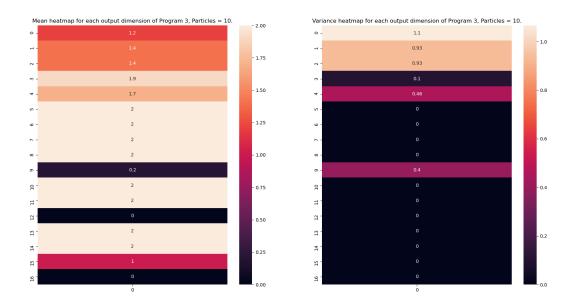


Figure 39: Program 3: Posterior Mean and Variance heatmaps with 10 Particles

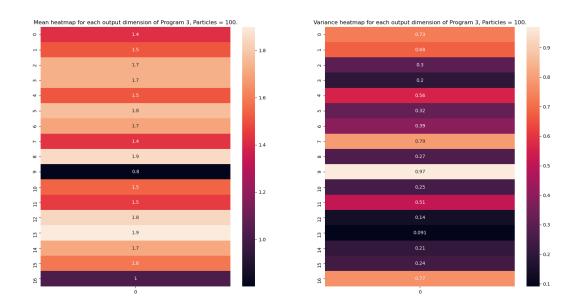


Figure 40: Program 3: Posterior Mean and Variance heatmaps with 100 Particles

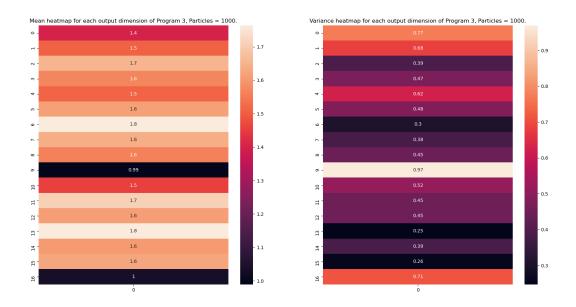


Figure 41: Program 3: Posterior Mean and Variance heatmaps with 1000 Particles

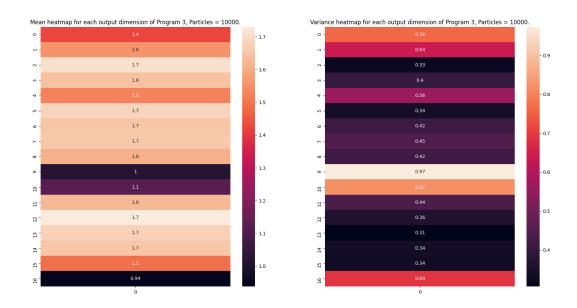


Figure 42: Program 3: Posterior Mean and Variance heatmaps with 10000 Particles

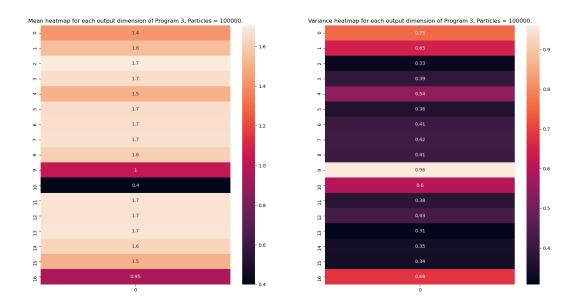


Figure 43: Program 3: Posterior Mean and Variance heatmaps with 100000 Particles

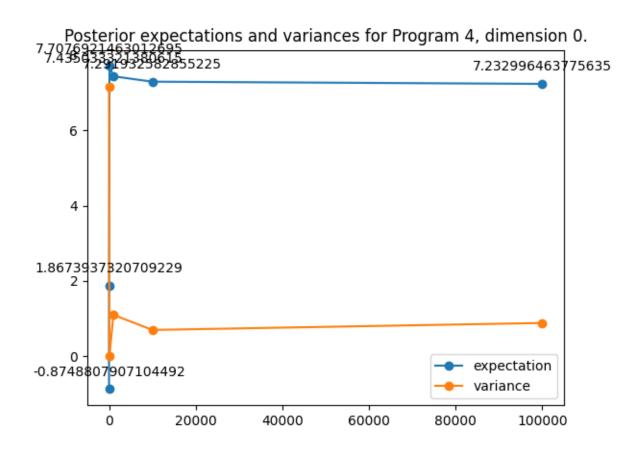


Figure 44: Posterior Means and Variances vs number of particles

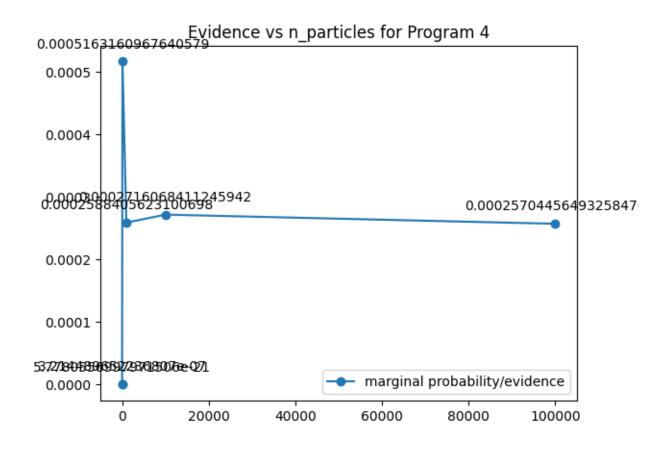


Figure 45: Marginal probability vs number of particles

Figure 46: P4 Histogram: 1 particles

-0.8

-0.6

-0.4

-1.0

-1.4

-1.2

Figure 47: P4 Histogram: 10 particles

Program 4, Particles = 100, dimension: 0

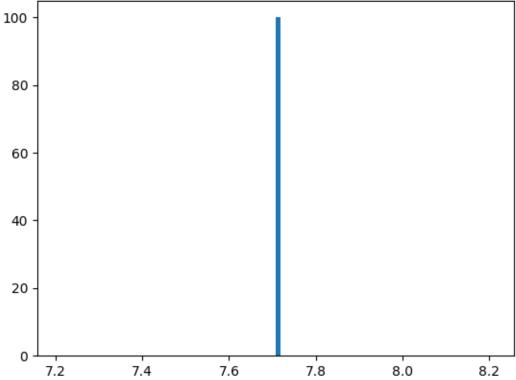


Figure 48: P4 Histogram: 100 particles

Program 4, Particles = 1000, dimension: 0 250 200 150 50 6 7 8 9

Figure 49: P4 Histogram: 1000 particles

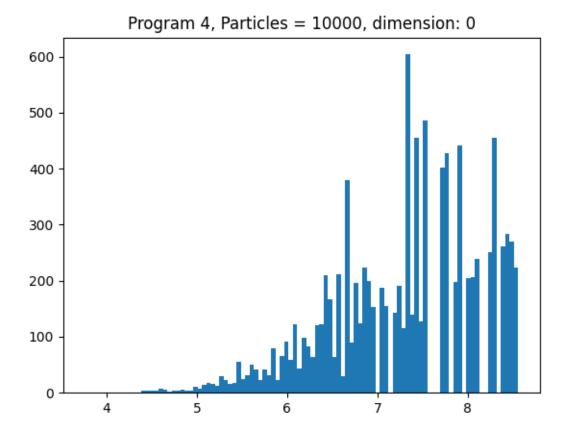


Figure 50: P4 Histogram: 10000 particles

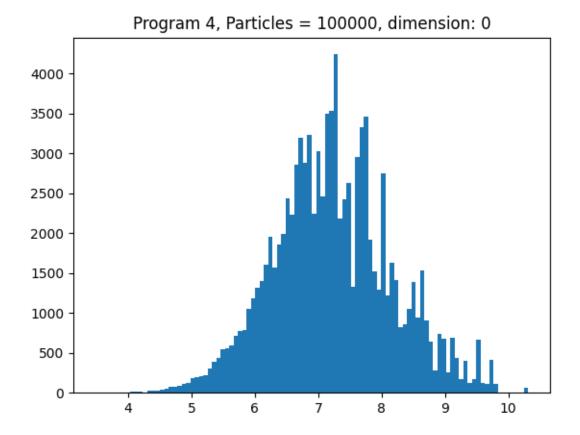


Figure 51: P4 Histogram: 100000 particles