Object SelectionObject selection

Final Year Project Final Report

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**Abstract**

In this thesis, we introduce the Graph Cut solution of interactive segmentation and its derivative – the Lazy Snapping.

The interactive Graph Cut segmentation for the multi-dimensional image provided by Jolly and Boykov in 2001. The hard constraints are the user marked pixels as “object” and “background” while the soft constraints involving both boundary and region properties.

The fast implementation provided by Boykov and Kolmogorov of min-cut max-flow is used to find the optimal segmentation. This solution gives the balance of boundary and region properties among all segmentation satisfying the constraints. The experimental results in term of photo editing are presented. It works quite well with small and medium resolution multi-dimensional images which have various color distribution.

In 2004, Li, Tang, Sun, and Shum published the Lazy Snapping method basing on Jolly and Boykov research. Instead of working directly on the pixel, the pre-segmentation step is used to grouping pixel into many segments. Each one is considered as super-pixels the graph and energy function is constructed similarly to Jolly-Boykov’s one.

We also renewed the existing Lazy Snapping method [2] by using another algorithm in the pre-segmentation step. By replacing the traditional watershed [14] in the Lazy Snapping framework with the SEEDs [8], we can achieve a simpler implementation and usable result. The experimental results show that we can reach the same accuracy as Lazy Snapping without using second refining step. Finally, our method is quite fast with some simple steps.

**Acknowledgements**

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We also want to share this moment with our family – who always believe and beside us. We will not go far this way without the unlimited love from them. And now, they can be proud of ourselves and what we did. It is best gift for our family. Thank you for always being by my side!

We cannot forget the truly friends who stayed, learned and tried in FPT University. We joined and shared valuable student time together. Thank you, guys! We will always remember CS0801.

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# Introduction

## The interactive image segmentation problem

An image is a set of sub-images that sometimes referred to as regions-of-interest, ROIs, or simply regions. One of the problem in image processing is image selection – how to cut out or select an area for later specific image processing operations.

Interactive single-image segmentation (image cutout or foreground/background separation), one of the typical case in region selection problem, is to select the object (e.g. human, flower) from the background that based on samples provided by the user. The result can be used to photo collaging or identifying.

The purpose of image cutout is to determine which parts of the original image belong to “object” and which belong to the background. On one hand, it is quite easy for human perspective to specify. On the other hand, the computer is not smart enough to achieve this purpose without human assistance. It would take a long way such that the computer understands cognitive image at the human level. So that, the user has to provide samples in both foreground and background individually, with pixel accuracy.

Although this problem has a long history in computer vision, how to find an efficiency solution with high accuracy in pixel level is still a challenge. Boykov and Jolly had provided an approach in 2001 [1]. They provided a very general energy minimization framework that is at the heart of many modern techniques. A user gives foreground/background strokes or a coarse bounding box of the object in the image. The algorithm is based on this information to learn foreground/background color feature, and then add constraints to make energy minimization problem easier. It on region-based methods – assigns pixels to a given region based on the degree of mutual similarity.

For the general F/B separation problem, based on the uses of samples, there are two primary methods: boundary-based and region-based. Both of them use the features of selected ones to automate foreground specification.

In the boundary-based method, the user surrounds and traces the object boundary while the system optimizes that curve. The user has to control the curve manually since there are many “minimum cost contour” for highly textured or un-textured image. The user should also have the ability to get progress overview in close control. For high-resolution images, enclosing entire boundary is very costly while zooming in or out at dragging borderline is not easy. Once it is finally computed, then the tool is no longer helpful, and errors must be cleared. Examples of this method include intelligent scissor [Mortensen and Barrett 1995; Mortensen and Barrett 1999], image snapping [Gleicher 1995] and Jetstream [Perez and Blake 2001].

In the region-based method, the user may specify some hints. The hint can be the region contain the object or some samples of object and background. Meanwhile, the underlying optimization extracts actual object boundary based on these. The user can operate at any scale they want. The process can show the partial results after each hint inputting. However, shadow, low-contrast edges or other ambiguous areas become troubles to hint or even must be manually made by hand. Some examples of this method are magic wand in Photoshop, intelligent paint [Reese and Barrett 2002; Barrett and Cheney 2002], marker drawing [Falcao et al. 2000], sketch-based interaction [Tan and Ahuja 2001], interactive graph cut image segmentation [Boykov and Jolly 2001], GrabCut [Rother et al. 2004]) and interactive image Photomontage [Agarwala et al. 2004].

In our thesis, we focus on interactive graph cut image segmentation [1], a typical example of the region-based approach for later solutions, and lazy snapping [2], a great combination of quick hinting (of region-based approach) and pixel-accurate boundary editing (of boundary-based approach).

## Image segmentation as graph cut

Interactive graph cut image segmentation [1] is a region-based method for segmenting N-dimensional image. It converts the image into network flow, which each internal node corresponds to a node, the source and sink are object and background terminal correspondingly. The edges of graph are weighting based on boundary and region properties of adjacency node. Then, max-flow is solved to find minimum cut correspond to optimal segmentation. A better max-flow algorithm is provided by Boykov and Kolmogorov.

## Improving lazy snapping

Image segmentation can be known as the division of an image into meaningful structures is often an essential step in image analysis, object representation, visualization, and many other image processing tasks.

In other words, image segmentation focus on methods that find the particular pixels that make up an “object”. There were many different segmentation approaches in the recently decades. In 2002, Li et al [24] divided the segmentation approaches into five categories that present in the following table:

Table 1. Segmentation approaches

|  |  |
| --- | --- |
| Threshold-based segmentation | Histogram thresholding and slicing techniques are used to segment the image. They may be applied directly, also combined with pre- and post-processing techniques |
| Edge-based segmentation | With this technique, detected edges are assumed to represent object boundaries and used to identify these objects. |
| Region-based segmentation | Where an edge-based technique may attempt to find the object boundaries and then locate the object itself by filling them in, a region-based takes the opposite approach, by (e.g.) starting in the middle of an object and then “growing” outward until it meets the object boundaries. |
| Clustering techniques | Clustering is known as a synonym for (agglomerative) segmentation. Here it is used to denote techniques that are primarily used in exploratory data analysis of high-dimensional measurement patterns. In this context, clustering methods attempt to group together patterns that are similar in some sense. This goal is very similar to what we want do when we segment an image, and indeed some clustering techniques can readily be applied for image segmentation. |
| Matching | When we know what an object we wish to identify in an image (approximately) looks like, we can use this knowledge to locate the object. This approach to segmentation is called matching. |

Lazy Snapping paper presents an interactive image cutout tool with two steps: a quick object marking step and a boundary editing step to separate objects from the background. With an improvement by combining graph cut with pre-computed segmentations, the results are accurate with less time than working on individual pixel level in object marking step. It also provides two simple events to increase the accuracy of the boundary. Moreover, Lazy Snapping provides instant visual feedback, based on the cutout contour to the actual object boundary despite the noise of ambiguous or low contrast edges. That makes the different of Lazy Snapping – the combination of region-based segmentation and edge-based segmentation.

Based on the Lazy Snapping paper, we have simple method overview:

* Goal: separate object from background
* First step: foreground/background selection
  + Samples are given by users in each part of image
  + Solve minimum cut problem on segment level
* Second step: boundary correction
  + User provides some strokes on incorrect parts of object
  + Solve minimum cut problem on pixel level

The new thing in Lazy Snapping method is a novel graph cut formulation which is built on a pre-computed image over-segmentation, instead of pixel. By using watershed algorithm [14] to divide the image into many small regions, each node in graph cut problem present for a segmented region. By that, we have a new network, while the nodes V are the set of all small regions from pre-segmentation step, and the edges E are the set of all arcs connecting adjacent regions.

By reducing the number of nodes and edges in the new network, the speed of new algorithm increases significantly. When watershed segmentation provides good segments, we can get good object without boundary editing step.

With the same idea of the authors in Lazy Snapping paper about a pre-computed image segmentation before apply to Graph Cut solution, I built my own framework with an understanding about several pre-segmentation methods:

* Watershed by Vicent and Soille, 1991
* Watershed by Meyer, 1992
* Kmeans by Duda and others, 2000
* SEEDs superpixels by M. van den Bergh et al, 2012
* SEEDs Revised Mean Pixels by D. Stutz, A. Hermans, B. Leibe, 2014

Step by step, my framework achieved different results with each method. Finally, the combination between SEEDs Revised Mean Pixels and Graph Cut Solution give acceptable results. In my experiment, I focus on improvement of Object Marking Step to separate objects without using boundary editing step. In general, the results of my framework are closed with results in Lazy Snapping paper.

SEEDs Revised Mean Pixels method is very useful by allowing developer control and change important parameters such as the number of segments and iterations as well as level of the smooth boundary. By that, we can avoid the over-segmentation problem but still can get acceptable results with reducing the time of the framework.

## Contributions

The main contribution of this thesis are:

* Testing implementations that replace traditional watershed [14] of Lazy Snapping with others segmentation algorithms such as K-means [13], Distanced Transform Watershed [15] and SEEDS [7].
* An implementation of **Silent Lazy Snapping** - an interactive image cutout framework which separate the foreground and background with some simple steps.
* A comparison between several segmentation algorithms which can be applied to pre-segmentation step that tested in Berkeley Segmentation Dataset and our own dataset.

The results of Berkeley Segmentation Dataset and my own dataset is made publicly available together with my implementation of Silent Lazy Snapping.

|  |  |  |
| --- | --- | --- |
| C:\Users\Sonata\Desktop\TestImage\12\12.jpg   1. Original image | E:\FPT\Graduation Assignment\Image\girl_LS.PNG   1. Lazy Snapping result **with** boundary editing | C:\Users\Sonata\Desktop\TestImage\12\1\object.jpg   1. Silent Lazy Snapping result **without** boundary editing |

Figure 1. Results of Lazy Snapping method and Silent Lazy Snapping method

Without boundary editing step, the result from Silent Lazy Snapping is usable. In this thesis, my contribution focuses on how to improve the efficiency and the speed of object marking step, not similar with original paper. There are many methods to the image-cutout problem so far, but it is not easy to solve this in one step. With the limitation of my knowledge in student level, I did some researches to create Silent Lazy Snapping method.

## Organizations

We will review related works in chapter 2, and our contributions in chapter 3 and chapter 5. Finally, we will summarize our works and future directions in chapter 5.

This thesis is organized to review the image segmentation problem and introduce two solutions.

Chapter 2 will show the literature review of image segmentation problem and some approaches. Basic concepts and some typically related works will be shortly described for betting understanding.

Chapter 3 and 4 introduces and describe interactive graph cut and lazy snapping correspondingly. At the end of each chapter are our experiments and the conclusion.

Chapter 5 is for conclusion.

# Literature Review

## On the lazy snapping framework

Let us review the Lazy Snapping framework [2] which creates the foundation for our modified algorithm in chapter 4.

Based on the energy minimization method provided by Yuri Boykov and Marie-Pierre Jolly [1] in 2001, the authors of Lazy Snapping paper had a new idea that uses watershed algorithm [14] to reduce the complexity before apply graph cut labeling solution. In marking step, the user needs to draw some strokes to give samples for object and background. Instead of processing in pixel level, graph cut solution will label all regions in segment level. Even if object marking step processes the boundary as accurately as possible, the errors are still existed, especially in hard cases such as low contrast or high color similarity. So that, boundary editing step will refine the object boundary by using Direct vertex editing or Overriding brush tools.

There are several ways to select objects from the background other than lazy snapping, such as GrabCut [3] and Drap-and-Drop pasting [4]. In the same year 2004, Carsten Rother and others introduced GrabCut method. Unlike Lazy Snapping, the user provides the samples by using a bounding box (rectangle) or a lasso (polygon) to mark the region-of-interest. GrabCut is also based on energy minimization method like Lazy Snapping, but it is not good enough to specify details for objects with arms or external details.

|  |  |
| --- | --- |
| E:\FPT\Graduation Assignment\Image\grabcut1.PNG | E:\FPT\Graduation Assignment\Image\grabcut2.PNG |

Figure 2. Result of GrabCut method (from [3])

In User Study session of [3], C. Rother shows some comparison of GrabCut method and Lazy Snapping method:

* Easy to use: Lazy Snapping is 20% fewer mistakes
* Speed: Lazy Snapping is 60% less time
* Accuracy: Lazy Snapping is 60% fewer wrong pixels

In 2006, the authors of Drag-and-Drop Pasting created a new objective function to compute an optimized boundary condition that based on Poisson image editing [Perez et al. 2003]. User only need to draw an outline of the object, then drag and drop it onto the output image. The result of this method depends on the way user draws the boundary because Poisson image editing may not always feedback good results. Therefore, with objects with external details, it is quite hard for the user to specify the boundary carefully. This method is a combination of GrabCut and image matting methods.



Figure 3. User define boundary and Drag-and-Drop Pasting results (from [4])

The improvement of Lazy Snapping method is pre-segmentation step – to pre-compute the source image by using watershed segmentation [14] to reduce the number of vertices in graph cut labelling solution, by that, reduce the run time of framework efficiently.

In 1991, Vincent and Soille presented Random access memories and waiting queue driven algorithms to procedure histogram of the image with purpose merge pixel with the same color similarity to a *super pixel*. It was an innovation that achieves new speed in digital image processing that time. However, the number of super pixels is big lead to the over-segmentation problem, so to get better segmentation is still an issue in image processing.

As presenting in [16], the watershed method has a long definitive history that linked with the technological development of the image processing devices. The first watershed transform started in the mid-seventies, and up to now, there are more and more approaches to solving image segmentation problem based on that starting point.

In 1992, Meyer presented different approach named *Watershed transformation* which is implemented in the openCV framework. It is also called *marker-based watershed* algorithm. But this approach gives us over-segmentation result because of noise in the image. The result of this algorithm existed regions with label 0 – not sure which region they belong to and the boundary of each region with label -1. So we have to duel with noises after apply graph cut labelling solution.

Up to now, 20 years later, there are many alternatives choices of the pre-segmentation algorithm. In 2000, K-means method [13] is a simple way to separate the image into small segments. However, this idea may not be a good way to apply to graph cut labelling solution because the information of color is not enough to give good segments, especially in cases the object and background have the similar color.

The SEEDS – Superpixels Extracted via Energy-Driven Sampling [7] is a giant step to achieve a new level of pre-segmentation that based on a simple hill-climbing optimization.

This method can handle over-segmentation problem by controlling the number of super pixels. based on that, the user can test and define how detail of segment needed for next step. The running time of this method depends on number of iterations, number of history bin and how smooth the boundary is. It can be setting by users to get necessary result. The weakness of this method is the border of each segment. It will be a great combination with boundary editing step of Lazy Snapping to have new object selection framework, but how can we get better a boundary from pre-segmentation step so that we do not need to refine it?

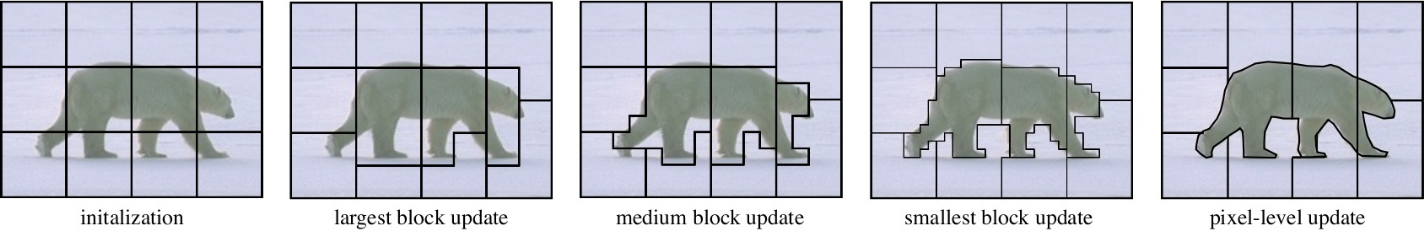


Figure 4. Process of SEEDS method (from [28])

In 2014, Stutz from RWTH Aachen University, Aachen, Germany defended his thesis for Bachelor Degree with Superpixel Segmentation using Depth Information. His research and experiments are the answer to the previous question. The method combines the advantages of SEEDS method and solves the existing problem about unsmooth boundary in the same case. For more detail, I will present in chapter 4.

The important graph-labelling method in Lazy Snapping framework was Graph Cut [11]. This new algorithm is presented by Yuri Boykov and Vladimir Kolmogorov in 2004. In most examples, this method worked 2-5 times faster than any other methods, including outperformace in typical vision graphs such as push-relabel or Dinic’s algorithms.

In 2009, Frank R. Schmidt et al introduced *Planar Graph Cut* algorithm in Computer Vision. With this method, we can segment a given image of pixels in which is incredible complexity for image segmentation problem.

In our new method, we will adopt the Lazy Snapping framework but we will modify the pre-segmentation step in order to achieve fast segmentation with few modifications in the boundary by using the overriding brush. In fact, we do not need to use the refining step in lazy snapping to achieve the same result as their paper.

## On max-flow and min-cut problem

As described in chapter 1, the image segmentation problem has two main approaches: region-based and boundary-based. However, both implementation focuses mainly on region-based approach. They are the applications of min-cut max-flow in computer graphics.

The Ford-Fulkerson method was described by L. R. Ford and D. R. Fulkerson on Canadian Journal of Mathematics in 1956 [9]. The method idea is finding shortest paths from source to sink that doesn’t reach maximum capacity (called “augmenting path”) and saturate the flow through that path until all augmenting paths are exhausted. In 1970, Yefim Dinitz published an algorithm that uses bread-first search to find augmenting path [14].

In 1988, Andrew V. Goldberg and Robert Tarjan described push-relabel algorithm [17]. The “preflow” is gradually converted to the maximum by moving flow between neighbor nodes by push operation in admissible network maintained by relabel operation.

In 2001, Boykov and Kolmogorov proposed a new max-flow algorithm [11] also based on finding augmenting path and comparing with some old algorithms in term of energy minimization in vision. Their main improvements are building two search trees and reusing these trees to increase actual performance.

Those papers are mainly written to how to solve the graph cut. In computer graphics, the remaining problem is how to construct the graph. In equivalent, they don’t describe the objective energy function that deprived in some ways from image for minimizing in graph cut.

In 1989, Greig et al. discovered the min-cut max-flow in combinatorial can be used to minimize the certain energy function in computer vision [19].

In 2001, Boykov and Jolly published the interactive graph cut [1]. It is a particular approach to the later solution. They provide a way for converting image segmentation to graph cut. In the detail level of pixels, the energy function is the balance of region and boundary properties that satisfies hard constraints provided by the user. The max-flow algorithm runs in constructed network and provides the result of labeling.

In 2004, Li, Tang, Sun and Shum described the lazy snapping that is the super-pixel graph cut with boundary editing [2]. Instead of detail level of pixels, the pixels were group into several segments by the watershed algorithm. Each of them is considered as a super-pixel to construct similar energy function. The boundary after running max-flow can be edited.

In the same year, Rother, Kolmogorov, and Blake also described the GrabCut [3]. That is an iterated graph cut involving both color and contrast information, with border matting for optimizing the boundary. From the inputted bounding box of the object, GMM estimates the color distribution of the target object. It is used to construct the Markov random fields with energy function of connected regions having the same label. Then running the graph cut based optimization to get their values. The procedure is repeated until convergence. Further additional user interaction points out misclassified regions and re-run the optimization. The preserve edges are corrected by border matting.

In 2008, S. Vicente, V. Kolmogorov, and C. Rother published the DijsktraGC [5]. This technique improves object segment by imposing the connectivity prior. After segmenting by graph cut, the user to input some parts belongs to object but are misclassified (thin details in this case). The Dijkstra algorithm as a heuristic way is used to extract these, produces a better result.

In 2009, Frank R. Schmidt, Eno Toppe and Daniel Cremers described a new algorithm [6] to solve minimum cut on planar graphs faster by always augmenting leftmost of all paths from source to sink.

# Interactive Graph Cut

## Problem statement

Technically, the object segmentation is a binary labelling problem that assigns the label of each pixel on image is either “object” or “background”. However, the computer is not capable of recognizing which “object” user want in the image. In our case, user has to label some pixel, called “seeds”, so that the technique can separate image in the interactive way.

## Constructing the graph from image segmentation

In Boykov and Jolly’ paper, the interactive object segmentation problem can be solved by using min-cut max-flow theorem to find global minimum of cost function among all segmentation that satisfy hard constraints imposed by user.

### The min-cut max-flow theorem on network flow

A graph is set  where  is the set of vertices and  is the set of edges connect these vertices.

A directed graph is a graph contains directed edges, that means edges  is different from .

A flow network is directed graph that satisfy:

* Each edge has a capacity and receives a flow. The flow on each edge doesn’t exceed the capacity.
* The total flow into a vertex is equal to the total flow out of it, except the sink (has only ongoing flow) and source (has only outgoing flow).

The min-cut max-flow duality theorem states that in a flow network, the maximum amount of flow from source to sink is also the minimum capacity, when removed in a specific way, such that no flow can pass from source to sink. The solution for min-cut problem is also the solution for max-flow problem and otherwise.

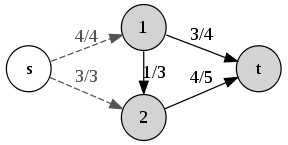


Figure 5. A network with the value of flow equals to the capacity of s-t cut (from [27])

This theorem has been proof by Ford and Fulkerson in 1956 [9]. They also provide a method for solving the max-flow problem in 1962 [10]. It is described more in next section about new algorithm from Yuri Boykov and Vladimir Kolmogorov in 2004 [11].

### Another max-flow algorithm

As mentioned, the object segmentation is interpreted as min-cut max-flow problem. Some solution, such as push-relabel algorithm and Ford-Fulkerson method, had been proposed.

* Ford-Fulkerson method’s main idea is sending flow through all *augmenting paths* from source to sink. The augmenting path concept is the path from source to sink that have available capacity on all edges of the path (e.g. not max flow). However, they didn’t provide a specific way to find augmenting path. In this thesis, the Dinic’s algorithm is used to demonstrate Ford-Fulkerson method [9]. It uses the breadth-first search on residual graph to find the shortest path along non-saturated edges.
* Push-relabel algorithm, also called preflow-push algorithm, initializes a preflow and convert it to maximum flow by *push* operations (moving flow between neighbor vertices) and *relabel* operations (maintaining admissible network). The generic algorithm was also called Goldberg-Tarjan algorithm [17].

In their experiments in paper [1], Yuri Boykov and Jolly used the algorithm proposed by Yuri Boykov and Vladimir Kolmogorov. It’s based on augmenting path. Their main ideas are:

* Building two search trees, one from source and the other from sink
* Reusing these trees and never start building trees from scratch

The algorithm is iterative of three stages until no search tree can grow anymore:

* Growth stage (Figure 6): the two search is grow until they are touch that a path from source to sink is found.
* Augmentation stage: the found path is augmented and the search trees break into forest.
* Adoption stage: the two search tree are restored.

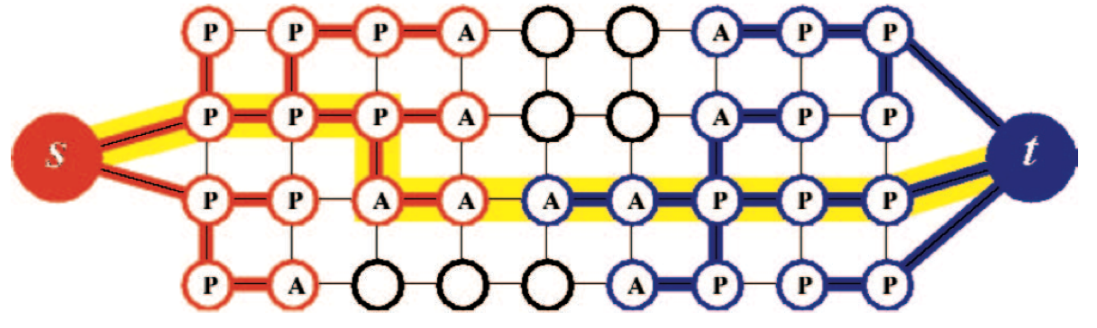


Figure 6. S and T tree at the end of growth stage (from [5])

### Object segmentation to graph cut

As described above, the object segmentation can be solved by using min-cut max-flow theorem. To convert the binary labeling to graph (Figure 7), Boykov and Jolly consider:

* The two destination labels Object () and Background () of object segmentation correspondingly as the source () and sink () in the flow network.
* All pixels in image are internal nodes.
* Each internal node has exactly one flow from source and one flow to sink. It describes how the corresponding pixel associate to object and background class. These flows are called t-links.
* The other flows connect nodes together describe how adjacent pixel related. These flow are called n-links. Since Boykov and Jolly use 4-neighbor of P, each internal node has at most 4 n-links.

The labeling problem now is finding a proper cut through the graph. Each internal node has exactly one t-link join the cut. That also means it “cuts” the relationship of corresponding pixel to the class of another side of that t-link and belongs to the remaining one: t-link from source joins cut, the pixel is background and otherwise.

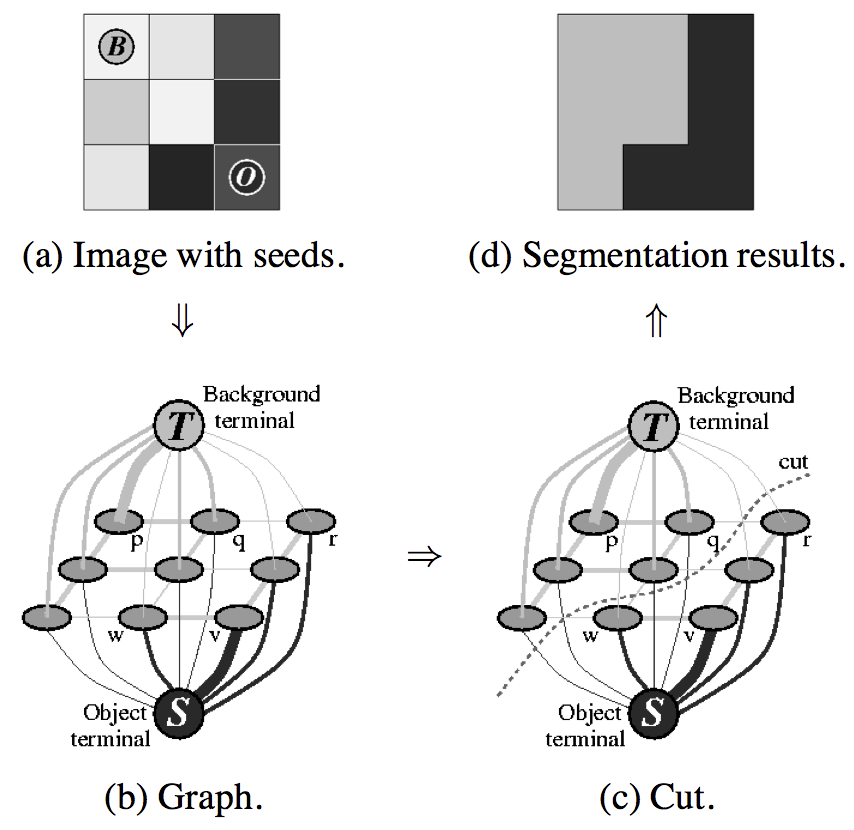


Figure 7. Image segmentation as a graph cut (from [1])

The graph cut separates vertices into two disjoint sets. Correspondingly, the image is separated into two segments. The minimum cost cut creates optimal segmentation, which is based on properties. This cost is built into edge weights.

### Objective function

From section 2.3, we can see the object segmentation as a graph cut.

Boykov and Jolly define feasible cut:

* Each internal node serves exact one t-link
* Each edge belongs to feasible cut if and only if two connected nodes are t-linked different terminal
* Seed nodes belong to feasible cut

In equivalent, the feature cut is respectively the segmentation in the image.

Let  is a  binary vector of pixels that defines a segmentation. Boykov and Jolly see the soft constraints imposed boundary and region properties of as an energy cost function :

 ,

where





and



* The regional term  assumes the penalties of assigning each pixel p to “object” or “background”, respectively  or , are given.  may just the intensity of pixel p fit intensity model of the object or background.
*  contains the boundary properties of . Each coefficient  is discontinuity penalty between two pixel  and . The larger  are, the more similar between  and , otherwise when it approach zero.
* The  term is the relative importance of region properties term  over the boundary term .

Meanwhile, there are some initial background and object pixel, called “seeds”, defined by user. The boundary segmentation must separate background seeds and object seeds. Boykov and Jolly define these hard constraints be the combining of region and boundary properties of segments.

The initial weight of edges in  is described as following table

Table 2. Weight of three types of edge

|  |  |  |
| --- | --- | --- |
| edge | weight (cost) | for |
|  |  |  |
|  |  |  |
|  |  |
|  |  |
|  |  |  |
|  |  |
|  |  |

where



When the user interactively adds or removes the “object” or “background” seeds, the weight of corresponding edges of those seeds is also changed. However, if the weight is changed according to the previous table, we can’t compute from initial flow due to reduction of some edge capacities. But if both t-links are increase a constant, it’s not a problem anymore. For example, user adds a new “object” seeds on pixel p, the new weight can be described as below

Table 3. Cost updating for reusing

|  |  |  |  |
| --- | --- | --- | --- |
| t-link | initial cost | add | new cost |
|  |  |  |  |
|  |  |  |  |

Boykov and Jolly has proved that:

* The minimum cut is a feasible cut
* The minimization of this cost function corresponds to the resulting labelling of the min-cut on the graph. The solution of max-flow min-cut is also the solution of labelling  that minimize energy function .

So, the object segmentation problem is solving the max-flow problem on the converted flow network. We use the Boykov-Kolmogorov algorithm (described in previous section) instead of standard algorithms.

## Experimental Results

In our implementation, the seeds are visualized as green “object” and blue “background”. The seeds have double uses: the hard constraints and the histogram of “object” and “background” intensity distribution. The regional penalties can be negative log-likelihood



We use 8-neighbor for adjacency edges. The boundary penalties are the ad-hoc function with the intensity and pixel-to-pixel distance use Euclidean distance.



Note that the experiment run on Intel Core i5 2.2Ghz. Our implementation use max-flow algorithm described in section 3.2.

### Berkeley segmentation dataset

Table 4. Experiments on Berkeley dataset

|  |  |  |
| --- | --- | --- |
| Image | Image with seeds | Final segmentation |
| 12003 |  |  |
| 35070 |  |  |
| 66075 | C:\Users\Sonata\Desktop\66075_hint.jpg |  |
| 85048 |  |  |
| 124084 |  |  |
| 176035 |  |  |
| 187029 | C:\Users\Sonata\Desktop\187029_hint.jpg |  |
| 187083 | C:\Users\Sonata\Desktop\187083_hint.jpg |  |
| 189011 |  |  |
| 207056 |  |  |
| 227092 | C:\Users\Sonata\Desktop\227092_hint.jpg |  |
| 296059 |  |  |

### Our dataset

Table 5. Experiments on our dataset

|  |  |  |
| --- | --- | --- |
| Name | Image with seeds | Final segmentation |
| 1 |  |  |
| 2 | 2_hint |  |
| 3 | 3_hint |  |
| 4 | 4_hint |  |
| 5 | 5_hint |  |
| 6 | 6_hint |  |
| 7 | 7_hint |  |
| 8 | 8_hint |  |
| 9 | 9_hint |  |
| 10 | 10_hint |  |
| 11 | 11_hint |  |
| 12 | 12_hint |  |

### Discussion

The interactive graph cut has some goods and limitations. In this sections, we will discuss more about limitations.

#### Performance

The most serious problem of interactive graph cut is its performance. For any image, it considers each pixel as a node and its relation to neighbours as edges. That make the graph size huge. For a 2M image, the graph has nearly 2 million nodes and 20 million edges. It surely takes a lot of time to compute the max-flow and consumes tremendous resources. This method is not a good solution for high resolution image which become more and more popular.

#### The effects of lambda

Figure 8 shows the result of segmentation of various lambda. In b, only boundary properties are used, only pixels that “close” (by both intensity difference and Euclidean distance meaning followed the ad-hoc function) to object seeds are shrunk. When region term has more affect (c-e), the color histogram makes the color distribution factor become more and more important over the Euclidean distance, and results in not only the boundary more detailed, but also some outside pixels labelled wrongly.

|  |  |  |  |
| --- | --- | --- | --- |
| 1. Image with seeds and selected red regions for zooming in in results | | | |
|  |  |  |  |

Figure 8. Results of graph cut segmentation with various lambda

The trouble is the “right” value of lambda can’t be automatically computed. The user should manually set until satisfied.

## Conclusion

This project is a simple implementation of the interactive graph cut. It still has many limits. The pixel level of accuracy makes the computation process slow and resource consumption high for high resolution image. Moreover, the balance of boundary and region terms is not easily archived to get satisfied result. However, it is a good base for later solution in term of conversion between image components and graph cut, also the energy function construction. The Lazy Snapping in next chapter is a good instance for such solutions.

# Lazy Snapping

## Problem statement

Interactive single-image segmentation (or image cutout) is one of the popular problems in Computer Vision. A user typically provides samples of foreground (the part that you want to cut out) and background by drawing some strokes in each parts or a coarse bounding box of the object in the image. Then the algorithm bases on the information with the added hard constraints for some pixels to separate the object from the alternative background. By the time, there would have had many improvement and new method to solve the problem. Yuri Boykov and Marie-Pierre Jolly [1] provided a method using energy minimization to solve the problem and up to now, that is the heart of most recent technique.

Computer is still long way to recognize objects in picture, so that, the user has to give samples of each region with high accuracy. In common, a user gives the sample data for both foreground and background that defined as foreground seeds *F* and background seeds *B*. All the another pixel that is not marked defined as “uncertain region” *U* in the image, as show in Figure 9.

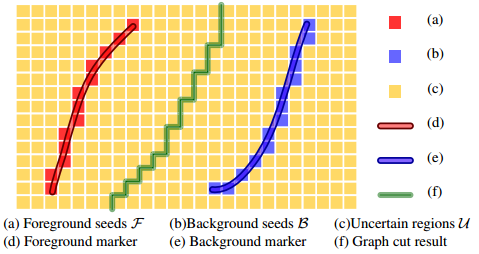


Figure 9. Sample pixels of background/foreground and uncertain region from paper [2]

To be more formal:

Suppose we have an input image ** and some sets of pixels:

* Foreground Set : set of all pixels that are sample for the object.
* Background Set : set of all pixels that are sample for the background.
* Uncertain Set : set of all pixels that are not in the both and .

How to figure out all the pixels belong to the object in the image and separate them from the background?

## Casting the problem as binary labelling problem

### Binary images: foreground, background and connectivity

A binary image is an image in which each pixel belongs to one of only two possible discrete, logical value: 1 or 0. In our problem, the logical value 1 is known as ‘object’, whilst the logical value 0 is described as ‘not object’. Base on the logical value in the binary image, we define the set of pixels which the logical value is 1/0 as the temp *foreground* pixel/*background* pixel. An *object* is created by groups of *connected* pixels.

There are 2 common definition of connection between pixels in the image:

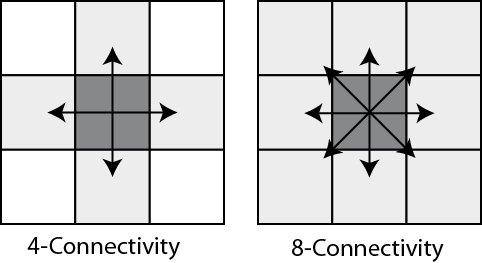


Figure 10. 4-connected pixel and 8-connected pixel examples from [23]

* If we required that a given foreground pixel must have at least on neighboring foreground pixel to 4 directions: north, south, east or west of itself to analyze them as parts of the object, then we are using 4-connection.
* However, in case we need 4 another direction: north-east, north-west, south-east or south-west to analyze, then we are using 8-connection.

### Formulation, constraint and energy function

Based on the approach present in [25], we can formulate our image cut-out problem as a binary labelling problem:

* For all image pixels, we need to assign a unique label 
* If a pixel is in , the label of it is foreground/background.
* If a pixel is not in and , the temporary label of it ‘uncertain’.

How to find a way to label all pixels in the image so that all the pixels belong to the object we want to select have same label, and so do to all the another pixel?

We define the constraints:

***Data constraint***: If a pixel has its colour similar to at least one pixel belongs to foreground seeds *F*, it is more likely to get foreground label, and so do with background seeds *B*.

***Prior constraint***: Pixels that belong to the object tend to group together, and pixels that belong to background tend to group together.

To find a labelling that satisfy our constraints, we have to formulate and minimize an energy function of labelling:

Let  be the label value of pixel , so that .

Firstly, we model the data constraint by using Data Penalty Function  that is defined as follows:



With the pixels that belong to ‘uncertain’ region, we follow some steps such as [2]:

1. Use K-means method to cluster the color of foreground seeds and background seeds . (In this experiment, we try with K = 64)

The mean colors of each set are denote as  and 

1. Suppose each node  has its color , we compute the minimum distance from its color to all clusters of each set, defined as  and :



Therefore, we complete the data constraint with the following table after model the constraint for ‘uncertain’ region



To figure out how image satisfy the data constraint, we sum up all pixels’ penalty function:



Before modeling the prior constraint, we will see two examples about ‘discontinuity’ in labelling  in following figure.

|  |  |
| --- | --- |
| 4   1. 8 discontinuities | 6   1. 31 discontinuities |

Figure 11. Example about discontinuities in binary image (from [26])

Pixel  and  exist a discontinuity if . By that, each pixel belongs to the object boundary have some discontinuities pixels around. We model the prior constraint as a function of the color gradient for all discontinuities:



where:

* + 
  + is the L2-Norm of RGB color difference between two pixels  and .

More detailed, we use Euclidean distance to compute. The more similar the colors or two neighbor pixels are, the less likely belong to different categories.

Finally, we have our final energy equation, which need to satisfy both data constraint and prior constraint:



Where know as a balancing parameter between the data constraint and the prior constraint, from [25], here is the conclusion:

* The larger the, the less discontinuities in the optimal labelling .
* The smaller the, the more the optimal labelling .

## Max flow/min cut problem

This section is short summarize that taken from [22].

### Network

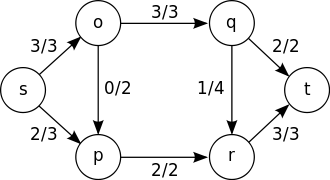


Figure 12. An example of maximum flow from source s to sink t (from [27])

Network is a directed graph  that have n vertices and m edges, include 2 separate vertices are “s” and “t”, where s is the source and t is the sink of the network. With each edge is assigned a non-negative number that is the capacity of that edge.

### The concept of flow in network

Suppose we have network . We have *flow* in network  is an operation that assign with a non-negative number that call a flow in the edge , satisfy 3 constraints:

* ***Capacity Constraint***: Flow in each edge have not to over than the capacity of that edge: 
* ***Skew symmetry***: , flow in edge  and flow in edge  have the same value but opposite sign:
* ***Flow Conservation***: Every vertices  that is not the source and the sink, sum of all in-flow that go to  equal to sum of all out-flow that go out :



The ‘value’ of a flow is defined as (sum of the edge that go out from the source) minus (sum of the edge that go in the source):



Because the value of the flow  in each edge is non-negative, we can also call  is positive flow in the network .

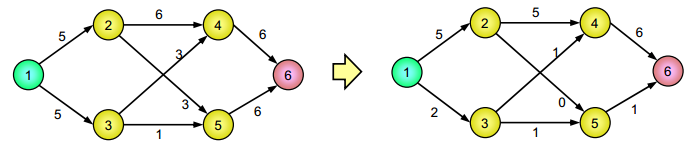


Figure 13. A sample of network with the capacity of each edge (1 is source, 6 is sink) and a flow of it with value is 7 (from [22]).

### Max flow problem

Suppose we have a network , find flowthat have maximum value?

Without loss of generality, in the max flow problem, we can suppose that with every flow, flow in edge  and flow in edge  are simultaneously positive. Because if we just decrease both  and  by a number that equal with, we will get a new flow which have the same value with original flow, include or.

### Basic properties

We have  and  are two subset of vertices set , we call the capacity from to is:



and the value of flow from to is:



*Theorem 1*:

1. , we have 
2. , we have 
3. , we have 
4. , we have 

Proof:

* , we have , both the value of  and  appear in the flow value. We also have (skew symmetric constraint), so 
* we have  and .  appears in  and  appears in , follow skew symmetric, we have 
* = =  +  = 
* , we have  (flow conservation constraint), so we have, then  (also ).

### The concepts of residual graph and augmenting path

#### Residual network

From a network  and a flow  in , we create a network  with the set of edges  is defined as the set of edges  without *fully saturated* edges (an edge is fully saturated if flow in the edge exactly equal to the capacity of that edge):



The capacity of edge  in is computed by:



with s is the source and t is the sink in .

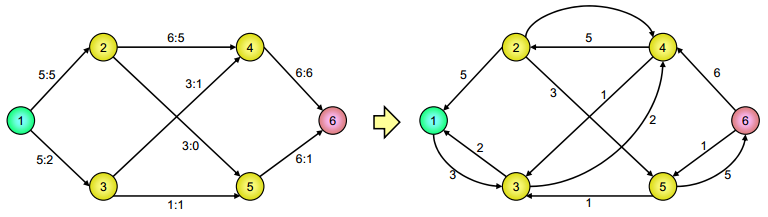


Figure 14. Network  and residual network  (from [22])

That is definition of  is called residual network of the network  that create by flow .

*Theorem 2*: Suppose we have network  and a flow . Call  is a flow in . Then  is also a flow in network  with flow value is . The flow  is defined as:



Proof: We prove that flow  satisfy 3 constraints of flow definition.

* ***Capacity Constraint***: .

Because  so 

* ***Skew symmetry***: .



* ***Flow Conservation***: .



About the value of flow, we have:



Theorem 2 is proved.

#### Augmenting Path

We have a network  and a flow , a path from A to B in network  is called an augmenting path.

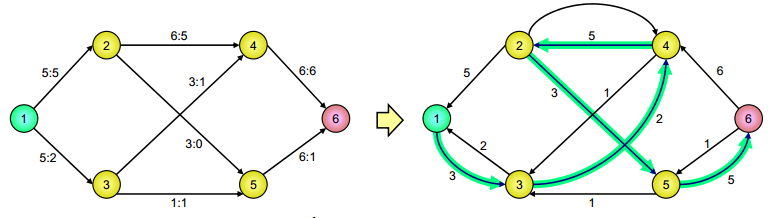


Figure 15. Residual network and an augmenting path (from [22])

With an augmenting path , we defined  is minimum value of capacities in each edges of .  is called residual capacity of .

*Theorem 3*: With  is an augmenting path then the value  is defined as:



is a flow in.

Proof: It is easy to prove  satisfy 3 constraints. Theorem 3 hold unconditionally.

*Theorem 4*: Suppose we have network  and flow, if is an augmenting path in residual network  then the operation  is a new flow in  which have value equal to .

Proof: From theorem 2 and 3, we have theorem 4 is proved.

Operation  is called increase flow follow augmenting path .

### Cut in network

We call a cut  is a way to separate the vertices set  to 2 different and not null subset  and . The cut that satisfy and is called s-t cut. Capacity of the cut  is defined as:



and the flow value of the cut  is defined as:



*Theorem 5*: Suppose we have network  and flow , then the flow pass through any s-t cut have value .

Proof:  is a s-t cut of the network.



*Theorem 6*: Suppose we have network  and flow , and  is a s-t cut, then the flow pass through cut  is not over than the capacity of the cut :



Proof:



Therefore, value of any flow  in network  is not over than the capacity of a s-t cut.

From theorem 2 and 3:



*Theorem 7*: If  is a flow in network  with source s and sink t, then three following clauses are equivalent:

1.  is maximum flow in 
2. Residual network  does not have any augmenting paths.
3. Exist a s-t cut  with 

Proof:

* 

We argue by contradiction that  has an augmenting path, then we have  is also a flow in network  and the value of new flow  is bigger than , when  is maximum flow in network , which mean that contradiction is wrong which proves the required claim.

* 

If  does not have any augmenting paths, we have:

* + 
  + 

which  (because there is not existed path from  to  ), we deduce  is a  cut.  and, we have  because if  then there exists an edge  in  so we have a path from  to  , contradict to the definition of cut. By that, we have .

* 

Follow theorem (3), the value of every flow in network  , so if the value of the flow  exactly equal to the capacity of the cut , then  have to be maximum flow value in the network.

**Definition**: s-t cut have smallest capacity (equal to maximum value in the network) is called minimum s-t cut of the network .

### Minimum cut problem

Suppose we have network , find a  cut that satisfy sum of all cost in edges set is minimum to disconnect s from t?

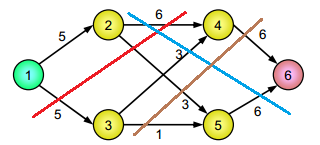


Figure 16. Which is minimum cut in network? (from [22])

## The graph-cut solution to the image cutout problem

Minimum cut problem gave us a new approach that is called ‘graph cut’. If we can represent the cut-out image problem as binary labelling problem, then model the problem to become a network G, the original problem will be solved. This section discusses details of the “**Silent Lazy Snapping**” approach that developed and implemented by Tran Hoang Nam, FPT University, Vietnam.

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| C:\Users\Sonata\Desktop\TestImage\2\2.jpg | C:\Users\Sonata\Desktop\TestImage\2\12\draw.jpg | E:\FPT\Graduation Assignment\Image\waterShed\flowers.jpg-kmeans.png | C:\Users\Sonata\Desktop\TestImage\2\12\object.jpg | C:\Users\Sonata\Desktop\13588844_10201521755641447_1668599256_o.jpg |
| C:\Users\Sonata\Desktop\TestImage\2\9\waterShed.bmp |
| C:\Users\Sonata\Desktop\TestImage\2\10\waterShed.bmp |
| C:\Users\Sonata\Desktop\TestImage\2\12\contours.png |
| 1. *Input image* | 1. *Object marking* | 1. *Presegmentation* | 1. *Final segmentation* | 1. *Output Composition* |
| *Silent Lazy Snapping is an interactive image cutout framework, consisting of two steps: a quick object marking step and a simple segment editing step. In [b], the (blue) lines are drawn to indicate the foreground, and another (red) line to indicate the background. In [c], we apply several method to separate pixels in the input image into super pixels. Based on result of SEEDs Revised Mean Value method [c – image in the bottom], a good final segmentation with accurate boundary can be obtained by simply clicking to non-object super pixels in [d]. Finally, the cut out is composed on another painting in [e].* | | | | |

Figure 17. An example of Silent Lazy Snapping process

### Sample define by users

Define action that user gives example to foreground/background. In this experiment, we use two following events:

* Press-button-f-event: allow user to change to foreground mode.
* Press-button-b-event: allow user to change to background mode.
* Left-mouse-click-event: allow user to visualize examples by drawing some strokes in the input image.
  + Every points in the strokes present for foreground will be display by blue point.
  + Every points in the strokes present for background will be display by red point.

|  |  |
| --- | --- |
|  |  |

Figure 18. Input image (left image) and image with examples given by user (right image)

* Reload-image-event: allow user to reload the input image in case their examples are not exactly what they want to draw.
  + More detailed, in this experiment, user can reload image when click ‘r’ button in the keyboard.

|  |  |
| --- | --- |
|  |  |

Figure 19. Image with wrong examples given by users (left image) and reload image (right image)

After finishing this step, we have pixels under markers as SEEDS.

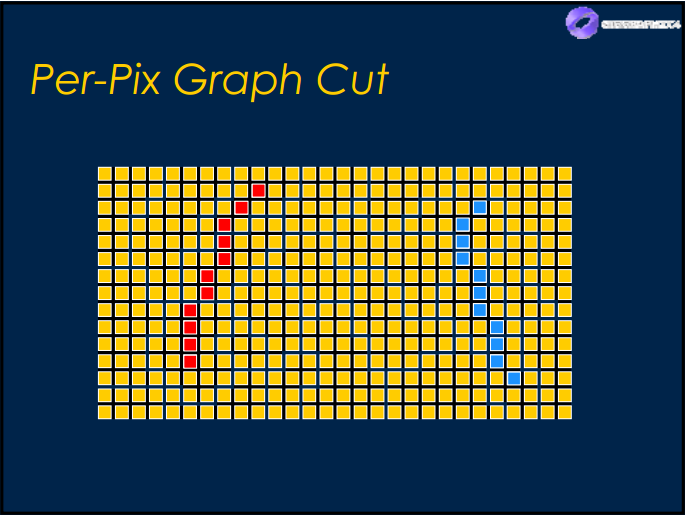


Figure 20. SEEDS pixels for foreground and background (from [25])

### Pre-segmentation

#### Experiment by using different methods

The original image will be segmented into small fragments using the watershed algorithm. Each fragment is represented by a *Super Pixel* with color is computed by mean color of the all pixels belong to the segment. The purpose of this step is to reduce the number or vertices need to add to graph. This initialization step increases the speed of algorithm.

In my experiment, I used 4 methods to pre-segment the image to compare the result that present in Table 6.

* K-means method (OpenCV 2.4.1.3 – Java Implementation)
* Watershed method (OpenCV 3.1.0 Library – C++ Implementation): This implementation is based on “Watersheds in digital spaces: an efficient algorithm based on immersion simulations” of [Vincent and Soille, 1991]
* SEEDs Superpixels method (OpenCV 3.1.0 – C++ Implementation): This implementation is based on a contributed module in Extened Image Processing – OpenCV 3.1.0
* SEEDs Revised Mean Pixels method (OpenCV 3.1.0 – C++ implementation) is based on Superpixel Segmentation using Depth Information, D. Stutz, A. Hermans, B. Leibe, 2014

Table 6. Results of different segmentation methods

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Image Size | Original Image | K-means method | Watershed method | SEEDs Superpixels method | SEEDs Revised Mean Pixels |
| 481 x 321 pixel | E:\FPT\Graduation Assignment\Image\waterShed\flowers.jpg  124084 | E:\FPT\Graduation Assignment\Image\waterShed\flowers.jpg-kmeans.png  1737 segments | C:\Users\Sonata\Desktop\TestImage\2\waterShed.bmp  504 segments | C:\Users\Sonata\Desktop\TestImage\2\11\waterShed.bmp  600 segments | C:\Users\Sonata\Desktop\TestImage\2\12\contours.png  800 segments |
| 481 x 321 pixel | E:\FPT\Graduation Assignment\Image\waterShed\mexicanhat.jpg  189011 | E:\FPT\Graduation Assignment\Image\waterShed\mexicanhat.jpg-kmeans.png  1194 segments | C:\Users\Sonata\Desktop\TestImage\19\waterShed.bmp  351 segments | C:\Users\Sonata\Desktop\TestImage\19\3\waterShed.bmp  800 segments | E:\FPT\Graduation Assignment\Demo\20160628_Demo11\Lazy_Snapping\LazySnappingExperiment\LazySnappingExperiment\contours.png  800 segments |
| 321 x 481 pixel | E:\FPT\Graduation Assignment\Image\waterShed\nemo.jpg  210088 | E:\FPT\Graduation Assignment\Image\waterShed\nemo.jpg-kmeans.png  1534 segments | C:\Users\Sonata\Desktop\TestImage\10\waterShed.bmp  436 segments | C:\Users\Sonata\Desktop\TestImage\10\2\waterShed.bmp  800 segments | E:\FPT\Graduation Assignment\Demo\20160628_Demo11\Lazy_Snapping\LazySnappingExperiment\LazySnappingExperiment\contours.png  800 segments |
| 321 x 481 pixel | E:\FPT\Graduation Assignment\Image\waterShed\standing.jpg  388016 | E:\FPT\Graduation Assignment\Image\waterShed\standing.jpg-kmeans.png  3160 segments | C:\Users\Sonata\Desktop\TestImage\20\waterShed.bmp  203 segments | C:\Users\Sonata\Desktop\TestImage\20\1\waterShed.bmp  800 segments | C:\Users\Sonata\Desktop\TestImage\20\2\contours.png  800 segments |
| 481 x 321 pixel | E:\FPT\Graduation Assignment\Image\waterShed\tiger-lake.jpg  108073 | E:\FPT\Graduation Assignment\Image\waterShed\tiger-lake.jpg-kmeans.png  4124 segments | C:\Users\Sonata\Desktop\TestImage\7\waterShed.bmp  212 segments | C:\Users\Sonata\Desktop\TestImage\7\2\waterShed.bmp  800 segments | E:\FPT\Graduation Assignment\Demo\20160628_Demo11\Lazy_Snapping\LazySnappingExperiment\LazySnappingExperiment\contours.png  800 segments |
| 481 x 321 pixel | E:\FPT\Graduation Assignment\Image\waterShed\swimmer.jpg  153077 | E:\FPT\Graduation Assignment\Image\waterShed\swimmer.jpg-kmeans.png  1045 segments | C:\Users\Sonata\Desktop\TestImage\1\waterShed.bmp  548 segments | C:\Users\Sonata\Desktop\TestImage\1\8\waterShed.bmp  800 segments | C:\Users\Sonata\Desktop\TestImage\1\9\contours.png  800 segments |
| 481 x 321 pixel | E:\FPT\Graduation Assignment\Image\waterShed\lantern.jpg  65019 | E:\FPT\Graduation Assignment\Image\waterShed\lantern.jpg-kmeans.png  2260 segments | C:\Users\Sonata\Desktop\TestImage\4\waterShed.bmp  742 segments | C:\Users\Sonata\Desktop\TestImage\4\12\waterShed.bmp  600 segments | E:\FPT\Graduation Assignment\Demo\20160628_Demo11\Lazy_Snapping\LazySnappingExperiment\LazySnappingExperiment\contours.png  800 segments |
| 481 x 321 pixel | C:\Users\Sonata\Desktop\TestImage\data-visioner\images\moose.jpg  41004 | C:\Users\Sonata\Desktop\TestImage\data-visioner\images\moose.jpg-kmeans.png  1862 segments | E:\FPT\Graduation Assignment\Demo\20160601_Demo1_Main\Lazy_Snapping\LazySnappingExperiment\LazySnappingExperiment\waterShed.bmp  278 segments | E:\FPT\Graduation Assignment\Demo\20160625_Demo10\Lazy_Snapping\LazySnappingExperiment\LazySnappingExperiment\waterShed.bmp  800 segments | E:\FPT\Graduation Assignment\Demo\20160628_Demo11\Lazy_Snapping\LazySnappingExperiment\LazySnappingExperiment\contours.png  800 segments |
| 481 x 321 pixel | C:\Users\Sonata\Desktop\TestImage\data-visioner\images\chetah.jpg  160068 | C:\Users\Sonata\Desktop\TestImage\data-visioner\images\chetah.jpg-kmeans.png  2784 segments | E:\FPT\Graduation Assignment\Demo\20160601_Demo1_Main\Lazy_Snapping\LazySnappingExperiment\LazySnappingExperiment\waterShed.bmp  328 segments | E:\FPT\Graduation Assignment\Demo\20160625_Demo10\Lazy_Snapping\LazySnappingExperiment\LazySnappingExperiment\waterShed.bmp  800 segments | E:\FPT\Graduation Assignment\Demo\20160628_Demo11\Lazy_Snapping\LazySnappingExperiment\LazySnappingExperiment\contours.png800 segments |
| 481 x 321 pixel | C:\Users\Sonata\Desktop\TestImage\17\17.jpg  296059 | C:\Users\Sonata\Desktop\My Test - Writing\data-visioner101\elephant.png  859 segments | E:\FPT\Graduation Assignment\Demo\20160601_Demo1_Main\Lazy_Snapping\LazySnappingExperiment\LazySnappingExperiment\waterShed.bmp  82 segments | E:\FPT\Graduation Assignment\Demo\20160625_Demo10\Lazy_Snapping\LazySnappingExperiment\LazySnappingExperiment\waterShed.bmp  800 segments | C:\Users\Sonata\Desktop\TestImage\17\2\contours.png800 segments |
| 481 x 321 pixel | C:\Users\Sonata\Desktop\TestImage\data-visioner\images\tiger.jpg  108005 | C:\Users\Sonata\Desktop\My Test - Writing\data-visioner101\tiger.png  4520 segments | E:\FPT\Graduation Assignment\Demo\20160601_Demo1_Main\Lazy_Snapping\LazySnappingExperiment\LazySnappingExperiment\waterShed.bmp  303 segments | E:\FPT\Graduation Assignment\Demo\20160625_Demo10\Lazy_Snapping\LazySnappingExperiment\LazySnappingExperiment\waterShed.bmp  800 segments | E:\FPT\Graduation Assignment\Demo\20160628_Demo11\Lazy_Snapping\LazySnappingExperiment\LazySnappingExperiment\contours.png800 segments |

#### Conclusion for pre-segmentation

The label of each segment base on pre-segmentation step is very important for initializing and processing graph cut algorithm. There are some problems in pre-segmentation step that need to define before go to conclusions:

* Over-segmentation: pixels belong to same object are classified as belonging to different segments. A single object may be represented by two or more segments.
* Under-segmentation: pixels belong to different objects are classified as belonging to the same object. A single segment may contain several objects.

|  |  |
| --- | --- |
|  | *(Top – Left) Original image*  *(Top – Right) Correct segmentation*  *(Bottom – Left) Over-segmentation*  *(Bottom – Right) Under-segmentation* |

Figure 21. Example about pre-segmentation (from [24])

In my experiment, after compare the results of each method, I have some following conclusions in Table 7.

Table 7. Comparison and conclusion of each method

|  |  |
| --- | --- |
| Method | Problem |
| K-means | C:\Users\Sonata\Desktop\TestImage\data-visioner\images\tiger-lake.jpg-kmeans.png4124 segments  (**Over-segmentation problem**)  Cannot control the number of segments.  The number of segments usually is usually bigger than other methods. Each segment is a set of pixels have same color, not a region in the image.  Easy to implement, but require a lot of time and memory spend for pre-segmentation step.  Based on segment information given by K-means, Graph Cut algorithm run slow and inaccuracy. |
| Watershed | C:\Users\Sonata\Desktop\TestImage\7\waterShed.bmp212 segments  (**Under-segmentation problem)**  Cannot control the number of segments.  The number of segment is usually smaller than other methods. There are many regions that include pixels belong to object and another pixel belong to background. Depend on the value of threshold parameter, so pre-segmentation step run unstably.  In some cases, the number of segment is small enough with good segments that make Graph Cut algorithm get good results in small time. But with each image, we have to do experiment with threshold value to get best result make this method hard to use. |
| SEEDs Superpixels | C:\Users\Sonata\Desktop\TestImage\7\2\waterShed.bmp800 segments  **(Under-fitting boundary problem)**  Can control the number of segments by setting parameter.  By that, the number of segment is small enough to make Graph Cut algorithm run in time. There are few regions, especially in the boundary of object that include pixels belong to object and another pixel belong to background make the boundary of the selected object is unsmooth and low accuracy.  Depend on the number of iteration parameter: the bigger iteration parameter is, the higher accuracy in each region, and the slower pre-segmentation step is and vice versa.  In most of cases, Graph Cut algorithm get exactly regions that belong to object based on segment information of this method. But boundary of the object is unsmooth even you increase iteration parameter as big as possible. |
| SEEDs Revised Mean Pixels | E:\FPT\Graduation Assignment\Demo\20160628_Demo11\Lazy_Snapping\LazySnappingExperiment\LazySnappingExperiment\contours.png800 segments  Can control the number of segments by setting parameter.  Not even make Graph Cut algorithm run in time, there are rarely regions that belong to both foreground and background. The boundary of each region is closed and smooth such as original image.  Depend on the number of iteration parameter (same as SEEDs Superpixels method)  In most of cases, Graph Cut algorithm get good final segmentation based on segment information of this method. Boundary of the object is smooth, but with low contract image or image that foreground and background have same color, it is still a hard problem. |

Table 8 will show more detailed about the different in same image “296059” of Berkeley dataset after pre-segmentation step between SEEDs Superpixels method and SEEDs Revised Mean Pixels:

Table 8. Detailed comparison about SEEDs Superpixels and SEEDs Revised Mean Pixels

|  |  |  |
| --- | --- | --- |
| Parameter | E:\FPT\Graduation Assignment\Image\e1.PNG | E:\FPT\Graduation Assignment\Image\e2.PNG |
| Number of iterations | 2000 | 500 |
| Number of super-pixel | 800 | 800 |
| Number of histogram bin | 10 | 10 |

Perfect image segmentation - each pixel is assigned to the correct object segment is a goal that cannot usually be achieved. On one hand, with image that object and background have different color, all method return good label results. On another hand, when the color of background is the same with color in object, it is hard to get good segments to separate these regions.

Each method has advantages and disadvantages, so we need to base on image information and the expected value of user to choose appropriate method.

### Transfer label data to vertices in graph

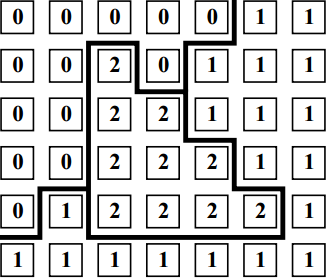


Figure 22. Marker matrix from pre-segmentation step (from [11])

Base on the segment result of pre-segmentation steps, we have marker matrix that present in Figure 12. Each segment has same label value.

To initialize the necessary information for Graph Cut algorithm to create a network, I do some following steps:

* Determine number of vertices in network by counting the number of segments
* Compute mean value of each segments – super pixel
* Determine number of edges in network by finding two pixels that have different label and create edge list.
* Based on samples given by user, we determine new label value of the corresponding sample pixel and mark vertices connect to terminal
  + If sample pixel ** belongs to foreground, we mark vertex  (the new label value of pixel ** is ) connect to source.
  + If sample pixel  belongs to background, we mark vertex  (the new label value of pixel  is ) connect to sink.
* Apply K-means function provided OpenCV to create information for “source” super pixel and “sink” super pixel.
* Compute edge in the edge list
  + Compute  energy – the cost for connecting a pixel and a terminal.
  + Compute  energy – the cost for every pairs of neighboring pixels.

Use information from marker matrix and SEEDS pixels, we finish this initialization step.

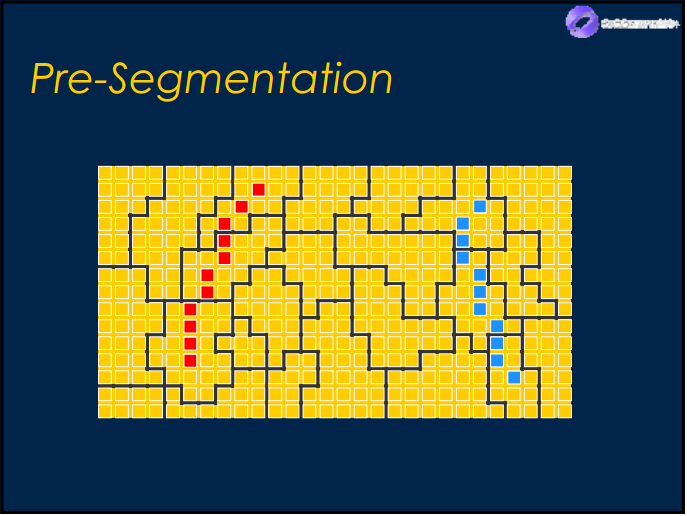


Figure 23. Combine information between marker matrix and SEEDS pixels (from [25])

### Graph cut algorithm and final segmentation

In this experiment, we use graph cut solution of Yuri Boykov and Vladimir Kolmogorov present in [7]. They provided a useful library to solve maximum flow problem, so that we just need to call max-flow() interface to get the result and labelling of each vertices.

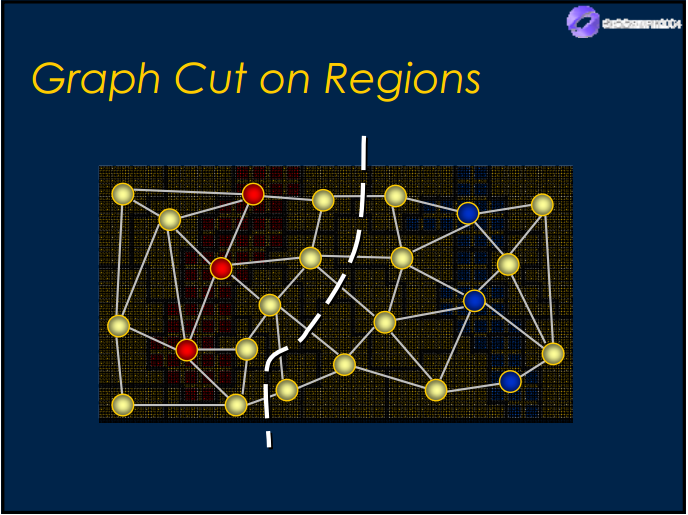


Figure 24. Apply Graph Cut solution on regions (from [25])

After running max flow algorithm, we have the image selection label of all vertices with the value defined as {GraphType::SOURCE, GraphType::SINK}.

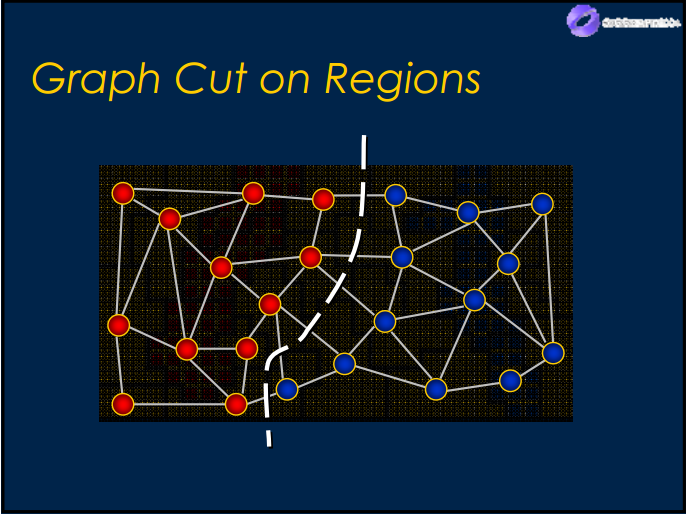


Figure 25. Vertices separate to 2 sets by minimum cut in network (from [25])

We transfer label value of vertices back to all regions in the original image, change color of background regions to get final segmentation – object selection.

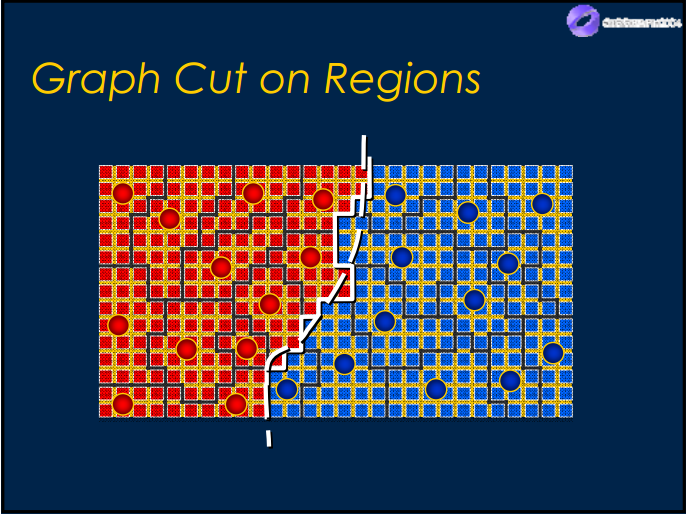


Figure 26. Transfer label back to original image (from [25])

## Experimental results

### Berkeley segmentation dataset

Table 9. Experiment of Nam's solution in Berkeley segmentation dataset

|  |  |  |
| --- | --- | --- |
| Image | Image with seeds | Final segmentation |
| 12003 | C:\Users\Sonata\Desktop\Image For Final Report - Writing\sea star\1\draw.bmp | C:\Users\Sonata\Desktop\Image For Final Report - Writing\sea star\1\object.jpg |
| 85048 | C:\Users\Sonata\Desktop\Image For Final Report - Writing\worker\1\draw.jpg | C:\Users\Sonata\Desktop\Image For Final Report - Writing\worker\1\object.jpg |
| 207056 | C:\Users\Sonata\Desktop\Image For Final Report - Writing\48\1\draw.jpg | C:\Users\Sonata\Desktop\Image For Final Report - Writing\48\1\object.jpg |
| 227092 | C:\Users\Sonata\Desktop\Image For Final Report - Writing\jar\4\draw.jpg | C:\Users\Sonata\Desktop\Image For Final Report - Writing\jar\4\object.jpg |
| 124084 | C:\Users\Sonata\Desktop\Image For Final Report - Writing\flower\2\draw.jpg | C:\Users\Sonata\Desktop\Image For Final Report - Writing\flower\2\object.jpg |
| 189011 | C:\Users\Sonata\Desktop\Image For Final Report - Writing\big_hat_boy\draw.bmp | C:\Users\Sonata\Desktop\Image For Final Report - Writing\big_hat_boy\object.bmp |
| 187029 | C:\Users\Sonata\Desktop\Image For Final Report - Writing\32\draw.jpg | C:\Users\Sonata\Desktop\Image For Final Report - Writing\32\object.jpg |
| 296059 | C:\Users\Sonata\Desktop\TestImage\17\2\draw.jpg | C:\Users\Sonata\Desktop\Image For Final Report - Writing\elephant\2\object.jpg |
| 66075 | C:\Users\Sonata\Desktop\Image For Final Report - Writing\44\draw.jpg | C:\Users\Sonata\Desktop\Image For Final Report - Writing\44\object.jpg |
| 176035 | C:\Users\Sonata\Desktop\TestImage\30\3\draw.jpg | C:\Users\Sonata\Desktop\TestImage\30\3\object.jpg |
| 187083 | C:\Users\Sonata\Desktop\Image For Final Report - Writing\old_woman\3\draw.jpg | C:\Users\Sonata\Desktop\Image For Final Report - Writing\old_woman\3\object.jpg |
| 35070 | C:\Users\Sonata\Desktop\Image For Final Report - Writing\chuon chuon\draw.jpg | C:\Users\Sonata\Desktop\Image For Final Report - Writing\chuon chuon\object.jpg |

### Our dataset

Table 10. Experiment of Nam's solution in his own dataset

|  |  |  |
| --- | --- | --- |
| Image | Image with seeds | Final segmentation |
| Nam\_1 | C:\Users\Sonata\Desktop\My Test - Writing\M2\1\draw.bmp | C:\Users\Sonata\Desktop\My Test - Writing\M2\1\object.bmp |
| Nam\_2 | C:\Users\Sonata\Desktop\My Test - Writing\M8\draw.jpg | C:\Users\Sonata\Desktop\My Test - Writing\M8\object.jpg |
| Emily\_Child | C:\Users\Sonata\Desktop\My Test - Writing\M18\2\draw.jpg | C:\Users\Sonata\Desktop\My Test - Writing\M18\2\object.jpg |
| Emily\_Dance | C:\Users\Sonata\Desktop\My Test\M30\1\draw.bmp | C:\Users\Sonata\Desktop\My Test - Writing\M30\object.jpg |
| Vango | C:\Users\Sonata\Desktop\My Test - Writing\L6\1\draw.jpg | C:\Users\Sonata\Desktop\My Test - Writing\L6\1\object.jpg |
| River\_Safari | C:\Users\Sonata\Desktop\My Test - Writing\M21\1\draw.bmp | C:\Users\Sonata\Desktop\My Test - Writing\M21\1\object.jpg |
| LSPaper | C:\Users\Sonata\Desktop\Image For Final Report - Writing\girl_with_birds\1\draw.jpg | C:\Users\Sonata\Desktop\Image For Final Report - Writing\girl_with_birds\1\object.jpg |
| WSPaper | C:\Users\Sonata\Desktop\Image For Final Report - Writing\elena\1\draw.jpg | C:\Users\Sonata\Desktop\Image For Final Report - Writing\elena\1\object.jpg |
| Flower | C:\Users\Sonata\Desktop\My Test - Writing\M6\2\draw.jpg | C:\Users\Sonata\Desktop\My Test - Writing\M6\2\object.jpg |
| Cat | C:\Users\Sonata\Desktop\Image For Final Report - Writing\cat\3\draw.jpg | C:\Users\Sonata\Desktop\Image For Final Report - Writing\cat\3\object.jpg |
| Horse | C:\Users\Sonata\Desktop\My Test - Writing\M50\draw.jpg | C:\Users\Sonata\Desktop\My Test - Writing\M50\object.jpg |
| Sona | C:\Users\Sonata\Desktop\My Test\L4\1\draw.jpg | C:\Users\Sonata\Desktop\My Test\L4\1\object.jpg |
| MocChau | C:\Users\Sonata\Desktop\My Test - Writing\L1\1\draw.jpg | C:\Users\Sonata\Desktop\My Test - Writing\L1\1\object.jpg |
| TrangAn | C:\Users\Sonata\Desktop\My Test - Writing\L2\1\draw.jpg | C:\Users\Sonata\Desktop\My Test - Writing\L2\1\object.jpg |

### 

### Results and Discussion

Some tests result that shown in two sections 5 and 6. There are some good segmentation that we can observe. However, there are 3 limitations I want to discuss in this section.

#### Pixel loss in thin area

We can see very clear in the test result of image “189080”. When the pixels belong to object are in very thin area, they can be segmented into fragments that include both background pixels. When the size of the area is too small, it will be merge into the Super Pixel around so that cannot be separated out.

|  |  |
| --- | --- |
| C:\Users\Sonata\Desktop\Image For Final Report - Writing\old_man_2\189080_draw.bmp | C:\Users\Sonata\Desktop\TestImage\16\1\189080_object.bmp |

Figure 27. Image with pixel loss in left and right shoulder of the old man (right picture)

#### Unsmooth boundary

The test result of image “Emily\_Dance” shows unsmooth boundaries of the segmentation. The reason is the colour similarity at the edge of the object and background.

|  |  |
| --- | --- |
| C:\Users\Sonata\Desktop\My Test\M30\1\draw.bmp | C:\Users\Sonata\Desktop\My Test - Writing\M30\object.jpg |

Figure 28. Image with unsmooth boundary in dress of the girl (right picture)

#### Poor performance when foreground and background have similar color distribution

When the foreground and the background have similar color distribution, the color difference between each segments has the same value, so the graph cut solution return inaccurate segmentation like we see in the test result of image “Vango”.

|  |  |
| --- | --- |
| C:\Users\Sonata\Desktop\My Test - Writing\L6\1\draw.jpg | C:\Users\Sonata\Desktop\My Test - Writing\L6\1\object.jpg |

Figure 29. Image with poor performance when the color of foreground and background are similar in the leg of the girl (right picture)

## Conclusion

This project is a simple implementation that based on Lazy Snapping paper to create an interactive segmentation tool. The algorithm and the implementation used openCV library (open source) and max-flow-v3.01 library (open source provided by Yuri Boykov research website). On my laptop (Processor Inter® Core™ i5-3210M 2.50GHz, 6.00 GB RAM), after initializing steps, the project returns final segmentation result quite fast (equal or less than 0.6 sec with Berkeley dataset). However, the boundaries sometimes are unsmooth. The higher accurate in pre-segmentation step when increase the iteration parameter, the better result return and the slower program run. Accept to get better result will pay by time and accept to run faster will pay by accuracy.

Unlike the original Lazy Snapping method [2], we replace the traditional watershed segmentation method [14] with super-pixel segmentation [8] method with the same purpose of dimensionality reduction. However, super-pixel segmentation shows its advantages, such as simpler implementation and better cutout result.

# 

# Conclusion

We have implemented the Graph Cut for Interactive Segmentation and Lazy Snapping. The key things are constructing the graph from the image and forming the energy function. In the Boykov-Jolly’s solution, each pixel is directly mapped to a node, and the energy involves both boundary and region properties. In Lazy Snapping, a node maps to a segment with objective function combines likelihood and prior energy.

To be more specific, we have read more about the min-cut max-flow algorithm and focused on the suggestion algorithm of Boykov and Kolmogorov. We also read, get and implemented the idea to convert the image to the graph: a pixel to a node, the neighbor relationship to the edge. Also, some example suggestion for detailed implementation was used, including the ad-hoc function for boundary and color histogram distribution for region term. We chose the 8-connected neighbor instead of 4-connected that was suggested to use more region properties and the Manhattan distance for color intensity difference in the multi-dimensional image. Finally, we built an automatic testing to process dataset in batch mode.

For Lazy Snapping, the pre-segmentation step groups pixel into segments. These are considered as super-pixels. We read, did some experiments and compared five popular segmentation algorithms. Based on the comparisons and conclusions, we renewed Lazy Snapping method by replacing the traditional watershed with SEEDs algorithm. Silent Lazy Snapping – our improvement from original method have been implemented and tested with the image in Berkeley Segmentation Dataset combine with our own dataset, and some usable results are presented in Experimental results session.

Our future direction for interactive Graph Cut Segmentation is using other feature descriptors, such as Histogram of Oriented Gradients, to find out a better way of describing terms. Due to working on raw pixel, this method can’t be used to process high resolution image without high hardware requirements, and other improvements (such as GrabCut, Lazy Snapping) are suggested to be alternatives. But the editing windows can be zooming freely for more accurate view. Additionally, some options will be added to GUI so that the end-user can control the lambda or add more seed until satisfied without touching the codes.

Based on the discussion about limitations of Silent Lazy Snapping framework, we will also investigate the boundary editing step in the Lazy Snapping method for more accuracy and simpler action from the user. We can combine other filters (Gaussian, Guided filter, etc.) with Silent Lazy Snapping method to get more details in the boundary to remove noises and JPEG block artifacts in the border of the selected subject.

# 

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