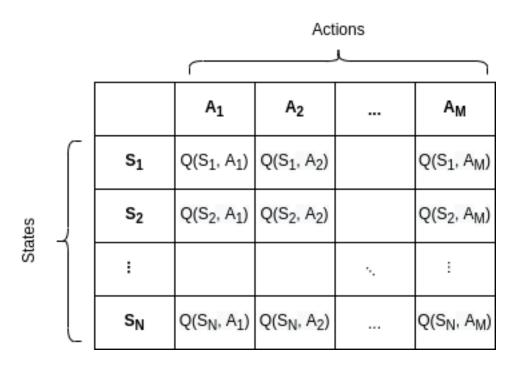


1	2	3	4	5
6	7 +1	8	9 GOAL	10
11 -1 	12	13 +1	14	15
16	17 -1	18	19	20
21	22	23	24	25

	†	↓	←	→
1	-	+1	-	+1
2	-	+1	-1	+1
3	-	+1	-1	+1
4	-	+1	-1	-1
5	-	+1	+1	-
23	+1	-	-1	+1
24	+1	-	-1	-1
25	+1	-	+1	-

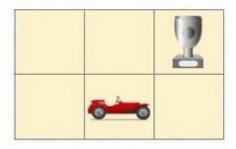


learned value

Source: https://en.wikipedia.org/wiki/Q-learning

$$Q^{new}(s_t, a_t) \leftarrow (1 - lpha) \cdot \underbrace{Q(s_t, a_t)}_{ ext{old value}} + \underbrace{lpha}_{ ext{learning rate}} \cdot \left(\underbrace{r_t}_{ ext{reward}} + \underbrace{\gamma}_{ ext{discount factor}} \cdot \underbrace{\max_a Q(s_{t+1}, a)}_{ ext{estimate of optimal future value}}
ight)$$

Game Board:



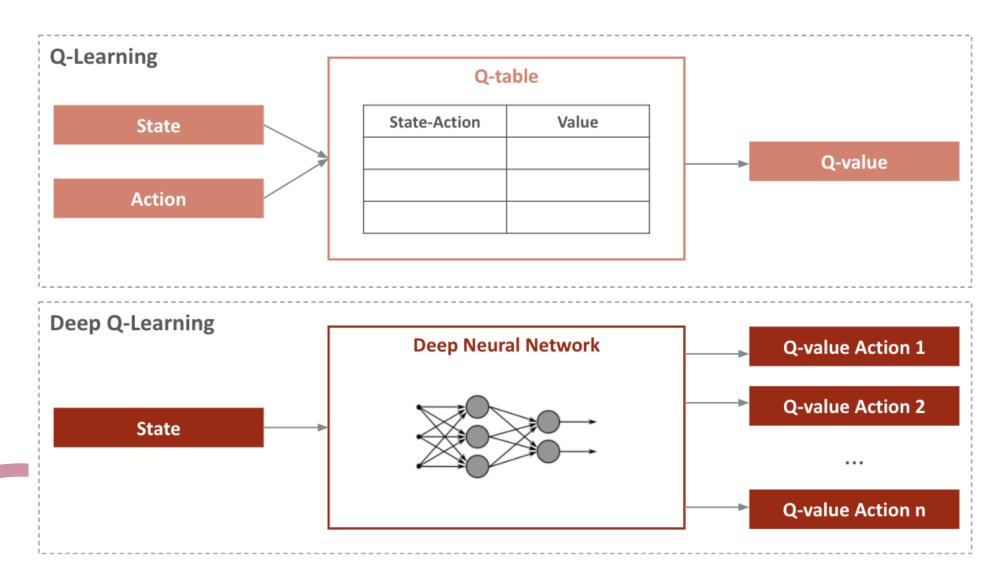
Current state (s): 0 0 0 0 0 1 0

Q Table:

y = 0.95

	000	0 0 0 0 1 0	0 0 0 0 0 1	100	0 1 0 0 0 0	0 0 1 0 0 0
Î	0.2	0.3	1.0	-0.22	-0.3	0.0
Ţ	-0.5	-0.4	-0.2	-0.04	-0.02	0.0
\Rightarrow	0.21	0.4	-0.3	0.5	1.0	0.0
\	-0.6	-0.1	-0.1	-0.31	-0.01	0.0

Deep Q-Learning



Why DQN?

- In an environment with a continuous state space it is impossible to go through all the possible states and actions repeatedly, since there are an infinite number of them and the Q-Table would be too big.
- DQN solves this problem by approximating the Q-Function through a Neural Network and learning from previous training experiences, so that the agent can learn more times from experiences already lived without the need to live them again, as well as avoiding the excessive computational cost of calculating and updating the Q-Table for continuous state spaces.

Main Neural Network

The Main NN tries to predict the expected return of taking each action for the given state.

Train and update every episodes

Target Neural Network

The Target Neural Network is used to get the target value for calculating the loss and optimizing it.

Will be updated every N timesteps with the weights of the main network.

Replay Buffer

The Replay Buffer is a list that is filled with the experiences lived by the agent.

An experience is represented by the current state, the action taken in the current state, the reward obtained after taking that action, whether it is a terminal state or not, and the next state reached after taking the action.

- State size
- Action size
- Gamma
- Episode
- Number of steps
- Epsilon value, epsilon decay
- Learning rate
- Target NN update rate

Action	Action Number	
0	Push cart left	
1	Push cart right	

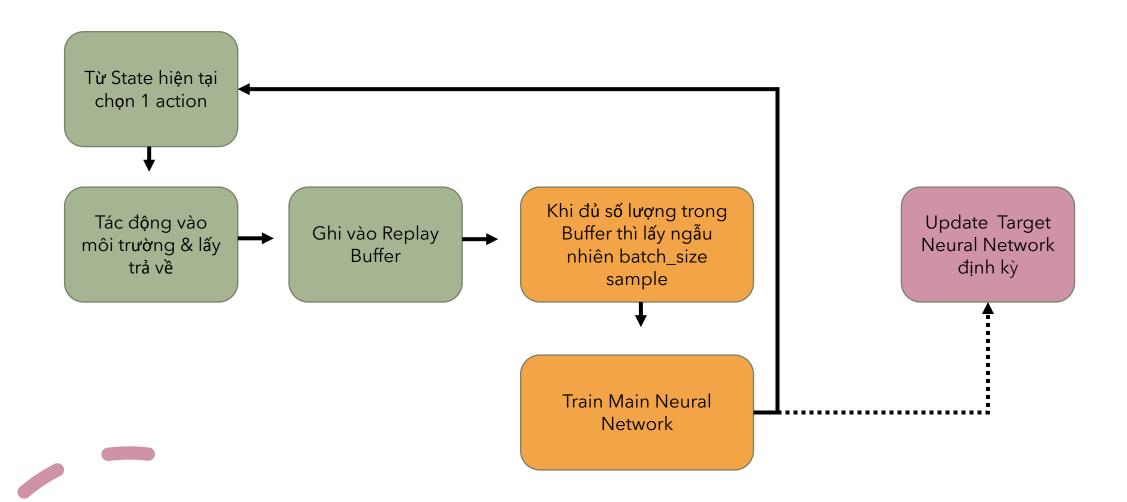
Index In array	Meaning	Min Value	Max value	
0	Cart Position on x axis	-4.8	4.8	
1	Cart Velocity on x axis	-00	∞	
2	Pole Angle	-0.418 rad	0.418 rad	
3	Pole Angular Velocity	-00	00	

DQN Flow

Algorithm 1 Deep Q-learning with Experience Replay

```
Initialize replay memory \mathcal{D} to capacity N
Initialize action-value function Q with random weights
for episode = 1, M do
    Initialise sequence s_1 = \{x_1\} and preprocessed sequenced \phi_1 = \phi(s_1)
    for t = 1. T do
         With probability \epsilon select a random action a_t
         otherwise select a_t = \max_a Q^*(\phi(s_t), a; \theta)
         Execute action a_t in emulator and observe reward r_t and image x_{t+1}
         Set s_{t+1} = s_t, a_t, x_{t+1} and preprocess \phi_{t+1} = \phi(s_{t+1})
         Store transition (\phi_t, a_t, r_t, \phi_{t+1}) in \mathcal{D}
         Sample random minibatch of transitions (\phi_j, a_j, r_j, \phi_{j+1}) from \mathcal{D}
         Set y_j = \begin{cases} r_j & \text{for terminal } \phi_{j+1} \\ r_j + \gamma \max_{a'} Q(\phi_{j+1}, a'; \theta) & \text{for non-terminal } \phi_{j+1} \end{cases}
         Perform a gradient descent step on (y_j - Q(\phi_j, a_j; \theta))^2 according to equation 3
    end for
end for
```

DQN Flow



Select Action

Epsilon Greedy Policy

1. Generate random number x between 0 and 1

2.
$$action = \begin{cases} random\ action & \text{if } x < \varepsilon \\ action\ with\ best\ Q-Value & \text{if } x \geqslant \varepsilon \end{cases}$$

Train Main NN

$$Loss = \left(\underbrace{r}_{reward} + \gamma * \max_{a'} Q(s', a') - \underbrace{Q(s, a)}_{Main \ Network \ output}\right)^{2}$$

$$Target \ Network \ output$$

$$for \ next \ state \ and \ action$$

Set
$$y_j = \begin{cases} r_j & \text{for terminal } \phi_{j+1} \\ r_j + \gamma \max_{a'} Q(\phi_{j+1}, a'; \theta) & \text{for non-terminal } \phi_{j+1} \end{cases}$$

Let's go!