

Homework9_SDS 315

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GitHub link: https://github.com/nancy1404/sds315_hw9.git

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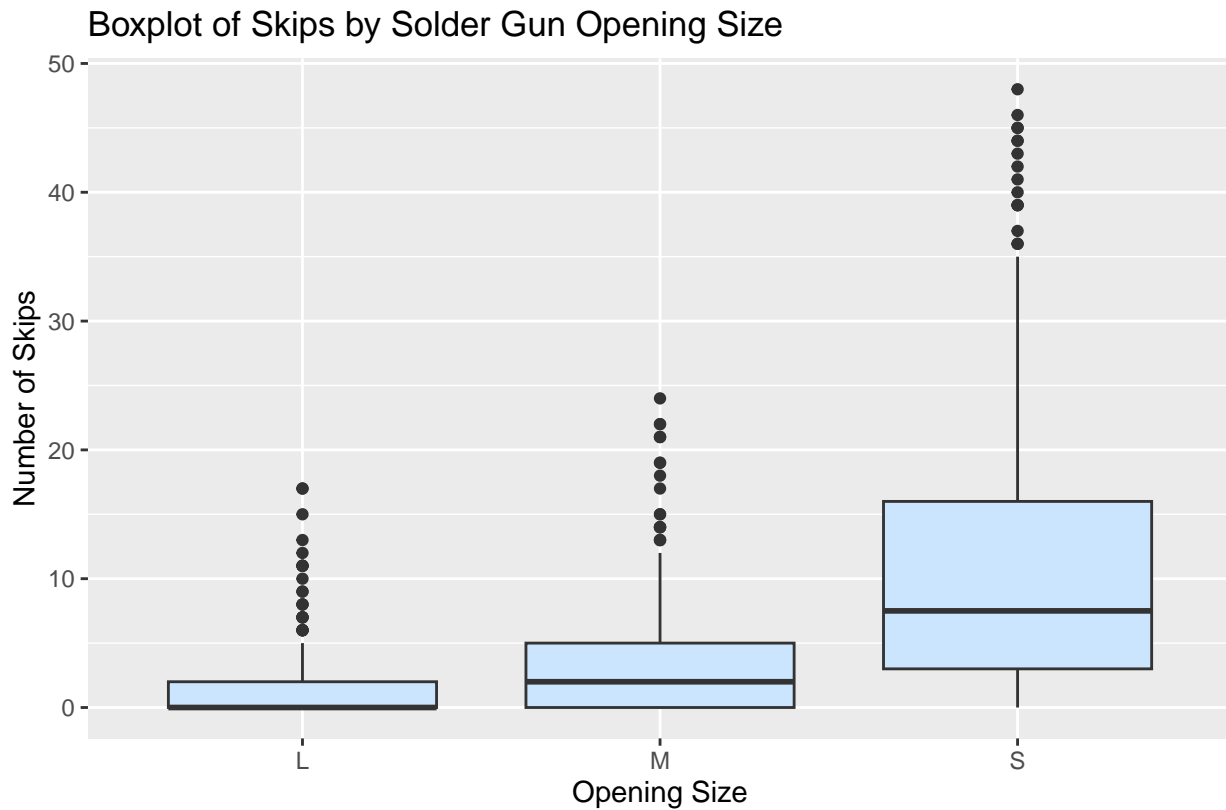
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PROBLEM 1: Manufacturing flaws in circuit boards

PART A.

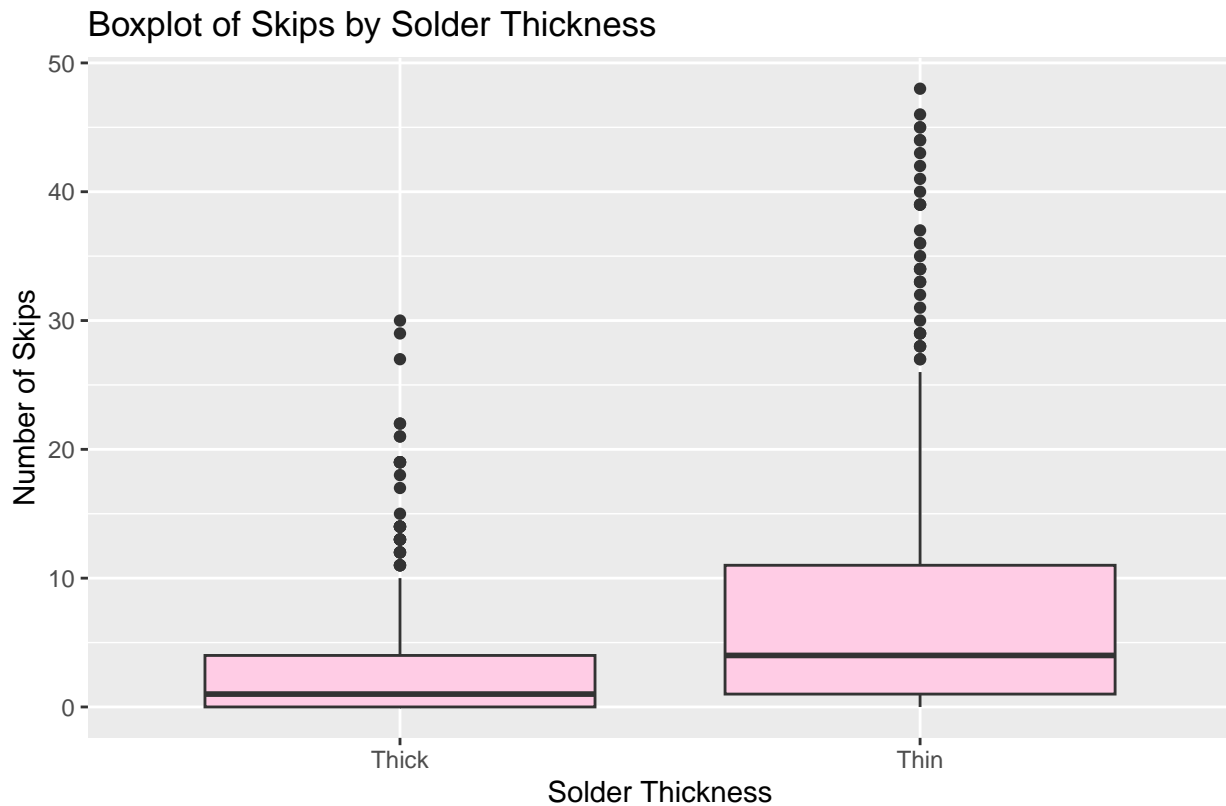
First Plot



* Skips increase as opening size decreases; small openings have the highest median.

- This boxplot shows that smaller solder gun openings are related more manufacturing flaws, or solder skips numbers. Boards manufactured with a small (S) opening seems to have highest median number of skips and a wide spread with many high outliers. Medium (M) openings show lower median skips and less variability, while Large (L) openings have the lowest median and the tightest spread, showing they are the most consistent in reducing defects.

Second Plot



* Thin solder results in more skips; thick solder shows lower variability and median.

- This boxplot shows that the thickness of the solder affects the number of skips. Boards soldered with thin alloy have a higher median number of skips and greater variability than those soldered with thick alloy. The thick solder group shows a tighter distribution and fewer high outliers, showing that thicker solder is generally more reliable in minimizing manufacturing flaws.

PART B.

term	estimate	std_error	statistic	p_value	lower_ci	upper_ci
intercept	0.393	0.520	0.756	0.450	-0.628	1.415
Opening: M	2.407	0.736	3.270	0.001	0.962	3.851
Opening: S	5.127	0.736	6.967	0.000	3.682	6.571
Solder: Thin	2.280	0.736	3.098	0.002	0.836	3.724
Opening: M:SolderThin	-0.740	1.041	-0.711	0.477	-2.782	1.302
Opening: S:SolderThin	9.653	1.041	9.276	0.000	7.611	11.696

PART C.

Intercept (0.393)

- The expected number of skips is approximately 0.393 when the Opening is Large and the Solder is Thick (our baseline).

OpeningM (2.407)

- Switching from Large to Medium Opening (while keeping Solder Thick) is associated with 2.407 more skips, on average.

OpeningS (5.127)

- Switching from Large to Small Opening (with Thick Solder) increases skips by 5.127, on average.

SolderThin(2.280)

- Using Thin Solder (with a Large Opening) increases skips by about 2.280, on average.

OpeningM:SolderThin (-0.740)

- When both Medium Opening and Thin Solder are used together, the combined number of skips is about 0.740 fewer than what would be expected by simply adding their individual effects. This is a slight negative interaction.

OpeningS:SolderThin (9.653)

- When both Small Opening and Thin Solder are used together, the number of skips is about 9.653 more than expected based on the sum of the individual effects. This is a strong positive interaction, indicating a synergistic increase in skips when both risk factors are present.

The worst-case scenario occurs when both Opening is Small and Solder is Thin where the significant increase in defects are shown beyond the main effects alone

PART D.

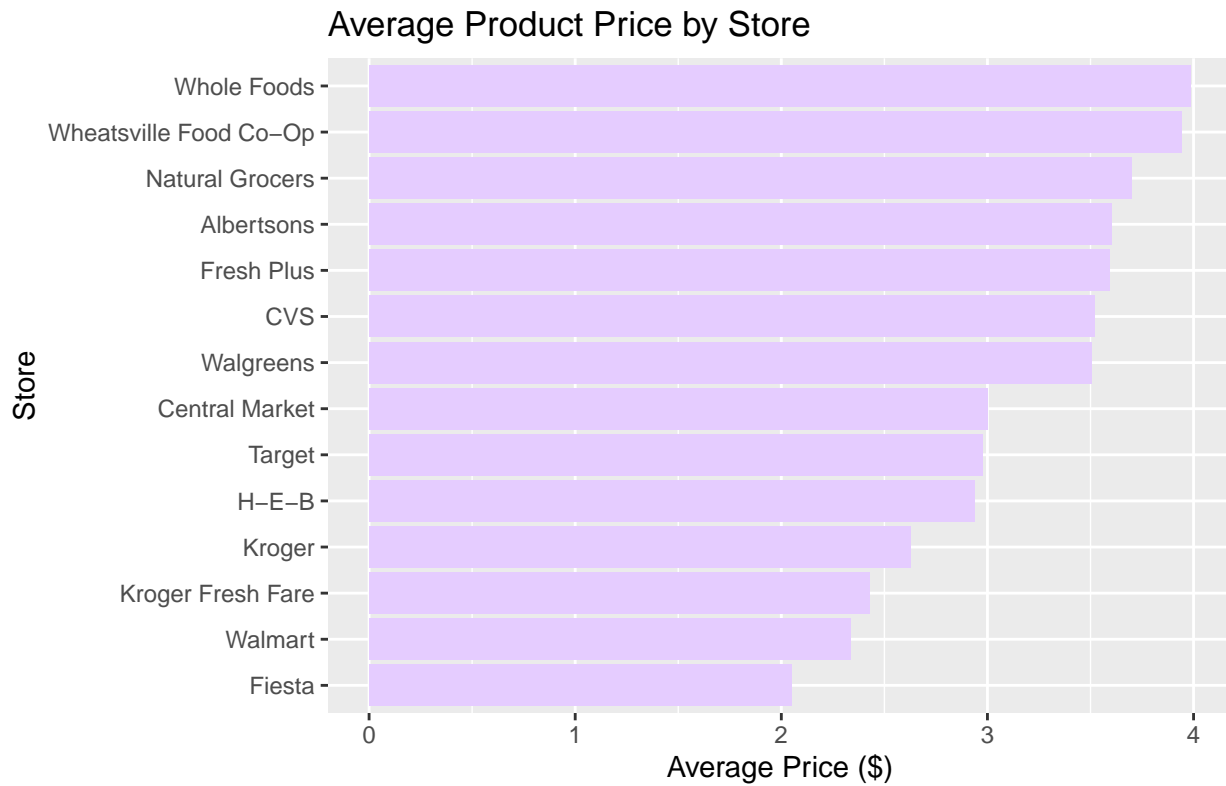
I would recommend using a Large Opening and Thick Solder combination for the soldering process based on the fitted regression model. This combination is the baseline group in the model and has the lowest expected number of skips (about 0.393 skips on average) which is lower than all the other combinations.

Other combinations (Medium or Small Opening, or Thin Solder) were associated with higher skip rates, and the combination of using Small Opening and Thin Solder led to the large positive interaction (9.653 skips more) which highly increases the risk of manufacturing defects.

Therefore, recommending the Large Opening with Thick Solder would be the most effective way to minimize solder skips and ensure higher manufacturing quality.

PROBLEM 2: Grocery store prices

PART A.



* Average product price by store shows price variation across stores, including convenience and high-end stores (like whole foods and CVS) generally charging more.

PART B.

Number of Stores Selling Each Product



* Staples like salt, milk, and eggs appear in all 16 stores, while niche products like Cinnamon Toast Crunch and El Milagros chips are less widely available.

This bar chart shows product availability across stores. While staple items like milk and eggs are sold in all 16 stores, niche and specialty products such as Cinnamon Toast Crunch or El Milagros Tortilla Chips are found in only a few, highlighting how product availability can differ widely by store.

PART C.

term	estimate	std_error	statistic	p_value	lower_ci	upper_ci
intercept	5.92	0.24	24.41	0.00	5.45	6.40
Product: 12 Pack Sprite	-0.02	0.31	-0.06	0.95	-0.63	0.60
Product: Almond milk	-2.20	0.33	-6.70	0.00	-2.85	-1.56
Product: Banana \$/lb	-4.88	0.30	-16.15	0.00	-5.48	-4.29
Product: Blue Bell Vanilla Ice Cream 16 oz	-2.95	0.41	-7.20	0.00	-3.75	-2.14
Product: Campbell's Chicken noodle	-3.46	0.33	-10.52	0.00	-4.11	-2.82
Product: Carton of eggs	-3.00	0.29	-10.24	0.00	-3.58	-2.42
Product: Cinnamon Toast Crunch 1lb	-1.00	0.44	-2.25	0.03	-1.87	-0.12
Product: El Milagros Tortilla Chips	-2.04	0.44	-4.59	0.00	-2.91	-1.17
Product: Frosted Flakes 1 lb	-1.25	0.44	-2.82	0.01	-2.12	-0.38
Product: Gold Medal Flour 5 lb	-2.17	0.34	-6.41	0.00	-2.84	-1.50
Product: Good Flow Honey 16 oz	1.00	0.37	2.73	0.01	0.28	1.72
Product: Granny Smith Apple \$/lb	-3.72	0.30	-12.31	0.00	-4.32	-3.13
Product: Greek Yogurt	-3.85	0.38	-10.03	0.00	-4.61	-3.10
Product: High Brew Black Coffee	-2.92	0.35	-8.31	0.00	-3.61	-2.23
Product: Honey Nut Cheerios	-1.73	0.31	-5.51	0.00	-2.34	-1.11
Product: Horizon 2% Milk Carton	-1.10	0.29	-3.76	0.00	-1.68	-0.52

term	estimate	std_error	statistic	p_value	lower_ci	upper_ci
Product: Imperial Sugar	-2.48	0.34	-7.33	0.00	-3.15	-1.82
Product: Iodized Salt	-3.87	0.30	-13.00	0.00	-4.45	-3.28
Product: JIF Peanut butter	-2.72	0.31	-8.86	0.00	-3.32	-2.12
Product: Justin's almond butter	6.81	0.37	18.55	0.00	6.08	7.53
Product: Kind Oats and Honey Bar	-1.86	0.35	-5.29	0.00	-2.56	-1.17
Product: La Croix Box	-1.07	0.33	-3.26	0.00	-1.72	-0.42
Product: Land o Lakes Half & Half	-3.30	0.34	-9.71	0.00	-3.96	-2.63
Product: Lucky Charms 1 lb	-1.50	0.44	-3.39	0.00	-2.37	-0.63
Product: Moms Tomato Sauce	1.45	0.37	3.94	0.00	0.72	2.17
Product: Natures Own Whole Wheat Bread	-2.42	0.41	-5.92	0.00	-3.22	-1.62
Product: Navel Orange	-3.96	0.37	-10.79	0.00	-4.68	-3.24
Product: Nut Thins 4.25 oz	-2.47	0.37	-6.75	0.00	-3.20	-1.75
Product: Original ramen	-5.06	0.38	-13.16	0.00	-5.81	-4.30
Product: Premium Saltine Crackers 1 lb	-2.33	0.37	-6.39	0.00	-3.05	-1.61
Product: Progress Chicken Noodle Soup	-3.07	0.35	-8.77	0.00	-3.76	-2.38
Product: San Pellegrino 25.3 floz	-3.65	0.34	-10.76	0.00	-4.32	-2.98
Product: Skinny Pop	-2.04	0.34	-6.02	0.00	-2.70	-1.37
Product: Smart Water 23.7 fl oz	-3.69	0.31	-11.79	0.00	-4.31	-3.08
Product: Stacy's Pita Chips	-1.81	0.35	-5.15	0.00	-2.50	-1.12
Product: Tostitos Bag	-1.68	0.41	-4.11	0.00	-2.49	-0.88
Product: Triscuits 9oz	-2.26	0.32	-7.05	0.00	-2.89	-1.63
Product: Welch's Grape Jelly	-2.94	0.33	-8.93	0.00	-3.58	-2.29
Product: Wheat Thins 8oz	-2.27	0.32	-7.08	0.00	-2.90	-1.64
Type: Grocery	-0.66	0.13	-5.20	0.00	-0.92	-0.41
Type: High-end Grocery	-0.30	0.15	-1.97	0.05	-0.59	0.00
Type: Natural	-0.09	0.16	-0.58	0.56	-0.40	0.22
Type: Small Format	-0.44	0.15	-2.90	0.00	-0.75	-0.14

term	estimate	std_error	statistic	p_value	lower_ci	upper_ci
Type: Grocery	-0.66	0.13	-5.2	0	-0.92	-0.41

“Compared with ordinary grocery stores (like Albertsons, HEB, or Krogers), convenience stores charge somewhere between \$0.41 and \$0.92 more for the same product.”

- These numbers came from the 95% CI for “Type: Grocery”, which is [-0.92, -0.41] – where Grocery stores charge \$0.41 to 0.92 less than Convenience stores, so we flipped sign.

PART D.

term	estimate	std_error	statistic	p_value	lower_ci	upper_ci
intercept	5.75	0.23	24.62	0.00	5.29	6.21
Product: 12 Pack Sprite	-0.02	0.29	-0.06	0.95	-0.58	0.55
Product: Almond milk	-2.29	0.30	-7.56	0.00	-2.89	-1.70
Product: Banana \$/lb	-4.86	0.28	-17.47	0.00	-5.40	-4.31
Product: Blue Bell Vanilla Ice Cream 16 oz	-3.08	0.38	-8.17	0.00	-3.82	-2.34
Product: Campbells Chicken noodle	-3.55	0.30	-11.71	0.00	-4.15	-2.96
Product: Carton of eggs	-2.98	0.27	-11.07	0.00	-3.51	-2.45

term	estimate	std_error	statistic	p_value	lower_ci	upper_ci
Product: Cinnamon Toast Crunch 1lb	-1.17	0.41	-2.87	0.00	-1.98	-0.37
Product: El Milagros Tortilla Chips	-1.91	0.41	-4.64	0.00	-2.72	-1.10
Product: Frosted Flakes 1 lb	-1.43	0.41	-3.49	0.00	-2.23	-0.62
Product: Gold Medal Flour 5 lb	-2.24	0.31	-7.18	0.00	-2.86	-1.63
Product: Good Flow Honey 16 oz	0.90	0.34	2.67	0.01	0.24	1.57
Product: Granny Smith Apple \$/lb	-3.70	0.28	-13.30	0.00	-4.24	-3.15
Product: Greek Yogurt	-3.93	0.35	-11.09	0.00	-4.63	-3.23
Product: High Brew Black Coffee	-3.01	0.32	-9.30	0.00	-3.65	-2.37
Product: Honey Nut Cheerios	-1.68	0.29	-5.84	0.00	-2.24	-1.11
Product: Horizon 2% Milk Carton	-1.08	0.27	-4.01	0.00	-1.61	-0.55
Product: Imperial Sugar	-2.60	0.31	-8.33	0.00	-3.21	-1.98
Product: Iodized Salt	-3.86	0.27	-14.11	0.00	-4.39	-3.32
Product: JIF Peanut butter	-2.63	0.28	-9.33	0.00	-3.19	-2.08
Product: Justin's almond butter	6.71	0.34	19.84	0.00	6.04	7.37
Product: Kind Oats and Honey Bar	-1.90	0.32	-5.85	0.00	-2.53	-1.26
Product: La Croix Box	-1.16	0.30	-3.82	0.00	-1.76	-0.56
Product: Land o Lakes Half & Half	-3.38	0.31	-10.81	0.00	-4.00	-2.77
Product: Lucky Charms 1 lb	-1.68	0.41	-4.10	0.00	-2.48	-0.87
Product: Moms Tomato Sauce	1.35	0.34	3.98	0.00	0.68	2.01
Product: Natures Own Whole Wheat Bread	-2.43	0.38	-6.43	0.00	-3.17	-1.69
Product: Navel Orange	-4.06	0.34	-12.00	0.00	-4.72	-3.39
Product: Nut Thins 4.25 oz	-2.57	0.34	-7.61	0.00	-3.24	-1.91
Product: Original ramen	-5.20	0.35	-14.70	0.00	-5.90	-4.50
Product: Premium Saltine Crackers 1 lb	-2.39	0.34	-7.10	0.00	-3.06	-1.73
Product: Progress Chicken Noodle Soup	-3.14	0.32	-9.71	0.00	-3.77	-2.50
Product: San Pellegrino 25.3 floz	-3.73	0.31	-11.94	0.00	-4.35	-3.12
Product: Skinny Pop	-2.19	0.31	-7.00	0.00	-2.80	-1.57
Product: Smart Water 23.7 fl oz	-3.66	0.29	-12.71	0.00	-4.22	-3.09
Product: Stacy's Pita Chips	-1.91	0.32	-5.91	0.00	-2.55	-1.28
Product: Tostitos Bag	-1.81	0.38	-4.81	0.00	-2.55	-1.07
Product: Triscuits 9oz	-2.12	0.30	-7.19	0.00	-2.70	-1.54
Product: Welch's Grape Jelly	-2.82	0.30	-9.34	0.00	-3.41	-2.22
Product: Wheat Thins 8oz	-2.13	0.30	-7.22	0.00	-2.71	-1.55
Store: Central Market	-0.57	0.18	-3.24	0.00	-0.92	-0.23
Store: CVS	0.19	0.18	1.06	0.29	-0.17	0.55
Store: Fiesta	-0.70	0.27	-2.61	0.01	-1.23	-0.17
Store: Fresh Plus	-0.04	0.16	-0.22	0.82	-0.35	0.28
Store: H-E-B	-0.65	0.15	-4.25	0.00	-0.95	-0.35
Store: Kroger	-0.70	0.23	-3.01	0.00	-1.16	-0.24
Store: Kroger Fresh Fare	-0.90	0.23	-3.87	0.00	-1.36	-0.44
Store: Natural Grocers	-0.08	0.20	-0.41	0.68	-0.47	0.31
Store: Target	-0.37	0.19	-1.97	0.05	-0.75	0.00
Store: Walgreens	0.22	0.18	1.19	0.23	-0.14	0.57
Store: Walmart	-0.99	0.23	-4.25	0.00	-1.45	-0.53
Store: Wheatsville Food Co-Op	0.29	0.18	1.62	0.11	-0.06	0.64
Store: Whole Foods	0.36	0.18	2.06	0.04	0.02	0.71

Based on the regression model controlling for product, Walmart (-0.99) and Kroger Fresh Fare (-0.90) appear to charge the lowest prices, on average, compared to Albertsons for the same product.

In contrast, Whole Foods (+0.36) and Wheatsville Food Co-Op (+0.29) charge the highest prices, on average,

for the same products when compared to Albertsons.

PART E.

To assess whether Central Market charges more than HEB for the same product, we inspect the coefficients from our regression model that controls for product: StoreCentral Market: -0.573, StoreH-E-B: -0.646, Difference: -0.573-(-0.646)=0.073.

This indicates that Central Market charges about \$0.07 more than HEB for the same product, on average which supports the first possibility: “Central market charges more than HEB for the same product”.

However, the difference is actually very small in magnitude. For the context, Walmart charges about \$0.99 less, Whole Food charges about \$0.36 more and Walgreens charges about \$0.22 more.

So even though Central Market does charge more than HEB, the difference is modest compared to how much other stores vary. This suggests that its reputation as a premium-priced store may be more about product mix or branding than substantial price discrimination.

PART F.

term	estimate	std_error	statistic	p_value	lower_ci	upper_ci
intercept	5.62	0.25	22.57	0.00	5.13	6.11
Product: 12 Pack Sprite	-0.02	0.33	-0.06	0.96	-0.66	0.63
Product: Almond milk	-2.11	0.34	-6.13	0.00	-2.79	-1.44
Product: Banana \$/lb	-4.91	0.32	-15.51	0.00	-5.53	-4.29
Product: Blue Bell Vanilla Ice Cream 16 oz	-2.91	0.43	-6.78	0.00	-3.75	-2.06
Product: Campbells Chicken noodle	-3.37	0.34	-9.79	0.00	-4.05	-2.69
Product: Carton of eggs	-2.97	0.31	-9.69	0.00	-3.58	-2.37
Product: Cinnamon Toast Crunch 1lb	-1.20	0.46	-2.57	0.01	-2.11	-0.28
Product: El Milagros Tortilla Chips	-2.00	0.46	-4.31	0.00	-2.91	-1.09
Product: Frosted Flakes 1 lb	-1.45	0.46	-3.12	0.00	-2.36	-0.54
Product: Gold Medal Flour 5 lb	-2.10	0.35	-5.92	0.00	-2.80	-1.40
Product: Good Flow Honey 16 oz	1.06	0.38	2.76	0.01	0.30	1.81
Product: Granny Smith Apple \$/lb	-3.75	0.32	-11.85	0.00	-4.37	-3.13
Product: Greek Yogurt	-3.92	0.40	-9.73	0.00	-4.71	-3.13
Product: High Brew Black Coffee	-2.82	0.37	-7.69	0.00	-3.55	-2.10
Product: Honey Nut Cheerios	-1.69	0.33	-5.16	0.00	-2.34	-1.05
Product: Horizon 2% Milk Carton	-1.07	0.31	-3.50	0.00	-1.68	-0.47
Product: Imperial Sugar	-2.42	0.35	-6.81	0.00	-3.11	-1.72
Product: Iodized Salt	-3.84	0.31	-12.32	0.00	-4.45	-3.23
Product: JIF Peanut butter	-2.75	0.32	-8.54	0.00	-3.38	-2.12
Product: Justin’s almond butter	6.86	0.38	17.93	0.00	6.11	7.61
Product: Kind Oats and Honey Bar	-1.69	0.37	-4.59	0.00	-2.41	-0.96
Product: La Croix Box	-0.98	0.34	-2.85	0.00	-1.66	-0.30
Product: Land o Lakes Half & Half	-3.17	0.36	-8.93	0.00	-3.87	-2.47
Product: Lucky Charms 1 lb	-1.70	0.46	-3.66	0.00	-2.61	-0.79
Product: Moms Tomato Sauce	1.50	0.38	3.92	0.00	0.75	2.25
Product: Natures Own Whole Wheat Bread	-2.47	0.43	-5.77	0.00	-3.31	-1.63
Product: Navel Orange	-3.91	0.38	-10.21	0.00	-4.66	-3.15
Product: Nut Thins 4.25 oz	-2.42	0.38	-6.33	0.00	-3.17	-1.67
Product: Original ramen	-4.98	0.40	-12.34	0.00	-5.77	-4.19
Product: Premium Saltine Crackers 1 lb	-2.25	0.38	-5.86	0.00	-3.00	-1.49
Product: Progress Chicken Noodle Soup	-3.02	0.37	-8.22	0.00	-3.75	-2.30

term	estimate	std_error	statistic	p_value	lower_ci	upper_ci
Product: San Pellegrino 25.3 floz	-3.52	0.36	-9.92	0.00	-4.22	-2.82
Product: Skinny Pop	-1.95	0.36	-5.50	0.00	-2.65	-1.25
Product: Smart Water 23.7 fl oz	-3.73	0.33	-11.38	0.00	-4.38	-3.09
Product: Stacy's Pita Chips	-1.68	0.37	-4.57	0.00	-2.40	-0.96
Product: Tostitos Bag	-1.64	0.43	-3.83	0.00	-2.49	-0.80
Product: Triscuits 9oz	-2.29	0.34	-6.83	0.00	-2.95	-1.63
Product: Welch's Grape Jelly	-3.01	0.34	-8.74	0.00	-3.69	-2.33
Product: Wheat Thins 8oz	-2.30	0.34	-6.86	0.00	-2.96	-1.64
Income10K	-0.01	0.01	-1.46	0.14	-0.03	0.00

term	estimate	std_error	statistic	p_value	lower_ci	upper_ci
Income10K	-0.01	0.01	-1.46	0.14	-0.03	0

Parameter	Std_Coefficient	CI	CI_low	CI_high
(Intercept)	1.0807133	0.95	0.8556340	1.3057925
Product12 Pack Sprite	-0.0090282	0.95	-0.3270297	0.3089733
ProductAlmond milk	-1.0410336	0.95	-1.3749993	-0.7070678
ProductBanana \$/lb	-2.4170040	0.95	-2.7235163	-2.1104917
ProductBlue Bell Vanilla Ice Cream 16 oz	-1.4319265	0.95	-1.8476062	-1.0162469
ProductCampbells Chicken noodle	-1.6610305	0.95	-1.9949962	-1.3270649
ProductCarton of eggs	-1.4643984	0.95	-1.7618643	-1.1669324
ProductCinnamon Toast Crunch 1lb	-0.5886045	0.95	-1.0387015	-0.1385075
ProductEl Milagros Tortilla Chips	-0.9848615	0.95	-1.4348857	-0.5348373
ProductFrosted Flakes 1 lb	-0.7141802	0.95	-1.1642772	-0.2640832
ProductGold Medal Flour 5 lb	-1.0337443	0.95	-1.3774734	-0.6900153
ProductGood Flow Honey 16 oz	0.5201525	0.95	0.1494513	0.8908537
ProductGranny Smith Apple \$/lb	-1.8457592	0.95	-2.1522715	-1.5392469
ProductGreek Yogurt	-1.9289786	0.95	-2.3190279	-1.5389293
ProductHigh Brew Black Coffee	-1.3902366	0.95	-1.7460668	-1.0344064
ProductHoney Nut Cheerios	-0.8345603	0.95	-1.1525619	-0.5165588
ProductHorizon 2% Milk Carton	-0.5287388	0.95	-0.8262047	-0.2312729
ProductImperial Sugar	-1.1896184	0.95	-1.5335023	-0.8457345
ProductIodized Salt	-1.8900385	0.95	-2.1918570	-1.5882199
ProductJIF Peanut butter	-1.3534426	0.95	-1.6653431	-1.0415420
ProductJustin's almond butter	3.3777821	0.95	3.0070808	3.7484834
ProductKind Oats and Honey Bar	-0.8307445	0.95	-1.1867283	-0.4747607
ProductLa Croix Box	-0.4830847	0.95	-0.8170504	-0.1491190
ProductLand o Lakes Half & Half	-1.5611775	0.95	-1.9051775	-1.2171774
ProductLucky Charms 1 lb	-0.8372931	0.95	-1.2873901	-0.3871961
ProductMoms Tomato Sauce	0.7382384	0.95	0.3675372	1.1089397
ProductNatures Own Whole Wheat Bread	-1.2167576	0.95	-1.6319151	-0.8016000
ProductNavel Orange	-1.9231169	0.95	-2.2938182	-1.5524156
ProductNut Thins 4.25 oz	-1.1921744	0.95	-1.5628756	-0.8214732
ProductOriginal ramen	-2.4520789	0.95	-2.8430091	-2.0611487
ProductPremium Saltine Crackers 1 lb	-1.1066269	0.95	-1.4782100	-0.7350439
ProductProgress Chicken Noodle Soup	-1.4889380	0.95	-1.8453873	-1.1324886
ProductSan Pellegrino 25.3 floz	-1.7351767	0.95	-2.0791767	-1.3911767
ProductSkinny Pop	-0.9616752	0.95	-1.3056898	-0.6176606

Parameter	Std_Coefficient	CI	CI_low	CI_high
ProductSmart Water 23.7 fl oz	-1.8391394	0.95	-2.1571605	-1.5211182
ProductStacy's Pita Chips	-0.8266557	0.95	-1.1826545	-0.4706570
ProductTostitos Bag	-0.8084865	0.95	-1.2241667	-0.3928064
ProductTriscuits 9oz	-1.1287807	0.95	-1.4539424	-0.8036189
ProductWelch's Grape Jelly	-1.4818623	0.95	-1.8154005	-1.1483240
ProductWheat Thins 8oz	-1.1332574	0.95	-1.4584192	-0.8080957
Income10K	-0.0315971	0.95	-0.0740660	0.0108718

Q: Do consumers in poorer ZIP codes seem to pay more or less for the same product, on average? How do you know?

Consumers in poorer ZIP codes tend to pay slightly more for the same product. We can see through the negative coefficient estimate on Income10K (-0.01), showing that prices decrease as ZIP code income increases. However, the p-value is 0.14 which means the association is not statistically significant at the 5% level, so the result should be interpreted cautiously.

Q: How large is the estimated size of the effect of Income10K on Price?

A one-standard deviation increase in ZIP code income is associated with a 0.03 standard-deviation decrease in price for the same product (standardized coefficient = -0.03). This effect is small when compared to other product-level effects, suggesting that income differences explain only a modest portion of the pricing variation across ZIP codes.

PROBLEM 3: redlining

Statement A

- ZIP codes with a higher percentage of minority residents tend to have more FAIR policies per 100 housing units

Figure A1 shows a clear upward linear trend between % Minority and FAIR Policies per 100 Housing Units. The regression model `model_A` has coefficient for minority of 0.014 and 95% CI of [0.009, 0.018] (positive) and p-value of 0.000 (statistically significant) and R^2 value of 0.516 (showing 51.6% of variation in FAIR policies is explained by minority %)

The statement is indeed **TRUE** since there is strong evidence that ZIP codes with a higher percentage of minority residents tend to have more FAIR policies per 100 housing units: - the positive slope and a significant p-value confirm a statistically significant positive association. - the CI does not include zero - the relationship explains a substantial proportion of the variation ($R^2 = 0.52$)

Statement B

- The evidence suggests an interaction effect between minority percentage and the age of the housing stock in the way that these two variables are related to the number of FAIR policies in a ZIP code.

There is also no model that shows the interaction between minority % and housing age for predicting FAIR policies.

The statement is **FALSE** since there is no evidence of interaction effect between minority percentage and housing age: - the housing age variable is not really related to minority percentage ($p = 0.125$) - there is no model tests whether interaction between % minority x housing age affects FAIR policies - the interaction referenced does not appear in any model output

CORRECTION “There is little to no evidence of an interaction effect between minority percentage and housing age on FAIR policies. In fact, housing age is only weakly associated with minority percentage, and no model includes an interaction term between these two variables.”

This is supported by the evidence that Figure B1 the scatterplot shows no strong visible trend between minority percentage and the percentage of housing built before WWII. Also the model_B's coefficient for age was 0.398, p-value was 0.125 (not statistically significant), 95% CI was [-0.116, 0.912] (includes 0, we can't rule out no effect), and R^2 of 0.06 which housing age explains only about 6% of variation in minority percentage. There is no regression model includes interaction between minority and age for predicting policies.

Statement C

- The relationship between minority percentage and number of FAIR policies per 100 housing units is stronger in high-fire-risk ZIP codes than in low-fire-risk ZIP codes.

Figure C1 shows the separate regression lines for high and low fire-risk ZIP codes. `model_C` includes the main effects for minority and `fire_riskLow`. We can see from the model output:

Term	Estimate	p-value	95% CI
minority	0.010	0.015	[0.002, 0.017]
fire_risk: Low	-0.443	0.112	[-0.995, 0.109]
minority x fire_risk: Low	-0.001	0.839	[-0.012, 0.010]

There is no statistical evidence that the relationship between minority percentage and FAIR policies is stronger in high-fire-risk ZIP codes. The interaction term `minority:fire_riskLow` in `model_C` has an estimate of -0.001, p value of 0.839, and a 95% CI of [-0.012, 0.010], which includes zero.

Therefore, the statement is indeed **FALSE** where the slope of minority percentage is not significantly different across high vs. low fire-risk groups.

CORRECTION “The relationship between minority percentage and number of FAIR policies per 100 housing units appears similar across ZIP codes with high and low fire risk.”

This is supported both by the non-significant interaction term in the regression and by parallel trend lines shown in Figure C1.

Statement D

- **Even without controlling for any other variables, income “explains away” all the association between minority percentage and FAIR policy uptake.**

model_D1 (policies ~ minority) has coefficient of 0.014 ($p < 0.001$) and model_D2 (policies ~ minority + income) has coefficient for minority of 0.01 ($p = 0.002$). Minority % is still significant even after controlling for income, which means the income does not explain it away entirely. The working “explains away all the association” is absolute and we can partially refute it.

(The coefficient drops from 0.014 to 0.010 (29% reduction) which is partial mediation but not really enough to say ‘explained away’.)

Since the phrase could imply total mediation and we only see partial reduction, we can say the statement is **UNDECIDABLE/AMBIGUOUS** since we would ideally want to compare coefficient changes directly (via % reduction in estimate maybe?) but not provided.

Statement E

- **Minority percentage and number of FAIR policies are still associated at the ZIP code level, even after controlling for income, fire risk, and housing age.**

This statement is **TRUE**. In model_E, the coefficient for minority is 0.008, with a p-value of 0.006 and a 95% CI of [0.003, 0.014], which indicates that even after controlling for income, fire risk, and age of housing stock, the percentage of minority residents in a ZIP code remains positively and significantly associated with the number of FAIR policies.

The racial composition of ZIP code is still an independent predictor of reliance on the FAIR insurance plan, suggesting unequal access to private insurance that can’t be fully explained by economic or environmental factors.