This is The code for Data Preprocessing. The Questions follow after this

```
In [2]:
         import numpy as np
         import pandas as pd
         import matplotlib.pyplot as plt
         import math
In [3]:
         # reading the dataset
         football data=pd.read csv(r'F:\MS IIITH\course structure and syllabus\Semester I\Data Analytics\Project\football data
         football data original set=football data
        Exploring the dimentions of the data
In [4]:
         football data.shape
Out[4]: (18207, 89)
In [5]:
         football data.columns
Out[5]: Index(['Unnamed: 0', 'ID', 'Name', 'Age', 'Photo', 'Nationality', 'Flag',
                'Overall', 'Potential', 'Club', 'Club Logo', 'Value', 'Wage', 'Special',
               'Preferred Foot', 'International Reputation', 'Weak Foot',
               'Skill Moves', 'Work Rate', 'Body Type', 'Real Face', 'Position',
                'Jersey Number', 'Joined', 'Loaned From', 'Contract Valid Until',
                'Height', 'Weight', 'LS', 'ST', 'RS', 'LW', 'LF', 'CF', 'RF', 'RW',
               'LAM', 'CAM', 'RAM', 'LM', 'LCM', 'CM', 'RCM', 'RM', 'LWB', 'LDM',
                'CDM', 'RDM', 'RWB', 'LB', 'LCB', 'CB', 'RCB', 'RB', 'Crossing',
               'Finishing', 'HeadingAccuracy', 'ShortPassing', 'Volleys', 'Dribbling',
               'Curve', 'FKAccuracy', 'LongPassing', 'BallControl', 'Acceleration',
                'SprintSpeed', 'Agility', 'Reactions', 'Balance', 'ShotPower',
                'Jumping', 'Stamina', 'Strength', 'LongShots', 'Aggression',
                'Interceptions', 'Positioning', 'Vision', 'Penalties', 'Composure',
                'Marking', 'StandingTackle', 'SlidingTackle', 'GKDiving', 'GKHandling',
                'GKKicking', 'GKPositioning', 'GKReflexes', 'Release Clause'],
              dtype='object')
In [6]:
         #Data preprocessing
         missing value matrix=football_data.isna()
```

In [7]:	missi	missing_value_matrix # this matix keeps a log of values that are missing in the given dataset													
Out[7]:		Unnamed: 0	ID	Name	Age	Photo	Nationality	Flag	Overall	Potential	Club	 Composure	Marking	StandingTackle	SlidingTackle
	0	False	False	False	False	False	False	False	False	False	False	 False	False	False	False
	1	False	False	False	False	False	False	False	False	False	False	 False	False	False	False
	2	False	False	False	False	False	False	False	False	False	False	 False	False	False	False
	3	False	False	False	False	False	False	False	False	False	False	 False	False	False	False
	4	False	False	False	False	False	False	False	False	False	False	 False	False	False	False
	18202	False	False	False	False	False	False	False	False	False	False	 False	False	False	False
	18203	False	False	False	False	False	False	False	False	False	False	 False	False	False	False
	18204	False	False	False	False	False	False	False	False	False	False	 False	False	False	False
	18205	False	False	False	False	False	False	False	False	False	False	 False	False	False	False
	18206	False	False	False	False	False	False	False	False	False	False	 False	False	False	False
	18207 rc	ows × 89 c	olumns	i											
	4														>
In [8]:	missin	<pre>missing_height_index=missing_value_matrix[missing_value_matrix['Height']==True].index.tolist()</pre>													
In [9]:	len(m:	<pre>len(missing_height_index)</pre>													
Out[9]:	48	18													
	The values that i feel contribute to heigt of a player can be it's nationality														
In [10]:	missing_value_matrix[missing_value_matrix['Nationality']==True].index														

```
# since the nationality is present for all the players so let us try to update tyhe values of the height based upon
          #height for that given nationality
Out[10]: Int64Index([], dtype='int64')
In [11]:
          unique nationalities=football data['Nationality'].unique()
In [12]:
          len(football data)
Out[12]: 18207
In [13]:
          nationality height averge values=pd.DataFrame()
In [14]:
          tempstr_int_cm=int(football_data['Height'][0][0])*30.48 + float(float(football_data['Height'][0][2])/12.0)*30.48
In [15]:
          tempstr int cm
Out[15]: 170.18
In [19]:
          float(float(football_data['Height'][0][2])/12.0)*30.48
Out[19]: 17.78
In [20]:
          tempstr int cm
Out[20]: 170.18
In [21]:
          #converting the height to centimeters from a string formatted feet and inches
          for i in range(len(football data['Height'])):
              if missing value matrix['Height'][i]==False:
```

```
tempstr int cm=int(football data['Height'][i][0])*30.48 + float(float(football data['Height'][i][2])/12.0)*3(
                  football data['Height'][i]=tempstr int cm
         <ipython-input-21-fc7e96f0a476>:5: SettingWithCopyWarning:
         A value is trying to be set on a copy of a slice from a DataFrame
         See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user guide/indexing.html#returning
         -a-view-versus-a-copy
           football data['Height'][i]=tempstr int cm
In [22]:
          # getting the unique nationalitites
          nationality height averge values['unique nationalities']=unique nationalities
          nationality height averge values['average height']=np.zeros(len(unique nationalities))
In [23]:
          # getting the average height as per nationality
          sum=0
          counter=0
          for i in range(len(unique nationalities)):
              for j in range(len(football data)):
                  if football data['Nationality'][j]==nationality height averge values['unique nationalities'][i] and missing \( \)
                      sum=sum+football data['Height'][j]
                      counter=counter+1
              nationality height averge values['average height'][i]=(sum/counter)
              sum=0
              counter=0
         <ipython-input-23-88612296aff8>:9: SettingWithCopyWarning:
         A value is trying to be set on a copy of a slice from a DataFrame
         See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user guide/indexing.html#returning
         -a-view-versus-a-copy
           nationality height averge values['average height'][i]=(sum/counter)
In [28]:
          # updating the missing height values as per the avg height of that nationality
          for i in range(len(football data['Height'])):
```

```
if missing_value_matrix['Height'][i]==True:
    for j in range(len(unique_nationalities)):
        if football_data['Nationality'][i]==nationality_height_averge_values['unique_nationalities'][j] :
            football_data['Height'][i]=nationality_height_averge_values['average_height'][j]
            missing_value_matrix['Height'][i]=False
            break

<ipython-input-28-5d655eb6d4f3>:6: SettingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
    football data['Height'][i]=nationality height averge values['average height'][j]
```

In [38]:

nationality_height_averge_values # looking at the average height as per nationality

Out	

	unique_nationalities	average_height
0	Argentina	172.559893
1	Portugal	174.131988
2	Brazil	174.668873
3	Spain	173.972213
4	Belgium	176.780077
159	Malta	167.640000
160	Belize	154.940000
161	South Sudan	200.660000
162	Indonesia	165.100000
163	Botswana	175.260000

164 rows × 2 columns

```
In [24]:
          # creating categorical subdivision of the data for easy pre-processing
          personal details=football data[['ID','Name','Age','Photo','Nationality','Height','Weight']]
          position details=[['LS', 'ST', 'RS', 'LW', 'LF', 'CF', 'RF', 'RW',
                 'LAM', 'CAM', 'RAM', 'LM', 'LCM', 'CM', 'RCM', 'RM', 'LWB', 'LDM',
                 'CDM', 'RDM', 'RWB', 'LB', 'LCB', 'CB', 'RCB', 'RB']]
          skills=football data[['Crossing',
                 'Finishing', 'HeadingAccuracy', 'ShortPassing', 'Volleys', 'Dribbling',
                 'Curve', 'FKAccuracy', 'LongPassing', 'BallControl', 'Acceleration',
                 'SprintSpeed', 'Agility', 'Reactions', 'Balance', 'ShotPower',
                 'Jumping', 'Stamina', 'Strength', 'LongShots', 'Aggression',
                 'Interceptions', 'Positioning', 'Vision', 'Penalties', 'Composure',
                 'Marking', 'StandingTackle', 'SlidingTackle', 'GKDiving', 'GKHandling',
                 'GKKicking', 'GKPositioning', 'GKReflexes']]
          club details=[['Club', 'Club Logo', 'Value', 'Wage', 'Special',
                 'Preferred Foot', 'International Reputation', 'Weak Foot',
                 'Skill Moves', 'Work Rate', 'Body Type', 'Real Face']]
In [36]:
          # converting the value in the columns of position details from string to integer , discarding anythhing after the + s
          for i in range(len(position details[0])):
              for j in range(len(football data)):
                  if missing value matrix[position details[0][i]][j]==False:
                      football data[position details[0][i]][j]=int(football data[position details[0][i]][j].split("+")[0])
         <ipython-input-36-e73ce568419a>:5: SettingWithCopyWarning:
         A value is trying to be set on a copy of a slice from a DataFrame
         See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user guide/indexing.html#returning
         -a-view-versus-a-copy
           football data[position details[0][i]][j]=int(football data[position details[0][i]][j].split("+")[0])
In [42]:
          # handling the missing values for columns falling under position deatils
          sum=0
          counter=0
          missing positions=[]
          for i in range(len(position details[0])):
              missing positions=missing value matrix[missing value matrix[position details[0]]==True].index.tolist()
              for j in range(len(football data)):
```

```
if missing value matrix[position details[0][i]][j]==False:
             sum=sum+football data[position details[0][i]][i]
             counter=counter+1
     avg=sum/counter
    for k in range(len(missing positions)):
        football data[position details[0][i]][missing positions[k]]=avg
        missing value matrix[position details[0][i]][missing positions[k]]=False
     sum=0
     counter=0
     avg=0
<ipython-input-42-43c68a9ea818>:13: SettingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame
See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user guide/indexing.html#returning
-a-view-versus-a-copy
  football data[position details[0][i]][missing positions[k]]=avg
<ipython-input-42-43c68a9ea818>:13: SettingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame
See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user guide/indexing.html#returning
-a-view-versus-a-copv
  football data[position details[0][i]][missing positions[k]]=avg
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See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user guide/indexing.html#returning
-a-view-versus-a-copy
  football data[position details[0][i]][missing positions[k]]=avg
```

```
<ipython-input-42-43c68a9ea818>:13: SettingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame
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```
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           football data[position details[0][i]][missing positions[k]]=avg
         <ipython-input-42-43c68a9ea818>:13: SettingWithCopyWarning:
         A value is trying to be set on a copy of a slice from a DataFrame
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         -a-view-versus-a-copv
           football data[position details[0][i]][missing positions[k]]=avg
         <ipython-input-42-43c68a9ea818>:13: SettingWithCopyWarning:
         A value is trying to be set on a copy of a slice from a DataFrame
         See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user guide/indexing.html#returning
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         <ipython-input-42-43c68a9ea818>:13: SettingWithCopyWarning:
         A value is trying to be set on a copy of a slice from a DataFrame
         See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user guide/indexing.html#returning
         -a-view-versus-a-copy
           football data[position details[0][i]][missing_positions[k]]=avg
         <ipython-input-42-43c68a9ea818>:13: SettingWithCopyWarning:
         A value is trying to be set on a copy of a slice from a DataFrame
         See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user guide/indexing.html#returning
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         <ipython-input-42-43c68a9ea818>:13: SettingWithCopyWarning:
         A value is trying to be set on a copy of a slice from a DataFrame
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         <ipython-input-42-43c68a9ea818>:13: SettingWithCopyWarning:
         A value is trying to be set on a copy of a slice from a DataFrame
         See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user guide/indexing.html#returning
         -a-view-versus-a-copy
           football data[position details[0][i]][missing positions[k]]=avg
In [57]:
         # checking for other missing values in various columns sequentially
          columns with missing values=[]
          for i in range(len(football data.columns)):
              tempstr=football data.columns[i]
```

```
if len(missing value matrix[missing value matrix[tempstr]==True].index )>0 :
                  columns with missing values.append(tempstr)
In [58]:
          columns with missing values # list of columns that still have missing values
Out[58]: ['Club',
          'Preferred Foot',
          'International Reputation',
          'Weak Foot',
          'Skill Moves',
          'Work Rate',
          'Body Type',
          'Real Face',
          'Position',
          'Jersey Number',
          'Joined',
          'Loaned From',
          'Contract Valid Until',
          'Weight',
          'Crossing',
          'Finishing',
          'HeadingAccuracy',
          'ShortPassing',
          'Volleys',
          'Dribbling',
          'Curve',
          'FKAccuracy',
          'LongPassing',
          'BallControl',
          'Acceleration',
          'SprintSpeed',
          'Agility',
          'Reactions',
          'Balance',
          'ShotPower',
          'Jumping',
          'Stamina',
```

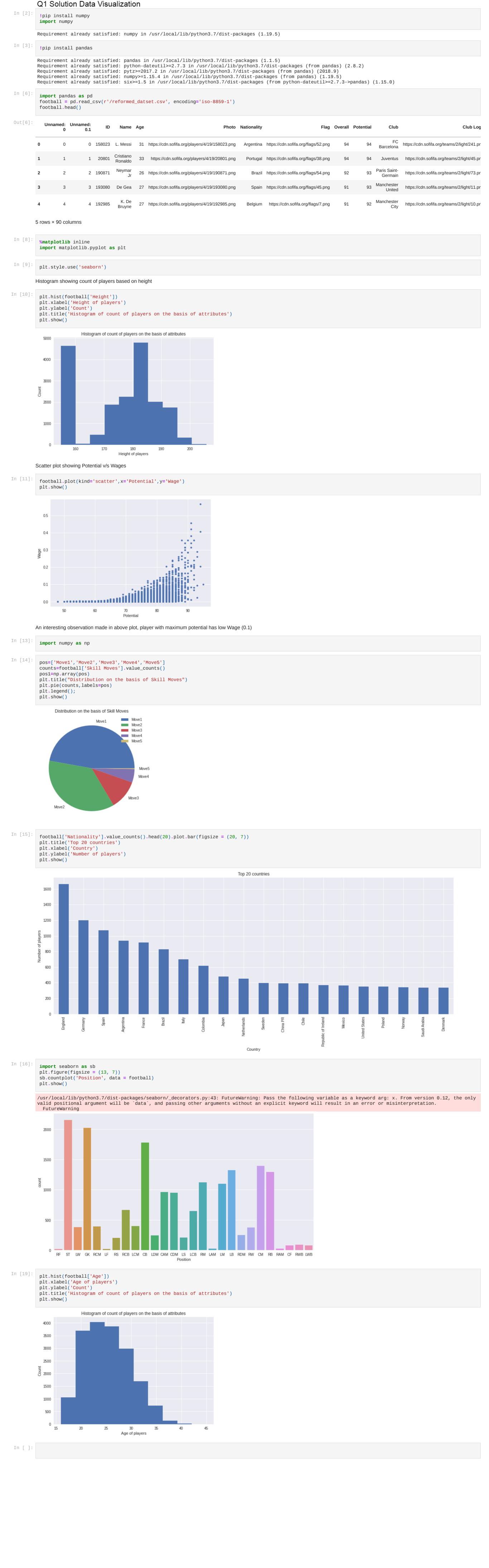
'Strength',
'LongShots',
'Aggression',
'Interceptions',

```
'Positioning',
          'Vision',
          'Penalties',
          'Composure',
          'Marking',
          'StandingTackle'.
          'SlidingTackle',
          'GKDivina'.
          'GKHandling',
          'GKKicking',
          'GKPositionina',
          'GKReflexes',
          'Release Clause'l
In [85]:
          # handing missing values for the release clause ( adding value =0 for missing atributes )
          #and converting the data to float from string
          for i in range(len(football data)):
              if missing value matrix['Release Clause'][i]==False:
                  if football data['Release Clause'][i].split("€")[1][-1]=='M':
                      football data['Release Clause'][i]=float(football data['Release Clause'][i].split('M')[0].split("€")[1])
                  else:
                      football data['Release Clause'][i]=(float(football data['Release Clause'][i].split("€")[1][:-1])/1000.0)
              else:
                  football data['Release Clause'][i]=0
                  missing value matrix['Release Clause'][i]=True
         <ipython-input-85-5317e881c387>:6: SettingWithCopyWarning:
         A value is trying to be set on a copy of a slice from a DataFrame
         See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user guide/indexing.html#returning
         -a-view-versus-a-copy
           football data['Release Clause'][i]=float(football data['Release Clause'][i].split('M')[0].split("€")[1])
         <ipython-input-85-5317e881c387>:10: SettingWithCopyWarning:
         A value is trying to be set on a copy of a slice from a DataFrame
         See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user guide/indexing.html#returning
         -a-view-versus-a-copy
           football data['Release Clause'][i]=0
         <ipython-input-85-5317e881c387>:8: SettingWithCopyWarning:
         A value is trying to be set on a copy of a slice from a DataFrame
```

```
See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user guide/indexing.html#returning
         -a-view-versus-a-copy
           football data['Release Clause'][i]=(float(football data['Release Clause'][i].split("€")[1][:-1])/1000.0)
In [115...
          # converting the column value and wage to float as well( as they don't have any missing values)
          listx=['Value','Wage']
          for j in range(len(listx)):
              for i in range(len(football data)):
                  if missing value matrix[listx[j]][i]==False:
                      if football data[listx[j]][i].split("€")[1][-1]=='M':
                          football data[listx[j]][i]=float(football data[listx[j]][i].split('M')[0].split("€")[1])
                      else:
                          if football data[listx[j]][i].split("€")[1]=='0':
                              football data[listx[j]][i]=0
                          else:
                              football data[listx[j]][i]=(float(football data[listx[j]][i].split("€")[1][:-1])/1000.0)
                  else:
                      football data[listx[i]][i]=0
                      missing value matrix[listx[j]][i]=True
         <ipython-input-115-15725b62b711>:7: SettingWithCopyWarning:
         A value is trying to be set on a copy of a slice from a DataFrame
         See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user guide/indexing.html#returning
         -a-view-versus-a-copv
           football data[listx[j]][i]=float(football data[listx[j]][i].split('M')[0].split("€")[1])
         <ipython-input-115-15725b62b711>:10: SettingWithCopyWarning:
         A value is trying to be set on a copy of a slice from a DataFrame
         See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user guide/indexing.html#returning
         -a-view-versus-a-copy
           football data[listx[i]][i]=0
         <ipython-input-115-15725b62b711>:12: SettingWithCopyWarning:
         A value is trying to be set on a copy of a slice from a DataFrame
         See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user guide/indexing.html#returning
         -a-view-versus-a-copy
           football data[listx[j]][i]=(float(football data[listx[j]][i].split("€")[1][:-1])/1000.0)
In [118...
          import os
          os.chdir("F:\MS IIITH\course structure and syllabus\Semester I\Data Analytics\Project")
```

In [119...

exporting the preprocessed dataset for using to solve the questions
football_data.to_csv("reformed_datset.csv")



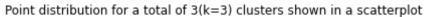
Q2(1) K Means code for K=3

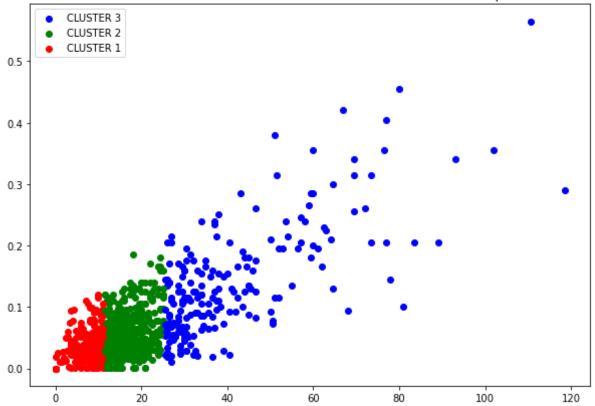
```
In [1]:
         import numpy as np
         import pandas as pd
         import matplotlib.pyplot as plt
         import math
         import random as rd
In [2]:
         dataset=pd.read csv(r'F:\MS IIITH\course structure and syllabus\Semester I\Data Analytics\Project\reformed datset.cs\
In [3]:
         # let us begin with implementing k means for value and wage
         dataset considered=pd.DataFrame()
         dataset considered['Value']=dataset['Value']
         dataset considered['Wage']=dataset['Wage']
In [4]:
         K=3# value of specified
In [5]:
         n iter=30# It defines the total no. of itterations for convergence
In [6]:
         m=dataset considered.shape[0] #number of training examples
         n=dataset considered.shape[1] #number of features. Here n=2
In [7]:
         #initialize centroids randomly from data points
         Centroids = pd.DataFrame(index=range(n),columns=range(10))
In [8]:
         for i in range(K):
             rand=rd.randint(0,m-1)
             Centroids[i][0]=dataset considered['Value'][rand]
             Centroids[i][1]=dataset considered['Wage'][rand]
In [9]:
         output= pd.DataFrame(index=range(len(dataset considered)),columns=range(K))
```

```
In [10]:
          def euclidean distance():
              #print("within elcid dist calculation ")
              # finding Euclidean distance between each point to all the centroids
              p = [0, 0]
              q = [0, 0]
              for i in range(len(dataset_considered)):
                  for j in range(K):
                      #print(i)
                      #print(i)
                      #print("----")
                      p[0]=Centroids[j][0]
                      p[1]=Centroids[j][1]
                      q[0]=dataset considered['Value'][i]
                      q[1]=dataset considered['Wage'][i]
                      output[j][i]=math.dist(p,q)
In [11]:
          def cluster labels():
              #print("within cluster label generation")
              # updating the cluster labels for points
              for i in range(1,len(cluster seg)+1):
                  valset=output.iloc[i-1].to list()
                  cluster seg[i-1]=valset.index(np.min(valset))
In [12]:
          val checker=pd.DataFrame(index=range(n+1),columns=range(K))
In [13]:
          counter value=np.zeros(K)
In [14]:
          def centroid updation(K):
              #print("within centroid updation")
              sum value=np.zeros(K)
              wage value=np.zeros(K)
              counter_value=np.zeros(K)
```

```
#updating the centroid value as per the points in the cluster
              for i in range(len(cluster seg)):
                  for j in range(K):
                      if cluster seg[i]==j :
                          sum value[j]=sum value[j]+dataset considered['Value'][i]
                          wage value[j]=wage value[j]+dataset considered['Wage'][i]
                          counter value[j]=counter value[j]+1
              for i in range(K):
                  for j in range(len(Centroids)):
                          if j==0:
                              Centroids[i][j]=(sum value[i]/counter value[i]) #value for cluster in centroid
                          else:
                              Centroids[i][j]=(wage value[i]/counter value[i])#wage for cluster 1 in centroid
In [15]:
          #def k means(K):
          #print("within kmeans calculation")
          for i in range(n iter):
              #print("itteration in k means")
              #print(i)
              #print("calling euclidean distance")
              euclidean distance()
              #creating an empty list to store the clusters where the points need to be fit
              cluster seg=[None]*len(output)
              cluster labels()
              centroid updation(K)
In [16]:
          plt.figure(figsize=(10, 7))
          c1=0
          c2=0
          c3=0
          c4 = 0
          c5=0
          c6=0
          c7 = 0
          for j in range(len(cluster seg)):
            if cluster seg[j]==0:
              if c1==0:
```

```
plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Red', label="CLUSTER 1")
      c1=c1+1
   else:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Red')
 if cluster seg[j]==1:
   if c2==0:
     plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j], c='Green', label="CLUSTER 2")
      c2=c2+1
   else:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Green')
 if cluster_seg[j]==2:
   if c3==0:
     plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Blue' , label="CLUSTER 3")
      c3=c3+1
   else:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Blue')
plt.title("Point distribution for a total of 3(k=3) clusters shown in a scatterplot")
plt.legend()
plt.show()
```





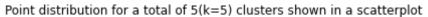
Q2(1) K Means Code for K=5

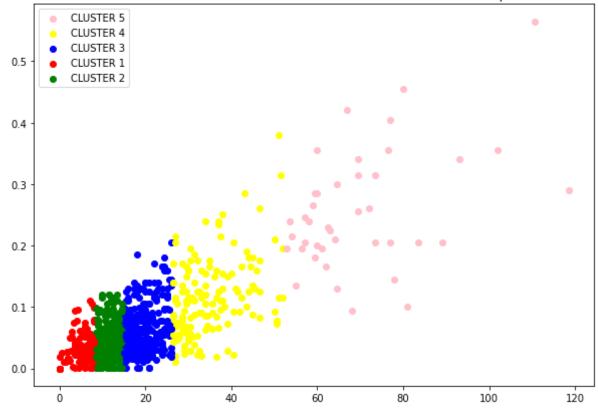
```
In [1]:
         import numpy as np
         import pandas as pd
         import matplotlib.pyplot as plt
         import math
         import random as rd
In [2]:
         dataset=pd.read csv(r'F:\MS IIITH\course structure and syllabus\Semester I\Data Analytics\Project\reformed datset.cs\
In [3]:
         # let us begin with implementing k means for value and wage
         dataset considered=pd.DataFrame()
         dataset considered['Value']=dataset['Value']
         dataset considered['Wage']=dataset['Wage']
In [4]:
         K=5# value of specified
In [5]:
         n iter=30# It defines the total no. of itterations for convergence
In [6]:
         m=dataset considered.shape[0] #number of training examples
         n=dataset considered.shape[1] #number of features. Here n=2
In [7]:
         #initialize centroids randomly from data points
         Centroids = pd.DataFrame(index=range(n),columns=range(10))
In [8]:
         for i in range(K):
             rand=rd.randint(0,m-1)
             Centroids[i][0]=dataset considered['Value'][rand]
             Centroids[i][1]=dataset considered['Wage'][rand]
In [9]:
         output= pd.DataFrame(index=range(len(dataset considered)),columns=range(K))
```

```
In [10]:
          def euclidean distance():
              #print("within elcid dist calculation ")
              # finding Euclidean distance between each point to all the centroids
              p = [0, 0]
              q = [0, 0]
              for i in range(len(dataset_considered)):
                  for j in range(K):
                      #print(i)
                      #print(i)
                      #print("----")
                      p[0]=Centroids[j][0]
                      p[1]=Centroids[j][1]
                      q[0]=dataset considered['Value'][i]
                      q[1]=dataset considered['Wage'][i]
                      output[j][i]=math.dist(p,q)
In [11]:
          def cluster labels():
              #print("within cluster label generation")
              # updating the cluster labels for points
              for i in range(1,len(cluster seg)+1):
                  valset=output.iloc[i-1].to list()
                  cluster seg[i-1]=valset.index(np.min(valset))
In [12]:
          val checker=pd.DataFrame(index=range(n+1),columns=range(K))
In [13]:
          counter value=np.zeros(K)
In [14]:
          def centroid updation(K):
              #print("within centroid updation")
              sum value=np.zeros(K)
              wage value=np.zeros(K)
              counter_value=np.zeros(K)
```

```
#updating the centroid value as per the points in the cluster
              for i in range(len(cluster seg)):
                  for j in range(K):
                      if cluster seg[i]==j :
                          sum value[j]=sum value[j]+dataset considered['Value'][i]
                          wage value[j]=wage value[j]+dataset considered['Wage'][i]
                          counter value[j]=counter value[j]+1
              for i in range(K):
                  for j in range(len(Centroids)):
                          if j==0:
                              Centroids[i][j]=(sum value[i]/counter value[i]) #value for cluster in centroid
                          else:
                              Centroids[i][j]=(wage value[i]/counter value[i])#wage for cluster 1 in centroid
In [15]:
          #def k means(K):
          #print("within kmeans calculation")
          for i in range(n iter):
              #print("itteration in k means")
              #print(i)
              #print("calling euclidean distance")
              euclidean distance()
              #creating an empty list to store the clusters where the points need to be fit
              cluster seg=[None]*len(output)
              cluster labels()
              centroid updation(K)
In [16]:
          plt.figure(figsize=(10, 7))
          c1=0
          c2=0
          c3=0
          c4 = 0
          c5=0
          c6=0
          c7 = 0
          for j in range(len(cluster seg)):
            if cluster seg[j]==0:
              if c1==0:
```

```
plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Red', label="CLUSTER 1")
      c1=c1+1
    else:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Red')
 if cluster seg[j]==1:
    if c2==0:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j], c='Green', label="CLUSTER 2")
      c2=c2+1
    else:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Green')
 if cluster seg[j]==2:
   if c3==0:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Blue' , label="CLUSTER 3")
      c3=c3+1
    else:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Blue')
 if cluster seg[j]==3:
   if c4==0:
     plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Yellow' , label="CLUSTER 4")
      c4 = c4 + 1
    else:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Yellow')
 if cluster seg[j]==4:
    if c5==0:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Pink' , label="CLUSTER 5")
      c5 = c5 + 1
    else:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Pink' )
plt.title("Point distribution for a total of 5(k=5) clusters shown in a scatterplot")
plt.legend()
plt.show()
```





In []:

Q2(1) K means code for K=7

```
In [1]:
         import numpy as np
         import pandas as pd
         import matplotlib.pyplot as plt
         import math
         import random as rd
In [2]:
         dataset=pd.read csv(r'F:\MS IIITH\course structure and syllabus\Semester I\Data Analytics\Project\reformed datset.cs\
In [3]:
         # let us begin with implementing k means for value and wage
         dataset considered=pd.DataFrame()
         dataset considered['Value']=dataset['Value']
         dataset considered['Wage']=dataset['Wage']
In [4]:
         K=7# value of specified
In [5]:
         n iter=30# It defines the total no. of itterations for convergence
In [6]:
         m=dataset considered.shape[0] #number of training examples
         n=dataset considered.shape[1] #number of features. Here n=2
In [7]:
         #initialize centroids randomly from data points
         Centroids = pd.DataFrame(index=range(n),columns=range(10))
In [8]:
         for i in range(K):
             rand=rd.randint(0,m-1)
             Centroids[i][0]=dataset considered['Value'][rand]
             Centroids[i][1]=dataset considered['Wage'][rand]
In [9]:
         output= pd.DataFrame(index=range(len(dataset considered)),columns=range(K))
```

```
In [10]:
          def euclidean distance():
              #print("within elcid dist calculation ")
              # finding Euclidean distance between each point to all the centroids
              p = [0, 0]
              q = [0, 0]
              for i in range(len(dataset_considered)):
                  for j in range(K):
                      #print(i)
                      #print(i)
                      #print("----")
                      p[0]=Centroids[j][0]
                      p[1]=Centroids[j][1]
                      q[0]=dataset considered['Value'][i]
                      q[1]=dataset considered['Wage'][i]
                      output[j][i]=math.dist(p,q)
In [11]:
          # creating an empty list to store the clusters where the points need to be fit
          #cluster seg=[None]*len(output)
In [12]:
          def cluster labels():
              #print("within cluster label generation")
              # updating the cluster labels for points
              for i in range(1,len(cluster seg)+1):
                  valset=output.iloc[i-1].to list()
                  cluster seg[i-1]=valset.index(np.min(valset))
In [13]:
          val checker=pd.DataFrame(index=range(n+1),columns=range(K))
In [14]:
          counter value=np.zeros(K)
In [15]:
          def centroid updation(K):
              #print("within centroid updation")
              sum value=np.zeros(K)
```

```
wage value=np.zeros(K)
              counter value=np.zeros(K)
              #updating the centroid value as per the points in the cluster
              for i in range(len(cluster seg)):
                  for j in range(K):
                      if cluster seg[i]==j :
                          sum value[j]=sum value[j]+dataset considered['Value'][i]
                          wage value[j]=wage value[j]+dataset considered['Wage'][i]
                          counter value[j]=counter value[j]+1
              for i in range(K):
                  for j in range(len(Centroids)):
                          if j==0:
                              Centroids[i][j]=(sum value[i]/counter value[i]) #value for cluster in centroid
                          else:
                              Centroids[i][j]=(wage value[i]/counter value[i])#wage for cluster 1 in centroid
In [16]:
          #def k means(K):
          #print("within kmeans calculation")
          for i in range(n iter):
              #print("itteration in k means")
              #print(i)
              #print("calling euclidean distance")
              euclidean distance()
              #creating an empty list to store the clusters where the points need to be fit
              cluster seg=[None]*len(output)
              cluster labels()
              centroid updation(K)
In [17]:
          plt.figure(figsize=(10, 7))
          c1=0
          c2=0
          c3=0
          c4 = 0
          c5=0
          c6=0
```

```
c7 = 0
for j in range(len(cluster seg)):
 if cluster seg[j]==0:
    if c1==0:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Red', label="CLUSTER 1")
      c1=c1+1
    else:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Red')
 if cluster seg[j]==1:
    if c2==0:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j], c='Green', label="CLUSTER 2")
      c2=c2+1
    else:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Green')
 if cluster seg[j]==2:
    if c3 == 0:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Blue' , label="CLUSTER 3")
    else:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Blue')
 if cluster seg[j]==3:
    if c4==0:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Yellow' , label="CLUSTER 4")
     c4 = c4 + 1
    else:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Yellow')
 if cluster seg[i]==4:
    if c5==0:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Pink' , label="CLUSTER 5")
      c5=c5+1
    else:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Pink' )
 if cluster seg[j]==5:
    if c6==0:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j],c='Grey', label="CLUSTER 6")
      c6 = c6 + 1
    else:
```

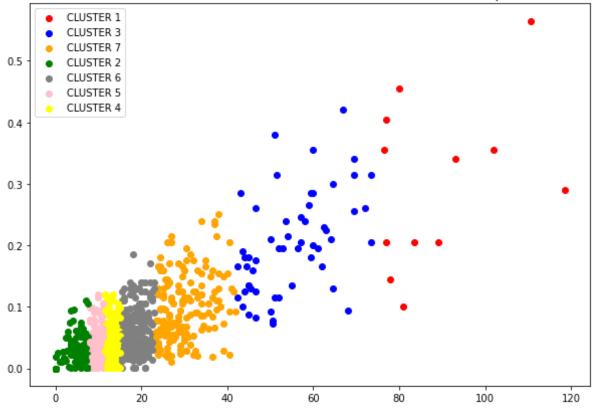
```
plt.scatter(dataset_considered['Value'][j], dataset_considered['Wage'][j],c='Grey')

if cluster_seg[j]==6:
    if c7==0:
        plt.scatter(dataset_considered['Value'][j], dataset_considered['Wage'][j],c='Orange', label="CLUSTER 7")
        c7=c7+1
    else:
        plt.scatter(dataset_considered['Value'][j], dataset_considered['Wage'][j],c='Orange')

plt.scatter(dataset_considered['Value'][j], dataset_considered['Wage'][j],c='Orange')

plt.title("Point distribution for a total of 7(k=7) clusters shown in a scatterplot")
plt.legend()
plt.show()
```

Point distribution for a total of 7(k=7) clusters shown in a scatterplot



Q2 Code for Elbow method and Silhouette Score

```
In [1]:
          import numpy as np
          import pandas as pd
          import matplotlib.pyplot as plt
          import math
          import random as rd
          from sklearn.metrics import silhouette score
In [2]:
          dataset=pd.read csv(r'F:\MS IIITH\course structure and syllabus\Semester I\Data Analytics\Project\reformed datset.cs\
In [3]:
          dataset.describe()
Out[3]:
                                 Unnamed:
                                                                                                                                          Internation
                                                      ID
                  Unnamed: 0
                                                                  Age
                                                                            Overall
                                                                                        Potential
                                                                                                        Value
                                                                                                                      Wage
                                                                                                                                 Special
                                       0.1
                                                                                                                                            Reputation
                 18207.000000
                              18207.000000
                                            18207.000000
                                                         18207.000000
                                                                       18207.000000
                                                                                    18207.000000
                                                                                                 18207.000000
                                                                                                               18207.000000
                                                                                                                            18207.000000
                                                                                                                                         18159.0000
          count
                                                                                                                   0.009731
          mean
                 9103.000000
                               9103.000000
                                          214298.338606
                                                             25.122206
                                                                          66.238699
                                                                                       71.307299
                                                                                                     2.410696
                                                                                                                             1597.809908
                                                                                                                                              1.1132
                  5256.052511
                                                             4.669943
                                                                           6.908930
                                                                                        6.136496
                                                                                                     5.594933
                                                                                                                   0.021999
                                                                                                                              272.586016
                                                                                                                                             0.3940
                               5256.052511
                                            29965.244204
            std
                    0.000000
                                  0.000000
                                               16.000000
                                                             16.000000
                                                                          46.000000
                                                                                       48.000000
                                                                                                     0.000000
                                                                                                                   0.000000
                                                                                                                              731.000000
                                                                                                                                             1.0000
           min
                 4551.500000
                              4551.500000 200315.500000
                                                             21.000000
                                                                          62.000000
                                                                                       67.000000
                                                                                                     0.300000
                                                                                                                   0.001000
                                                                                                                             1457.000000
                                                                                                                                             1.0000
           25%
                 9103.000000
                                                             25.000000
                                                                          66.000000
                                                                                       71.000000
                                                                                                     0.675000
                                                                                                                   0.003000
                                                                                                                             1635.000000
                                                                                                                                             1.0000
           50%
                              9103.000000 221759.000000
                 13654.500000 13654.500000
                                          236529.500000
                                                             28.000000
                                                                          71.000000
                                                                                       75.000000
                                                                                                     2.000000
                                                                                                                   0.009000
                                                                                                                             1787.000000
                                                                                                                                             1.0000
           max 18206.000000 18206.000000 246620.000000
                                                                          94.000000
                                                                                       95.000000
                                                                                                    118.500000
                                                                                                                   0.565000
                                                                                                                                             5.0000
                                                             45.000000
                                                                                                                             2346.000000
         8 rows × 75 columns
In [4]:
          # let us begin with implementing k means for value and wage
          dataset considered=pd.DataFrame()
          dataset considered['Value']=dataset['Value']
          dataset considered['Wage']=dataset['Wage']
```

```
In [5]:
          m=dataset_considered.shape[0] #number of training examples
          n=dataset considered.shape[1] #number of features. Here n=2
 In [6]:
 Out[6]: 1000
 In [7]:
Out[7]: 2
 In [8]:
          n iter=30 # total no of itterations for k to converge
 In [9]:
          K=10 # number of clusters( initial value )
In [10]:
          #initialize centroids randomly from data points
          Centroids = pd.DataFrame(index=range(n), columns=range(10))
In [11]:
          Centroids.shape
Out[11]: (2, 10)
         Centroids is a n x K dimentional matrix, where each column will be a centroid for one cluster.(2 x 5)
In [12]:
          for i in range(K):
              rand=rd.randint(0,m-1)
              Centroids[i][0]=dataset considered['Value'][rand]
              Centroids[i][1]=dataset considered['Wage'][rand]
In [13]:
          Centroids
```

```
# zeroth row is value
          # first row is wage
Out[13]:
                          2
                                          5
                                                6
                                                     7
                                                           8
                                                                 9
            13.0
                  34.0
                       21.5 45.0
                                  10.5
                                         8.5
                                              50.0
                                                   10.5
                                                          8.5 17.5
         1 0.026 0.085 0.021 0.18 0.046 0.037 0.092 0.023 0.024 0.037
In [14]:
          output= pd.DataFrame(index=range(len(dataset considered)),columns=range(K))
In [17]:
          def euclidean distance():
              print("within elcid dist calculation ")
              # finding Euclidean distance between each point to all the centroids
              p = [0, 0]
              q = [0, 0]
              for i in range(len(dataset considered)):
                  for j in range(K):
                      #print(i)
                      #print(j)
                      #print("----")
                      p[0]=Centroids[j][0]
                      p[1]=Centroids[j][1]
                      q[0]=dataset considered['Value'][i]
                      q[1]=dataset considered['Wage'][i]
                      output[j][i]=math.dist(p,q)
In [20]:
          # creating an empty list to store the clusters where the points need to be fit
          cluster seg=[None]*len(output)
In [21]:
          def cluster labels():
              print("within cluster label generation")
              # updating the cluster labels for points
              for i in range(1,len(cluster seg)+1):
                  valset=output.iloc[i-1].to list()
```

```
cluster seg[i-1]=valset.index(np.min(valset))
In [23]:
          val checker=pd.DataFrame(index=range(n+1),columns=range(K))
In [24]:
          counter value=np.zeros(K)
In [25]:
          def centroid updation(K):
              print("within centroid updation")
              sum value=np.zeros(K)
              wage value=np.zeros(K)
              counter value=np.zeros(K)
              #updating the centroid value as per the points in the cluster
              for i in range(len(cluster seg)):
                  for j in range(K):
                      if cluster seg[i]==j :
                          sum value[j]=sum value[j]+dataset considered['Value'][i]
                          wage value[j]=wage value[j]+dataset considered['Wage'][i]
                          counter value[j]=counter value[j]+1
              for i in range(K):
                  for j in range(len(Centroids)):
                          if j==0:
                              Centroids[i][j]=(sum value[i]/counter value[i]) #value for cluster in centroid
                          else:
                              Centroids[i][j]=(wage value[i]/counter value[i])#wage for cluster 1 in centroid
In [28]:
          def k means(K):
              print("within kmeans calculation")
              for i in range(n iter):
                  print("itteration in k means")
                  print(i)
                  print("calling euclidean distance")
                  euclidean distance()
```

```
# creating an empty list to store the clusters where the points need to be fit
                  cluster seg=[None]*len(output)
                  cluster labels()
                  centroid updation(K)
In [30]:
          #wcss calculation (elbow method) Within Cluster Sum of Squares (WCSS)
          def wcss calculation():
              print("within wcss calculation ")
              WCSS=0
              wcss final=0
              distance=0
              counter=0
              v1=[0,0]
              v2 = [0, 0]
              for j in range(1):
                  for i in range(len(cluster seg)):
                      if cluster seg[i]==2:
                          v1[0]=dataset_considered['Value'][i]
                          v1[1]=dataset considered['Wage'][i]
                          v2[0]=Centroids[cluster seg[i]][0]
                          v2[1]=Centroids[cluster seg[i]][1]
                          distance=math.dist(v1.v2)
                          distance=math.pow(distance,2)
                          wcss=wcss+distance
                          counter=counter+1
                  if counter >0:
                      wcss=wcss/counter
                  else:
                      wcss=0
                  wcss_final=wcss_final+wcss
                  counter=0
                  v1=[0,0]
                  v2=[0,0]
                  wcss=0
              wcss_final=wcss_final
              return wcss final
```

```
In [34]:
          wcss final values=[]
          silhouettescore values=[]
          for i in range(1,11):# loop is just to provide with the flexibility of doing calculations for multiple k values
              #print("calling k means for time")
              print(i)
              #print("kmeans called ")
              k means(i)
              print("calling wcss calculation")
              wcss result=wcss calculation()
              #print("wcss result obtained for times:")
              #print(i)
              silhouettescore values.append(silhouette score(dataset considered, cluster seg))
              wcss final values.append(wcss result)
         within kmeans calculation
         itteration in k means
         calling euclidean distance
         within elcid dist calculation
         within cluster label generation
         within centroid updation
         itteration in k means
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calling euclidean_distance
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within centroid updation itteration in k means

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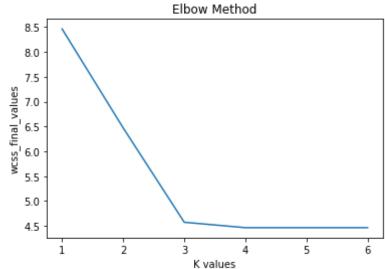
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         calling euclidean distance
         within elcid dist calculation
         within cluster label generation
         within centroid updation
         calling wcss calculation
         within wcss calculation
In [35]:
          # the silhouettescore values for K=1, 2,3,4,5,6,7,8,9,10 are as under
          silhouettescore values
Out[35]: [0.28151386005829737,
          0.28174167139517303,
          0.2868111714876412,
          0.2870625364201909,
          0.3970160591390798,
          0.5009924565312796,
          0.505824589332642,
          0.5202671113083313,
          0.529359709365208,
          0.5292515923417874]
```

```
In [36]:
          wcss_final_values
Out[36]: [8.461596433566438,
          6.4708793333333335,
          4.572737801426452,
          4.463905137963228,
          4.463905137963228,
          4.463905137963228,
          6.12809866884214,
          8.100667120752984,
          8.391650772130177,
          5.721483756768014]
In [49]:
          kmn=np.arange(1,7)
          plt.plot(kmn,wcss_final_values[0:6] )
          plt.title("Elbow Method")
          plt.xlabel("K values")
          plt.ylabel("wcss_final_values")
          plt.show()
```



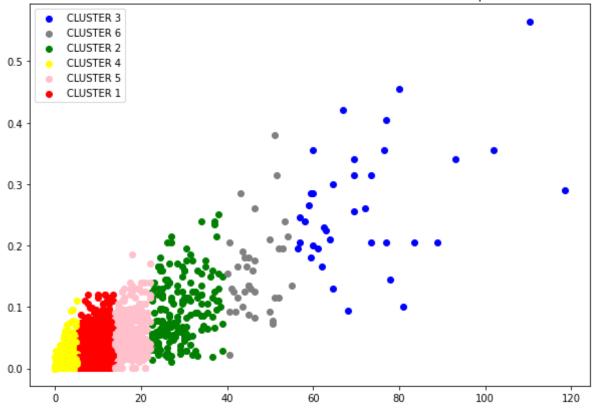
Q3 Hierarchical clustering(Agglomerative method)

```
In [12]:
            import pandas as pd
            import numpy as np
            import matplotlib.pyplot as plt
            %matplotlib inline
            import math
 In [2]:
            data=pd.read csv('/content/drive/MyDrive/reformed datset.csv')
            data.head()
 Out[2]:
              Unnamed: Unnamed:
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                                                                                                        Belgium
                                               Bruvne
          5 rows × 90 columns
 In [ ]:
 In [3]:
            dataset considered=pd.DataFrame()
            dataset considered['Value']=data['Value']
            dataset considered['Wage']=data['Wage']
```

```
#dataset considered['Height']=data['Height']
         #dataset considered['Weight']=data['Weight']
In [4]:
         import scipy.cluster.hierarchy as sho
In [5]:
         #Agglomerative Clustering done for 6 clusters
         from sklearn.cluster import AgglomerativeClustering
         cluster = AgglomerativeClustering(n clusters=6, affinity='euclidean', linkage='ward')
         cluster.fit predict(dataset considered)
Out[5]: array([2, 2, 2, ..., 3, 3, 3])
In [8]:
         plt.figure(figsize=(10, 7))
         c1=0
         c2=0
         c3=0
         c4 = 0
         c5=0
         c6 = 0
         for j in range(len(cluster.labels )):
           if cluster.labels [j]==0:
             if c1==0:
               plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Red', label="CLUSTER 1")
               c1=c1+1
             else:
               plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Red')
           if cluster.labels [j]==1:
             if c2==0:
               plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Green' , label="CLUSTER 2")
               c2=c2+1
             else:
               plt.scatter(dataset_considered['Value'][j], dataset_considered['Wage'][j] ,c='Green')
           if cluster.labels_[j]==2:
             if c3==0:
               plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Blue' , label="CLUSTER 3")
               c3=c3+1
```

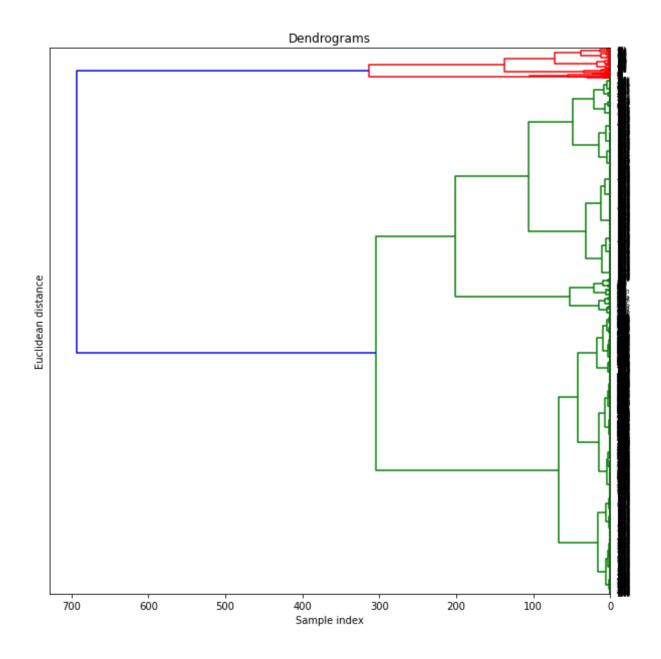
```
else:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Blue')
 if cluster.labels [j]==3:
   if c4==0:
     plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j], c='Yellow', label="CLUSTER 4")
   else:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Yellow')
 if cluster.labels [j]==4:
   if c5==0:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Pink' , label="CLUSTER 5")
      c5=c5+1
   else:
      plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j] ,c='Pink' )
 if cluster.labels [j]==5:
   if c6==0:
     plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j],c='Grey', label="CLUSTER 6")
      c6=c6+1
   else:
       plt.scatter(dataset considered['Value'][j], dataset considered['Wage'][j],c='Grey')
plt.title("Point distribution for a total of 6 clusters shown in a scatterplot")
plt.legend()
plt.show()
```

Point distribution for a total of 6 clusters shown in a scatterplot



```
import scipy.cluster.hierarchy as shc
plt.figure(figsize=(10, 10))
plt.title("Dendrograms")
dend = shc.dendrogram(shc.linkage(dataset_considered, method='ward'), orientation='left',p=30)#limiting the levels at
plt.xlabel('Sample index')
plt.ylabel('Euclidean distance')
```

Out[7]: Text(0, 0.5, 'Euclidean distance')



Q3 Hierarchical clustering (Divisive Method)

```
In [8]:
            import pandas as pd
            import numpy as np
            import matplotlib.pyplot as plt
            %matplotlib inline
            import math
 In [9]:
            data=pd.read csv('/content/drive/MyDrive/reformed datset.csv')
            data.head()
 Out[9]:
              Unnamed: Unnamed:
                                         ID
                                               Name Age
                                                                                            Photo Nationality
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                                                                                                      Belgium
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          5 rows × 90 columns
In [11]:
            # slicing the dataset
            dataset considered=pd.DataFrame()
            dataset considered['Value']=data['Value']
            dataset considered['Wage']=data['Wage']
In [14]:
            # Couputation of distance matrix
```

```
Distance matrix=pd.DataFrame(index=range(len(dataset considered['Value'])),columns=range(len(dataset considered['Wage
In [15]:
          p = [0, 0]
          q = [0, 0]
          for i in range(len(Distance matrix)):
            for j in range(len(Distance matrix)):
              p[0]=dataset considered['Value'][j]
              p[1]=dataset considered['Wage'][j]
              q[0]=dataset considered['Value'][i]
              q[1]=dataset considered['Wage'][i]
              #Distance matrix[i][j]=math.dist(dataset considered['Value'][i],dataset considered['Wage'][j])
              dist=math.sqrt(( (q[0]-p[0])**2)+((q[1]-p[1])**2))
              Distance matrix[i][j]=dist
In [16]:
          num clusters = 0
          all elements=Distance matrix.columns.tolist()
          dissimilarity matrix=Distance matrix
In [17]:
          # Average dissimilarity calculation within a cluster
          def avg dissimilarity within group element(ele, element list):
              max diameter = -np.inf
              sum dissimilarity = 0
              for i in element list:
                  sum dissimilarity += dissimilarity matrix[ele][i]
                  if( dissimilarity matrix[ele][i] > max diameter):
                      max diameter = dissimilarity matrix[ele][i]
              if(len(element list)>1):
                  avg = sum dissimilarity/(len(element list)-1)
              else:
                  avg = 0
              return avg
In [18]:
          # calculation of average dissimalrity across clusters
          def avg_dissimilarity_across group element(ele, main list, spl list):
              if len(spl list) == 0:
                  return 0
```

```
sum dissimilarity = 0
              for j in spl list:
                  sum dissimilarity = sum dissimilarity + dissimilarity matrix[ele][j]
              avg = sum dissimilarity/(len(spl list))
              return avg
In [19]:
          def dissimilarity calc(main list, dissimilarity calc group): #calculation of disimilarity for the matrix elements
              most dissimilar = -np.inf
              most dissimilar = None
              for ele in main list:
                  x = avg dissimilarity within group element(ele, main list)
                  y = avg dissimilarity across group element(ele, main list, dissimilarity calc group)
                  diff= x -y
                  if diff > most dissimilar:
                      most dissimilar = diff
                      most dissm object index = ele
              if(most dissimilar>0):
                  return (most dissm object index, 1)
              else:
                  return (-1, -1)
In [20]:
          def split(element list):# splitting a cluster
              main list = element list
              dissimilarity calc group = []
              (most dissm object index,flag) = dissimilarity calc(main list, dissimilarity calc group)
              while(flag > 0):
                  main list.remove(most dissm object index)
                  dissimilarity calc group.append(most dissm object index)
                  (most dissm object index,flag) = dissimilarity calc(element list, dissimilarity calc group)
              return (main list, dissimilarity_calc_group)
In [21]:
          def max diameter(cluster list): # calculation of maximum diameter of a given cluster
              max diameter cluster index = None
              max diameter cluster value = -np.inf
              index = 0
              for element list in cluster list:
                  for i in element list:
```

```
for j in element_list:
    if dissimilarity_matrix[i][j] > max_diameter_cluster_value:
        max_diameter_cluster_value = dissimilarity_matrix[i][j]
        max_diameter_cluster_index = index

index +=1

if(max_diameter_cluster_value <= 0):
    return -1

#print("The max diameter cluster index is{0}".format(max_diameter_cluster_index))
return max_diameter_cluster_index</pre>
```

```
In [22]:
          current clusters = ([all elements])
          level = 1
          index = 0
          counterz=0# to count the total number of clusters formed
          while(index!=-1):
              if counterz==5 :# Total clusters set to (5+1)=6 clusters
                break# Ending while loop when the desired cluster is achieved
              print(level, current clusters)
              print(type(current clusters[0]))
              counterz=counterz+1# my mod
              (sub cluster 1, sub cluster 2) = split(current clusters[index])
              del current clusters[index]
              current clusters.append(sub cluster 1)
              current clusters.append(sub cluster 2)
              index = max diameter(current clusters)
              level +=1
          print(level, current clusters) # printing the final cluster segregation
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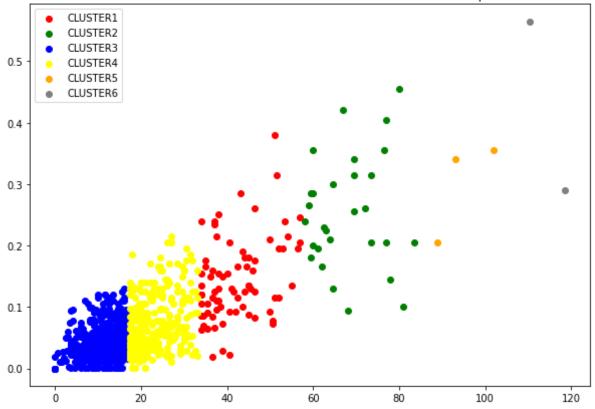
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```
In [23]:
          value cluster 1 points=[]
          value cluster 2 points=[]
          value cluster 3 points=[]
          value cluster 4 points=[]
          value cluster 5 points=[]
          value cluster 6 points=[]
          wage cluster 1 points=[]
          wage cluster 2 points=[]
          wage cluster 3 points=[]
          wage cluster 4 points=[]
          wage cluster 5 points=[]
          wage cluster 6 points=[]
In [24]:
          for i in range(len(current clusters[0])):
              value cluster 1 points.append(dataset considered['Value'][current clusters[0][i]])
              wage cluster 1 points.append(dataset considered['Wage'][current clusters[0][i]])
```

```
for i in range(len(current clusters[1])):
              value cluster 2 points append(dataset considered['Value'][current clusters[1][i]])
              wage cluster 2 points.append(dataset considered['Wage'][current clusters[1][i]])
          for i in range(len(current clusters[2])):
              value cluster 3 points.append(dataset considered['Value'][current clusters[2][i]])
              wage cluster 3 points append(dataset considered['Wage'][current clusters[2][i]])
          for i in range(len(current clusters[3])):
              value cluster 4 points.append(dataset considered['Value'][current clusters[3][i]])
              wage cluster 4 points append(dataset considered['Wage'][current clusters[3][i]])
          for i in range(len(current clusters[4])):
              value cluster 5 points.append(dataset considered['Value'][current clusters[4][i]])
             wage cluster 5 points.append(dataset considered['Wage'][current clusters[4][i]])
          for i in range(len(current clusters[5])):
              value cluster 6 points.append(dataset considered['Value'][current clusters[5][i]])
             wage cluster 6 points.append(dataset considered['Wage'][current clusters[5][i]])
In [26]:
          plt.figure(figsize=(10, 7))
          plt.scatter(value cluster 1 points, wage cluster 1 points ,c='Red')
          plt.scatter(value cluster 2 points, wage cluster 2 points ,c='Green')
          plt.scatter(value cluster 3 points, wage cluster 3 points ,c='Blue')
          plt.scatter(value cluster 4 points, wage cluster 4 points ,c='Yellow')
          plt.scatter(value cluster 5 points, wage cluster 5 points ,c='Orange')
          plt.scatter(value cluster 6 points, wage cluster 6 points ,c='Grey')
          plt.title("Point distribution for a total of 6 clusters shown in a scatterplot")
          plt.legend(["CLUSTER1","CLUSTER2","CLUSTER3","CLUSTER4","CLUSTER5","CLUSTER6"])
          plt.show()
```

Point distribution for a total of 6 clusters shown in a scatterplot



```
import plotly.figure_factory as ff
fig = ff.create_dendrogram(dataset_considered, orientation='left')
fig.update_layout(width=1000, height=700)
fig.show()
```

