CS 558 Programming Languages

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1 Big Step Semantics

1.1 Assign

 $\frac{\langle e,\sigma\rangle\!\!\Downarrow\!\langle n,\sigma'\rangle}{\langle := \!\!\mathbf{x}\ \mathbf{e},\sigma\rangle\!\!\Downarrow\!\!\sigma'[x \mapsto \! n]}$

1.2 Leq

1.3 Add

$$\begin{array}{ccc} \underline{\langle e_1,\sigma\rangle \psi \langle n_1,\sigma'\rangle} & \langle e_2,\sigma\rangle \psi \langle n_2,\sigma"\rangle & n{=}n_1{+}n_2 \\ & \langle +n_1n_2,\sigma\rangle \psi \langle n,\sigma\rangle & \end{array}$$

1.4 While

1.5 Variable

 $\tfrac{n = \sigma(x)}{\langle x, \sigma \rangle \Downarrow \langle n, \sigma \rangle}$

1.6 If

$$\frac{\langle c,\sigma\rangle \psi \langle n,\sigma'\rangle \quad \langle f,\sigma\rangle \psi \langle n,\sigma''\rangle}{\langle \mathbf{if}\ \mathbf{c}\ \mathbf{t}\ \mathbf{f},\sigma\rangle \psi \langle s_1,\sigma'\rangle}$$

1.7 Seq

$$\frac{\langle s_1,\sigma\rangle \psi \langle n_1,\sigma'\rangle \qquad \langle s_2,\sigma\rangle \psi \langle n_2,\sigma'\rangle}{\langle seqs_1s_2\rangle \psi \langle n,\sigma'\rangle}$$

1.8 Skip

2 Additional Task

The expression that yielded different results is as follows:

$$(\mathrm{seq}\ (*\ 0\ 7)\ (:=\ a\ (+\ 2\ (*\ 2\ (/\ 9\ (:=\ a\ (+\ a\ 2)))))))$$

For TestInterp1 ($left \longrightarrow right$) the answer is 6 whereas for TestInterp1b ($right \longrightarrow left$) it is 10.