(CS1.301) Algorithm Analysis and Design (Monsoon 2022)

Date: 19.10.2022

Deep Quiz 2

Alloted time: 45 minutes

Total marks: 15

Instructions:

- There are a total of 3 questions.
- Discussions amongst the students are not allowed. No electronic devices nor notes/books of any
- Any dishonesty shall be penalized heavily.
- Place your identity cards on the table for verification.
- · Be clear in your arguments. Partial marking is available but vague arguments shall not be given any

Question 1

Let G=(V,E) be a directed graph and for every edge $u \to v \in E$, a capacity $c(u \to v)$ is defined. Let $f(u \to v)$ (for all $u \to v \in E$) be a given feasible flow. Compute the residual capacities and the residual graph, with respect to f.

Question 2

Let n be an integer which is much larger than 5. Formulate a recursive function to compute the number of ways of providing change for n rupees only using (sufficient supply of) 1 rupee and 2 rupee coins.

Question 3

Suppose you are given three strings, S_1 , S_2 , and S_3 , where $|S_1|=n$, $|S_2|=m$, and $|S_3|=m+n$. We say that S_3 is an interleaf of S_1 and S_2 if and only if S_3 can be formed by interleaving sequences of characters from S_1 and S_2 in a way that maintains the left-to-right ordering of S_1 and S_2 . For example, "split" is an interleaving of "spit" and "l", but "splti" is not, and "cchocohilaptes" is an interleaf of "chocolate" and "chips".

Give an efficient dynamic programing algorithm1 that takes S1, S2, and S3 as parameters and determines whether S_3 is an in interleaf of S_1 and S_2 . chaconidaptes

dhadbedel

¹Hint: Memoization matrix could take True or False values in each entry where True in entry $M_{i,j}$ could represent if the first i+j letters of S_3 are formed by interleaving of first i letters of S_1 and first j letters of S_2 .