

Feature Engineering & Feature Selection

Agenda



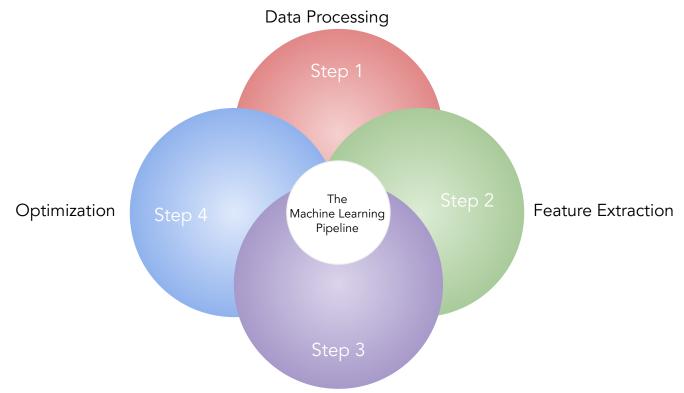
- Feature Transformation
- Feature Scaling
- Feature Selection
 - Forward Selection
 - Backward elimination
 - Stepwise selection
 - Recursive Feature Elimination (RFE)



Machine Learning Pipeline



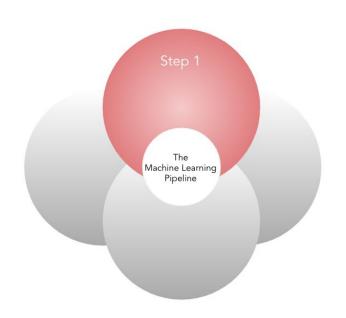
The ML pipeline



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The ML pipeline: Data processing

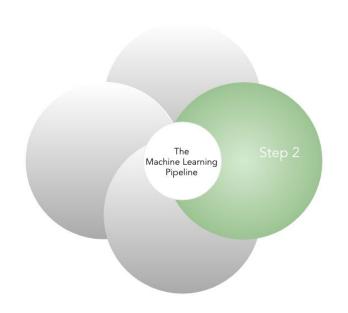


DATA PROCESSING

- Collection
- Formatting
- Labelling



The ML pipeline: Feature extraction

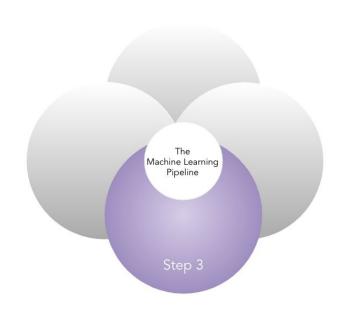


FEATURE EXTRACTION

- Feature Transformation
- Feature Engineering
- Feature Selection



The ML pipeline: Modeling



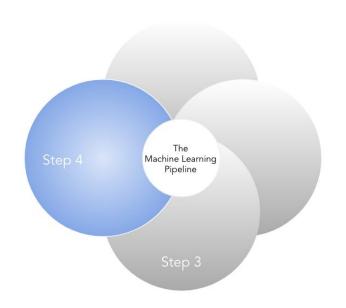
MODELING

- Model Building
- Model Evaluation

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The ML pipeline: Optimization

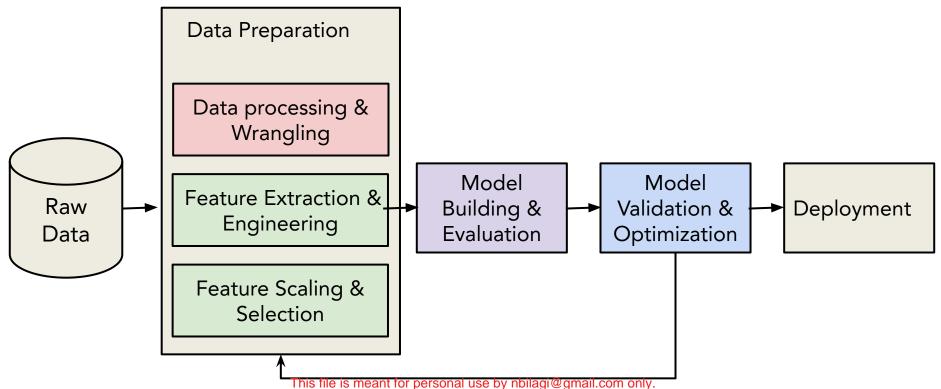


OPTIMIZATION

- Prediction Evaluation
- Model Validation
- Fine Tuning



The ML pipeline



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Data Processing

Data processing



DATA PROCESSING

- Collection
- Formatting
- Labelling

- Collection: To extract data from various sources. Generally obtained in the raw form and not immediately suitable for analysis
- Formatting: Organizing the datasets as required for analysis
- Labelling: Manually labelling data



Feature Extraction

Feature



- Feature or attribute is an independent variable that acts as input to our model
- The columns of a dataset are considered as features

	Features 						
Product ID	Store	City					
FD_234	A	Chennai					
DR_543	Α	Bangalore					
FD_176	В	Mumbai					
DR_621	Α	New Delhi					

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Feature Extraction



FEATURE EXTRACTION

- Feature Transformation
- Feature Engineering
- Feature Selection

- Feature Transformation: Replacing the existing features by function of these feature
- Feature Engineering: Creating new features based on empirical relationships
- Feature Selection: Fitting a model of significant features



Feature Transformation



Why do we need feature transformation?

- Incase of skewed (predictor and/or dependent) variable, we transform it to reduce the skewness
- If the assumptions of linear regression are not met, transformation of skewed target variable can be used for making the error terms more compatible to the assumptions
- If the relationship between a predictor and the response variable is non-linear, it can be linearized using transformation





Assumption of normality

The parametric methods used to compute test statistics or confidence intervals on the predictor variables assume the data to follow a normal distribution

Hence it is favourable that features have approximately normal distribution

Recap: The parametric methods are used when sample statistics adequately represent the population



Rule for transformed variables

Comparison of model performance should be done using the original units for the target variable and not the units after transformation

Transformation methods



- Logarithmic transformation
- Square root transformation
- Reciprocal transformation
- Exponential transformation
- Box-cox transformation

Transformation methods



- Logarithmic transformation
- Square root transformation
- Reciprocal transformation
- Exponential transformation
- Box-cox transformation



Logarithmic transformation

- To linearize, values of a variable are replaced with its natural log
- It cannot be used on a categorical variable after dummy encoding since In(0) is undefined
- Also if a variable takes zero or negative values, logarithmic transform cannot be used on it





• If the relationship between x and y is given by:

$$y = mx^k \varepsilon$$

To transform to a linear relationship take logarithm on both sides:

$$ln(y) = ln(m) + k * ln(x) + ln(\epsilon)$$

$$Y = \beta_0 + \beta_1 X + \epsilon'$$

Υ	In(y)
β_0	In(m)
β ₁	k
Х	ln(x)
ε'	ε

Now a regression line can be estimated for this relationship

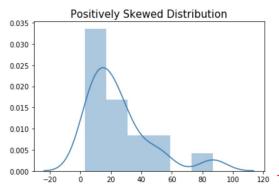


Example of log transformation

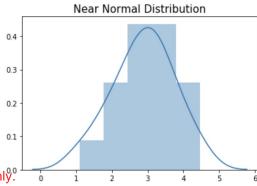
Consider the following data:

Note: Values are rounded to 1 decimals

Х	12	9	3	6	24	13	21	6	16	13	54	23	46	32	87	23	34
ln(X)	2.5	2.2	1.1	1.8	3.2	2.6	3.1	1.8	2.7	2.6	3.9	3.1	3.8	3.4	4.5	3.1	3.5







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- Logarithmic transformation
- Square root transformation
- Reciprocal transformation
- Exponential transformation
- Box-cox transformation



Square root transformation

Values of a variable are replaced with its square root

To reduce right skewness, we may use square root transformation

It can be applied even when the variable takes a zero value

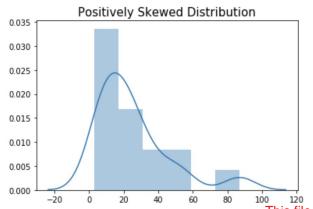


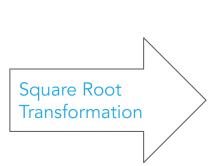
Example of square root transformation

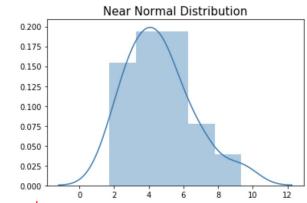
Consider the following data:

Note: Values are rounded to 1 decimals

Х	12	9	3	6	24	13	21	6	16	13	54	23	46	32	87	23	34
√X	3.5	3	1.7	2.4	4.9	3.6	4.6	2.4	4	3.6	7.4	4.8	6.8	5.7	9.3	4.8	5.8







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- Logarithmic transformation
- Square root transformation
- Reciprocal transformation
- Exponential transformation
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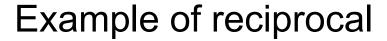
Reciprocal transformation

Values of a variable are replaced with its reciprocal

• It can not be applied only when the variable takes zero values

However, can be applied to negative values

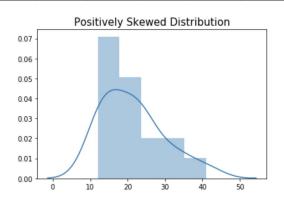
Example: population per area (population density) transforms to area per person

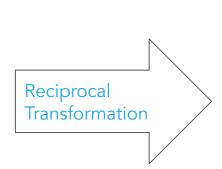


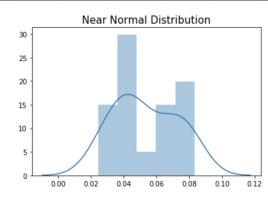


Consider the following data:

X	12	19	23	16	14	13	21	13	16	13	24	23	41	32	27	23	34
1/X	.08	.05	.04	.06	.07	.08	.05	.08	.06	.08	.04	.04	.02	.03	.04	.04	.03







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- Logarithmic transformation
- Square root transformation
- Reciprocal transformation
- Exponential transformation
- Box-cox transformation



Exponential transformation

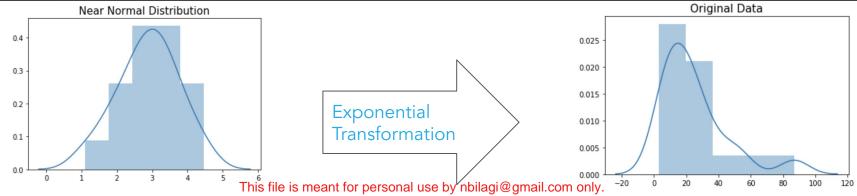
- Values of a variable are replaced with its exponential
- It is generally used to transform logarithmic transformed data to get the original data back



Example of exponential transformation

Consider the data used in logarithmic transformation.

X	12	9	3	6	24	13	21	6	16	13	54	23	46	32	87	23	34
In(X)	2.5	2.2	1.1	1.8	3.2	2.6	3.1	1.8	2.7	2.6	3.9	3.1	3.8	3.4	4.5	3.1	3.5
exp(X)	12	9	3	6	24	13	21	6	16	13	54	23	46	32	87	23	34



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- Logarithmic transformation
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It is defined as

$$X^{\lambda} = egin{cases} rac{X^{\lambda}-1}{\lambda} & ext{if} \lambda > 0 \ \ln(X) & ext{if} \lambda = 0 \end{cases}$$

Here, X is the variable and λ is the transformation parameter and can be tuned according to the data.

- The Box-Cox transformation can only be used on positive variables
- Generalized form of logarithmic transformation
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Feature Scaling





It is a technique used to transform the data into a common scale

 Since the features have various ranges, it becomes a necessary step in data preprocessing while using machine learning algorithms

 Since most machine learning algorithms use distance calculations, features taking higher values will weigh in more in the distance compared to features taking values of low magnitude





 In a dataset which has variables age and income. The age of a person is measured in years which can takes values between 18 to 65 (retirement age) and income of a person is in thousands
 So it is necessary to bring the two features in the same scale to assign appropriate weights

In some parts of the world height is measured using metric system (centimetres), while in some other parts the imperial system is used (feet/inches).
 So the results would be different if the height value is 152 cm or 5 feet, when if converted they refer to the exact same height value.



Feature scaling methods

- Normalization
- Standardization





Normalization is the process of rescaling features in the range 0 to 1

$$x' = rac{x - \min(x)}{\max(x) - \min(x)}$$

Standardization



- Standardization rescales the feature such that it has mean 0 and unit variance
- The procedure involves subtracting the mean from observation and then dividing by the standard deviation

$$x'=rac{x-\overline{x}}{\sigma}$$

When to use Normalization? When to use Standardization?

Normalization is a good technique to use when you do not know the distribution of your data or when you know the distribution is not Gaussian (a bell curve).

Standardization assumes that your data has a Gaussian (bell curve) distribution. This does not strictly have to be true, but the technique is more effective if your attribute distribution is Gaussian.



Normalization or Min-Max normalization tries to get the values closer to mean, but when there are outliers in the data which are important and we don't want to lose their impact, we go with Standardization or Z score normalization

Min- Max tries to get the values closer to mean. But when there are outliers in the data which are important and we don't want to lose their impact, we go with Z score. In this case, we rescale an original variable to have a mean of zero and a standard deviation of one. It does not have any units: hence is useful for comparing variables expressed in different units. Standardization makes no difference to the shape of a distribution.



Feature Selection

Feature selection



- Feature selection is the process of including the significant features in the model
- This can be achieved by:
 - Forward selection method
 - Backward elimination method
 - Stepwise method
- To understand the above methods let $X_1, X_2, ..., X_k$ be k predictor variables and Y be the response variable



Forward selection method

Procedure

- 1. Start with a null model (with no predictors)
- 2. Obtain the correlation between Y and each variable. The variable with highest correlation gets added to the model (say X_m). Build a model Y ~ X_m
- Obtain the correlation between Y and remaining (k-1) variables. The next variable (say X_p) is included, which has the highest correlation with Y after removing X_m
- 4. Build a model $Y \sim X_m + X_p$. If X_p is significant include it in the model else discard
- 5. Repeat steps (3) and (4) until reaching the stopping rule or running out of variables

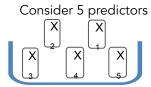




Start with a NULL MODEL (a model with no predictors)

Y~

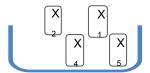
Obtain the most significant predictor (predictor having highest correlation with Y)



Model with most significant variable (say X_3)

$$Y \sim \beta_0 + \beta_1 X_3$$

Add to the model

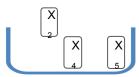


Obtain the next most significant predictor (from the remaining 4 predictor)

Model with most significant variable (say X_1)

$$Y \sim \beta_0 + \beta_1 X_3 + \beta_2 X_1$$

Add to the model



Continue until reaching the stopping rule or running out of

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Backward elimination method

Procedure

- 1. Start with a full model (model with all k predictors)
- 2. Remove the variable which is least significant (variable with largest p-value)
- 3. Fit a new model with remaining (k-1) regressors
- 4. The next variable (say X_p) is removed if it is least significant
- 5. Repeat steps (3) and (4) until reaching the stopping rule or all variables are significant



Backward elimination method

Start with a FULL MODEL (a model with all the 5 predictors)

$$Y \sim \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \beta_3 X_3 + \beta_4 X_4 + \beta_5 X_5$$

Model after removing the least significant variable (say X_3 the least significant)

$$Y \sim \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \beta_3 X_4 + \beta_4 X_5$$

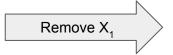
Model after removing the least significant variable (say X_1 is least significant)

$$Y \sim \beta_0 + \beta_1 X_2 + \beta_2 X_4 + \beta_3 X_5$$

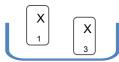
Obtain the least significant predictor (predictor having highest p-value)



Obtain the next least significant predictor (predictor having highest p-value after removing X₂)







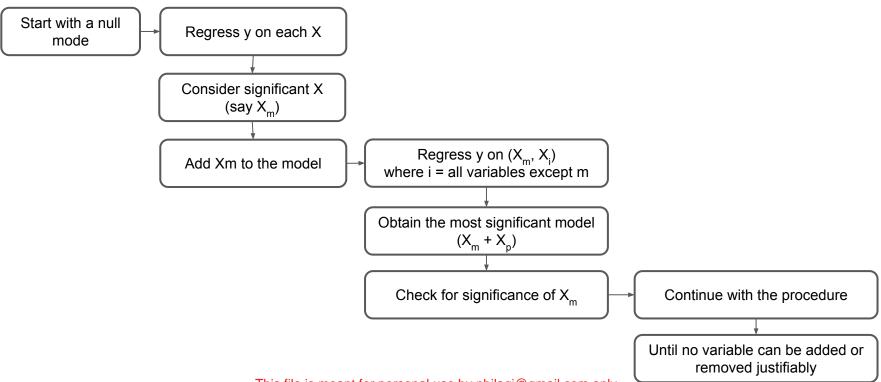




- It is a combination of forward selection and backward elimination method
- Procedure:
 - Start with a null model (with no predictors)
 - At each step add or remove variable based on its corresponding p-value
 - Stop when no variable can be added or removed justifiably

PES

Stepwise regression



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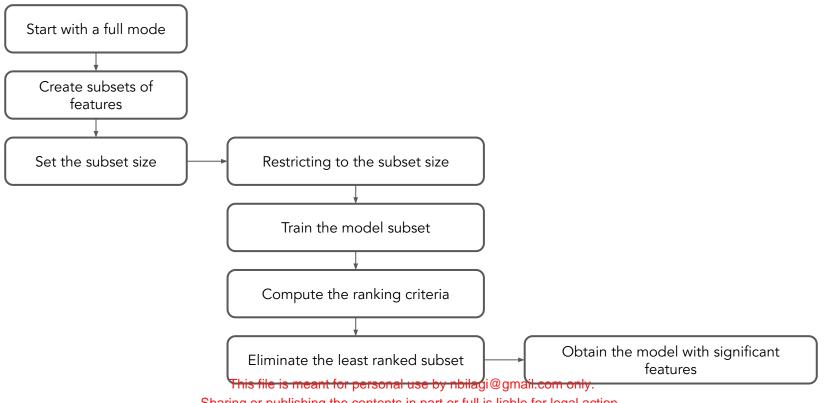


Recursive feature elimination (RFE)

- It is an instance of backward feature elimination
- Procedure:
 - Train a full model
 - Create subsets for features
 - Set the subset size
 - Compute the ranking criteria for each feature subset
 - Remove the feature subset that has the least ranking



Recursive feature elimination (RFE)



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Recursive feature elimination (RFE)

Algorithm 1: Recursive feature elimination

- 1.1 Tune/train the model on the training set using all predictors
- 1.2 Calculate model performance
- 1.3 Calculate variable importance or rankings
- 1.4 for Each subset size S_i , $i = 1 \dots S$ do
- 1.5 Keep the S_i most important variables
- 1.6 [Optional] Pre-process the data
- 1.7 Tune/train the model on the training set using S_i predictors
- 1.8 Calculate model performance
- 1.9 [Optional] Recalculate the rankings for each predictor
- 1.10 end
- 1.11 Calculate the performance profile over the S_i
- 1.12 Determine the appropriate number of predictors
- 1.13 Use the model corresponding to the optimal S_i