```
s = 0.06; \lambda_{\mu} = 0.455170; \lambda_{qd} = 42.472; \lambda_{d} = 0.053;
 a = 1/3 (1-s) \phi Subscript[\lambda, d] - \phi Subscript[\lambda, d] - Subscript[\lambda, \mu]
 -0.45517 - 0.0363933 \phi
 Simplify[a]
 -0.45517 - 0.0363933 \,\phi
b = 1/3 (1-s) \phi Subscript[\lambda, q] + \phi Subscript[\lambda, qd]
 42.472 \phi + 0.313333 \phi \lambda_{q}
c = 2/3 (1-s) \phi Subscript[\lambda, d]
 0.0332133 \phi
e = -\phi \, \text{Subscript}[\lambda, \, \mathbf{q}] + 2 \, / \, 3 \, (1 - \mathbf{s}) \, \phi \, \text{Subscript}[\lambda, \, \mathbf{q}] - \phi \, \text{Subscript}[\lambda, \, \mathbf{q}d] - \text{Subscript}[\lambda, \, \mu]
 -0.45517 - 42.472 \phi - 0.373333 \phi \lambda_{q}
Clear[d]
\lambda_1 = (a+e-(a^2+4bc-2ae+e^2)^0.5)/2
\frac{1}{2} (-0.91034 - 42.5084 \phi - 0.373333 \phi \lambda_{\rm q} -
                       ((-0.45517 - 0.0363933 \, \phi)^2 - 2 \, (-0.45517 - 0.0363933 \, \phi) \, (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.3733333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.3733333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.3733333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.3733333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.3733333 \, \phi \, \lambda_{\rm g}) + (-0.45517 - 42.472 \, \phi - 0.3733333 \,
                                          (-0.45517 - 42.472 \phi - 0.373333 \phi \lambda_g)^2 + 0.132853 \phi (42.472 \phi + 0.313333 \phi \lambda_g))^{0.5}
FullSimplify[\lambda_1]
 -0.45517 - 21.2542 \phi - 0.186667 \phi \lambda_{\sigma} - 0.5 (0. + 1806.42 \phi^2 + \phi^2 (31.7269 + 0.139378 \lambda_{\sigma}) \lambda_{\sigma})^{0.5}
\lambda_2 = (a + e + (a^2 + 4bc - 2ae + e^2)^0.5) / 2
\frac{1}{2} \left( -0.91034 - 42.5084 \phi - 0.373333 \phi \lambda_{q} + \right.
                      ((-0.45517 - 0.0363933 \, \phi)^2 - 2 \, (-0.45517 - 0.0363933 \, \phi) \, (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.45517 - 42.472 \, \phi - 0.373333 \, \phi \, \lambda_g) + (-0.4
                                          (-0.45517 - 42.472 \phi - 0.373333 \phi \lambda_{q})^{2} + 0.132853 \phi (42.472 \phi + 0.313333 \phi \lambda_{q}))^{0.5}
FullSimplify[\lambda_2]
 -0.45517 - 21.2542 \phi - 0.186667 \phi \lambda_{q} + 0.5 (0. + 1806.42 \phi^{2} + \phi^{2} (31.7269 + 0.139378 \lambda_{q}) \lambda_{q})^{0.5}
X = ((a-e)^2 + 4bc)^0.5
  \left(0.132853\,\phi\,\left(42.472\,\phi+0.313333\,\phi\,\lambda_{\rm q}\right)+\left(0.+42.4356\,\phi+0.373333\,\phi\,\lambda_{\rm q}\right)^2\right)^{0.5}
```

$$(0. + 1806.42 \phi^2 + \phi^2 (31.7269 + 0.139378 \lambda_g) \lambda_g)^{0.5}$$

0.333333 (
$$\phi$$
 (-0.39856 (1.36551 + 0.10918 ϕ) + ϕ (127.307 + 1.12 λ_{q}) 2)) $^{0.5}$

$$X1 = ((a-e) - X) / (2c)$$

$$\frac{1}{\phi}$$
15.0542 (0. + 42.4356 ϕ + 0.373333 ϕ $\lambda_{\rm q}$ -

$$\left(0.132853\,\phi\,\left(42.472\,\phi+0.313333\,\phi\,\lambda_{\mathrm{q}}\right)\,+\,\left(0.\,+\,42.4356\,\phi+0.373333\,\phi\,\lambda_{\mathrm{q}}\right)^{\,2}\right)^{\,0.5}\right)$$

FullSimplify[X1]

$$638.834 + 5.62023 \ \lambda_{\rm q} - \frac{1}{\phi} 15.0542 \ (0. + 1806.42 \ \phi^2 + \phi^2 \ (31.7269 + 0.139378 \ \lambda_{\rm q}) \ \lambda_{\rm q})^{0.5}$$

$$X2 = ((a-e) + X) / (2c)$$

$$\frac{1}{\phi} 15.0542 (0. + 42.4356 \phi + 0.373333 \phi \lambda_{q} +$$

$$(0.132853\,\phi\,\,(42.472\,\phi\,+\,0.313333\,\phi\,\,\lambda_{\rm q})\,+\,(0.\,+\,42.4356\,\phi\,+\,0.373333\,\phi\,\,\lambda_{\rm q})^{\,2})^{\,0.5})$$

FullSimplify[X2]

$$638.834 + 5.62023 \lambda_{q} + \frac{15.0542 (0. + 1806.42 \phi^{2} + \phi^{2} (31.7269 + 0.139378 \lambda_{q}) \lambda_{q})^{0.5}}{\phi}$$

 $\phi = 0.05$

0.05

$$\lambda_q = 3.98$$

3.98

FullSimplify[X]

2.19938

FullSimplify[X1]

-0.994644

FullSimplify[X2]

1323.4

$$a1 = (2X2 - 1) / (3(X2 - X1))$$

0.665914

```
a2 = (1-2X1) / (3(X2-X1))
0.000752366
{\tt FullSimplify}[\lambda_1]
-2.65472
{\tt FullSimplify}[\lambda_2]
-0.455338
Simplify[a-e]
2.19607
Simplify[X1]
-0.994644
Simplify[c]
0.00166067
Simplify[a]
-0.45699
Simplify[e]
-2.65306
\texttt{FullSimmplify[(($\lambda_d$ X1 + $\lambda_q$) (2 X2 - 1)) / (($\lambda_d$ X2 + $\lambda_q$) (1 - 2 X1))]}
FullSimmplify[46.897]
FulSimplify[a1/a2]
FulSimplify[885.094]
```