

Responsible AI:

Seminar on Fairness, Safety, Privacy and more

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Discussion

- **Ethical Implications:** How does improving adversarial robustness in AI models intersect with ethical considerations? For instance, does making a model more robust also make it more or less likely to propagate biases or misinformation?
- **Trade-offs:** There are inherent trade-offs between adversarial robustness, model performance, and computational efficiency. How do these trade-offs impact the ethical deployment of these models?
- **Transparency and Explainability:** How can transparency and explainability in AI models help in understanding and mitigating adversarial attacks? Is there a tension between the complexity required for robustness and the need for understandable models?
- **Fairness and Equity in Robust AI Systems:** In what ways might efforts to increase adversarial robustness impact the fairness and equity of AI systems? How can we ensure that these efforts do not exacerbate existing inequalities?
- **LLMs:** How do adversarial attacks on large language models differ from those on other types of machine learning models, and what unique challenges do they present?
- **Responsibility and Accountability:** Who should be held accountable for failures in AI systems due to adversarial attacks – the developers, the users, or the AI itself?
- **Global Perspectives on AI Robustness:** How do perspectives on AI robustness and ethics vary across different cultures and countries? What can be learned from these diverse viewpoints?

Differential Privacy

Foundations and Applications

Part I: Foundation

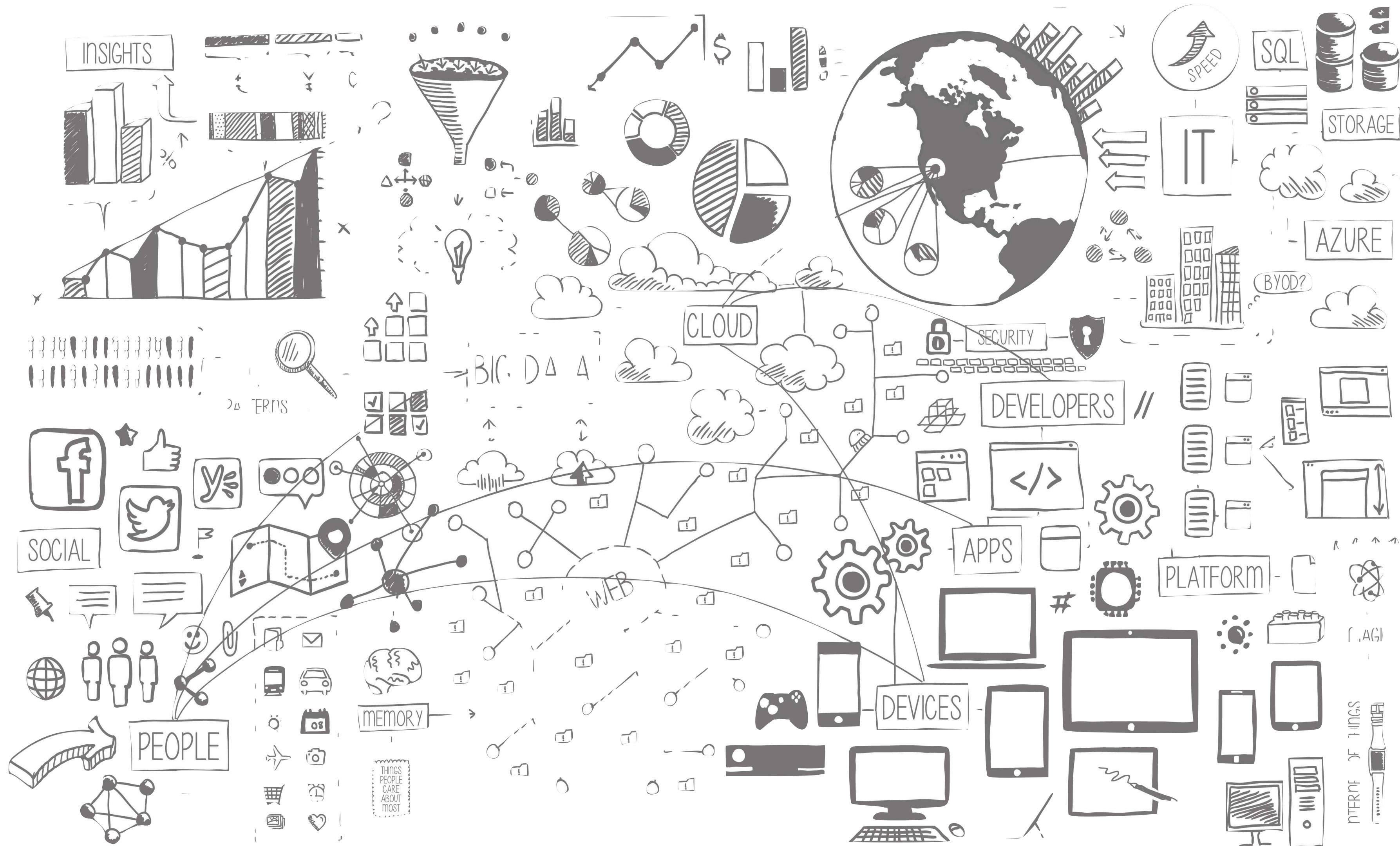
- Privacy and Attack models
- Differential Privacy
- Common algorithms

Part II: DP issues

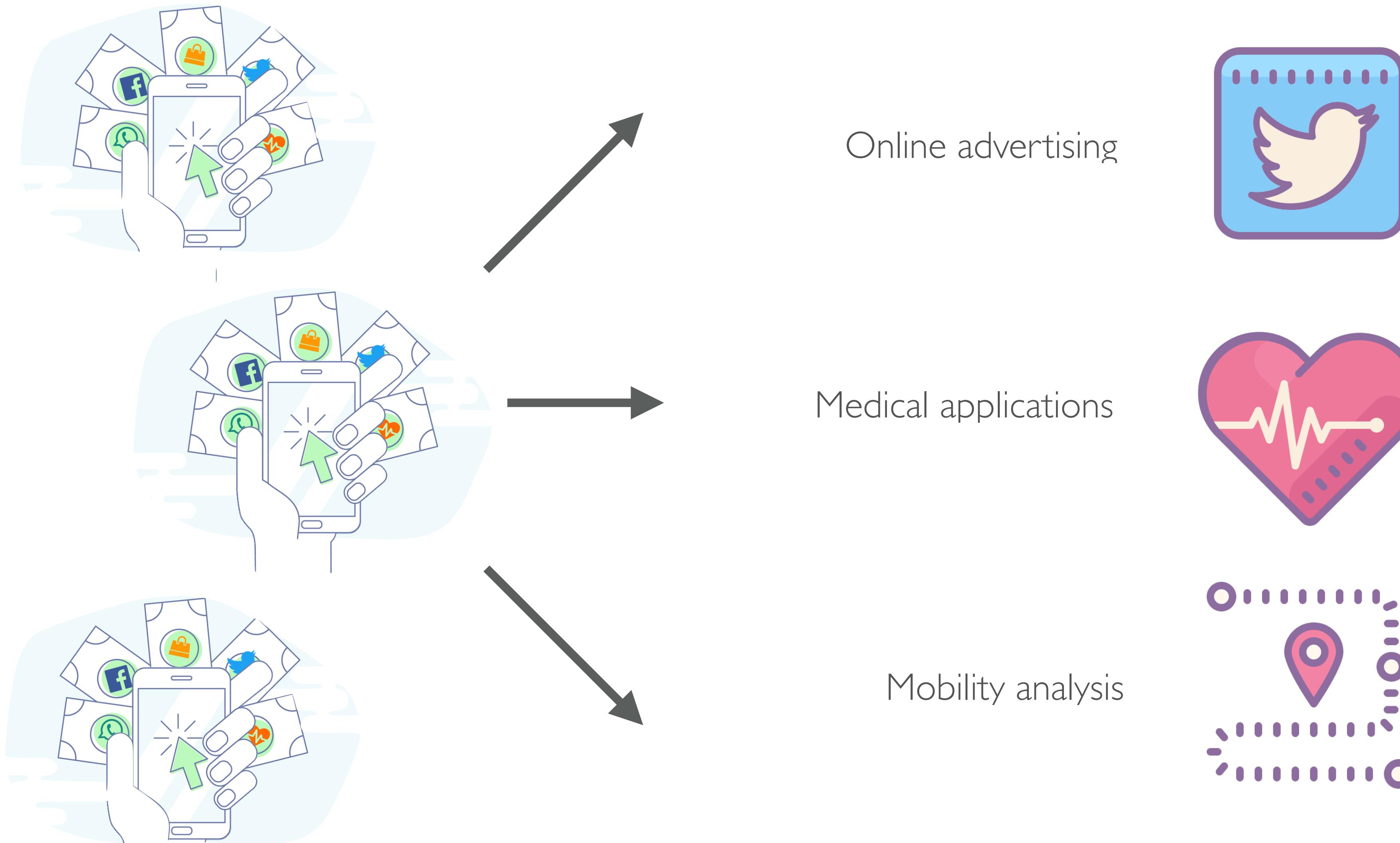
- Consistency

Part I: Foundation

We live in a data-driven world



Aggregated Personal Data is Invaluable



Releasing Personal Data can be Harmful Beyond Your Consent



Would your
relatives consent?

Major DNA testing company is sharing genetic data with the FBI

By BLOOMBERG FEB 01, 2019 | 2:55 PM



Releasing Personal Data can be Harmful Beyond Your Consent



Fitness tracking app Strava gives away location of secret US army bases

Data about exercise routes shared online by soldiers can be used to pinpoint overseas facilities

Data Breaches and Cost of Privacy

The average global cost of data breaches is \$3.86M (2019)

[IBM study]

The screenshot shows three news articles from NBC News:

- The total cost of a data breach – including lost business – keeps growing** (Headline: "Failure to respond urgently, transparently, and with empathy can result in a near extinction-level event.")
- How Snapchat's new Snap Map is stoking privacy and terrorism fears** (Published: July 30, 2018, 3:15 PM EDT / Updated July 30, 2018, 3:15 PM EDT)
- Facebook's worst year ever is now over. Here's how its scandals affected the stock** (List items: After a year of scandals, Facebook's stock ended the year lower than the previous one for the first time since its debut on the public market in 2012. The stock tanked 25.7 percent in 2018.)

The screenshot shows two news articles from Vox and Recode:

Vox **recode**

23andMe laid off 100 employees due to slowing DNA kit sales

Privacy concerns likely factored into decreased demand.

By Rani Molla | @ranimolla | Jan. 22, 2020, 2:50 pm EST

CNBC **TECH** **MARKETS** **BUSINESS** **INVESTING** **TECH** **POLITICS** **CNBC TV** **Q**

Ancestry to lay off 6% of workforce because of a slowdown in the consumer DNA-testing market

PUBLISHED WED, FEB 5 2020 5:07 PM EST | UPDATED WED, FEB 5 2020 5:40 PM EST

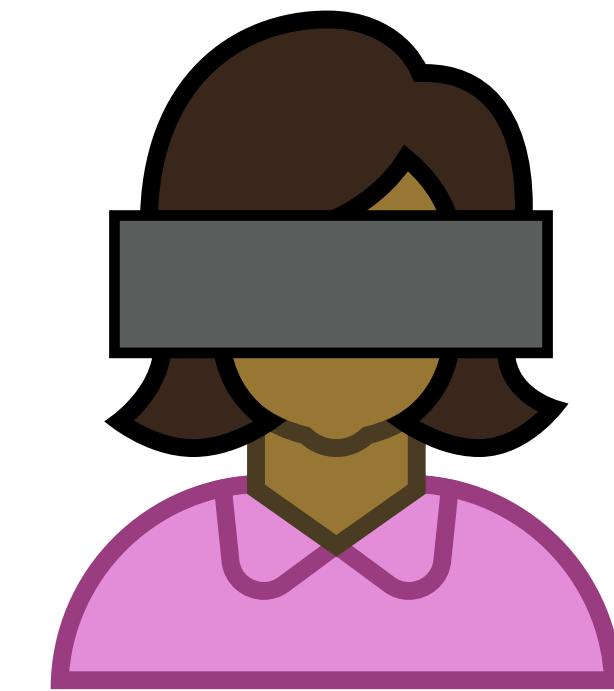
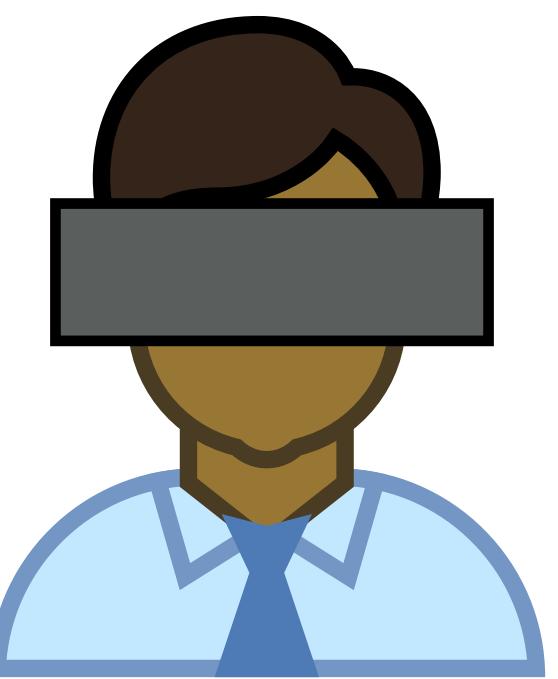
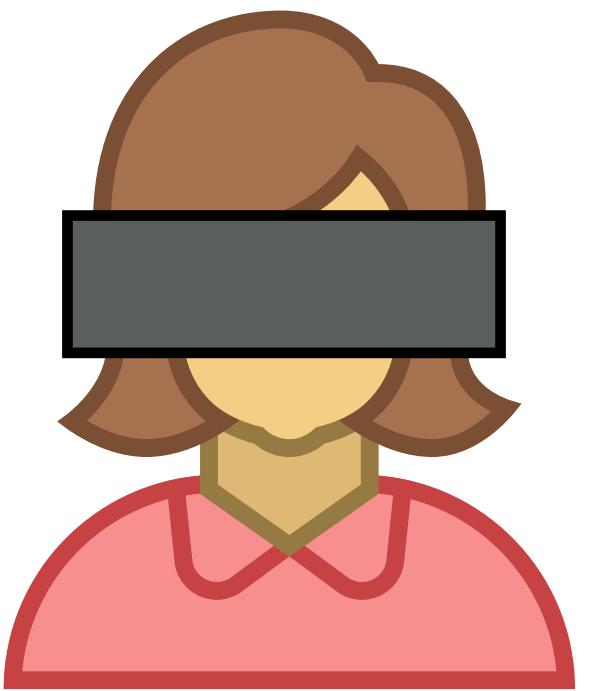
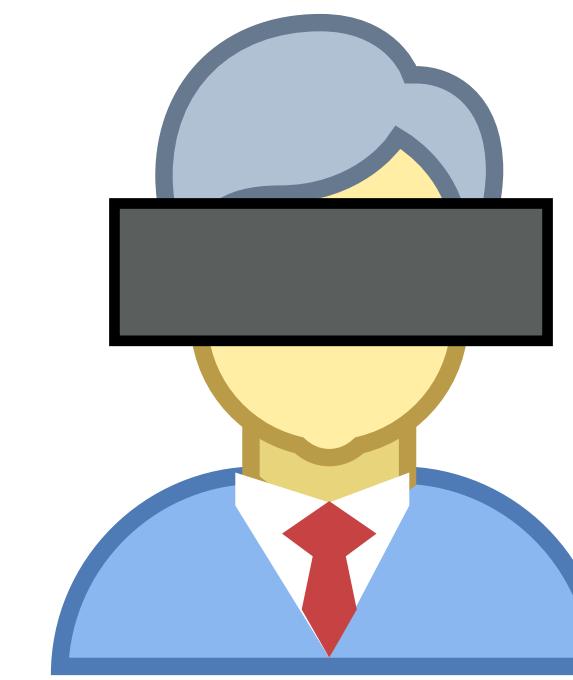
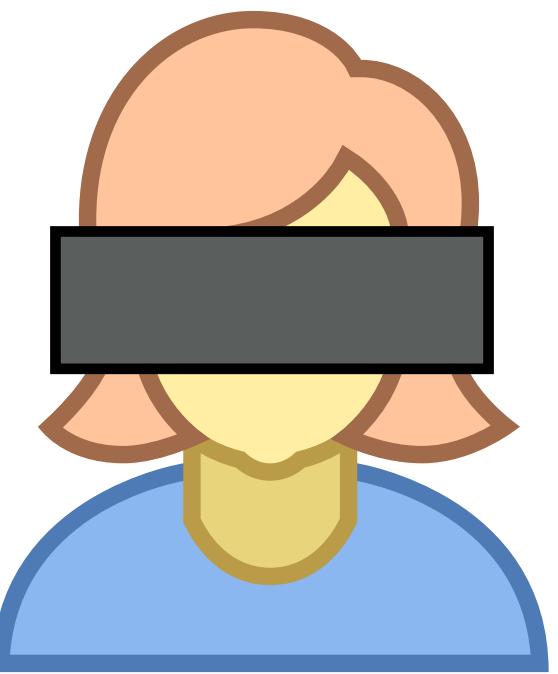
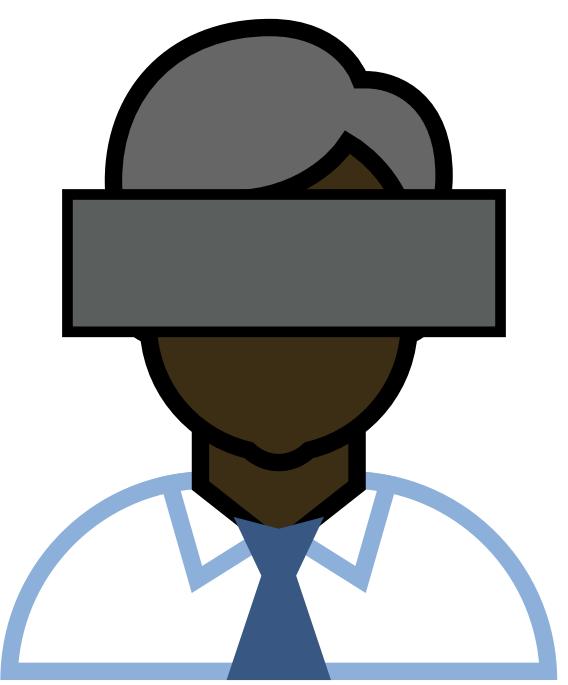
Christina Farr
@CHRISSEYFARR

SHARE

KEY POINTS

- Ancestry, following 23andMe, made the decision to lay off some employees. It confirmed to CNBC that the cuts affected 6% of its workforce.
- A spokesperson described the decision as one the company "did not take lightly."
- Sales of consumer DNA tests are down, and privacy is likely a major factor.

Data Anonymization



How do you keep survey data private?

- The census bureau is supposed to keep the collected information confidential.
- How can you retain privacy while publishing results about the survey?

user	age	gender
Margaret	31	F
Luis	49	M
Maria	26	F
Carl	19	M
Isabelle	27	F

How do you keep survey data private?

- How can you retain privacy while publishing results about the survey?
- **Database Reconstruction Theorem:** Every information released contributes to violate the privacy of an individual. The more information it is publicly released the more privacy is violated.

user	age	gender	
Margaret	31	F	Avg.: 30.4
Luis	49	M	
Maria	26	F	Avg.: 34
Carl	19	M	Male
Isabelle	27	F	Avg.: 28
			Female

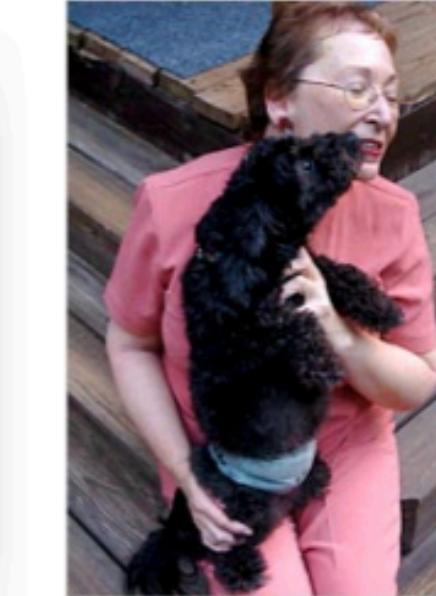


Anonymization is not Enough

A Face Is Exposed for AOL Searcher No. 4417749

By MICHAEL BARBARO and TOM ZELLER Jr.
Published: August 9, 2006

 SIGN IN TO E-
THIS



Why 'Anonymous' Data Sometimes Isn't

By Bruce Schneier  12.13.07

Last year, Netflix published 10 million movie rankings by 500,000 customers, as part of a challenge for people to come up with better recommendation systems than the one the company was using.

The Scientist » The Nutshell

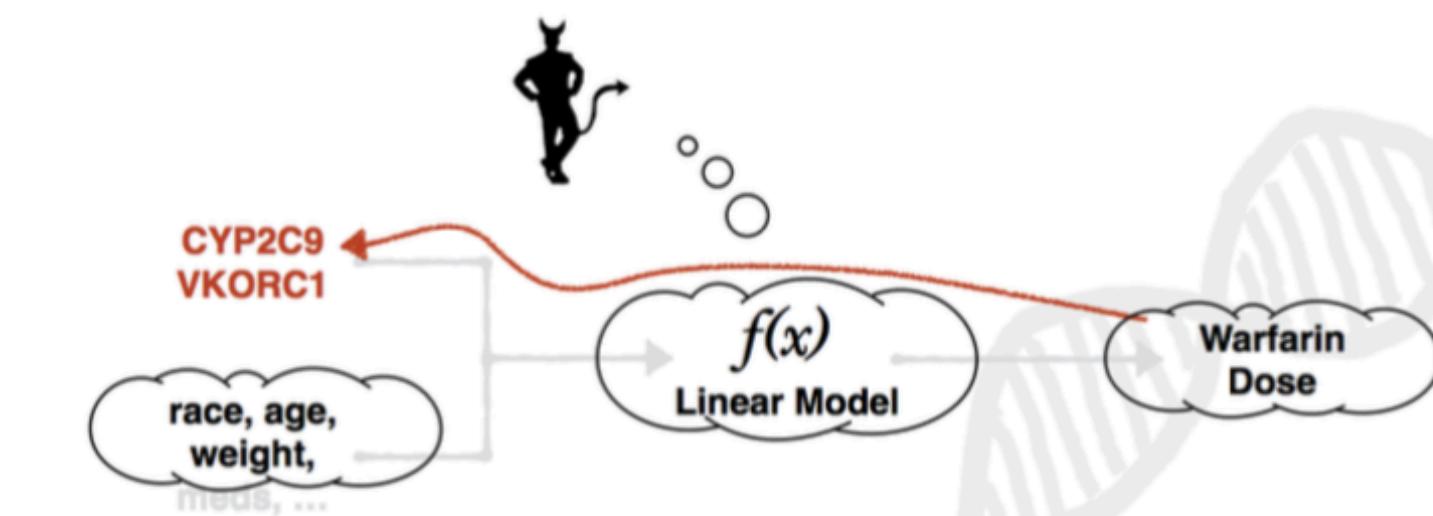
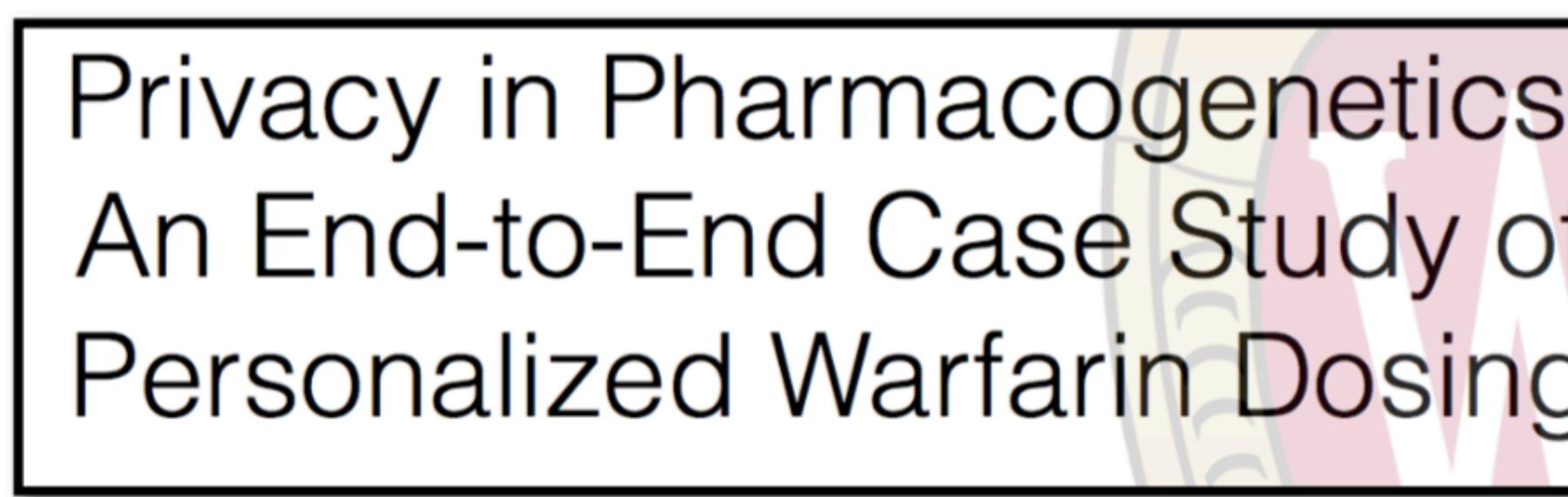
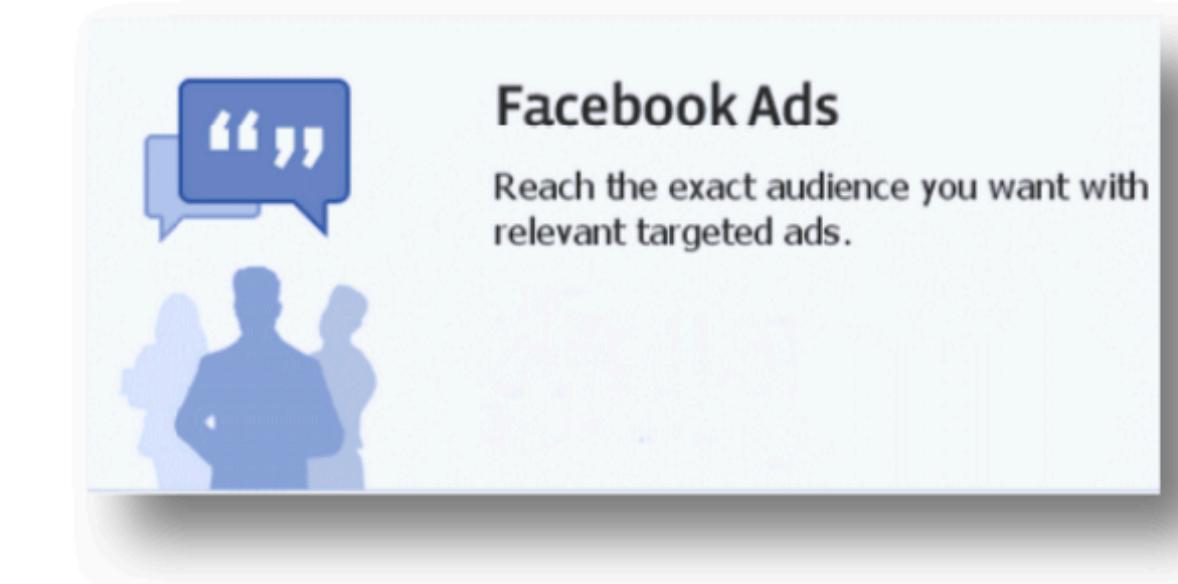
“Anonymous” Genomes Identified

The names and addresses of people participating in the Personal Genome Project can be easily tracked down despite such data being left off their online profiles.

By Dan Cossins | May 3, 2013



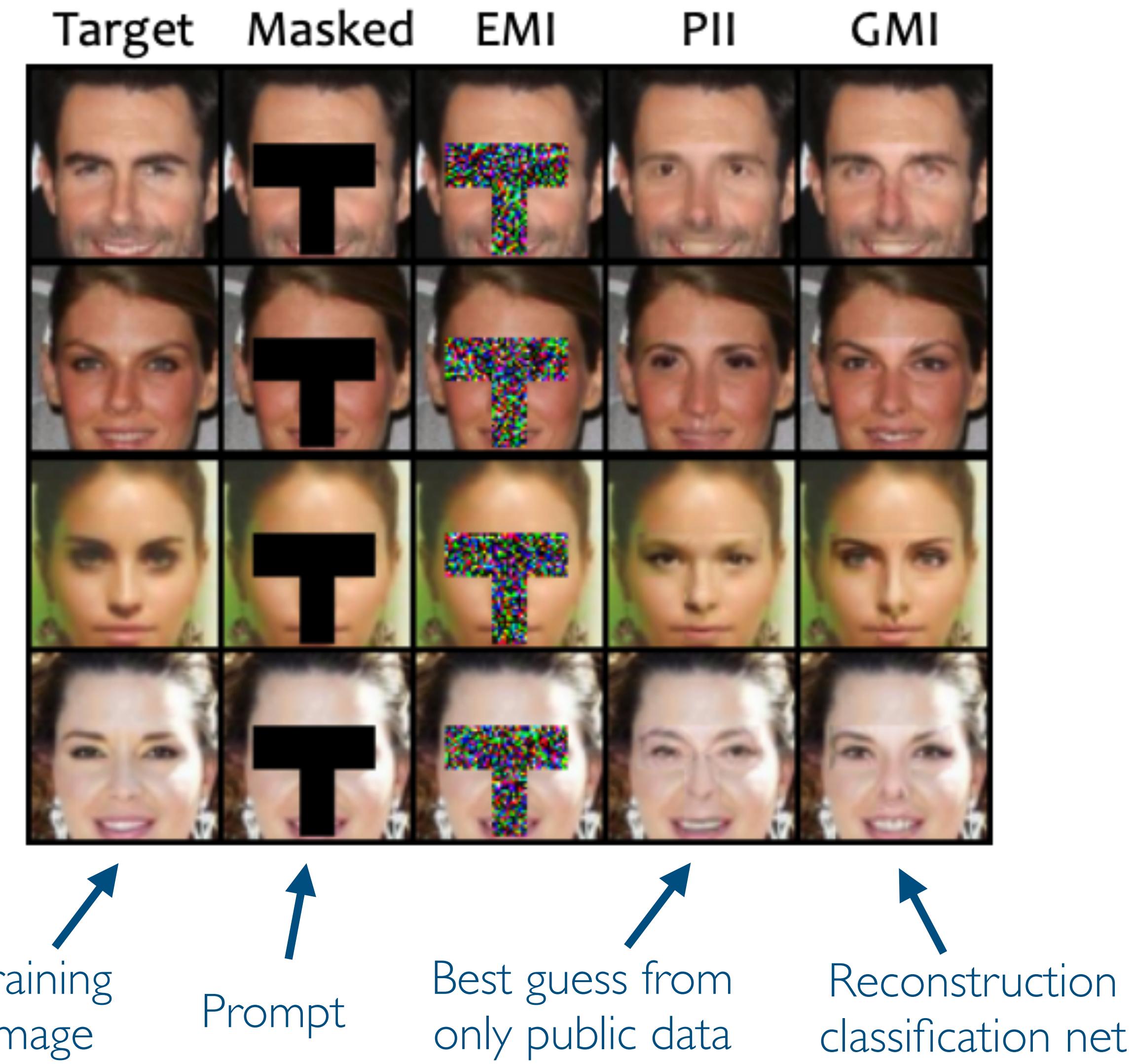
Anonymization is not Enough



Why Anonymization is Hard?

Model inversion attacks

- Even if you don't release the raw data, the weights of a trained network might reveal sensitive information.
- Model inversion: recover information about the training data from the trained model.
- Example from a face recognition dataset, given a classifier trained on this dataset and a generative model trained on an unrelated dataset of publicly available images.

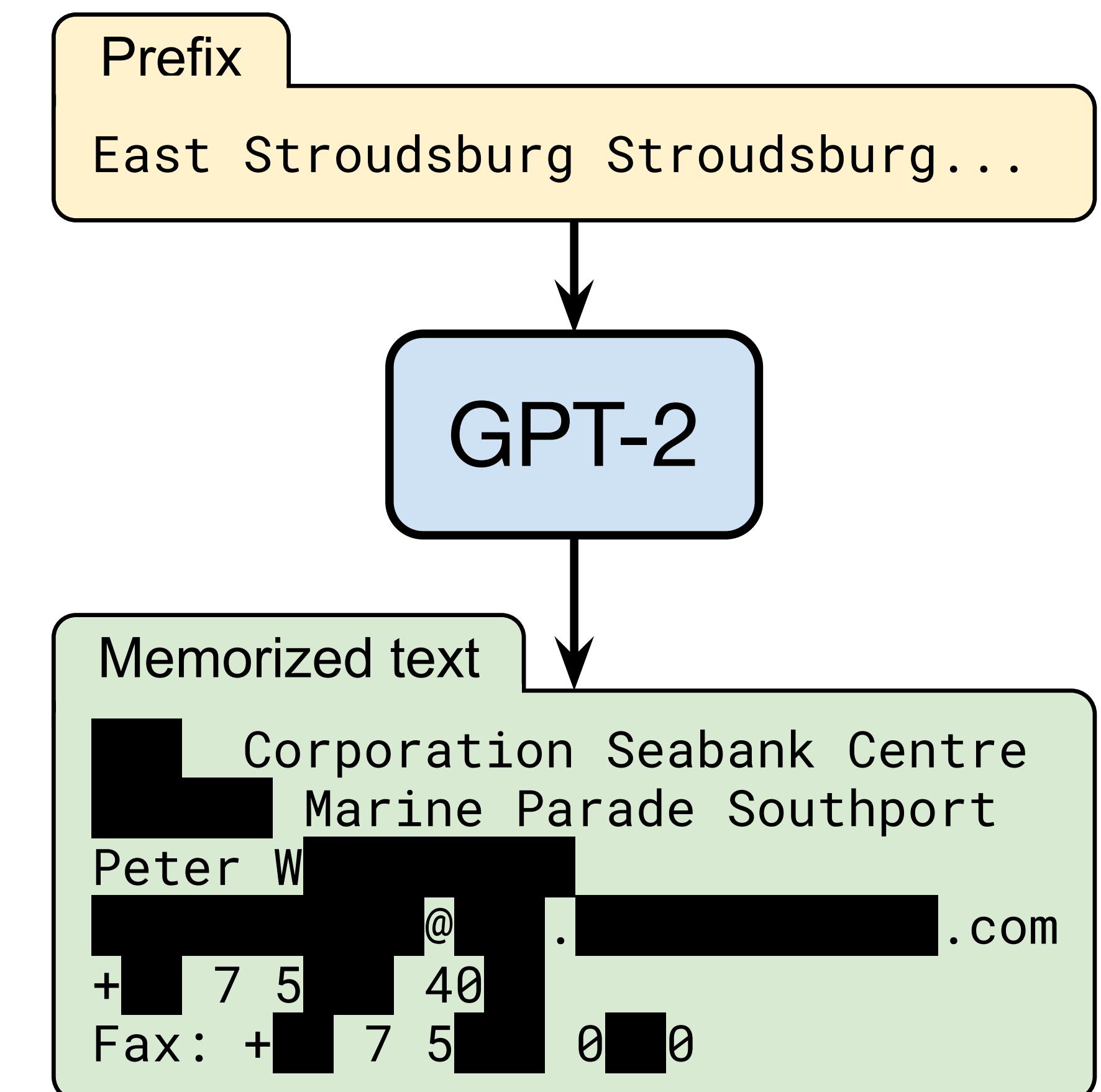


Source: Zhang et al., "The secret revealer: Generative model-inversion attacks against deep neural networks." <https://arxiv.org/abs/1911.07135>

Why Anonymization is Hard?

Extraction attacks

- Language models trained on scrapes of the public Internet.
- Extraction attack: extracts verbatim text sequences from the model's training data.
- Example from a GPT-2 model. Given query access, it extracts an individual person's name, email address, phone number, fax number, and physical address.



Why Anonymization is Hard?

Reconstruction attacks



U.S. Department of Commerce
Economics and Statistics Administration
U.S. CENSUS BUREAU
census.gov



Commercial databases

308,745,548 people in 2010 release which implements some “protection”

Linkage Attacks — Results from UC Census:

- Census blocks correctly reconstructed in all 6,207,027, inhabited blocks.
- Block, sex, age, race, ethnicity reconstructed:
 - Exactly: 46% of population (142M).
 - Allowing age +/- 1 year: 71% of population (219M).
- Name, block sex, age, race, ethnicity:
 - Confirmed re-identification: 38% of population.

Why Anonymization is Hard?

Needs for guarantees

- It's hard to guess what capabilities attackers will have, especially decades into the future.
- **Analogy with crypto:** Cryptosystems today are designed based on what quantum computers might be able to do in 30 years.
- To defend against unknown capabilities, **we need mathematical guarantees.**
- **Want to guarantee:** no individual is directly harmed (e.g. through release of sensitive information) by being part of the database, even if the attacker has tons of data and computation.



Part I: Foundation

Privacy Definitions

Privacy is NOT Encryption

- **Encryption:**
 - Alice sends a message to Bob s.t. Trudy (the attacker) does not learn the message.
 - Bob should get the correct message
- **Statistical Dataset Privacy :**
 - Trudy can access the dataset
 - It must learn aggregate statistics, but
 - Must **not learn new info** about the individuals in the dataset

Privacy is NOT Secure multiparty computation

- **Secure Multiparty Computation:**
 - A set of agents, each with private input x_i
 - Want to compute a function $f(x_1, \dots, x_k)$
 - Each agent can learn the true answer, but must not learn any other info than what can be inferred from their private input and the answer.
- **Statistical Dataset Privacy :**
 - The function output **must not disclose** individual inputs.

What is privacy?

Privacy breach

A private mechanism $M(D)$ that allows an unauthorized party P to learn sensitive information about any individual in D that P could not have learnt with access to $M(D)$

What is privacy?

The smoking causes cancer case

Alice



Alice has
Cancer

Is this a privacy breach?

What is privacy?

Privacy Breach (revisited)

A private mechanism $M(D)$ that allows an unauthorized party P to learn sensitive information about any individual x in D that P could not have learnt with access to $M(D)$, **if x was not in D**

Brief Summary

- Statistical dataset privacy is the problem of releasing aggregate statistics while not disclosing individual records
- The problem is distinct from encryption and secure computation
- Defining privacy is non-trivial:
 - Requirements include resilience to background knowledge, as well as composition and closure under post-processing.

Randomized Response

Early privacy

Randomized response is a survey technique that ensures some level of privacy.

Example: Have you ever dodged your taxes?

1. Flip a coin.
2. If the coin lands Heads, then **answer truthfully**.
3. If it lands Tails, then flip it again.

Probability of responses

1. If it lands Heads, then answer **Yes**.
2. If it lands Tails, then answer **No**.

	Yes	No
Dodge	$\frac{3}{4}$	$\frac{1}{4}$
No Dodge	$\frac{1}{4}$	$\frac{3}{4}$

Randomized Response

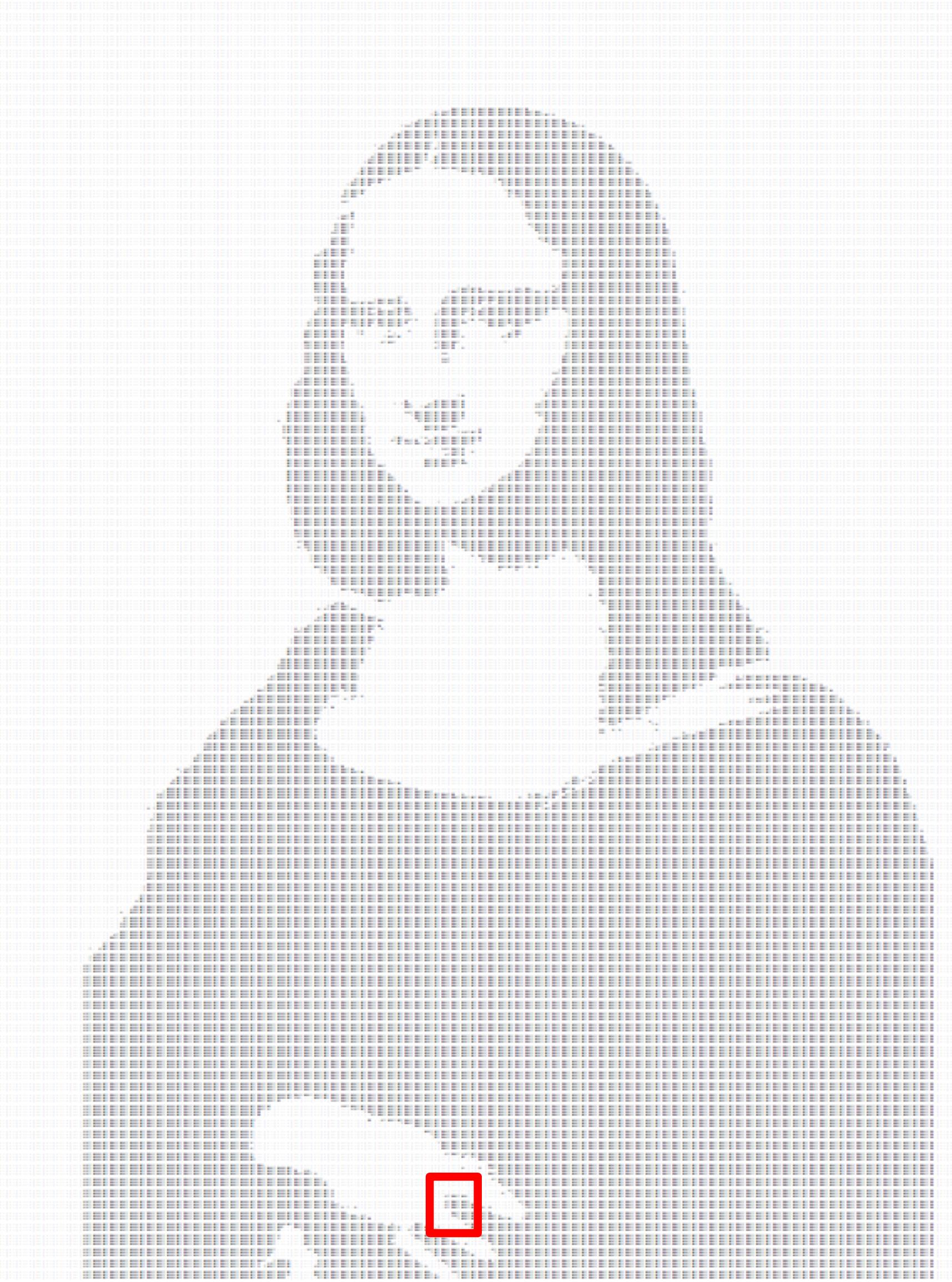
Early privacy

- Tammy, the tax investigator assigns a prior probability of 0.02 to Bob having dodged his taxes. Then she noticed he answered **Yes** to the survey.
- What is her posterior probability?

$$\begin{aligned}\Pr(\text{Dodge} \mid \text{Yes}) &= \frac{\Pr(\text{Dodge}) \Pr(\text{Yes} \mid \text{Dodge})}{\Pr(\text{Dodge}) \Pr(\text{Yes} \mid \text{Dodge}) + \Pr(\text{NoDodge}) \Pr(\text{Yes} \mid \text{NoDodge})} \\ &= \frac{0.02 \cdot \frac{3}{4}}{0.02 \cdot \frac{3}{4} + 0.98 \cdot \frac{1}{4}} \\ &\approx 0.058\end{aligned}$$

- Tammy's beliefs haven't shifted too much.
- Randomness turns out to be a useful technique for preventing information leakage.

A Metaphor for Private Learning



A Metaphor for Private Learning

An individual's training data

A Metaphor for Private Learning

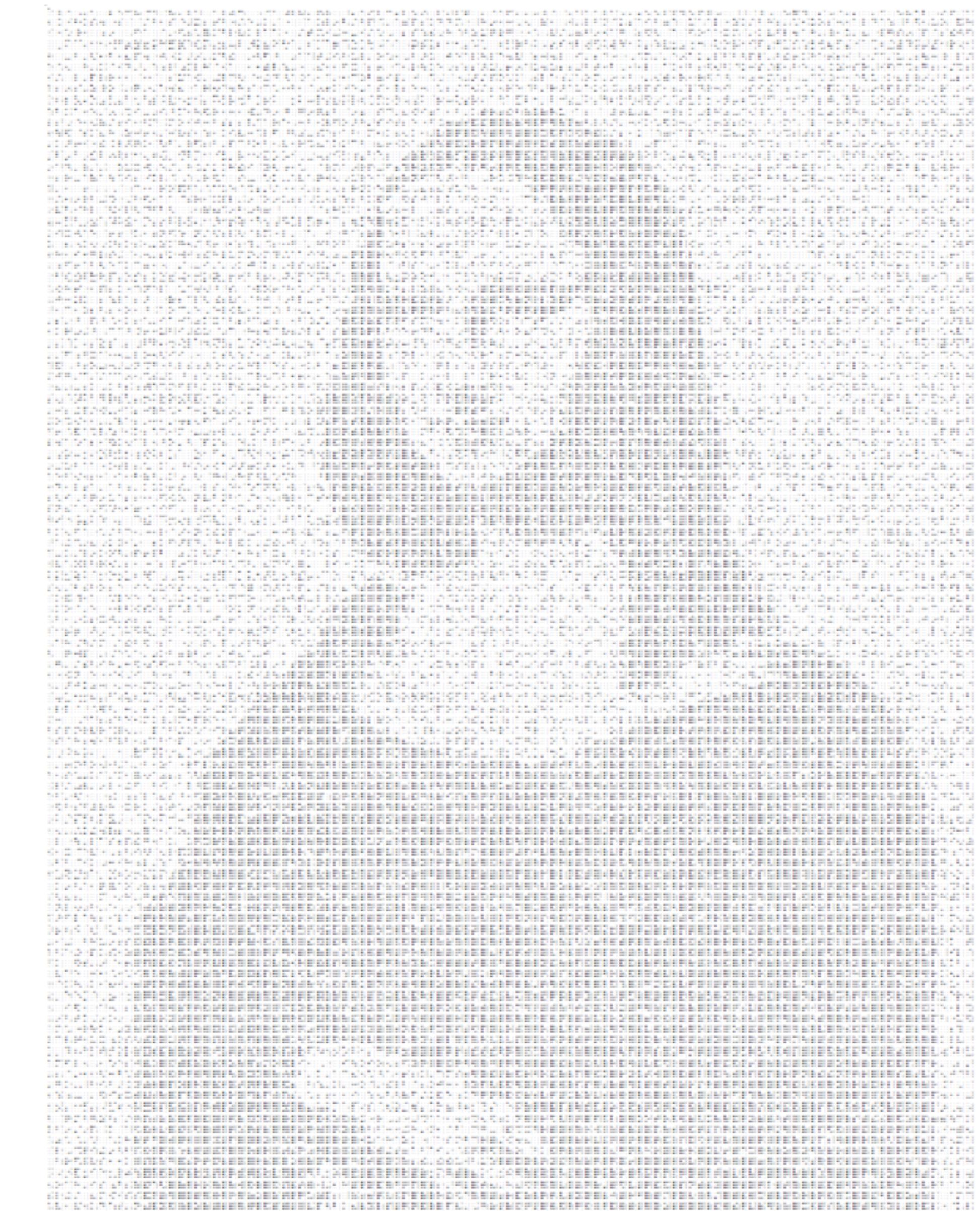
An individual's training data

Each bit is flipped with probability 51%

.....M.....MM.M.....MMM.M..
.....M.....MM.....MM...MMMM...
....M..MM.MM..MMM.M.MM.M...M..MM..
.MM.....MM.....MMMMMM...M...MM
.M.....M.....MM..MM...MM...M...
M.....M..MM.MMM...MM...MM...M...
....M....M.M.M.MMM...MM...MM...
...M....M.MM.M.MM..M..M..MM.MMM...
M...M.M....M.M..M..MM.MMM...MM...
.MM.M....M.M.M....MM...MM...M

A Metaphor for Private Learning

Big picture remains!

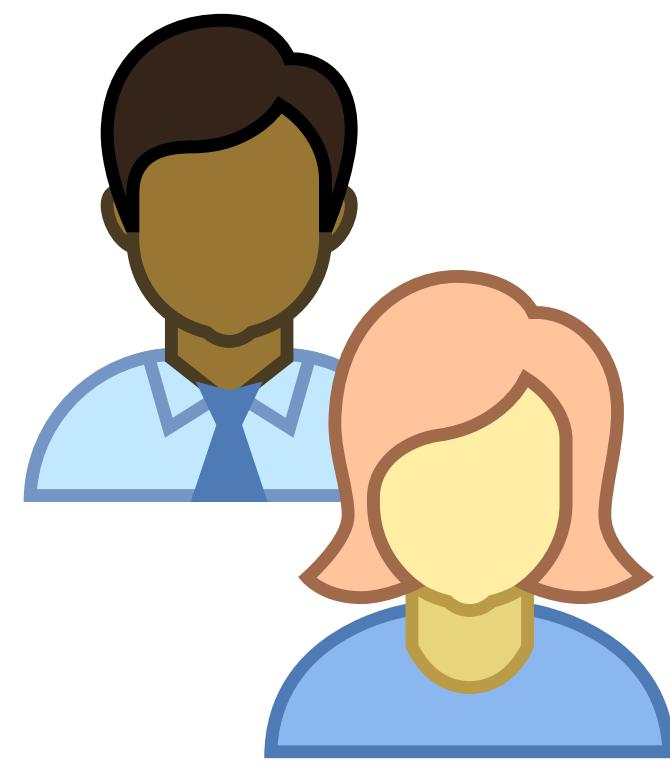


Part I: Foundation

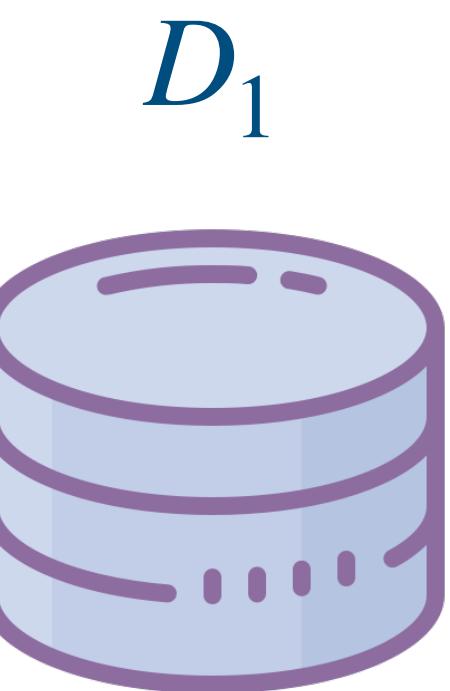
Differential Privacy

Differential Privacy

Intuition



Dataset

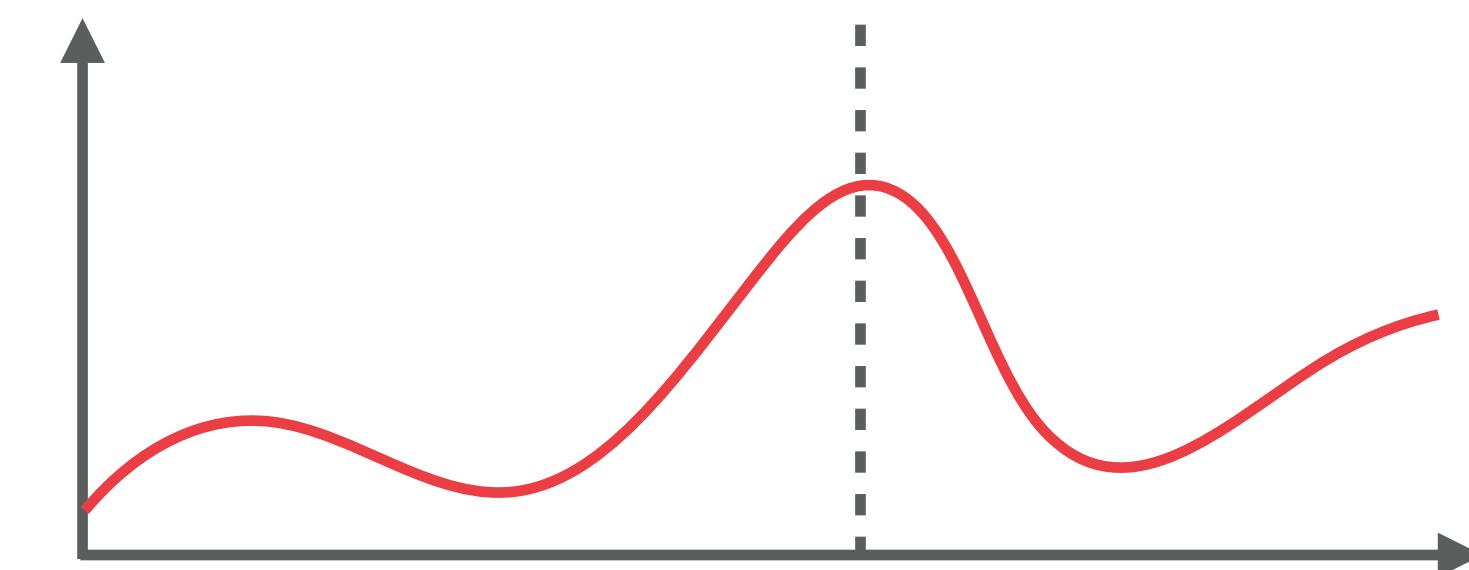


query/alg.

$A(D_1)$

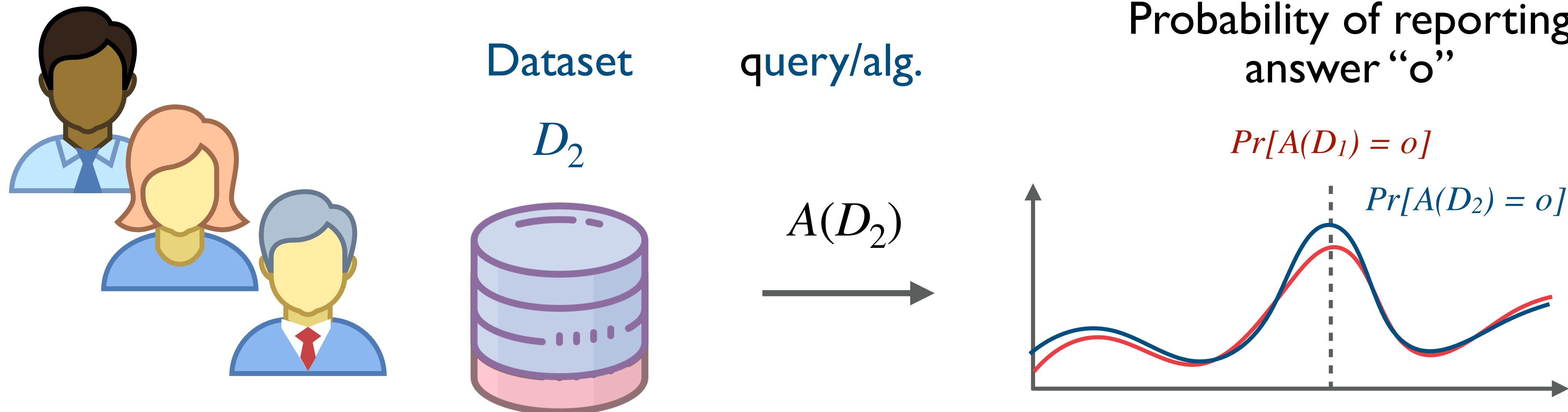
Probability of reporting
answer “o”

$$Pr[A(D_1) = o]$$



Differential Privacy

Intuition

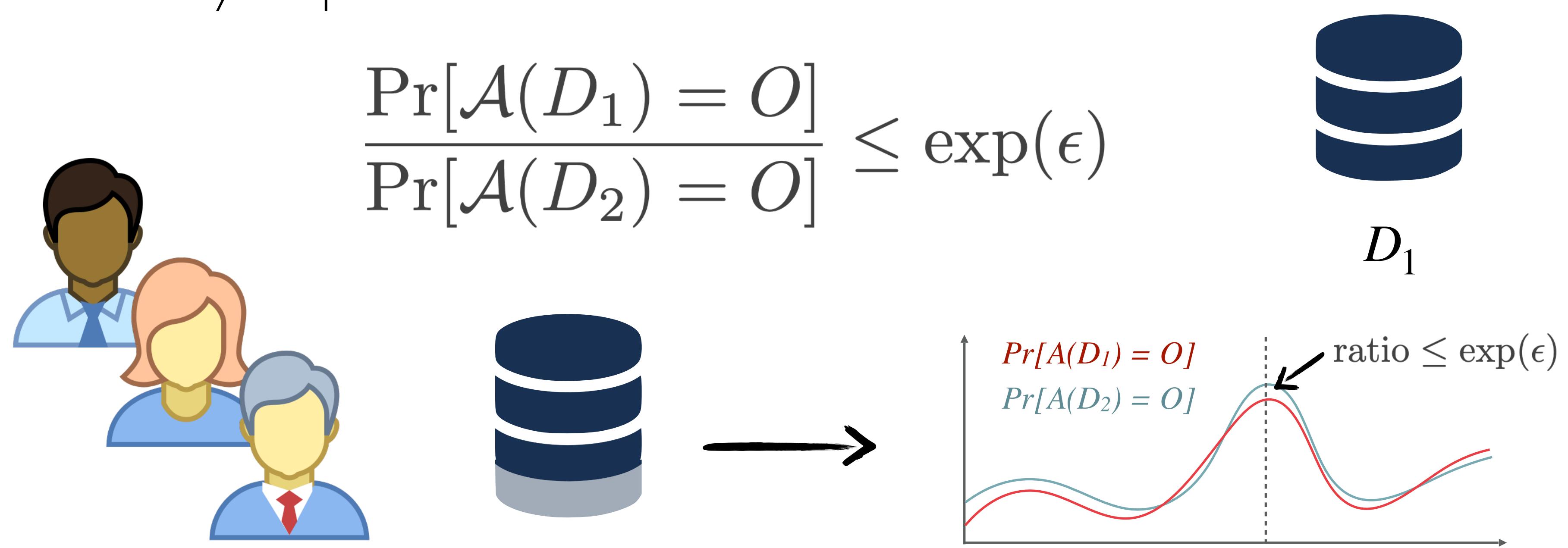


Should not be able do distinguish between weather the input was D1 or D2 no matter what the output is

Differential Privacy

Definition

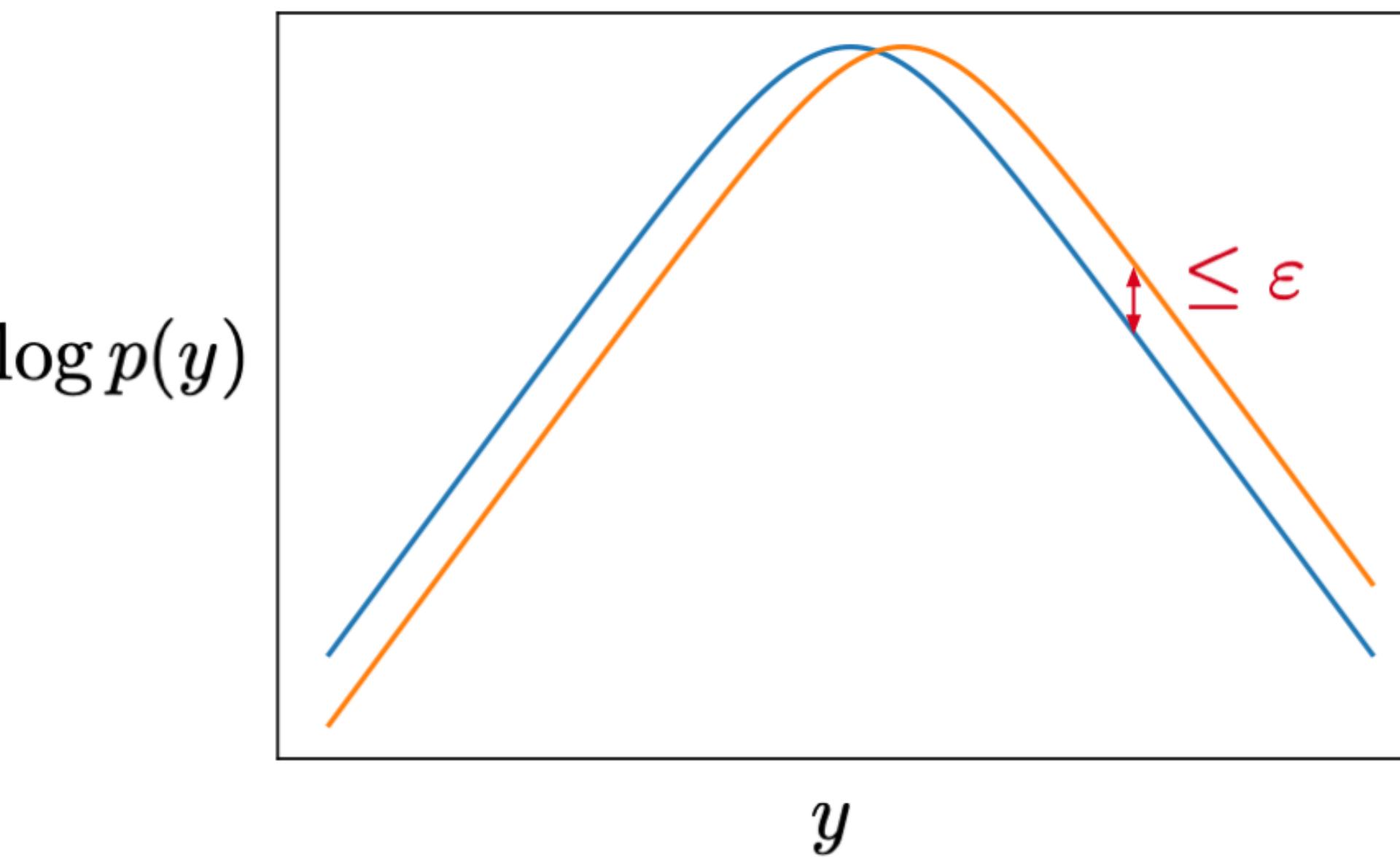
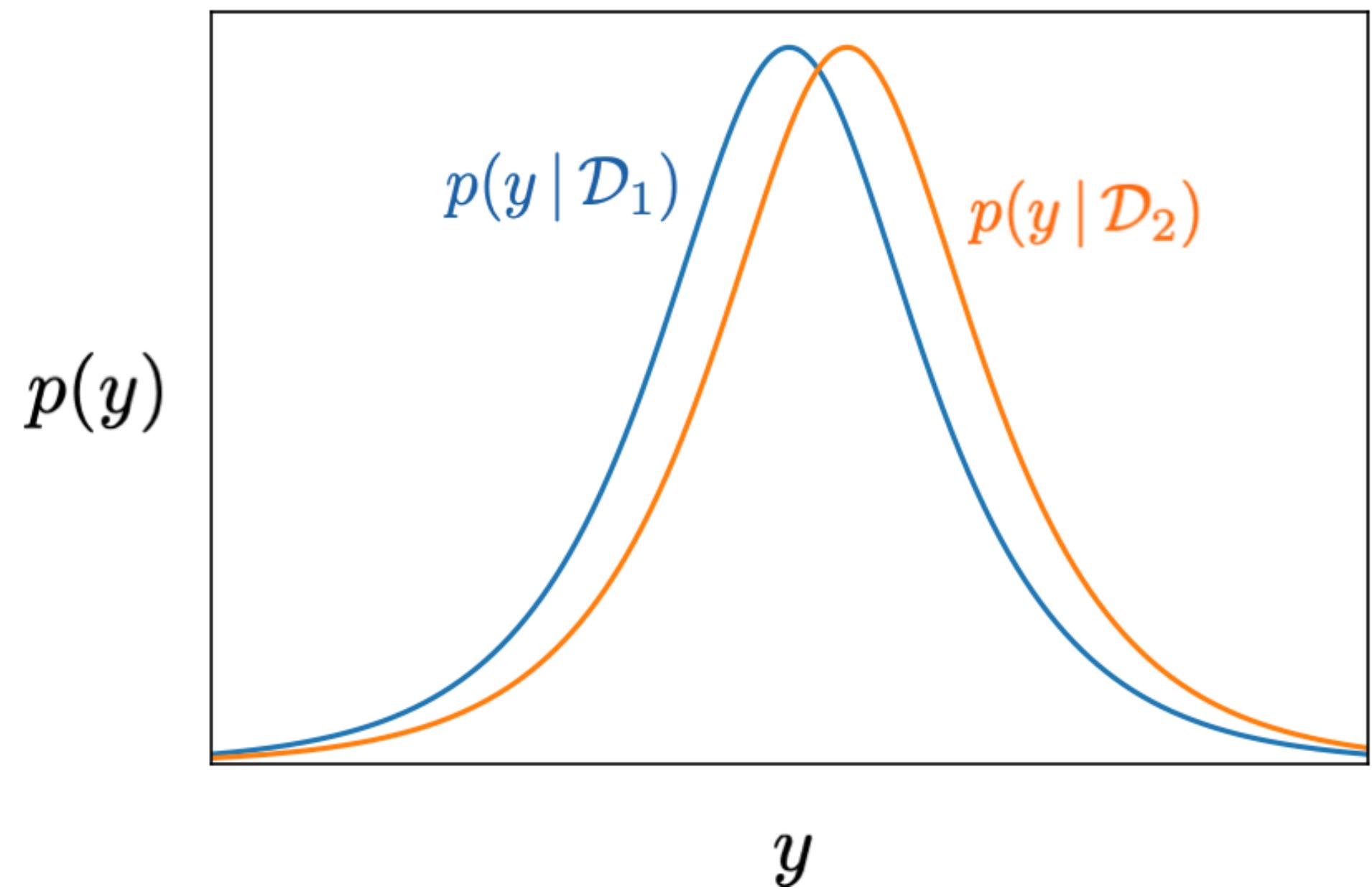
A randomized algorithm \mathcal{A} is ϵ -differentially private if, for all pairs of inputs D_1, D_2 , differing in one entry, and for any output O :



Intuition: An adversary should not be able to use output O to distinguish between any D_1 and D_2 .

Differential Privacy

Visually



- Notice that the tail behavior is important!

Differential Privacy

What can we infer?

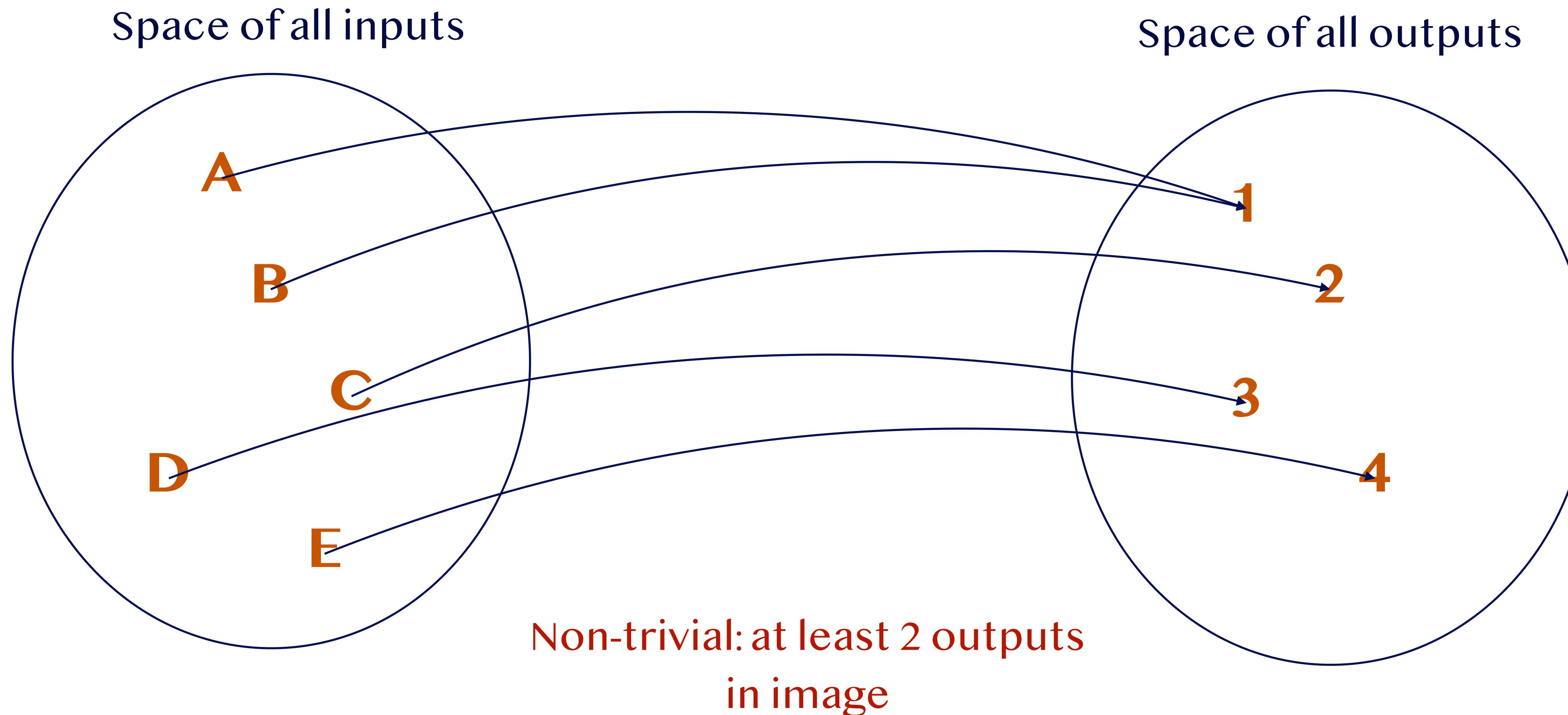
- Alice is an attacker who wants to figure out if $\text{Bob}(x)$ is in the cancer database D . Her prior for him being in the database is **0.4**. D is ϵ -differentially private. She makes a query and gets back $y = M(D)$.
- After observing y , she computes the posterior using Bayes' rule:

$$\begin{aligned}\Pr(x \in D | y) &= \frac{\Pr(x \in D) \Pr(y | x \in D)}{\Pr(x \in D) \Pr(y | x \in D) + \Pr(x \notin D) \Pr(y | x \notin D)} \\ &\geq \frac{\Pr(x \in D) \Pr(y | x \in D)}{\Pr(x \in D) \Pr(y | x \in D) + \exp(\epsilon) \Pr(x \notin D) \Pr(y | x \in D)} \\ &= \frac{\Pr(x \in D)}{\Pr(x \in D) + \exp(\epsilon) \Pr(x \notin D)} \\ &\geq 0.4 \exp(-\epsilon)\end{aligned}$$

- Similarly $\Pr(x \in D | y) \leq 0.4 \exp(\epsilon)$ so Alice hasn't learned much about Bob.

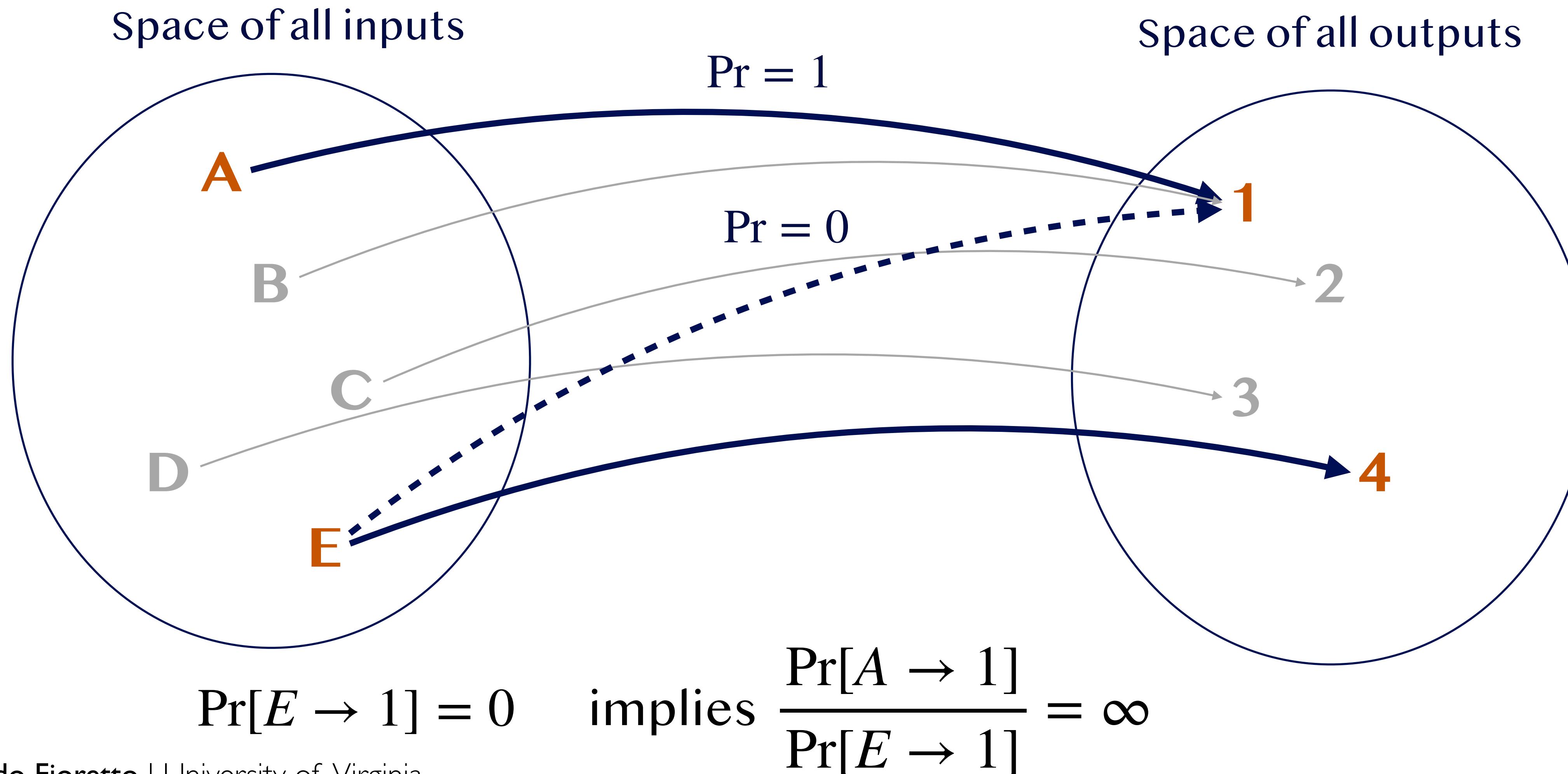
Differentially Private Algorithms

Can Non-trivial Deterministic Algorithms Satisfy DP?

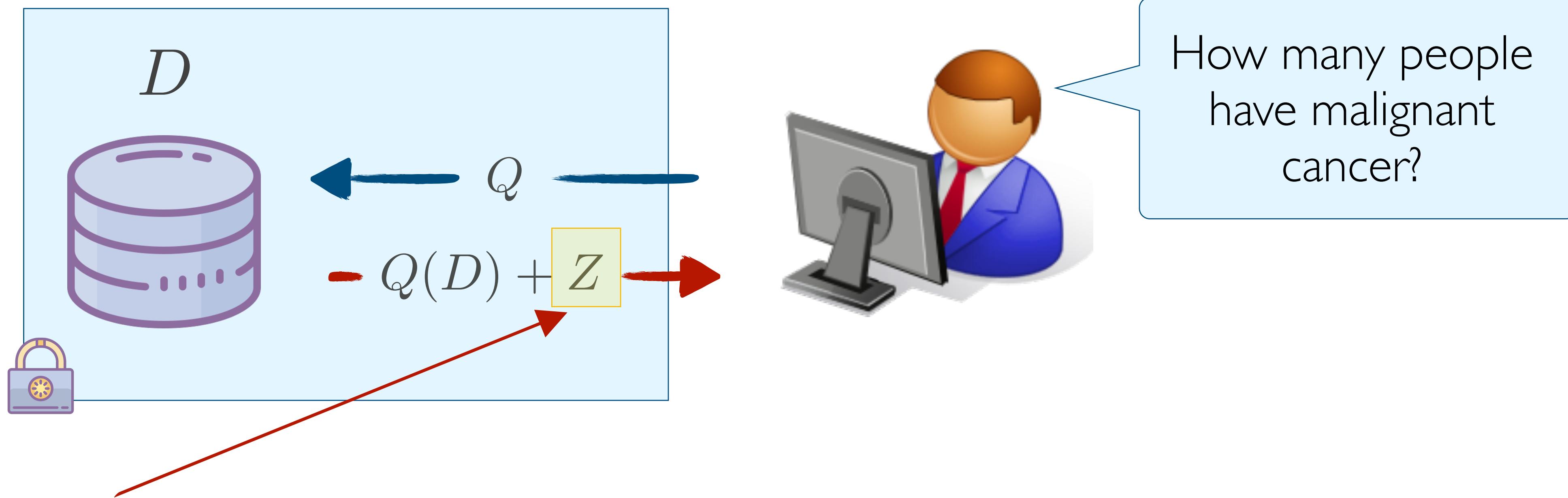


Differentially Private Algorithms

Can Non-trivial Deterministic Algorithms Satisfy DP?



How do we design DP algorithms?

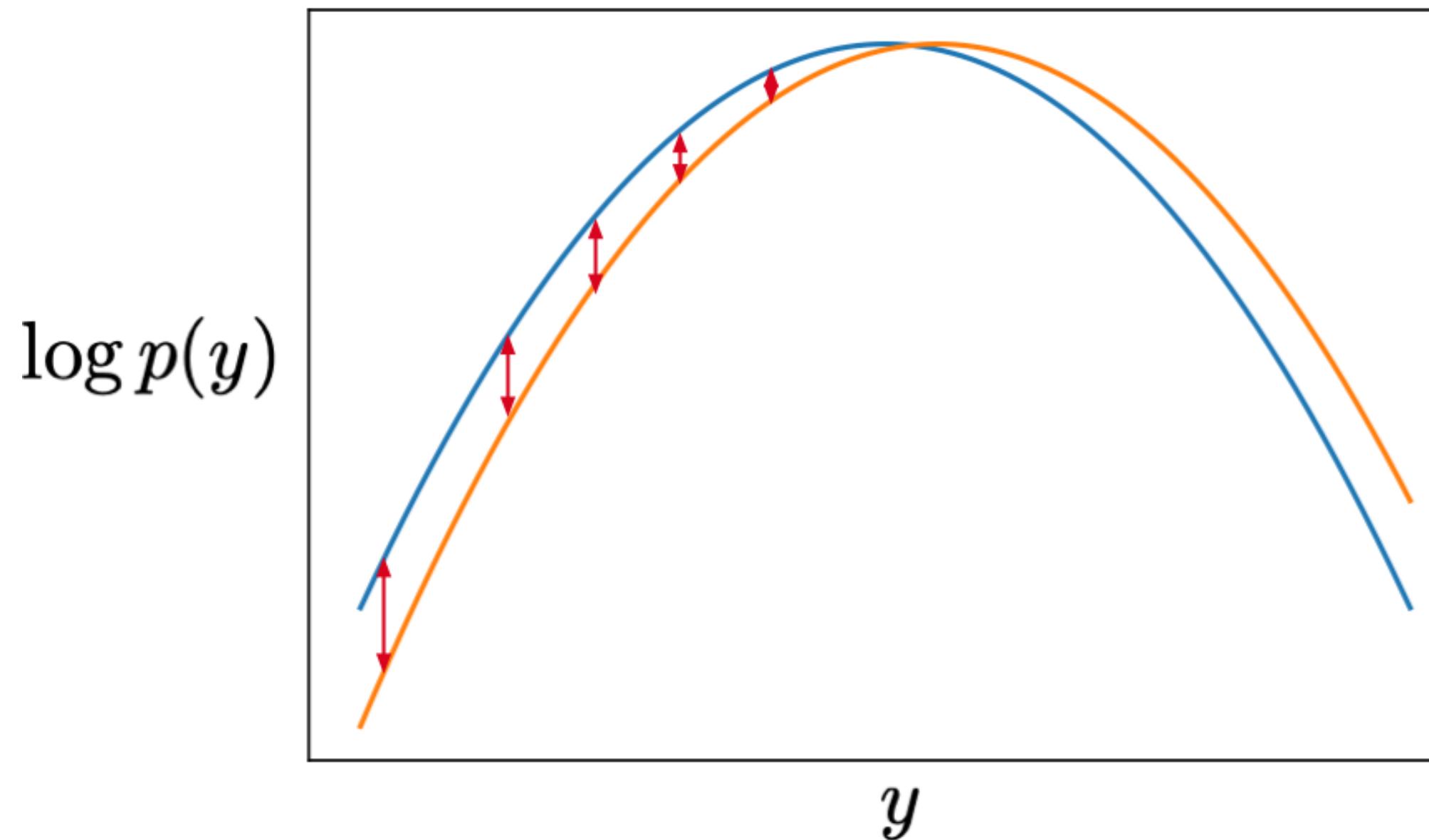
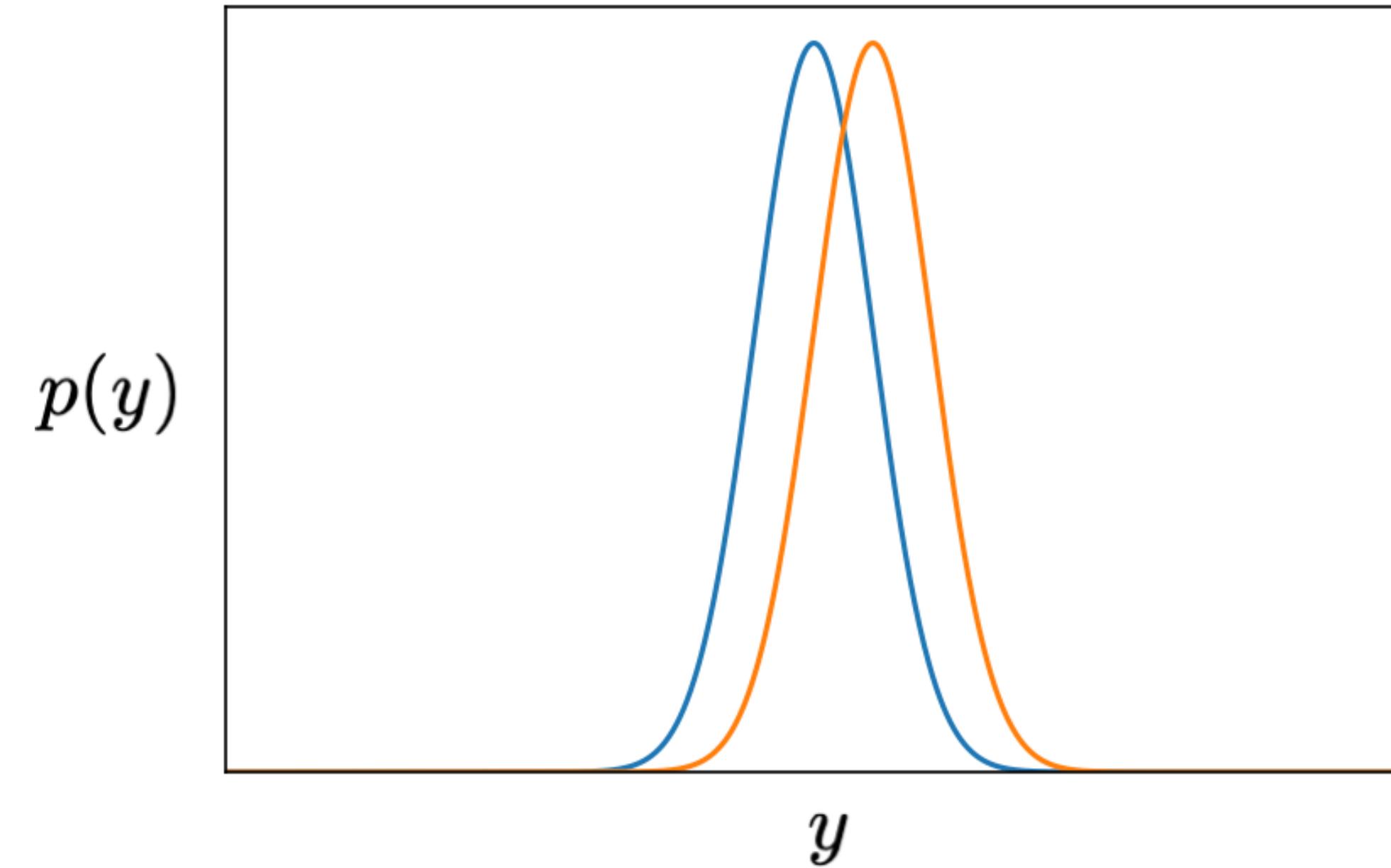


Add **noise** to the true answer such that:

1. Each answer does not leak too much information about the dataset
2. Noisy answers are close to the original ones

What kind of noise?

Gaussian Noise (first attempt)



Gaussian noise violates our definition, but only because of the tails. It satisfies a different definition of differential privacy which allows violating the ϵ constraint with small probability, but that's beyond the scope of this slide.

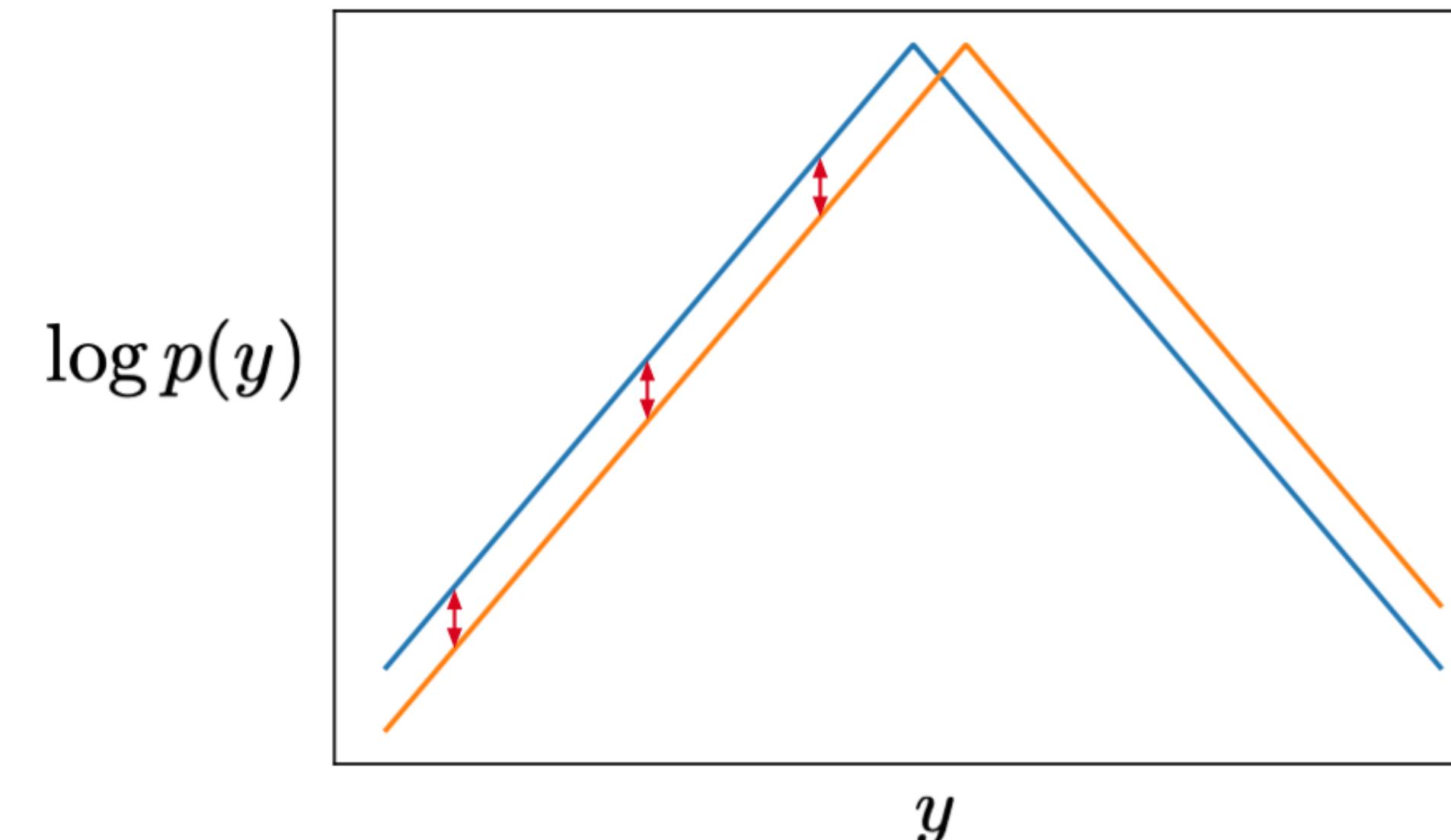
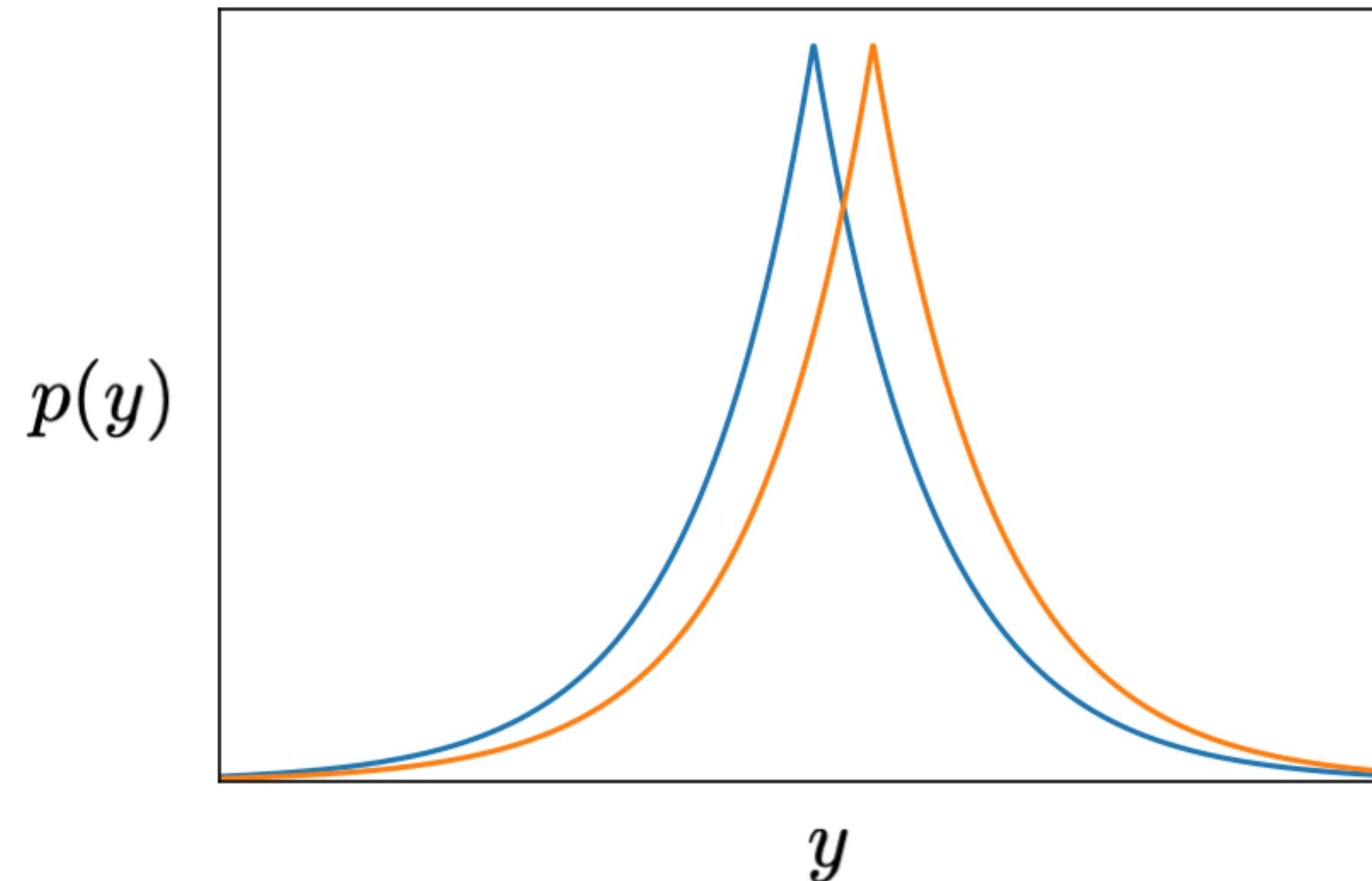
What kind of noise?

Laplace noise

The Laplace distribution

$$p(y; \mu, b) = \frac{1}{2b} \exp\left(-\frac{|y - \mu|}{b}\right)$$

Variance = $2b^2$ (b is a parameter determining the scale of the distribution)



Is exactly what we need!

Laplace Mechanism

- **Global sensitivity:** Let f be a deterministic vector-valued function of a dataset. The L^1 **sensitivity of f** is defined as:

$$\Delta f = \max_{\substack{\mathcal{D}_1, \mathcal{D}_2 \\ \text{neighbours}}} \|f(\mathcal{D}_1) - f(\mathcal{D}_2)\|_1.$$

Recall that $\|x\|_1 = \sum_i |x_i|$

- **Laplace mechanism** : returns a vector \mathbf{y} whose entries are independently sampled from Laplace distributions

$$y_i \sim \text{Laplace} \left(f(\mathcal{D})_i, \frac{\Delta f}{\varepsilon} \right),$$

where $f(\mathcal{D})_i$ denotes the i -th entry of $f(\mathcal{D})$

Noise **calibrated** to the privacy requirement:
Higher **sensitivity functions** and tighter **privacy constraints** imply more noise

Sensitivity: Count query

D	Cancer	D'
	Y	
	N	
	N	
	N	
	N	
	Y	
	N	
	N	
	Y	
	Y/N	

3 3 or 4



How many people have malignant cancer?

$$\tilde{y} = f(D) + \text{Lap}\left(\frac{1}{\epsilon}\right)$$

What is the sensitivity of this query?

$$\Delta f = \max_{\substack{\mathcal{D}_1, \mathcal{D}_2 \\ \text{neighbours}}} \|f(\mathcal{D}_1) - f(\mathcal{D}_2)\|_1.$$

$$\max(|3 - 3|, |3 - 4|) = 1$$

Sensitivity: SUM query

- Suppose all values x are in $[a, b]$, with $a, b \geq 0$
- What is the sensitivity of the $\text{SUM} = \sum_{x \in D}$ query?
- Sensitivity: **b**

E.g., $a=3, b=5$

value
3
4
5
3
5
4

24

value
3
4
5
3
5
4

[3, 5]

[27, 29]

Laplace Mechanism Privacy

- Consider neighboring datasets D1 and D2
- Consider some output O
-

$$\begin{aligned}\frac{\Pr[M(D_1) = O]}{\Pr[M(D_2) = O]} &= \frac{\Pr[Q(D_1) + Z = O]}{\Pr[Q(D_2) + Z = O]} \\ &= \frac{\exp(-|O - Q(D_1)|/b)}{\exp(-|O - Q(D_2)|/b)}\end{aligned}$$

By triangle inequality

$$\begin{aligned}&\leq \exp(|Q(D_1) - Q(D_2)|/b) \\ &\leq \exp(\Delta_Q/\epsilon) = \exp(\epsilon)\end{aligned}$$

$$f(x \mid \mu = 0, b) = \frac{1}{2b} \exp\left(-\frac{|x|}{b}\right)$$

$$b = (\Delta_Q/\epsilon)$$

Laplace Mechanism

Example

- Example: What fraction of Danish have blue eyes?
- Mechanism returns the counts (ξ_1, ξ_2) of Danish with and without blue eyes, plus Laplace noise.
- We'd like to satisfy a privacy constraint of $\epsilon = 0.1$.
How much Laplace noise should we add?
- Ans: $\Delta f / \epsilon = 1/0.1 = 10$.
- The noise scale is **independent of the population size!**
- I.e., you can answer the query to within about ± 10 people, out of the population of Denmark. So you can obtain very accurate answers to queries over large populations.
-

Error of the Laplace Mechanism

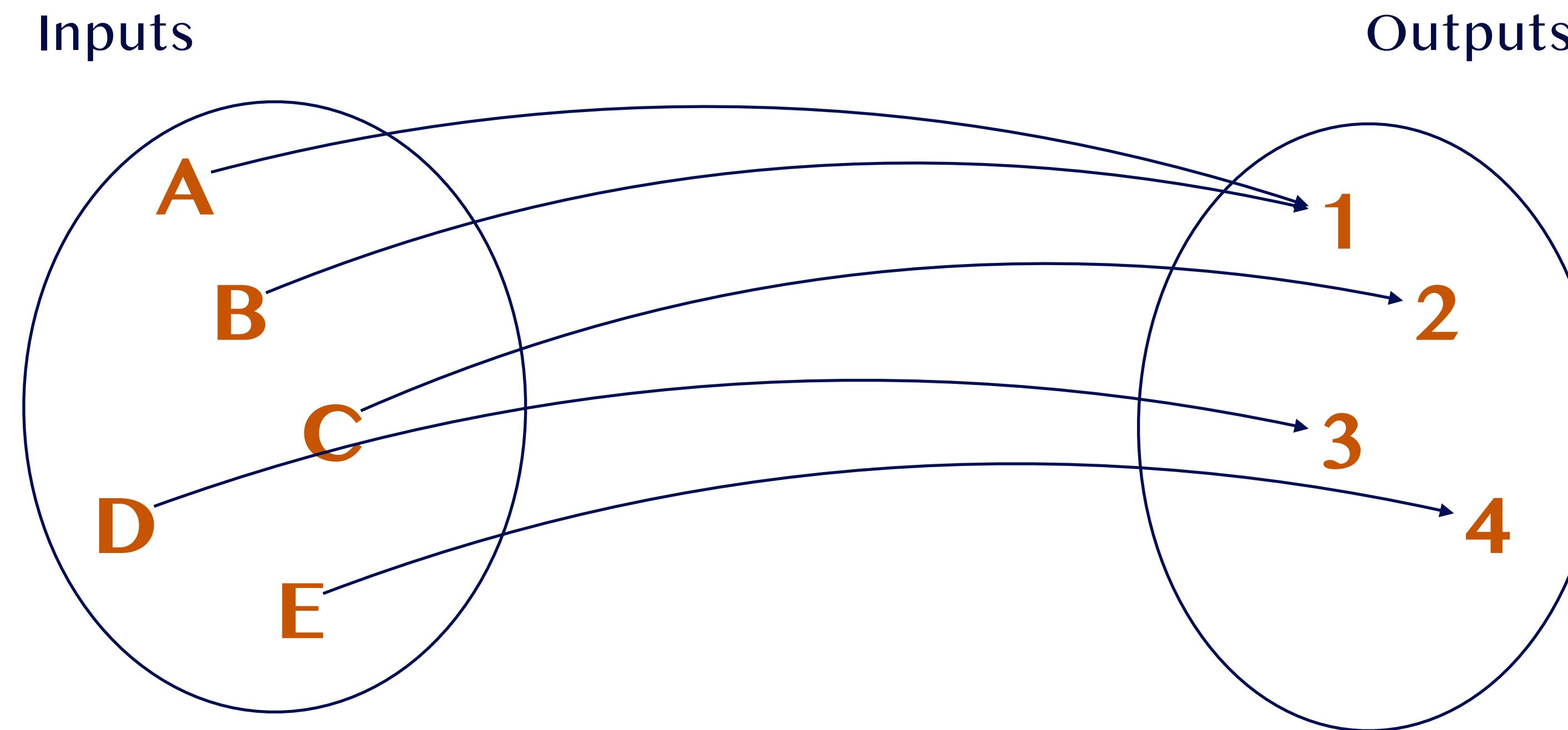
- Laplace mechanism works for any function that returns a real number
- Mean squared error:

$$\mathbb{E} [\tilde{x} - x]^2 = \text{Var} \left(\text{Lap} \left(\frac{\Delta_f}{\epsilon} \right) \right) = 2 \left(\frac{\Delta_f}{\epsilon} \right)^2$$

Exponential Mechanism

Discrete mappings

- Consider some mapping f (can be deterministic or probabilistic):



How to construct a differentially private version of f ?

Exponential Mechanism

- Suppose the goal is to make a decision $f(D)$.
- We have a **scoring function** $\mathcal{L} : \mathcal{D} \times \mathcal{R} \rightarrow \mathbb{R}_+$
- **Example:**
 - D = dataset of nationality of a set of people
 - $f(D)$: most frequent nationality in D
 - $\#_D(o)$: number of people in D with nationality “o”
 - $\mathcal{L}(D, o) = |\#_D(o) - \#_D(f(D))|$

Exponential Mechanism

- Given a function $f: \mathcal{D} \rightarrow \mathcal{R}$ and a loss function $\mathcal{L}: \mathcal{D} \times \mathcal{R} \rightarrow \mathbb{R}_+$
- Randomly sample an output o from \mathcal{R} with probability:

$$\Pr(Y = y) \propto \exp\left(-\frac{\epsilon}{2\Delta\mathcal{L}}\mathcal{L}(D, y)\right)$$

- Where $\Delta_{\mathcal{L}} = \max_{o \in \mathcal{R}} \max_{D, D' \in \mathcal{D}} |\mathcal{L}(D, o) - \mathcal{L}(D', o)|$ is the sensitivity of the loss function
- The result is basically a softmax of $-\mathcal{L}$
- Note: for every output o , $\Pr[o \text{ is selected}] > 0$.

Exponential Mechanism

- The exponential mechanism is ϵ -DP
- For two neighboring datasets D_1, D_2 , and any value y

$$\begin{aligned} \frac{p(y | D_1)}{p(y | D_2)} &= \frac{\exp\left(-\frac{\varepsilon}{2\Delta\mathcal{L}}\mathcal{L}(y, D_1)\right)}{\sum_{y'} \exp\left(-\frac{\varepsilon}{2\Delta\mathcal{L}}\mathcal{L}(y', D_1)\right)} \\ &\quad \frac{\exp\left(-\frac{\varepsilon}{2\Delta\mathcal{L}}\mathcal{L}(y, D_2)\right)}{\sum_{y'} \exp\left(-\frac{\varepsilon}{2\Delta\mathcal{L}}\mathcal{L}(y', D_2)\right)} \\ &= \underbrace{\frac{\exp\left(-\frac{\varepsilon}{2\Delta\mathcal{L}}\mathcal{L}(y, D_1)\right)}{\exp\left(-\frac{\varepsilon}{2\Delta\mathcal{L}}\mathcal{L}(y, D_2)\right)}}_{\leq \exp(\varepsilon/2)} \cdot \underbrace{\frac{\sum_{y'} \exp\left(-\frac{\varepsilon}{2\Delta\mathcal{L}}\mathcal{L}(y', D_2)\right)}{\sum_{y'} \exp\left(-\frac{\varepsilon}{2\Delta\mathcal{L}}\mathcal{L}(y', D_1)\right)}}_{\leq \exp(\varepsilon/2)} \end{aligned}$$

- Hence $\frac{p(y | D_1)}{p(y | D_2)} \leq \exp(\epsilon)$

Part I: Foundation

Properties of Differential Privacy

Privacy Leakage

Dinur/Nissim Result

- To ensure some utility on the query answers, some information about each individual in the dataset must be leaked.
- We can only hope **to bound the amount of disclosure**.
- Therefore: There is a limit on the number of queries that can be answered.



Privacy Leakage

Dinur/Nissim Result

- To ensure some utility on the query answers, some information about each individual in the dataset must be leaked.
- We can only hope **to bound the amount of disclosure**.
- Therefore: There is a limit on the number of queries that can be answered.
- **Dinur/Nissim:** Given a dataset D of size n , a vast majority of records in D **can be reconstructed** when $n \log(n)^2$ queries are answered privately.
- True even if each query is altered with error up to $o(\sqrt{n})$



Composition

Sequential Composition

- Given A_1, \dots, A_n algorithms that access a dataset D such that each satisfy ϵ_i -DP
- Then running all n algorithms **sequentially** satisfies:

$$\left(\sum_{i=1}^n \epsilon_i \right)$$
-differential privacy

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- Then running all n algorithms **sequentially** satisfies:

$$\left(\sum_{i=1}^n \epsilon_i \right)$$
-differential privacy

Parallel Composition

- If A_1, \dots, A_n are algorithms that access **disjoint** datasets D_1, \dots, D_n such that each satisfy ϵ_i differential privacy
- Then running all k algorithms **in parallel** satisfies

$$\max\{\epsilon_1, \dots, \epsilon_n\}$$
-differential privacy

Post-processing Immunity

- Post-processing immunity: If A enjoys ϵ -differential privacy and g is an arbitrary data-independent mapping, then $g \circ A$ is ϵ -differential private.

Part I: Foundation Summary

- Privacy breaches and no control on accessing side information
- Differential private algorithm ensure an attacker can't infer if an individual was in or not a dataset, based on any output
- Building blocks:
 - Laplace, exponential mechanism, (many others)
- Composition rules help using building blocks to create complex algorithms

Responsible AI: Seminar on Fairness, Safety, Privacy and more

Thank you!

-  <https://nandofioretto.com>
-  nandofioretto@gmail.com
-  [@nandofioretto](#)

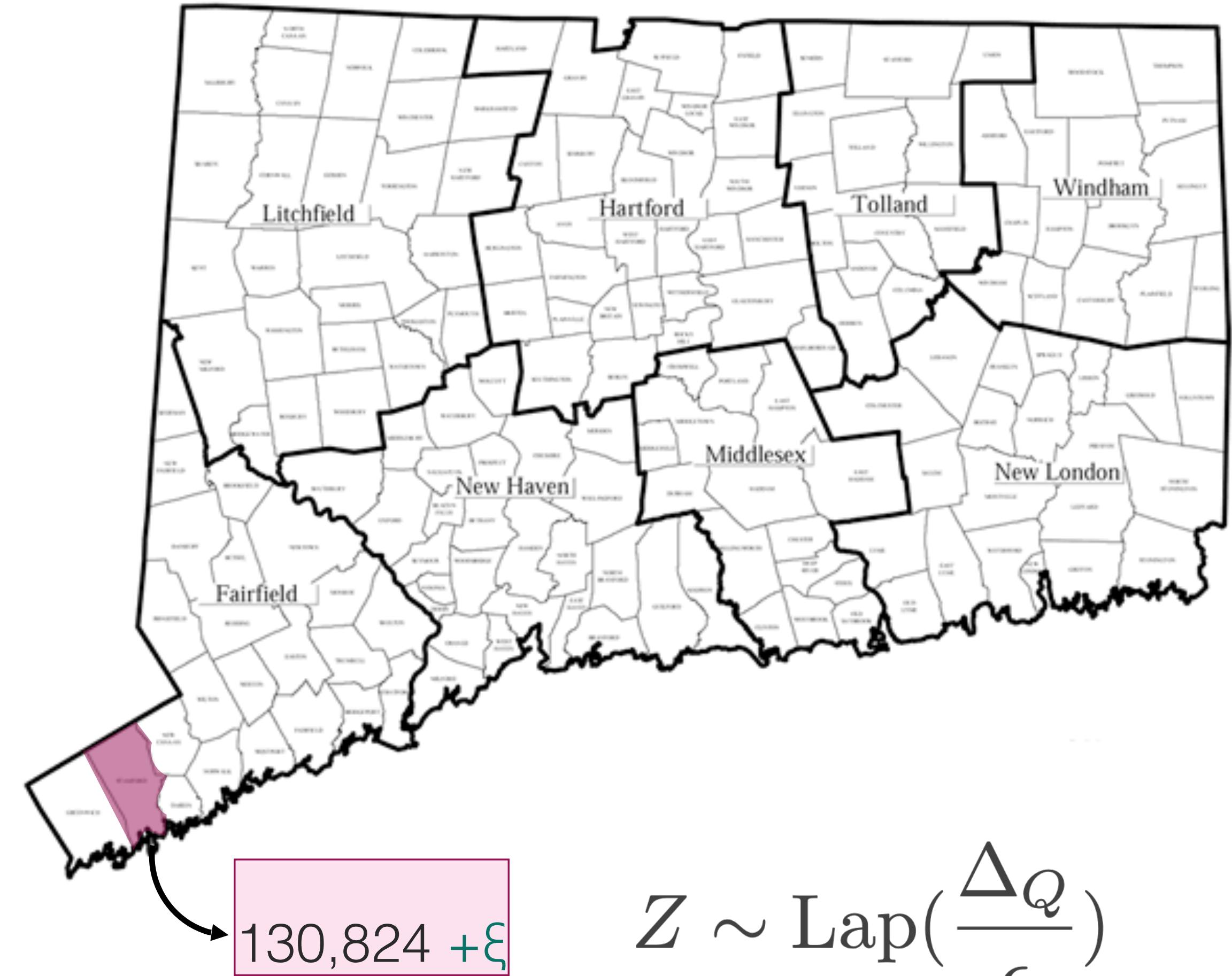
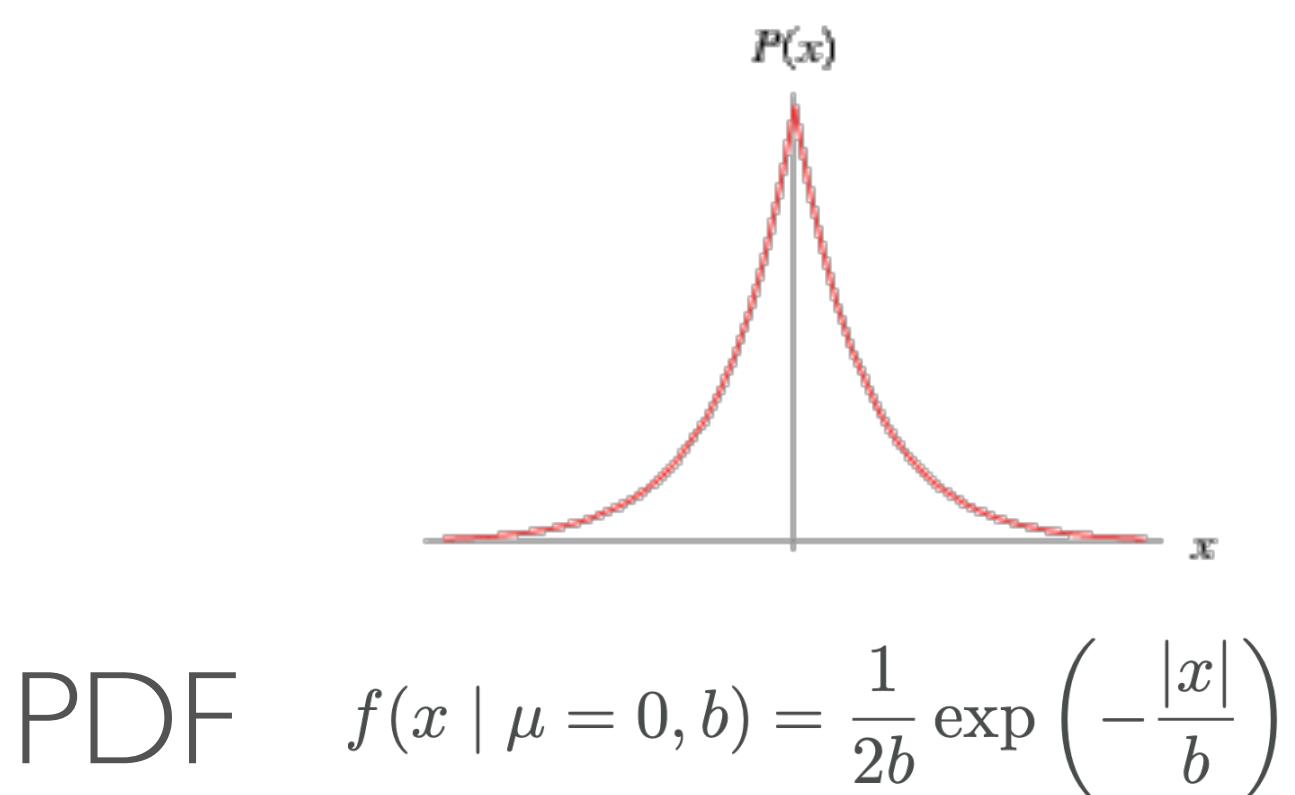


Part II: Algorithms and Consistency Issues

The Census Data Release Problem

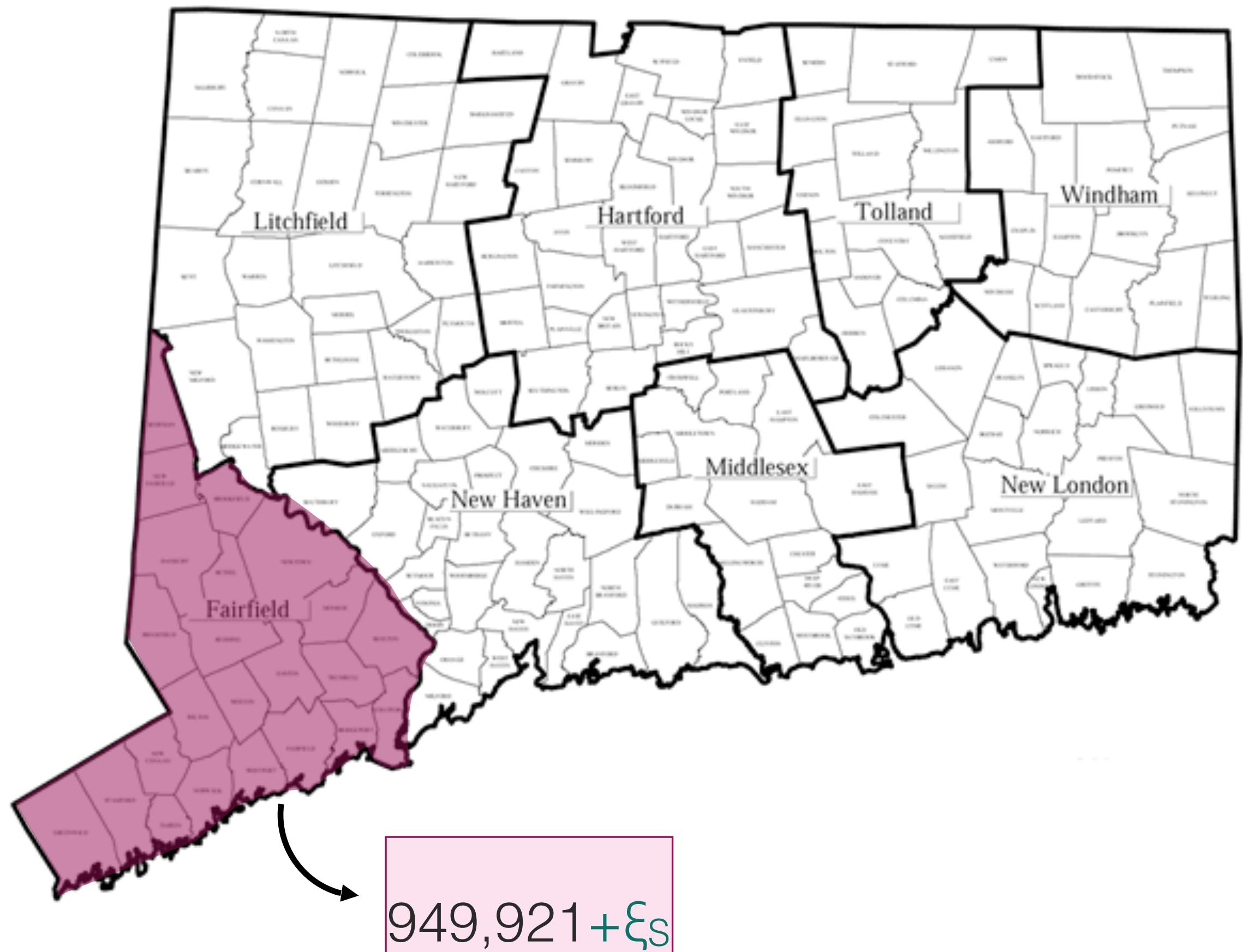
- GOAL: Release socio-demographic feature of the population grouped by:

1. Census blocks
2. Counties
3. States
4. National level



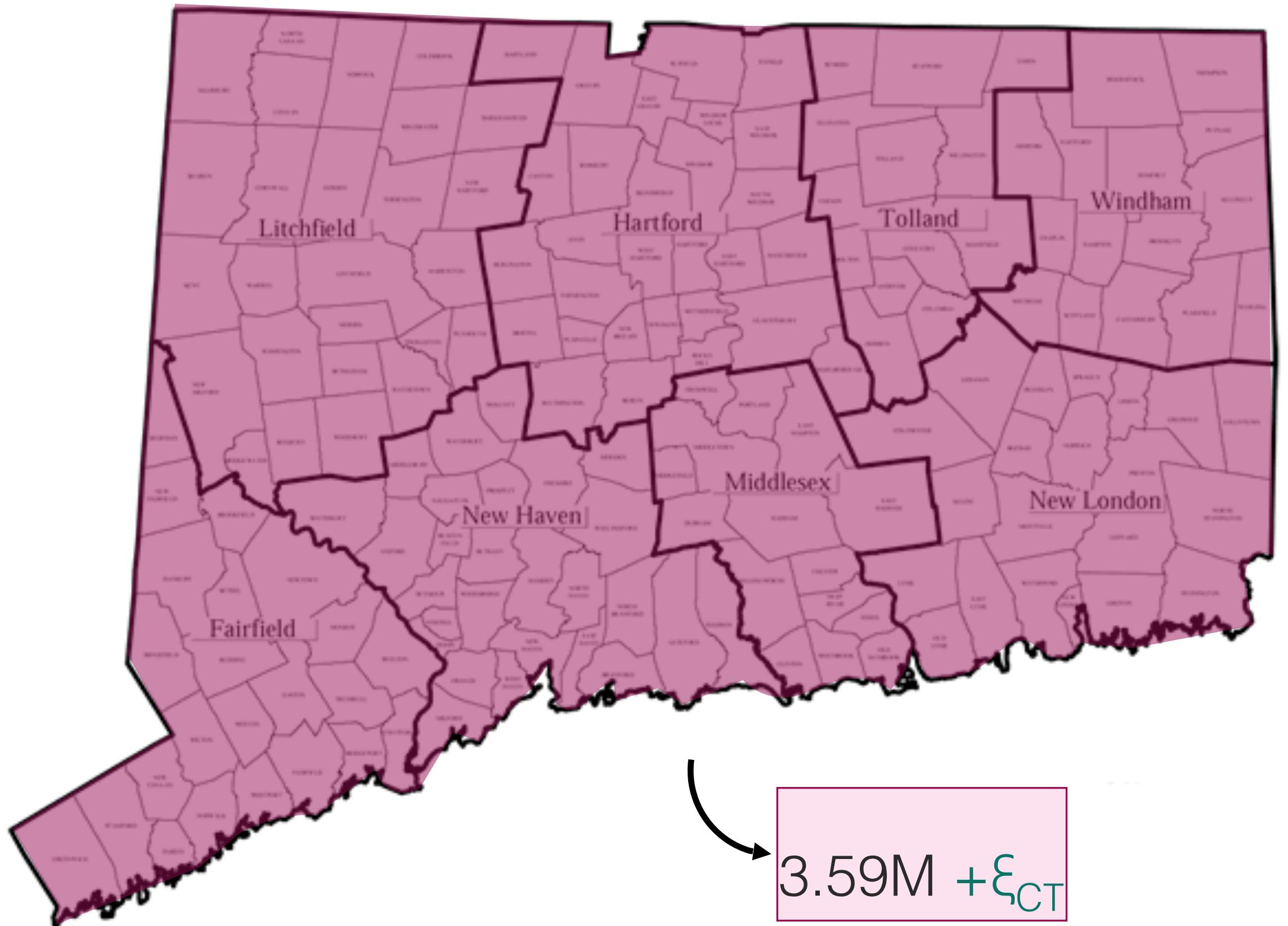
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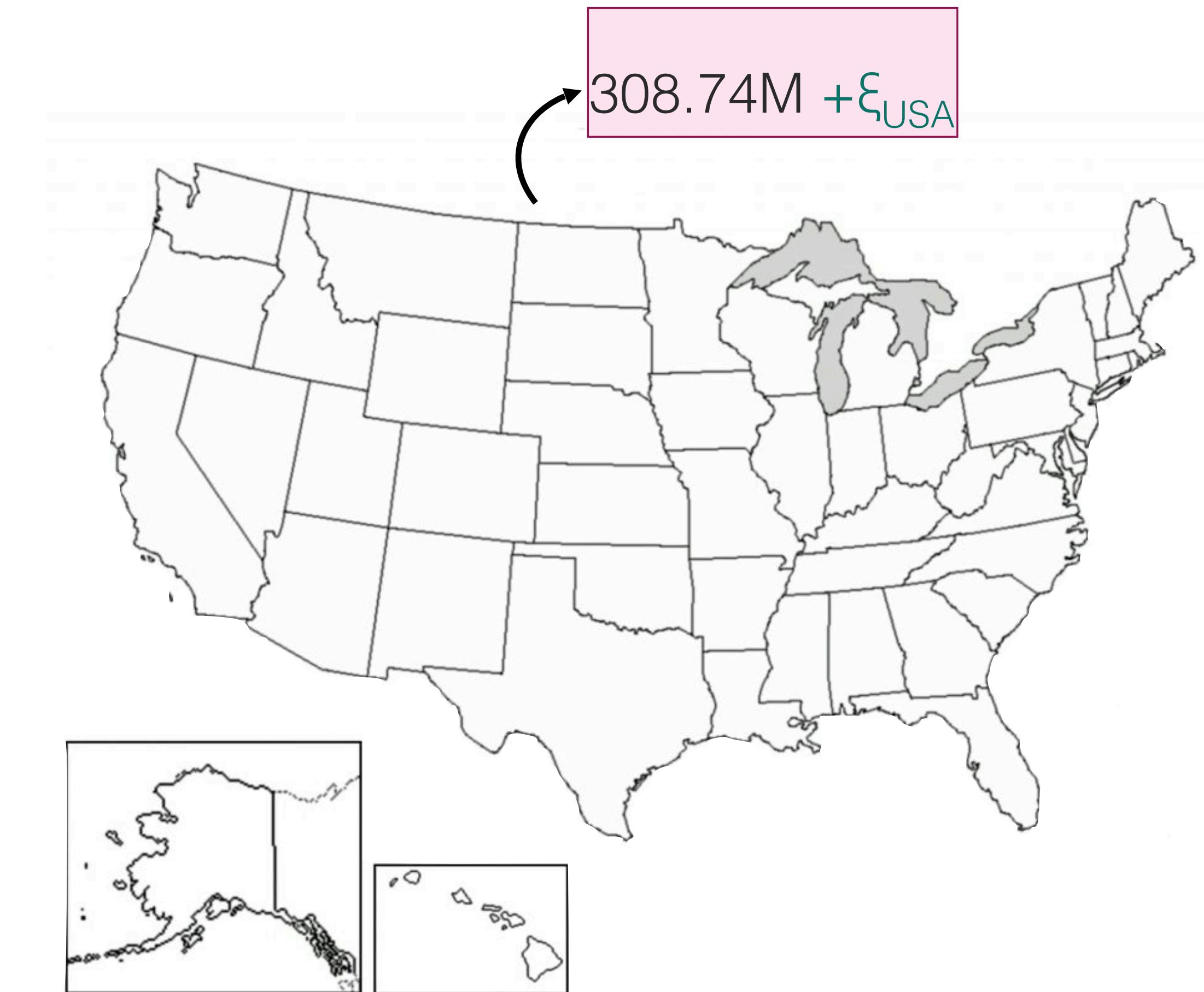
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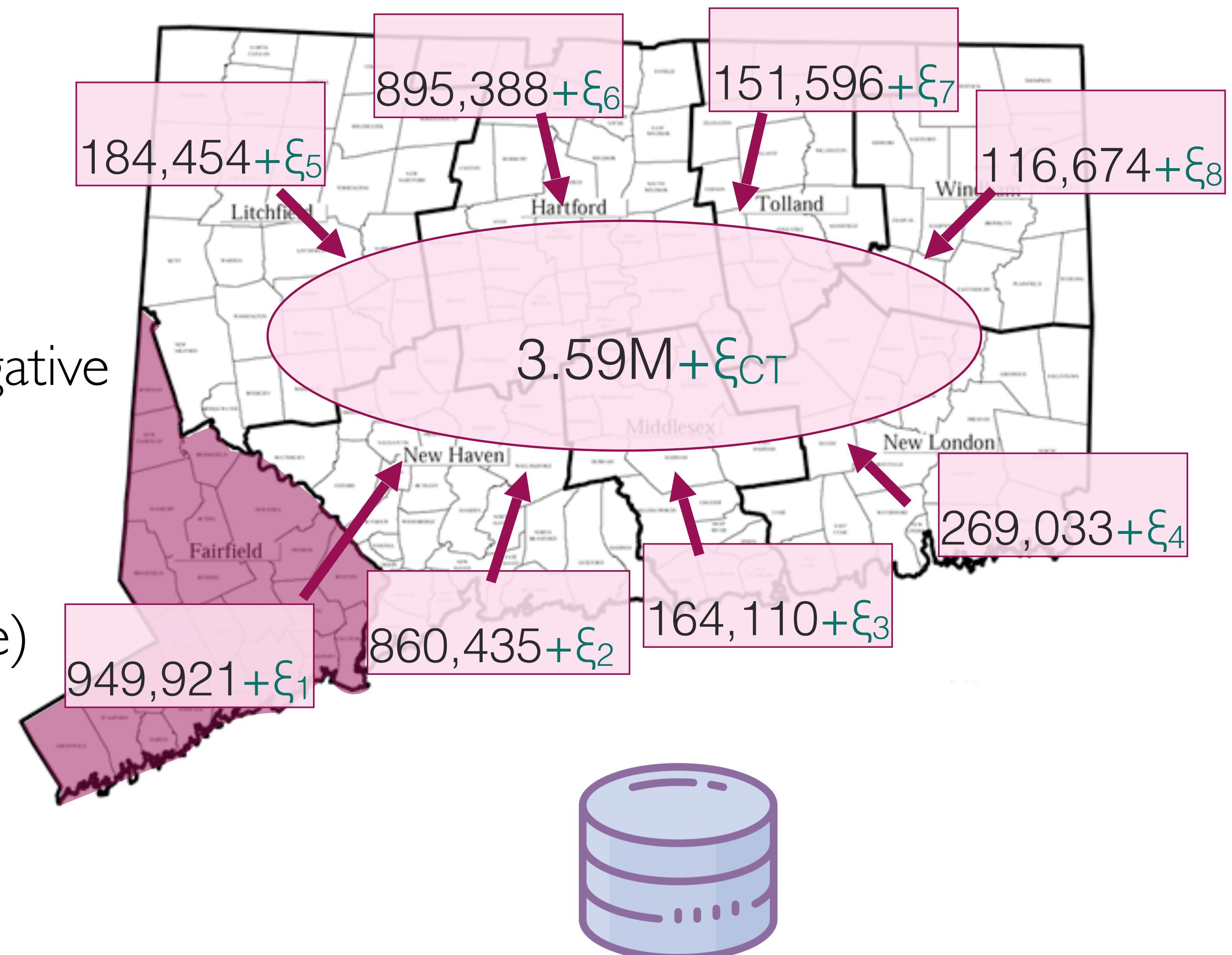
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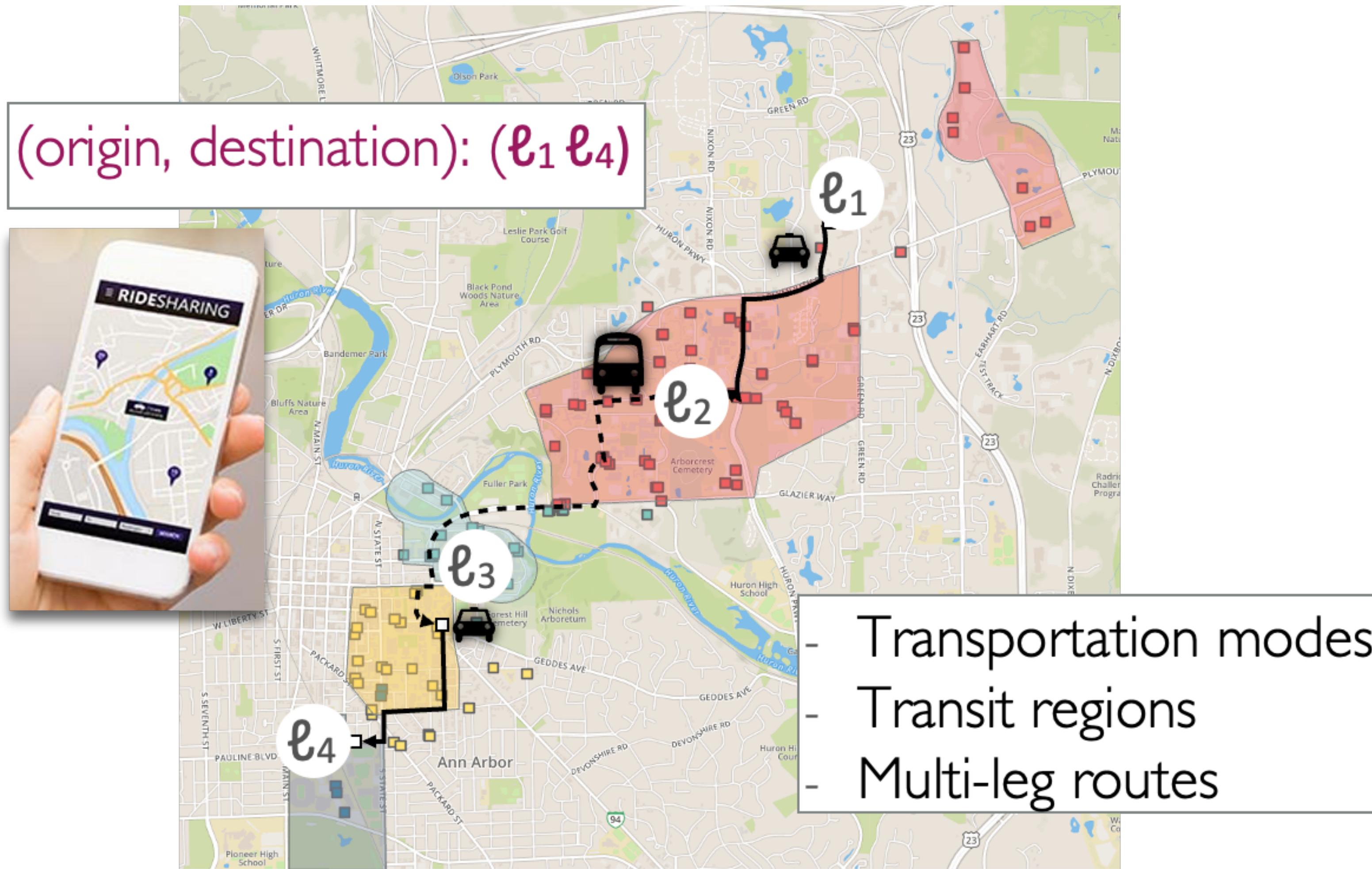


The consistency issue

- Requirements:
 1. Privacy
 2. Hierarchical **Consistency**
 3. **Validity:** The private values are non-negative
- Noise is applied independently to each estimate
- The noisy quantities at a “level” (e.g., state) are **inconsistent** with the sum of the noisy quantities at the “children levels” (e.g., counties of that state)

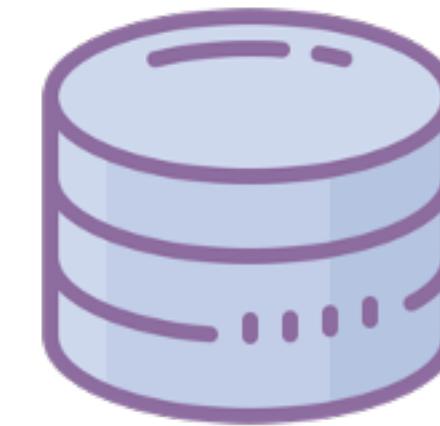


Transportation Application

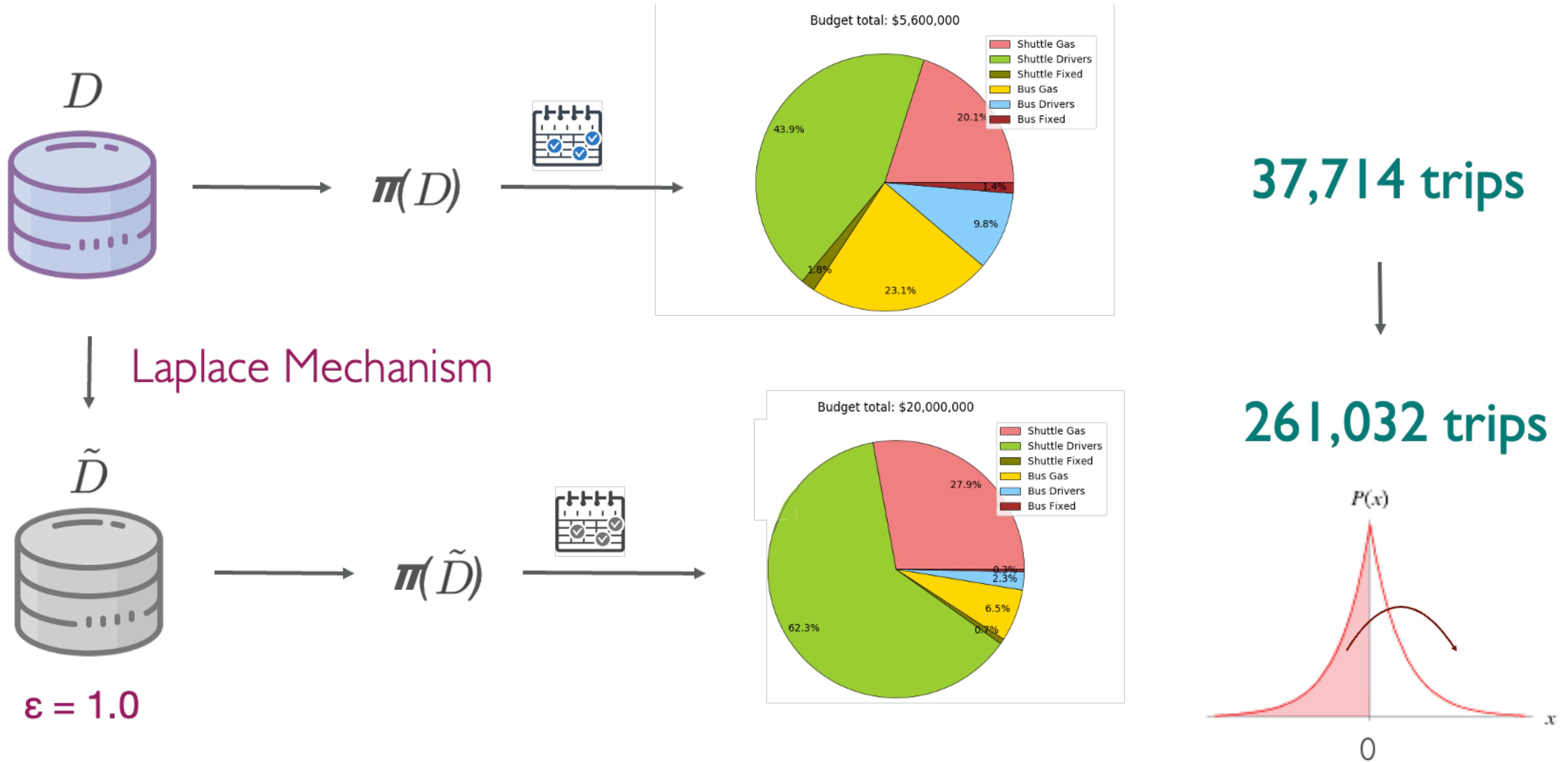


Data universe: ~30k OD-pairs

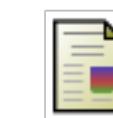
time	origin	destination	count
8:00-8:30	bbr	eecs	34
8:00-8:30	food_crtl	nw2	0
8:00-8:30	lsa	ort3	1
8:00-8:30	sprt	nw4	0
8:00-8:30	bbb	chi	12
...



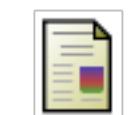
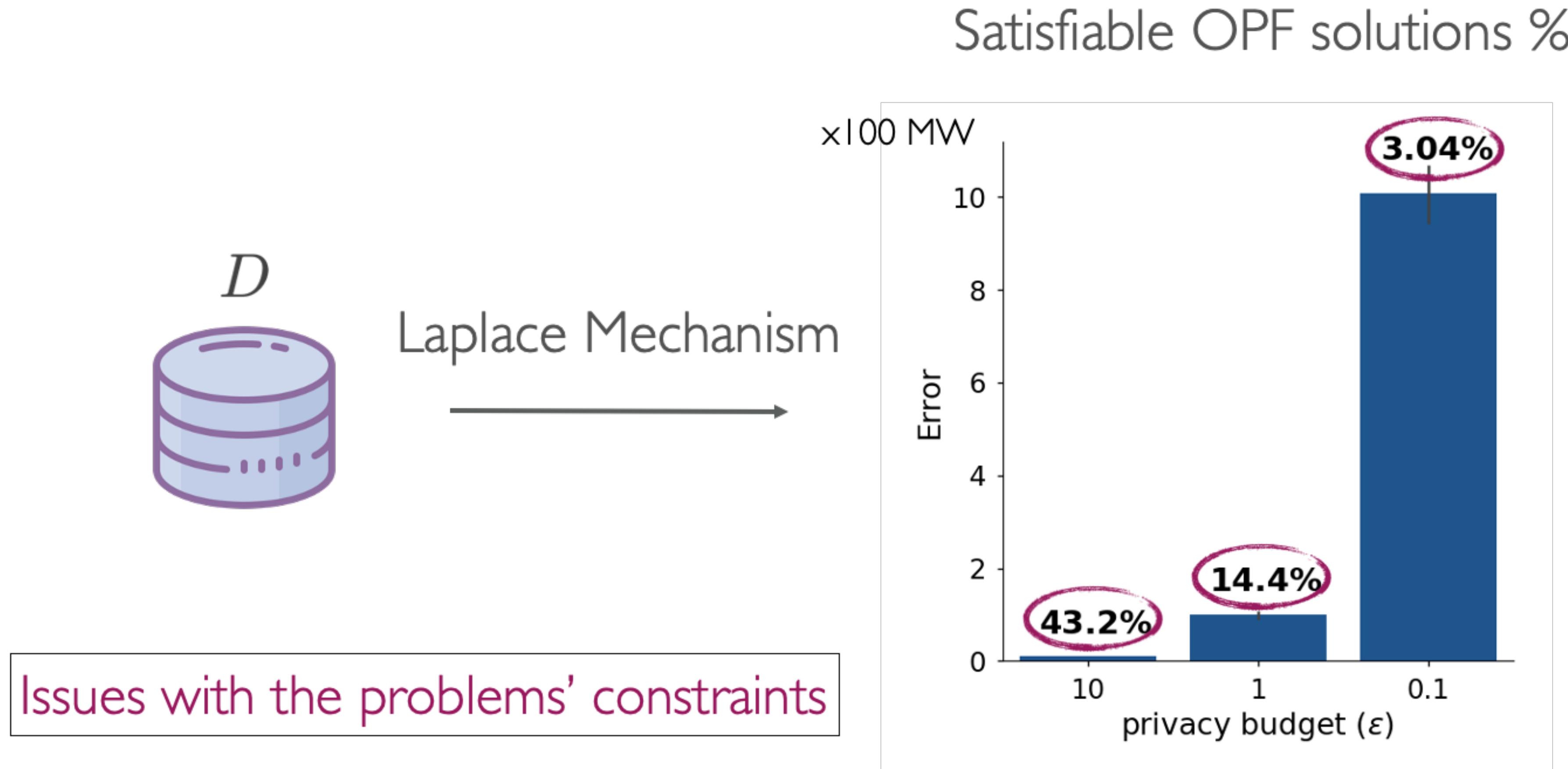
Differential Privacy Challenge for Mobility



Energy Optimization



Differential Privacy Challenge for Energy



Fiorotto:CPAIOR-18; IEEE-TPS:20, IEEE-TSG:20

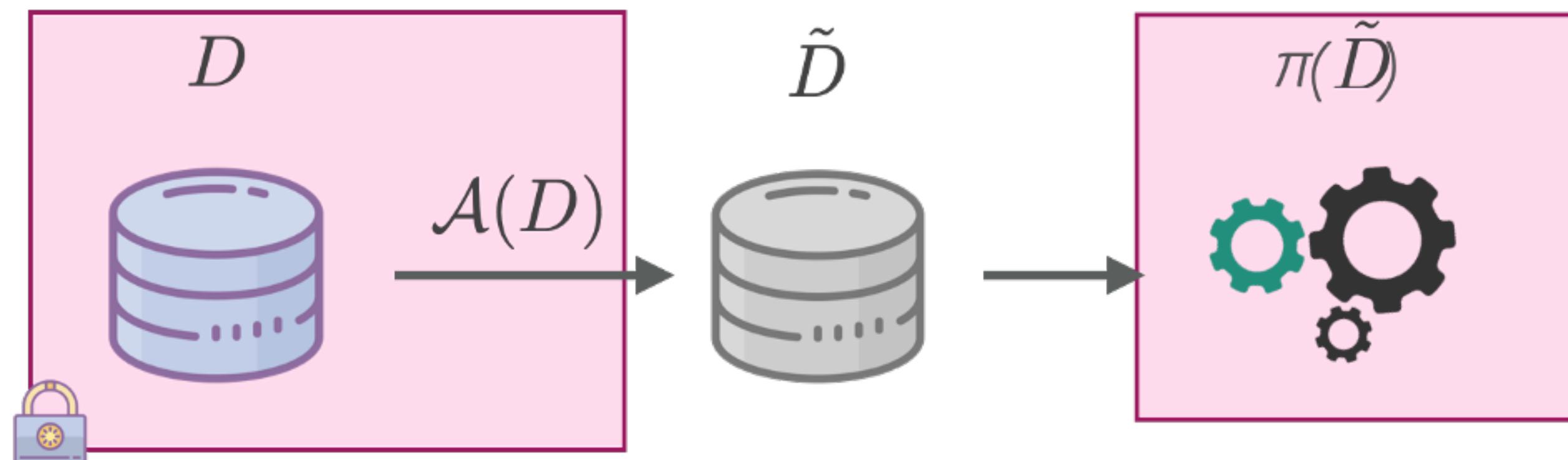
**Differential Privacy is oblivious to the
structure of the dataset and the
constraints of the underlying problem**

Constrained based DP

We are interested in solving:

$$\begin{aligned} & \text{minimize}_{\mathbf{x} \in \mathbb{R}^n} \quad f(\tilde{D}, \mathbf{x}) \\ & \text{subject to} \quad g_i(\tilde{D}, \mathbf{x}) \leq 0, \quad i = 1, \dots, p \end{aligned}$$

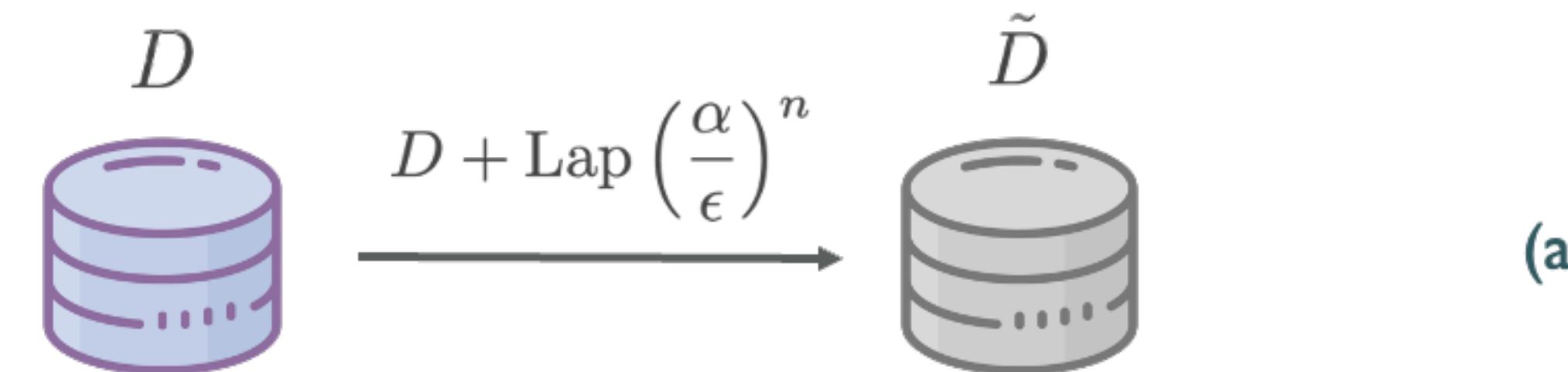
Sensitive Data



Constrained based DP

Consider a dataset $D \in \mathbb{R}^n$ of values

#1



#2

$$\text{minimize}_{\hat{D}, \mathbf{x} \in \mathbb{R}^n} \|\hat{D} - \tilde{D}\|_2^2$$

$$\text{subject to } |f(\hat{D}, \mathbf{x}) - f^*| \leq \beta$$

$$g_i(\hat{D}, \mathbf{x}) \leq 0, i = 1, \dots, p$$

(a)

(b)

(c)

#3

Release \hat{D}



Constrained based DP

Properties

- : CBDP achieves ϵ -DP
 - By application of the privacy-preserving mechanism on D to calibrated noise, and composition
- **Efficiency**: When the constraint space is convex, CBDP runs in polynomial time in the size of the universe and number of constraints
- **Accuracy**: For convex problems, the optimal solution to the optimization model of CBDP satisfies:
 - $\|x^* - c\|_{2,w} \leq \|\tilde{c} - c\|_{2,w}$
 -

Constrained-based DP

Properties

- **Privacy:** CBDP achieves generalized ε -Differential Privacy
 - By the properties of the (Polar) Laplace mechanism.
- **Accuracy:** The optimal solution to the optimization model of CBDP satisfies:

$$\|\hat{S}^* - S\|_2 \leq 2\|\tilde{S} - S\|_2$$

that is, it is away from optimality by at most a factor of 2.

Constrained-based DP

Geometrical intuition

- Let Q_1, Q_2, \dots, Q_k be a collection of queries.
- Let $\tilde{q}_1, \tilde{q}_2, \dots, \tilde{q}_k$ be their private, noisy, answers.
- Constraint $\mathbb{C}(Q_1, Q_2, \dots, Q_k)$ is satisfied (in all data sets) on the true query answers, but does not on noisy answers

Objective: Find x_1, x_2, \dots, x_k such that:

1. Close to $\tilde{Q}_1, \tilde{Q}_2, \dots, \tilde{Q}_k$
2. Satisfy $\mathbb{C}(x_1, x_2, \dots, x_k)$

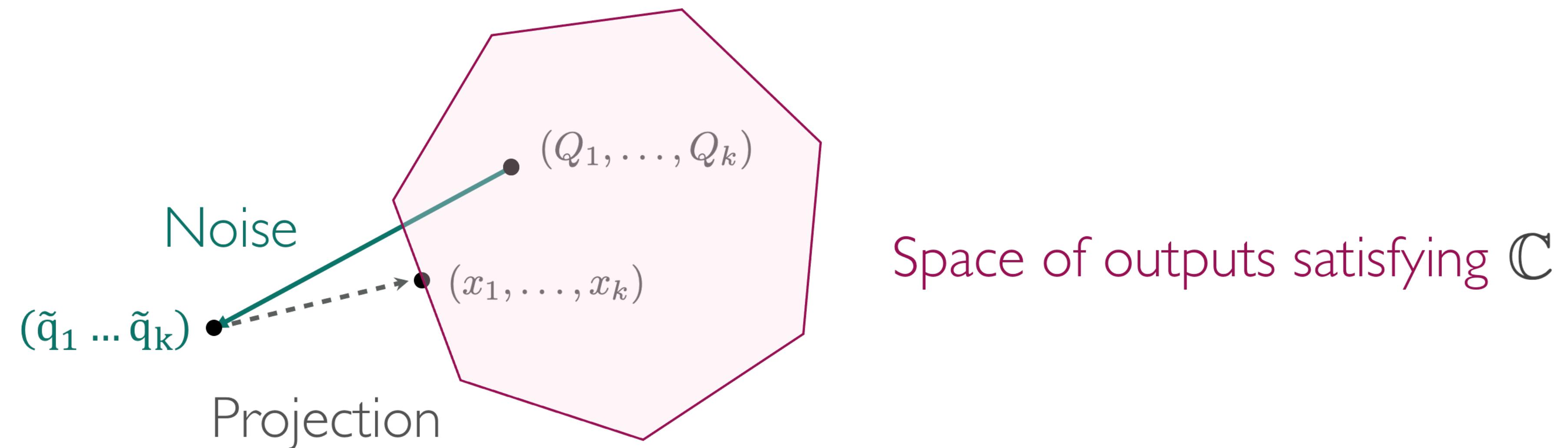
Constrained-based DP

Geometrical intuition

- Consider a set of queries $\{Q_1, \dots, Q_k\}$ with private answers $\tilde{q}_1, \dots, \tilde{q}_k$

$$\min \sum_{i=1}^k (x_i - \tilde{q}_i)^2$$

$$\text{s.t.: } \mathbb{C}(x_1, x_2, \dots, x_k)$$



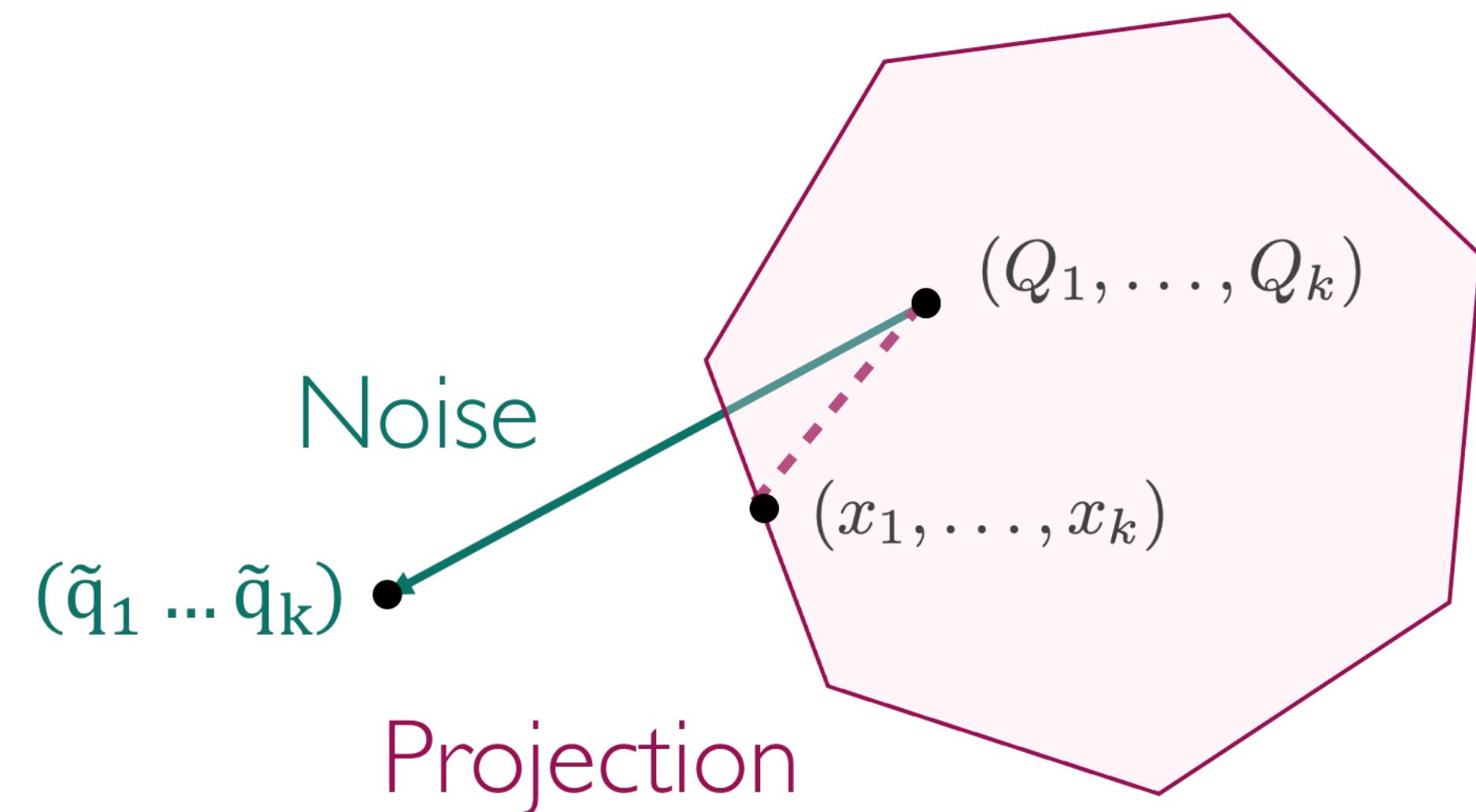
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$$\|x - Q\|_2 \leq \|\tilde{Q} - Q\|_2$$

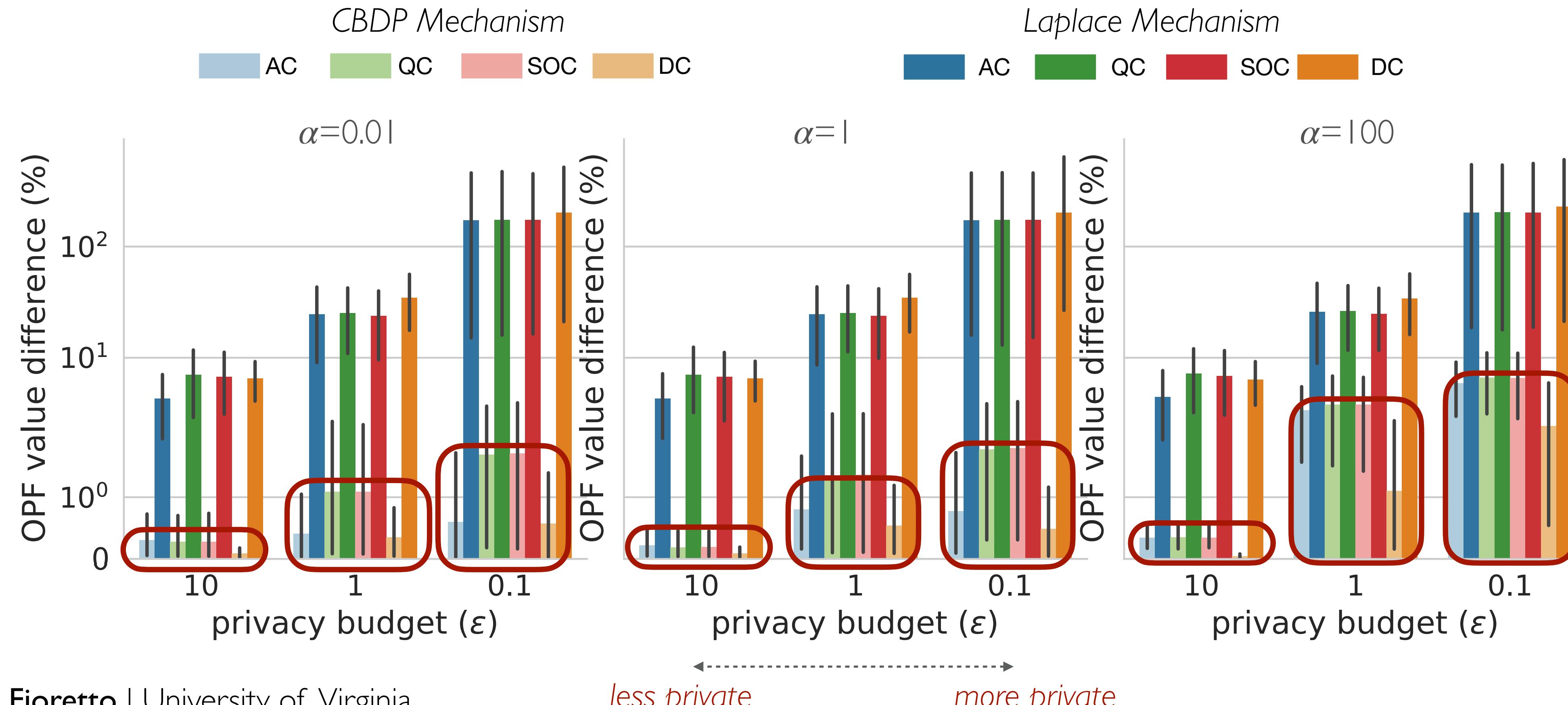
When \mathbb{C} forms
a convex space

Protecting Loads

Analysis of the OPF

Summary:

- 1-2 order of magnitude improvements, for all ϵ and α
- Difference of OPF values between BiLevel-DP and original data is $< 10\%$



Summary of Results

Mobility



- Features: Total trips (2), Operating zones (3), Transit modes (4)
- Baselines: **Laplace** [Dwork:08], **Hierarchical** [Hay:10, Cormode:13]
- Key results: ≥ 1 order magnitude improvement

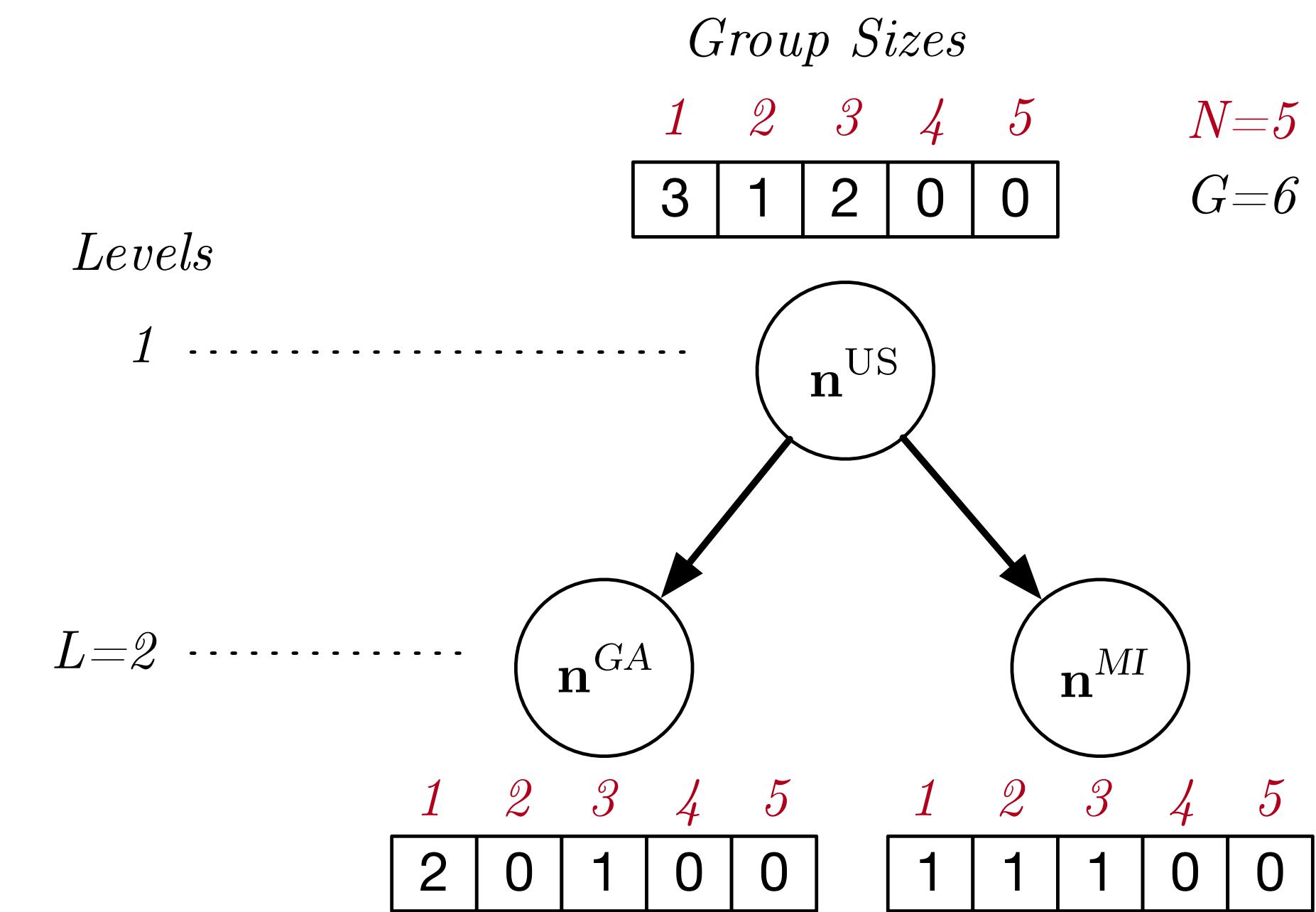
A Differentially Private Optimization Approach

I. Apply Geometrical Noise with parameter $\lambda = \frac{2L}{\epsilon}$

$$\tilde{\mathbf{n}}^r = \mathbf{n}^r + \text{Geom}\left(\frac{2L}{\epsilon}\right)^N$$

2. Postprocess output $\tilde{\mathbf{n}}$ to enforce consistency

$\underset{\{\hat{\mathbf{n}}^r\}_{r \in \mathcal{R}}}{\text{minimize}} \sum_{r \in \mathcal{R}} \ \hat{\mathbf{n}}^r - \tilde{\mathbf{n}}^r\ _2^2$ (H1)
$\text{s.t.: } \sum_{s \in [N]} \hat{n}_s^r = G \quad \forall r \in \mathcal{R}$ (H2)
$\sum_{c \in ch(r)} \hat{n}_s^c = \hat{n}_s^r \quad \forall r \in \mathcal{R}, s \in [N]$ (H3)
$\hat{n}_s^r \in D_s^r \quad \forall r \in \mathcal{R}, s \in [N]$ (H4)



← Satisfies DP due to post-processing immunity

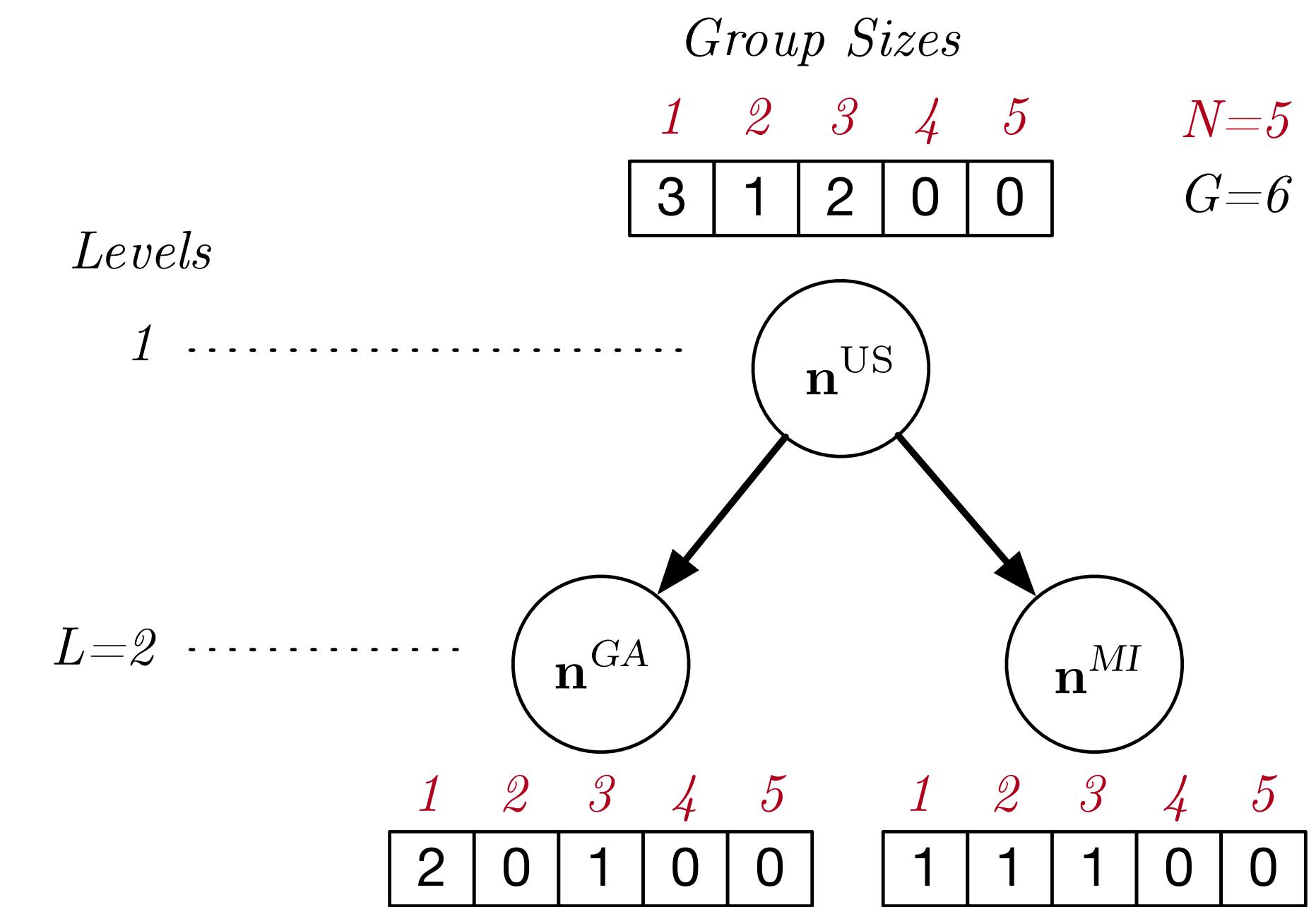
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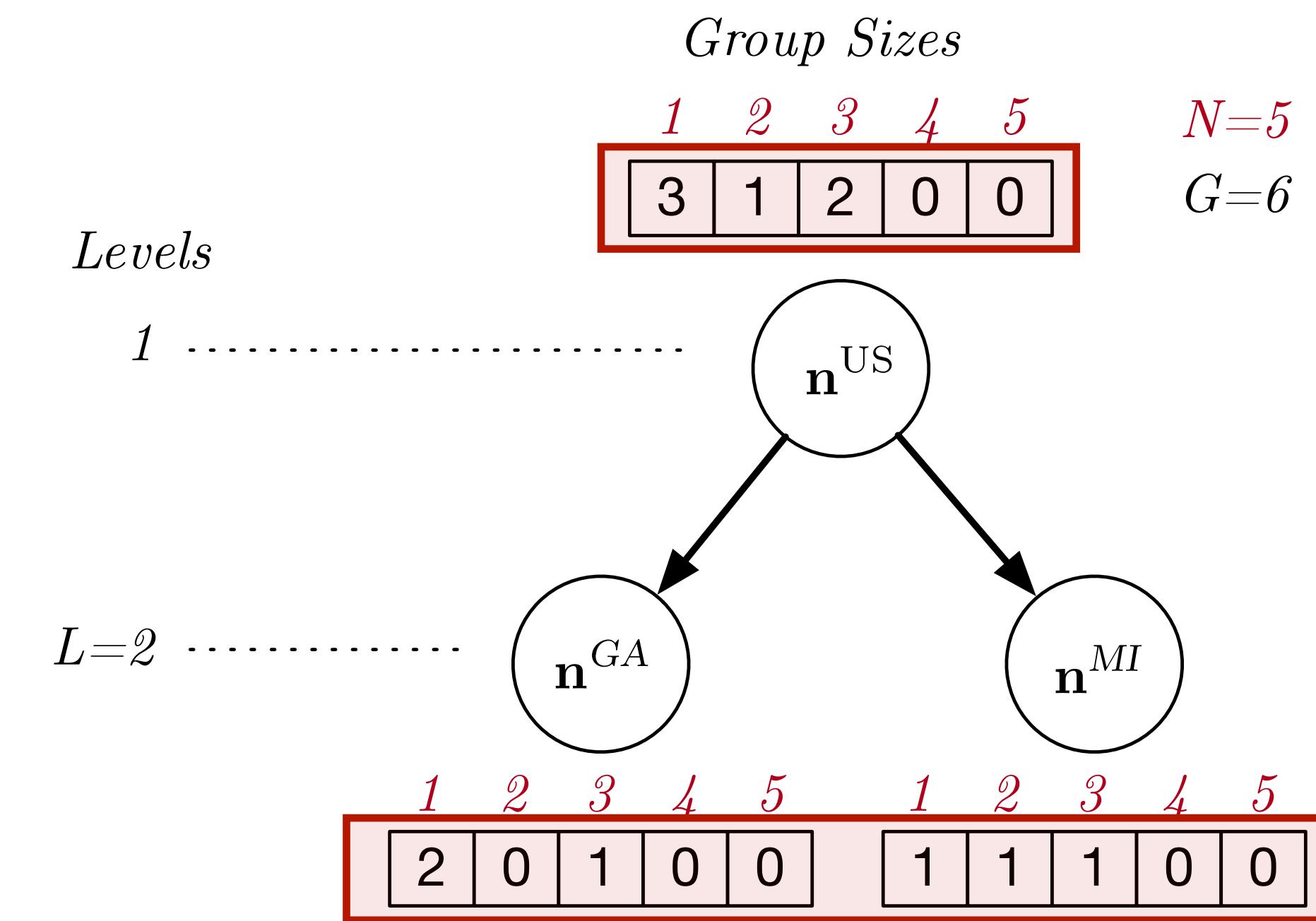
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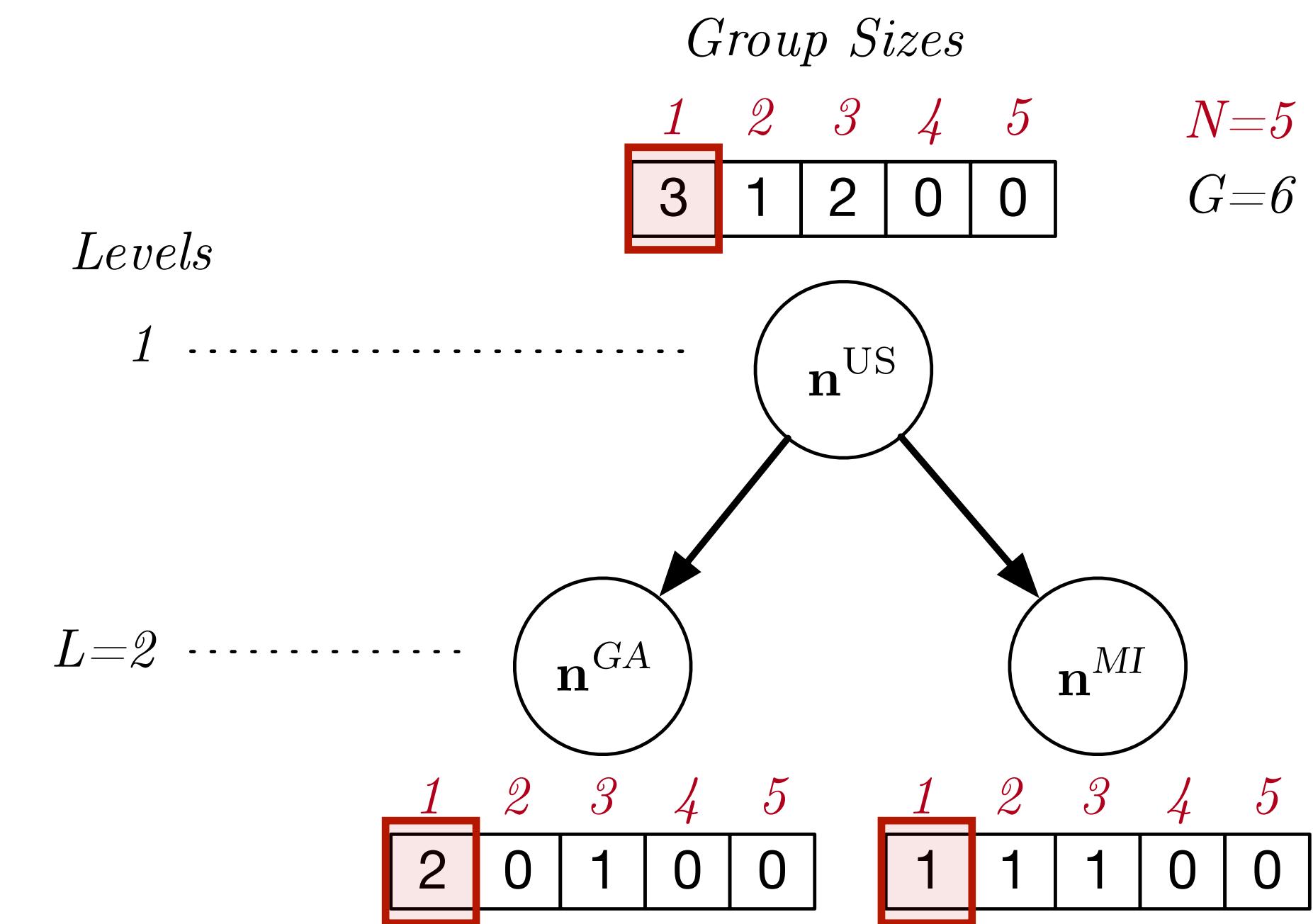
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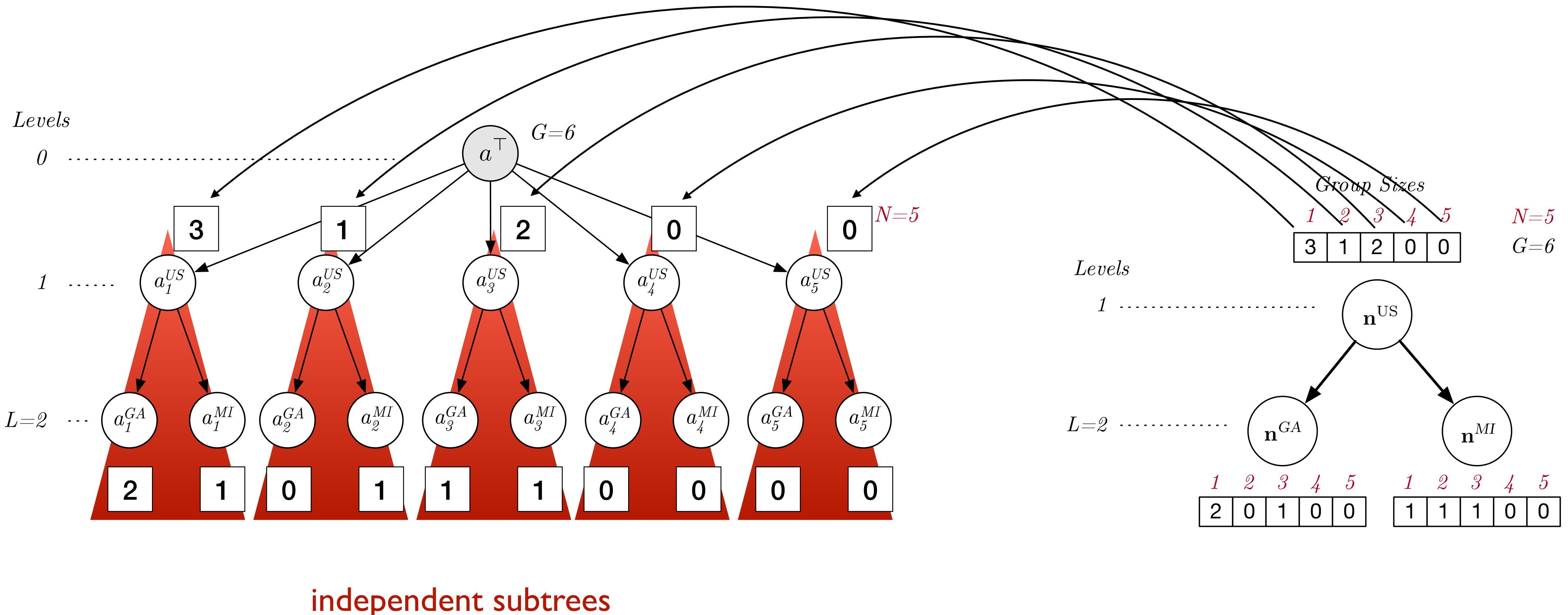
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$$\hat{n}_s^r \in D_s^r \quad \forall r \in \mathcal{R}, s \in [N] \quad (\text{H4})$$

- Solving this QIP is intractable for the datasets of interest to the census bureau.
- Relax the integrality constraint.
- The resulting optimization problem becomes convex but presents two limitations:
 1. Its final solution may violate the **consistency** and **faithfulness** conditions
 2. The mechanism is still too slow for very large problems!

Exploiting the Problem Structure

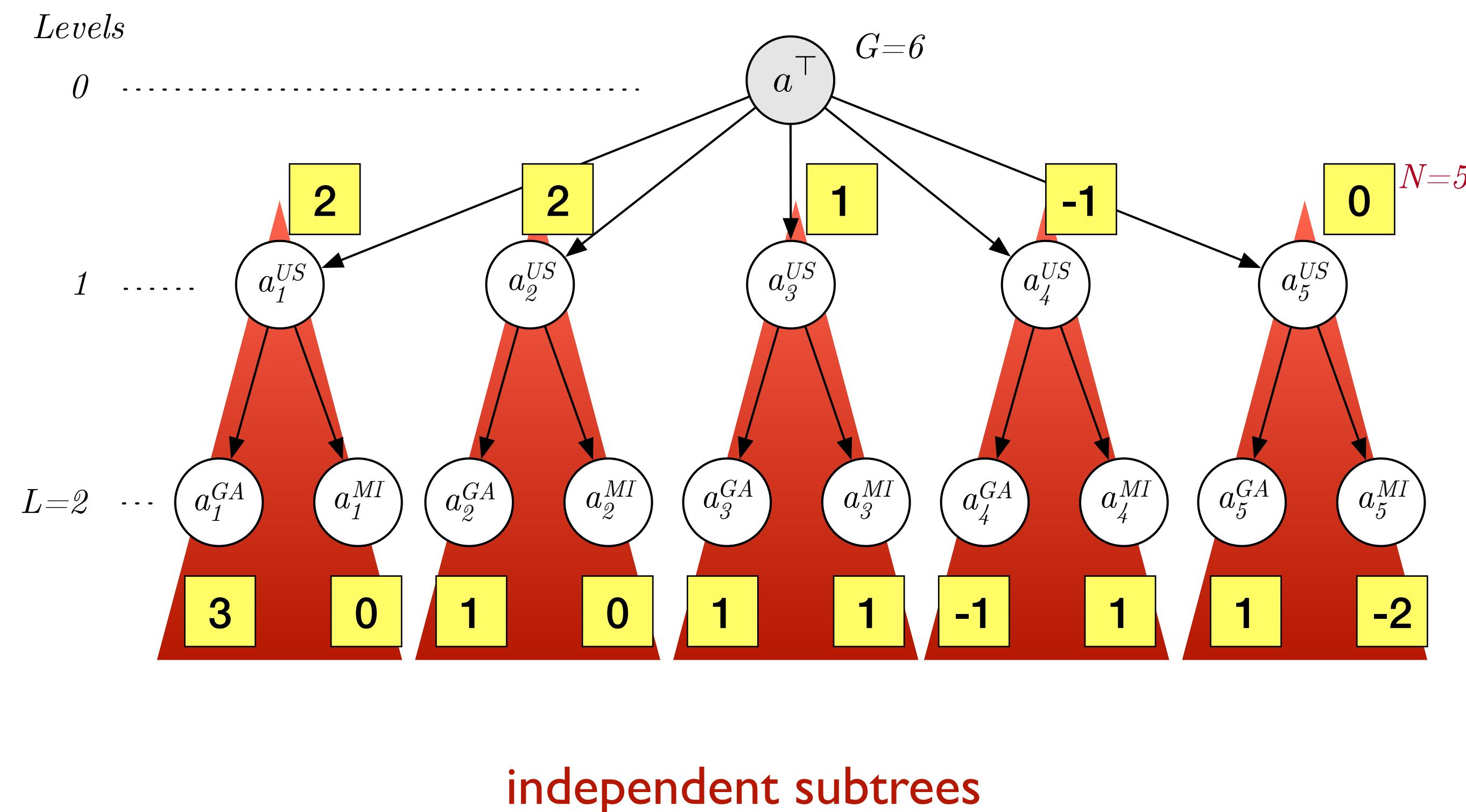
A Dynamic Programming Solution



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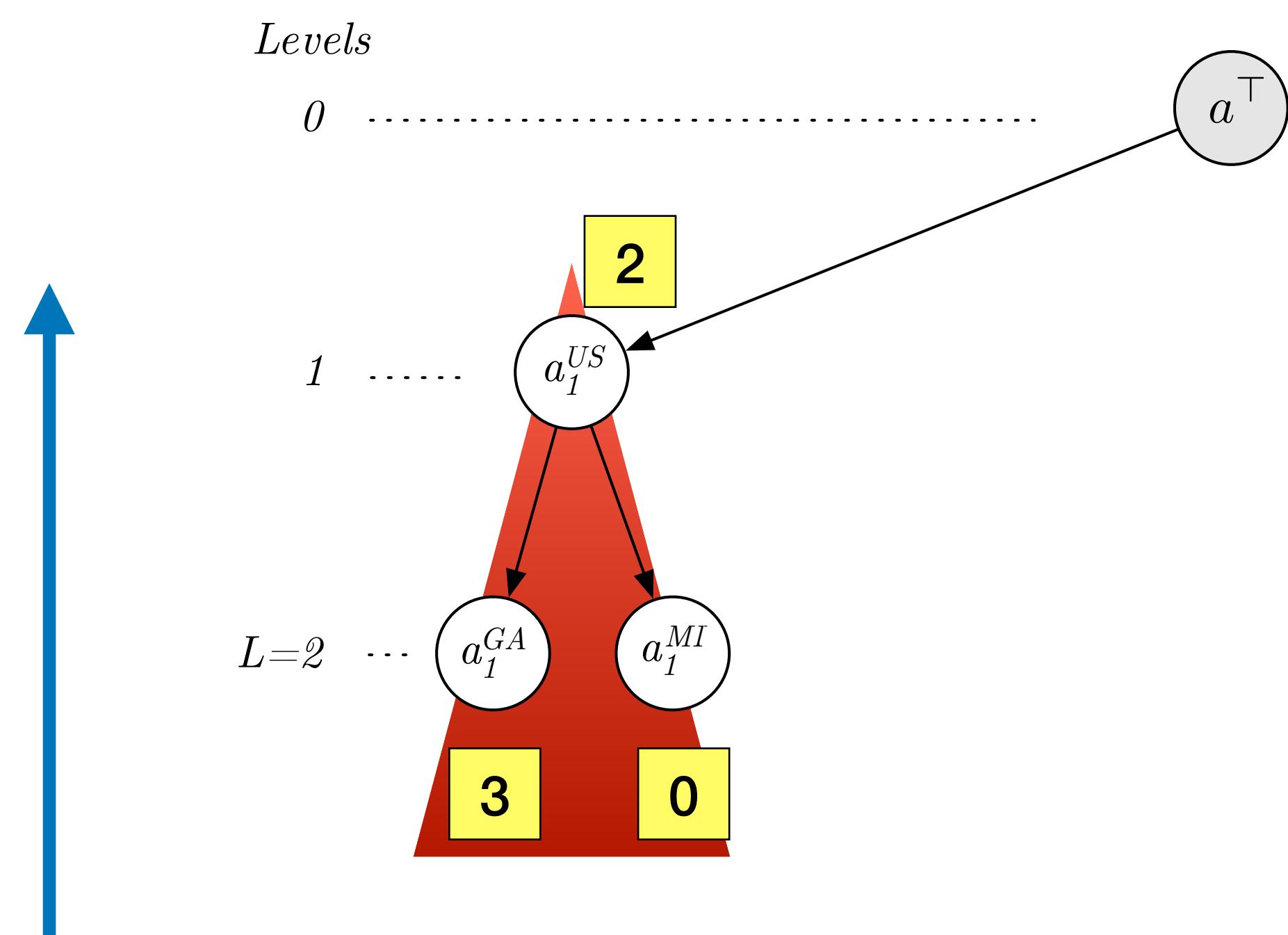
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Exploiting the Problem Structure

A Dynamic Programming Solution

2. Bottom-up phase

- Find new, group sizes \hat{n}^r that satisfy the consistency properties.
- Each node of the tree, computes a table $\tau^r : D^r \rightarrow \mathbb{R}_+$ mapping values (group sizes) to costs.
- $\tau^r(v)$ is the optimal cost for \hat{n}^r in the subtree rooted at region r when $\hat{n}^r = v$
- The optimal cost for $\tau^r(v)$ can be computed from the cost table τ^c of region r children $c \in ch(r)$



$$\tau^r(v) = (v - \tilde{n}^r)^2 + \quad (d1)$$

$$\phi^r(v) = \min_{\{x_c\}_{c \in ch(r)}} \sum_{c \in ch(r)} \tau^c(x_c) \quad (d2)$$

$$\text{s.t. } \sum_{c \in ch(r)} x_c = v \quad (d3)$$

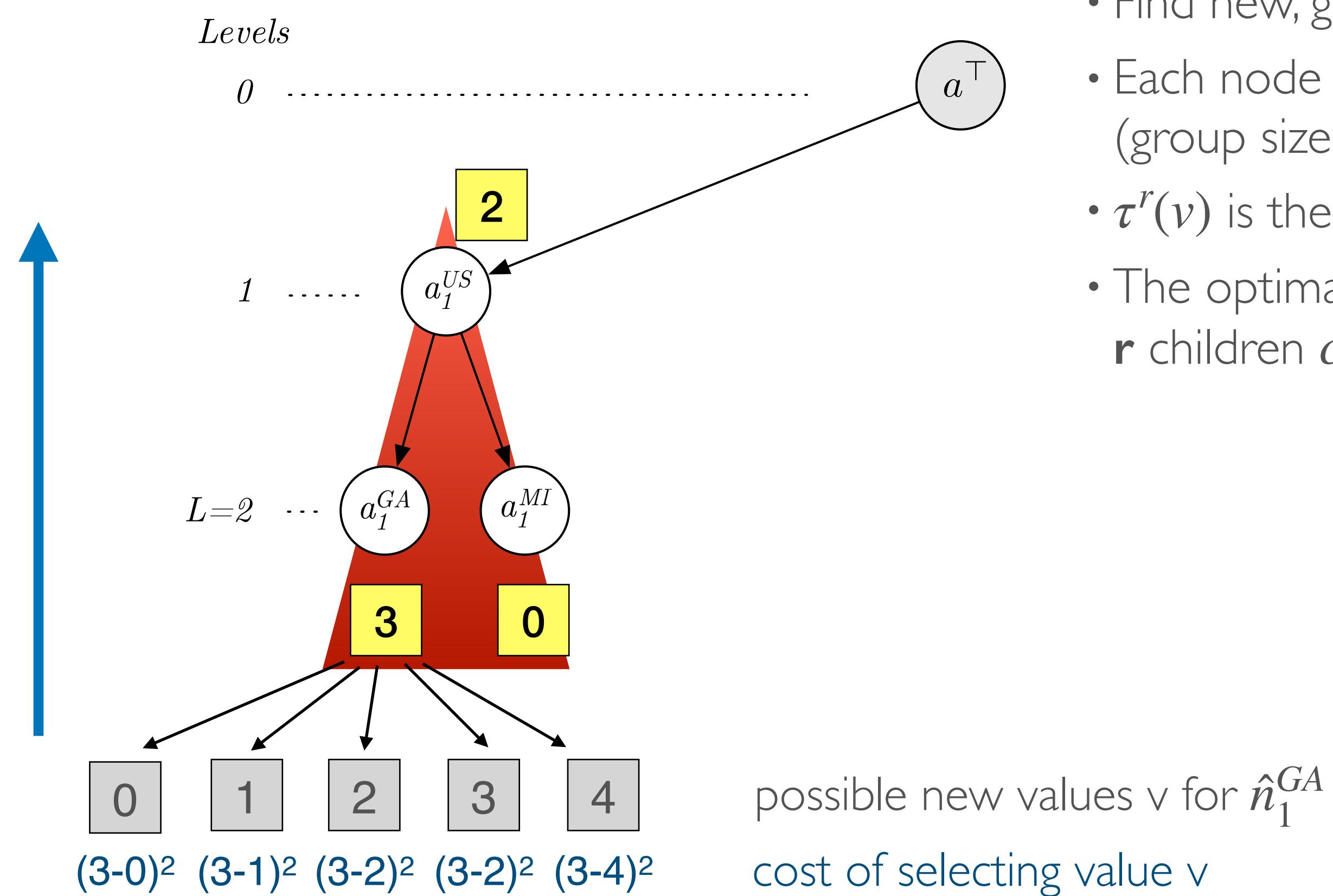
$$x_c \in D^c \quad \forall c \in ch(r) \quad (d4)$$

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A Dynamic Programming Solution

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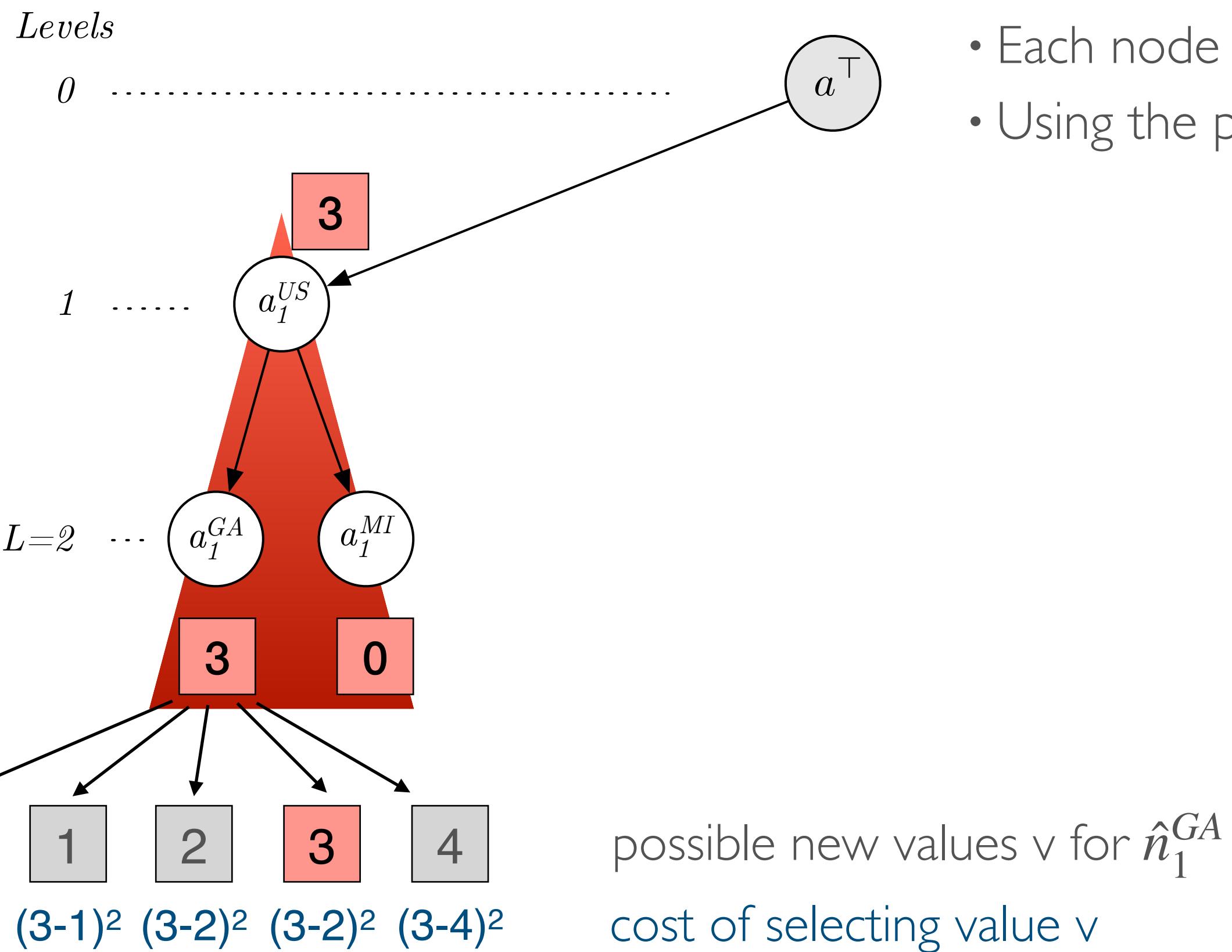
cost tables

v	τ_1^{GA}	τ_1^{MI}	τ_1^{US}
0	9	0	$4 + \min(9+0)$
1	4	1	$1 + \min(9+1; 4+0)$
2	1	4	$0 + \min(0+4; 4+1; 1+0)$
3	0	9	$1 + \min(0+0; 1+1; 4+4; 9+9)$
4	1	16	$4 + \min(1+0; 0+1; 1+4; \dots)$

Exploiting the Problem Structure

A Dynamic Programming Solution

3. Top-down phase



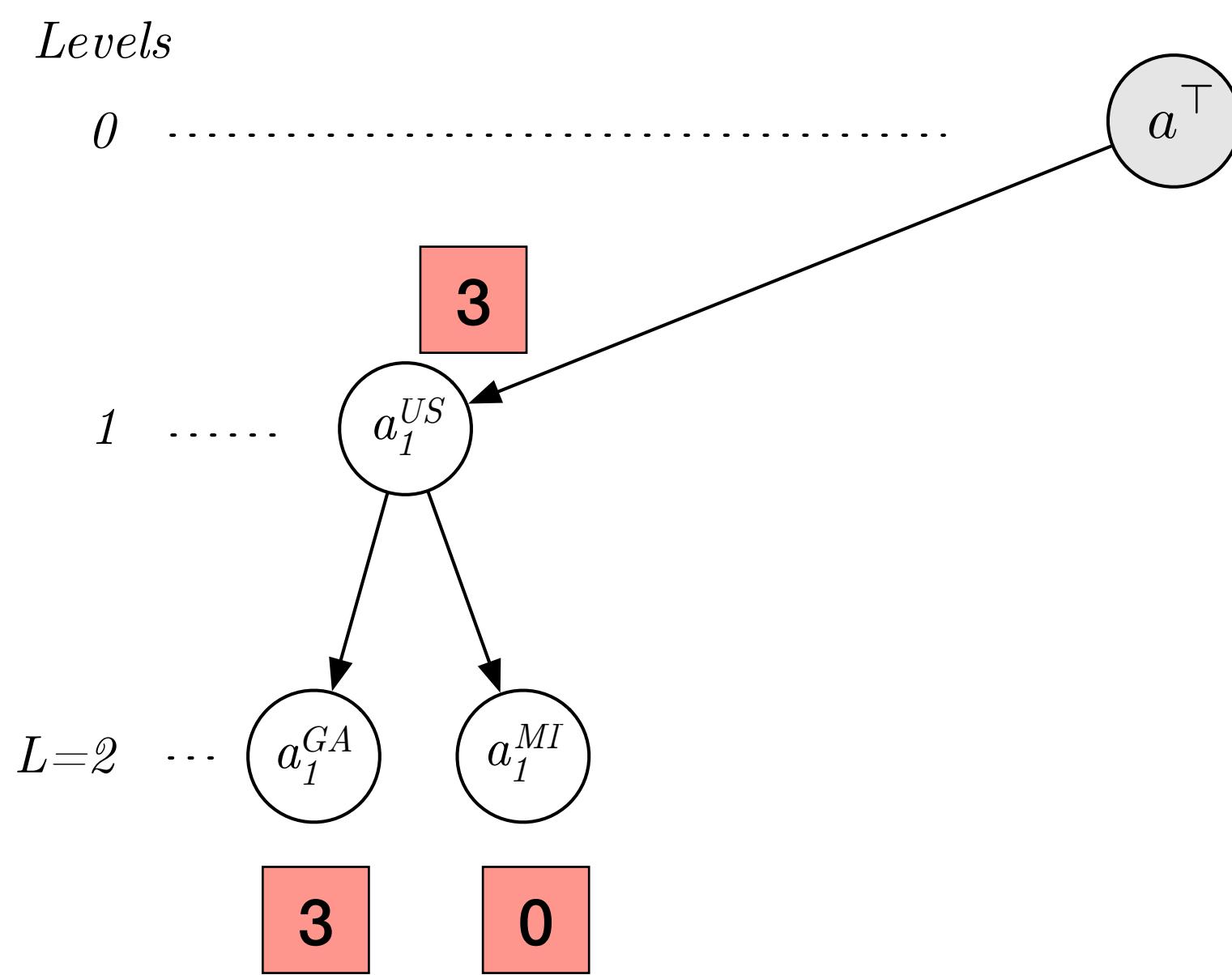
- Each node select the value v that minimizes its cost table
- Using the parent value, choice each children repeats the process

cost tables

v	τ_1^{GA}	τ_1^{MI}	τ_1^{US}
0	9	0	$4 + \min(9+0)$
1	4	1	$1 + \min(9+1; 4+0)$
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4	1	16	$4 + \min(1+0; 0+1; 1+4; \dots)$

Exploiting the Problem Structure

A Dynamic Programming Solution



The issue

- The construction of the data hierarchy requires solving $O(|R|N\bar{D})$ optimization problems, with $\bar{D} = \max_{s,r} |D_s^r|$
 $R = \text{regions}, s = \text{groups sizes } (1, 2, 3, \dots)$

$$\tau^r(v) = (v - \tilde{n}^r)^2 \quad (d1)$$

$$\phi^r(v) = \min_{\{x_c\}_{c \in ch(r)}} \sum_{c \in ch(r)} \tau^c(x_c) \quad (d2)$$

$$\text{s.t. } \sum_{c \in ch(r)} x_c = v \quad (d3)$$

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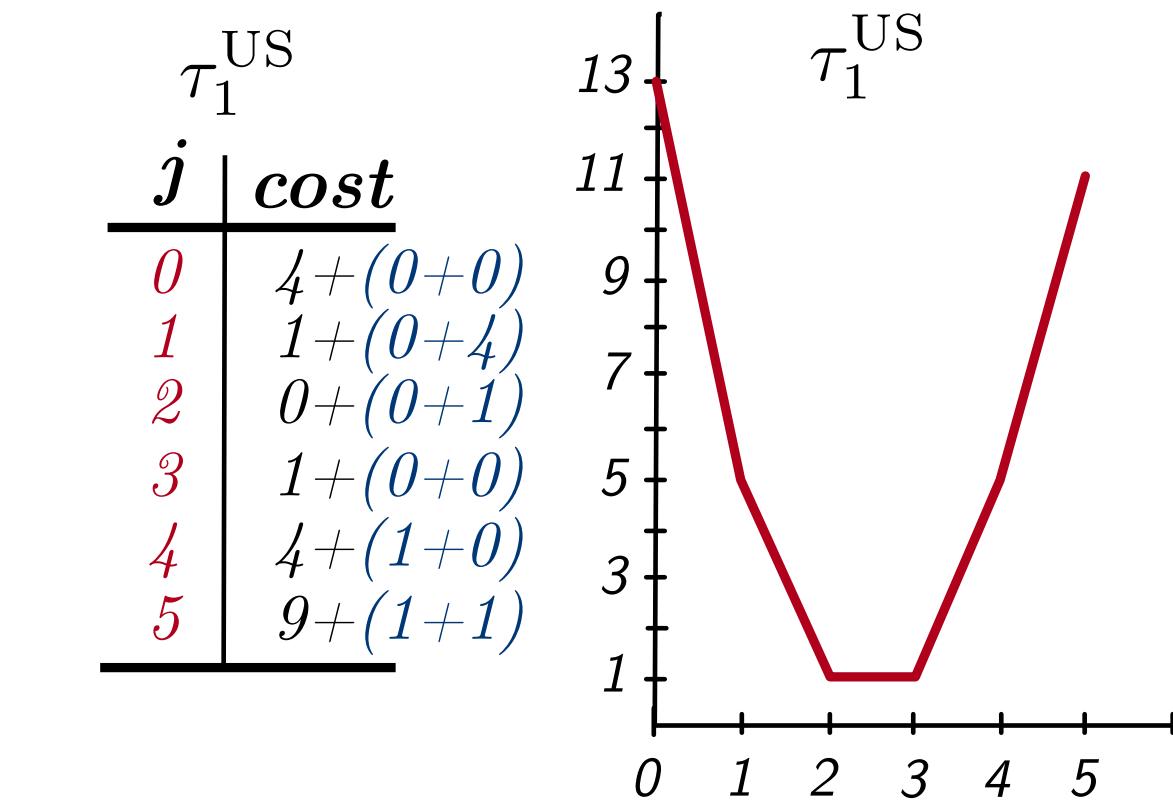
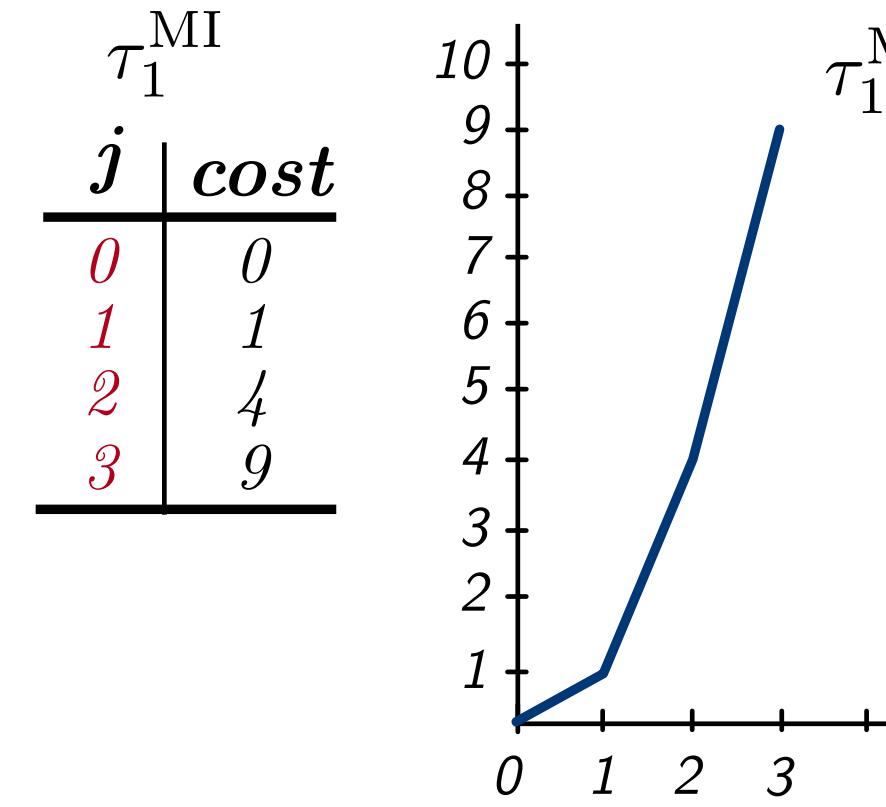
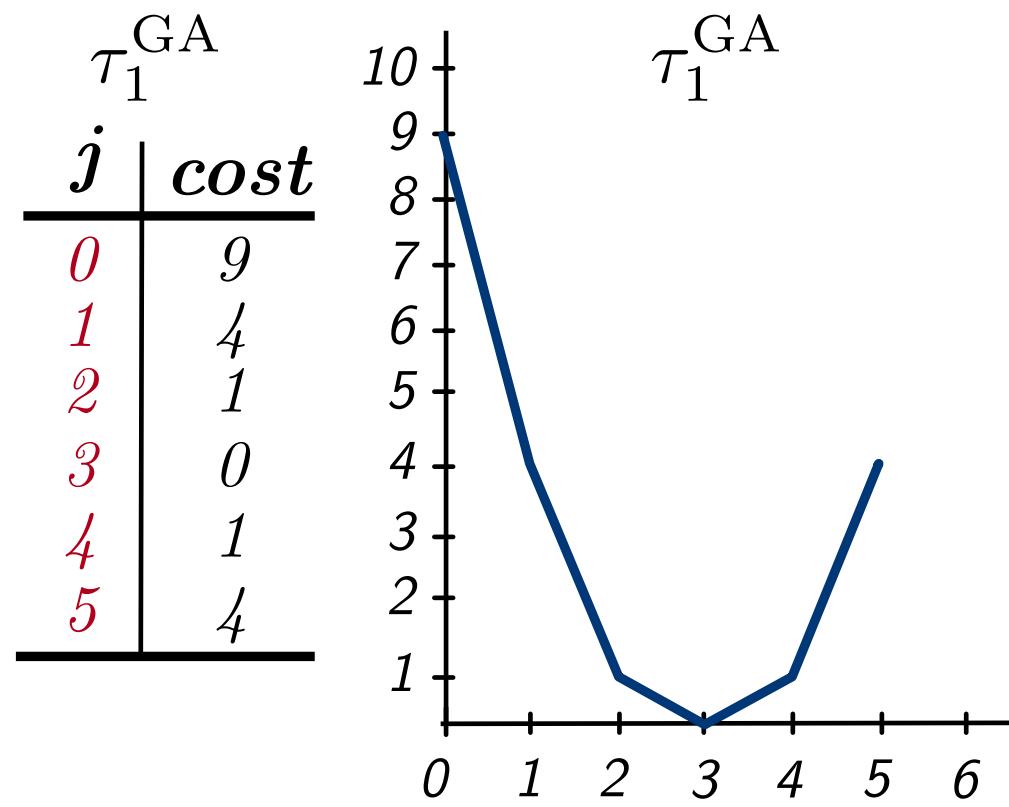
Exploiting the Cost Functions Structure

A Polynomial Time Mechanism

Main Result: The function ϕ_s^r used to compute the values $\tau_s^c(v)$ convex piecewise linear (CPWL)

$$v_c^k = \begin{cases} v_c^{k-1} + 1 & \text{if } c = \operatorname{argmin}_c \tau^c(v_c^{k-1} + 1) - \tau^c(v_c^{k-1}) \\ v_c^{k-1} & \text{otherwise.} \end{cases}$$

$$\begin{aligned} \tau^r(v) &= (v - \tilde{n}^r)^2 & (d1) \\ \phi^r(v) &= \min_{\{x_c\}_{c \in ch(r)}} \sum_{c \in ch(r)} \tau^c(x_c) & (d2) \\ \text{s.t. } \sum_{c \in ch(r)} x_c &= v & (d3) \\ x_c \in D^c & \forall c \in ch(r) & (d4) \end{aligned}$$

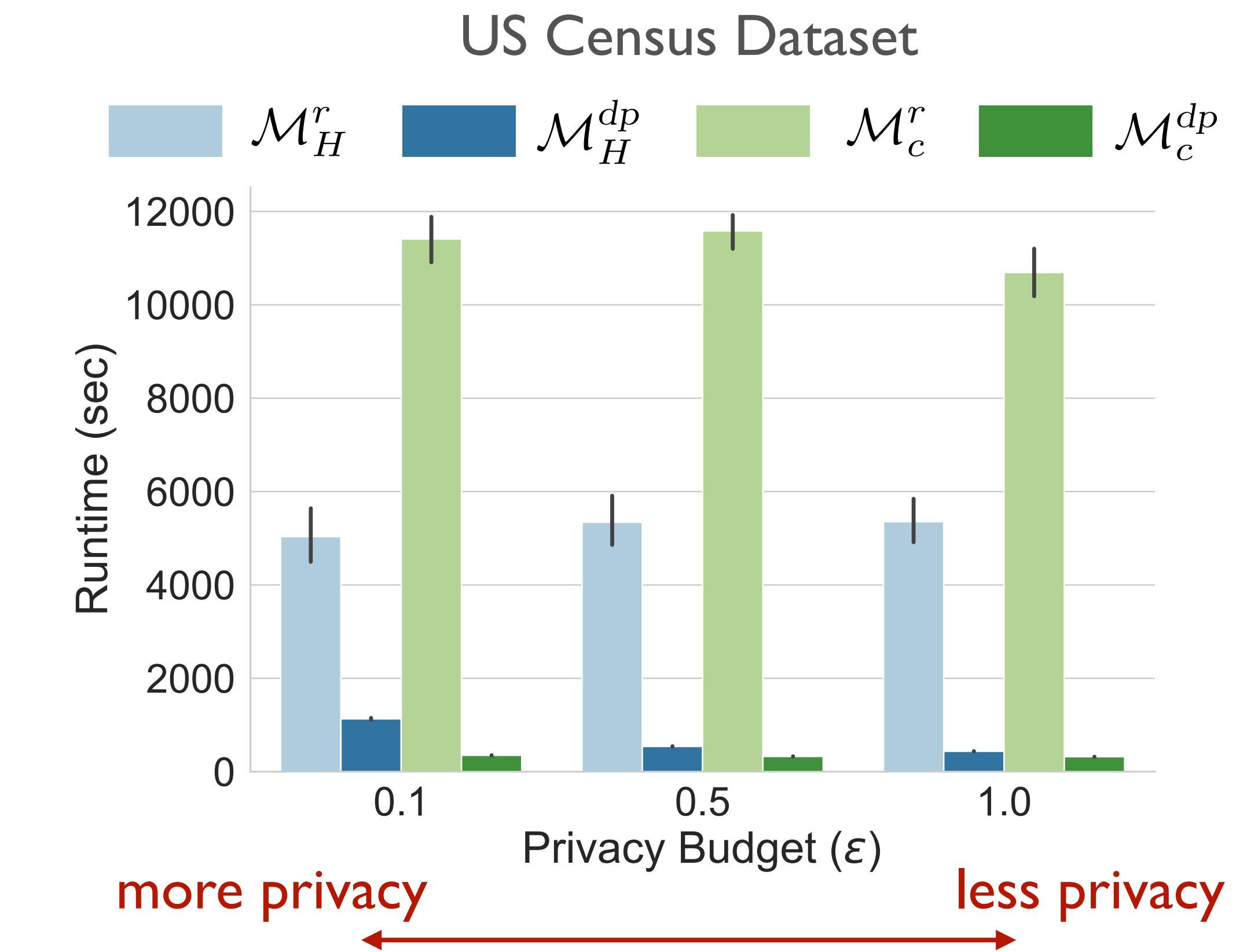
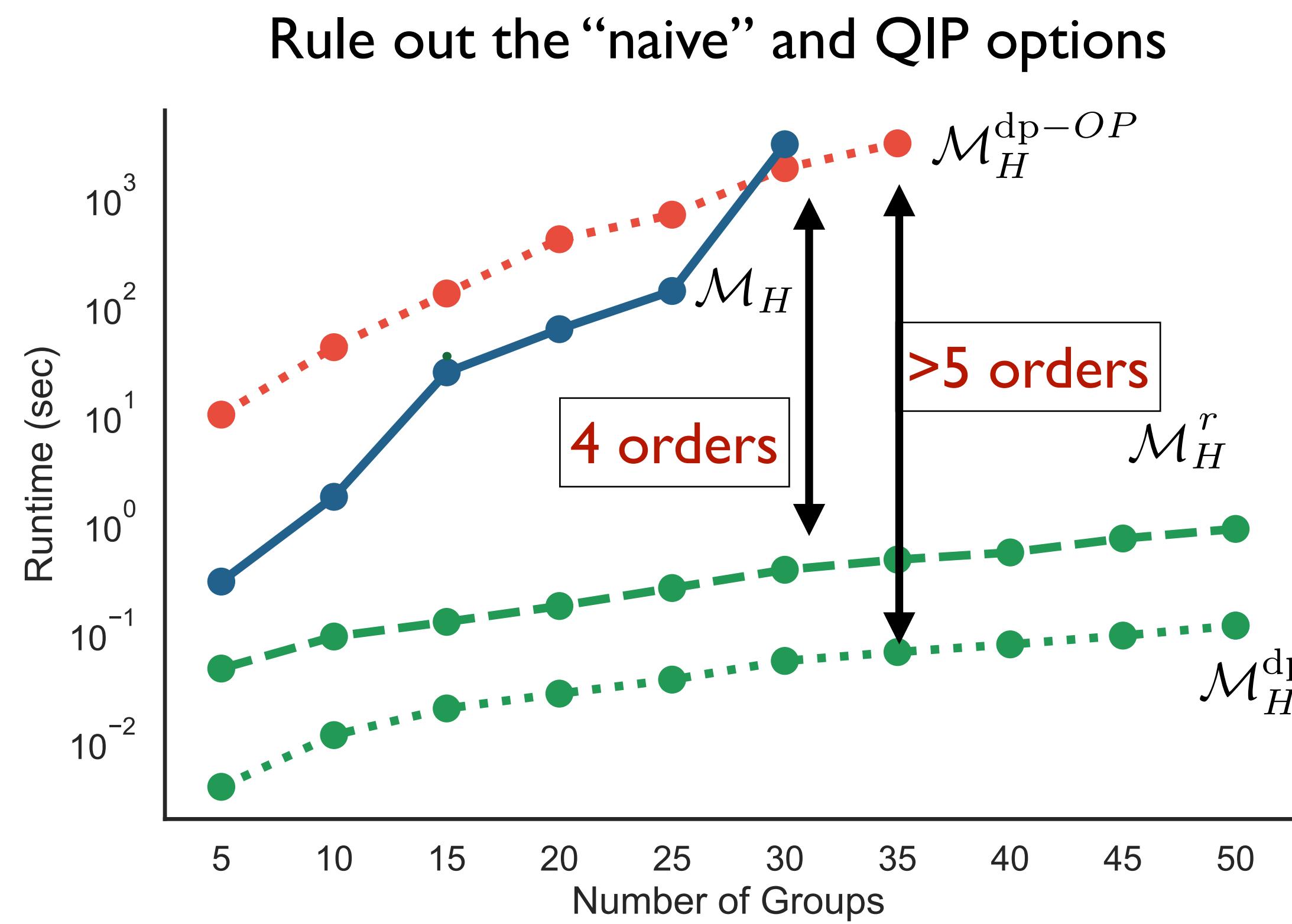


Corollary: The cost table function of each node of the tree is CPWL

Experimental Evaluation

Runtime

Main Result: Exploiting convexity and structure of the problem provides up to **2 order magnitude improvements** w.r.t. the relaxed QIP method



Discussion

- **A bit of quizzing:**
 - Can you explain the concept of ' ϵ ' (epsilon) in Differential Privacy? How does changing its value affect privacy and data utility?
 - What are some common mechanisms (like Laplace or Gaussian mechanisms) used to achieve Differential Privacy? How do they work?
- **Practical thinking:**
 - Discuss a real-world scenario where DP could be effectively applied. What challenges might arise in this implementation?
 - How would you approach the trade-off between data utility and privacy when implementing DP in a large-scale public dataset?
- **Responsible use:**
 - What are the ethical implications of not using Differential Privacy in data-driven projects?
 - Can DP always guarantee the protection of individual's data? Are there any scenarios where it might fail?
 - If you had to argue against the use of DP, what points would you raise?
 - How might advances in technology (like quantum computing) impact the effectiveness of Differential Privacy?
 -

Discussion

- **Balancing Privacy and Public Good:**
 - In situations where AI can benefit public health or safety, how should the balance between individual privacy and the collective good be managed?
 - Should there be exceptions to privacy rules for AI applications in critical areas like healthcare, criminal justice, or national security?
- **Consent and Awareness:**
 - How should informed consent be obtained or considered especially when data is used for AI training?
 - What level of understanding should individuals have about Differential Privacy before their data is used? How can this be realistically achieved?
- **Transparency:**
 - Should organizations be required to disclose the use of DP in their AI systems?
 - Who should be held accountable when an AI system, using differentially private data, makes an erroneous or harmful decision?
- **Long-term Effects and Society:**
 - What could be the long-term societal impacts of widespread adoption of Privacy in AI. Could it lead to a more privacy-conscious culture or create new challenges?
 - How might the evolution of AI technologies influence the future development and implementation of DP principles?

Responsible AI: Seminar on Fairness, Safety, Privacy and more

Thank you!

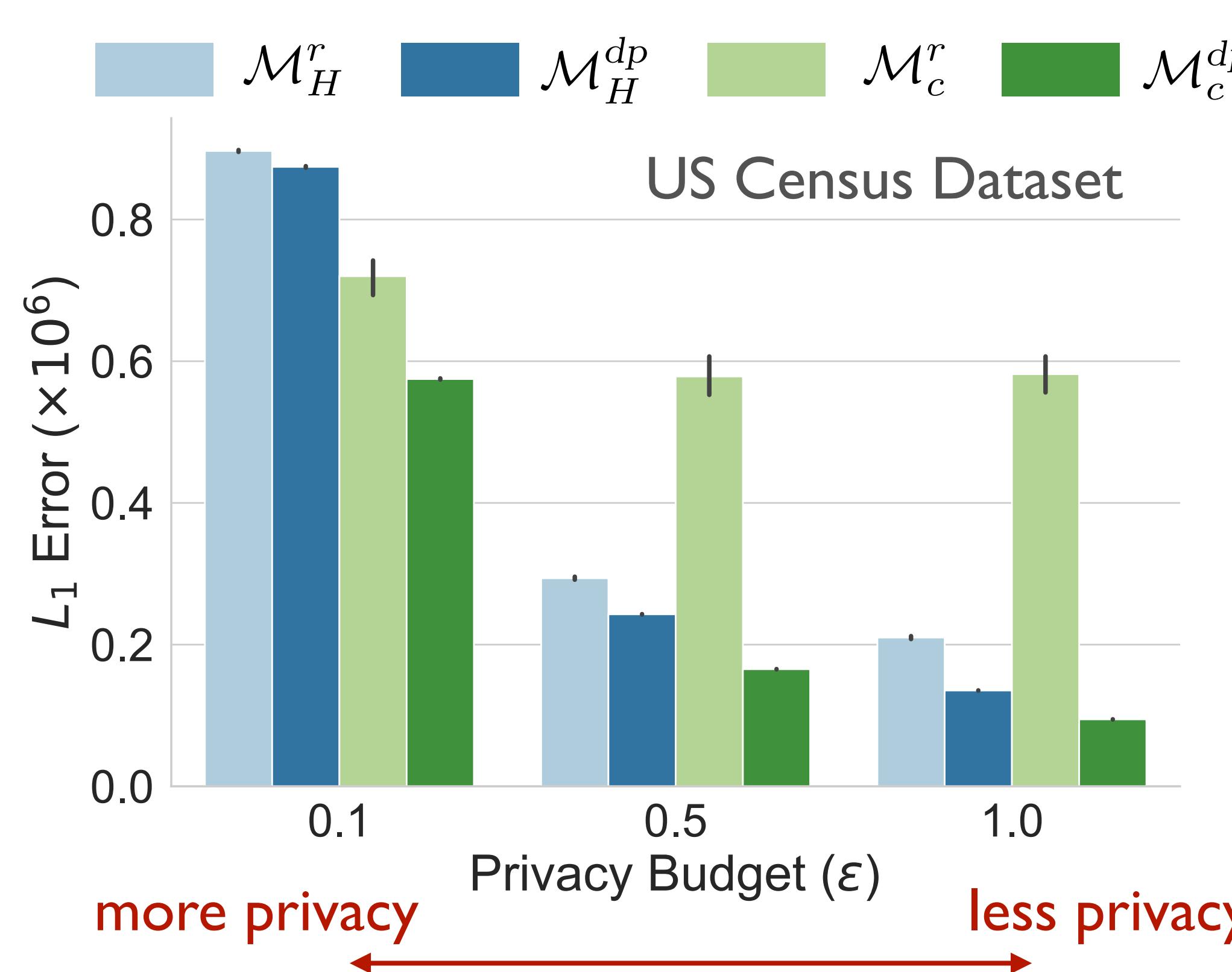
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Experimental Evaluation

Accuracy

Main Result: The CPWL-dynamic programming versions produces **less errors** than the QP counterparts **violating no constraints**



ϵ	Alg	Taxi Data			Census Data			#CV	
		Lev 1	Lev 2	Lev 3	Lev 1	Lev 2	Lev 3		
0.1	\mathcal{M}_H^r	25.4	158.7	904.4	18206	40.3	54.3	802.1	1966
	\mathcal{M}_H^{dp}	26.6	121.9	915.7	0	10.3	38.4	825.4	0
	\mathcal{M}_c^r	47.9	153.2	551.6	19460	23.1	64.5	632.2	1715
	\mathcal{M}_c^{dp}	19.9	65.6	644.3	0	0.9	23.2	550.6	0
0.5	\mathcal{M}_H^r	8.6	81.2	364.2	18591	39.4	37.9	216.3	1990
	\mathcal{M}_H^{dp}	5.5	31.0	408.9	0	2.4	9.4	230.8	0
	\mathcal{M}_c^r	46.7	153.5	450.7	19531	23.1	61.0	494.2	1718
	\mathcal{M}_c^{dp}	4.0	16.4	352.9	0	0.2	5.8	159.1	0
1.0	\mathcal{M}_H^r	7.7	77.2	279.0	18085	40.7	39.2	130.0	1989
	\mathcal{M}_H^{dp}	3.1	19.8	328.5	0	1.2	5.1	128.8	0
	\mathcal{M}_c^r	47.1	154.2	447.1	19706	24.1	63.0	494.5	1728
	\mathcal{M}_c^{dp}	2.0	8.7	307.8	0	0.1	3.2	91.0	0