

# Partially Supervised Feature Selection with Regularized Linear Models

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# 1 Partially Supervised Feature Selection with Regularized Linear Models

## 1.1 Feature selection methods overview

This item is based on the first paper.

### Goals of feature selection

Scenarios related to few tens of samples but thousands dimensions: microarray data,

1. To avoid overfitting and improve model performance, prediction performance in the case of supervised classification and better cluster detection in unsupervised scenarios.
2. To provide more efficient models
3. To gain a deeper insight into the underlying processes that generated the data. The excess of dimensionality difficult the understanding.

The problem is related to find the optimal model parameters for the optimal feature subset. So, the model parameters becomes dependent of the features selected and need to be computed more or less coupled with the guessing of model parameters.

From less (zero) to more coupled computation, we have three strategies:

1. Filter techniques. Two step process, first the filtering, then the training of the model. Take into account only the properties of the data and in some cases a certain amount of prior knowledge. Therefore it's independent of the classification method. In its most simplest form ignores dependences on the data (univariate).

Examples: Euclidean distance, i-test Information gain, Markov blanket filter

2. Wrapper methods. Once selected a candidate subset of features, the classification model is evaluated by training and testing the model. This is iterated over a ensemble of candidate subsets, and the model (with his feature subsets) selected is the model with the best accuracy.

It's very important to construct a good searching algorithm of subsets, in order to reduce the number of sets to model with. This methods are dependent of the classifier, model feature dependencies and have the risk to be bind to a local optima. With randomizing techniques this problem is bypassed to some extent.

Examples: Sequential forward selection (SFS) , Sequential backward elimination, Simulated annealing, Randomized hill climbing, Genetic algorithms.

3. Embedded methods. The search of the optimal subset of features is built into the classifier. Have the advantage that they include the interaction with the classification model, while at the same time being far less computationally intensive than wrapper methods.

Examples: Decision trees Weighted naive Bayes, Feature selection using the weight vector of SVM, AROM

### 1.1.1 AROM methods

The acronym derives from *Approximation of Minimization zeRO-norm*

The problem is obtain a linear predictor  $h$ , minimizing the number of independent variables (features) without loss of accuracy:

$$h(\mathbf{x}) = \text{sign}(\mathbf{w} \cdot \mathbf{x} + b)$$

for  $n$  samples  $x_i \in \mathbb{R}^n$  and  $m$  labels  $y_i \in \{\pm 1\}$ .

The accuracy constraint requires correspondence of sign

$\text{sign}(y_i) \cdot \text{sign}(h_i) > 0$  or in other form  $y_i \cdot h_i = 1$

or less restrictive, enabling  $\mathbf{w}$  to scale freely  $y_i \cdot h_i \geq 1$

so

$$y_i(\mathbf{w} \cdot \mathbf{x} + b) \geq 1$$

The minimization is done with a norm defined over the vectorial space of  $\mathbf{w}$ . One approach is to minimize the zero-norm, that is, the number of components of the vector (number of non null  $w_i$ ). But it's known to be a NP-Hard problem.

It's more adequate compute over a 1-norm or a 2-norm. In the second paper, the author deduce a suitable form for the function that could be minimized, taken into account the former constraint:

$$\sum_{j=1}^n \ln(|w_j| + \epsilon)$$

The term  $\epsilon$  is included to protect from zero values inside logarithm.

AROM methods are therefore feature selection embedded methods.

**I1-AROM** and **I2-AROM** (in this case by means of a 2-norm minimization) algorithms optimize this algorithm by iterative rescaling of inputs and doing a smooth feature selection since the weight coefficients along some dimensions progressively drop below the machine precision while other dimensions become more significant.

### 1.1.2 AROM semi-supervised

Third and Fourth papers explore a improvement of these previous described methods.

#### Goal

Classification of microarray data: few tens of samples against several thousand dimensions (genes).

#### Key differential strategy

Extend AROM methods by means of partial supervision on the dimensions of a feature selection procedure. The technique proposes to use of prior knowledge to guide feature selection, but flexible enough to let the final selection depart from it if necessary to optimize the classification objective.

The preferential features are previously selected from similar datasets in large microarray databases because it's known that different sub-samples of patients lead to very similar sets of biomarkers, as expected if we are aware that the biological process explaining the outcome is common among different patients.

This datasets are called source datasets and we expect that the prediction for a similar feature vector is the same than the prediction for this vector in our dataset (the target).

*In third paper prior knowledge is incorporated by biological information*

So, if we have some knowledge on the relative importance of each feature (either from actual prior knowledge or from a related dataset), the supervised AROM objective can be modified by adding a prior relevance vector  $\beta = [\beta_1, \dots, \beta_n]$  defined over the  $n$  dimensions and where  $\beta_j > 0$  is the prior relevance of the  $j$  feature.

So in this case, the function to minimize in the case of 1-norm is:

$$\sum_{j=1}^n \frac{1}{\beta_j} \ln(|w_j| + \epsilon)$$

In the case of L2-NORM, is necessary to minimize:

$$\min_{\vec{w}} \|\vec{w}\|_2^2$$

To do so, the authors Helleputte & Dupont define an iterative method over  $k$ :

1. At step  $k = 0$ , initialize  $\vec{w}_0 = \vec{w}_0 = \vec{\beta}$
2. Iterate until convergence:
  - a. Calculate  $\min_{\vec{w}} \|\vec{w}\|_2^2$  constrained to  $y_i(\vec{w}(\vec{x}_i * \vec{w}_k) + b) \geq 1$
  - b. With this  $\vec{w}$  set the following iteration vector:  $\vec{w}_k * \vec{w} * \vec{\beta} \rightarrow \vec{w}_{k+1}$

## 1.2 L2-AROM and PS-L2-AROM

Describe how the provided implementation of L2-AROM works. See [2, 3, 4] for specific details. Next, implement a variable ranking approach based on the PS-L2-AROM method, as described in [4], using the provided implementation of L2-AROM.

You should introduce the possibility in the previous implementation to specify the initial value of the scaling vector  $\vec{z}$ . By default this vector should be equal to a vector with all components equal to one. By increasing or reducing these values, one should be able to favor, or make more difficult the selection of specific features. This will lead to the method PS-L2-AROM, in which some sort of prior-knowledge about the importance of each feature can be considered.

### 1.2.1 Implementation

The implementation provided is based in iterative algorithm showed at the end of the previous section but without introduction of previous knowledge. We change the notation, the iterative weight/coefficients vector is  $\vec{z}_k$  replacing  $\vec{w}_k$

1. At step  $k = 0$ , initialize
$$\vec{z}_0 = (1, \dots, 1)$$
2. Iterate until convergence:
  - a. Calculate
$$\min_{\vec{w}} \|\vec{w}\|_2^2 \text{ constrained to : } y_i(\vec{w}(\vec{x}_i * \vec{z}_k) + b) \geq 1$$
  - b. With this  $\vec{w}$  set the following iteration vector:

$$\vec{z}_k * \vec{w} \rightarrow \vec{z}_{k+1}$$

The step 2.a is implemented by a linear fit over a SVM algorithm. We see it commenting over the code:

```
def variable_ranking(X, Y, C = 1, threshold = 1e-10):
    """
    """
    # X is the samples*features matrix and Y the labels of each sample
```

```

final_X = X.copy()
# Initialization of z (equation (6))
z = np.ones(X.shape[1])

length = z.shape[0]

# Array that stores the elimination order, being the higher number the first attribute
# that is eliminated and 1 the last one
elimination_order = np.zeros(length, dtype = int)

original_feature_indices = np.arange(0, length, dtype = int)
# This is the definition of the linear classifier for the equation (7)
clf = SVC(kernel = "linear", C = C, random_state = 0)

iter_without_dropping = 0
n_removed_features = 0

# The iteration stops if there are 20 iterations not able to drop new features, and
# if the remaining number of features are less than 10
while iter_without_dropping < 20 and length > 10:

    # Fit the SVC and obtain the solution  $w = \text{clf.coef\_}[0]$ .
    # This is the resolution of equation (7)
    clf.fit(final_X * np.outer(np.ones(X.shape[0]), z), Y)
    # Compute the new z rescaling the coefficients, equation (8).
    z *= np.abs(clf.coef_[0])
    n_features_to_drop = np.sum(z < threshold)
    if n_features_to_drop == 0:
        iter_without_dropping += 1
    else:
        iter_without_dropping = 0
        # We filter z retaining the components with values over the threshold
        # Then we store in remove_order the positions of these components according
        # to these values, the index of the smallest, the first.
        remove_order = np.argsort(z[ z < threshold ])
        # We recompute elimination order, increasing only the indexes
        # of the features removed and
        # in the order provided by remove_order,
        # so the first removed feature (that one with smallest z)
        # has a new index of 0 (in this case no modification),
        # the following and index of one, and so on
        # The values assigned are referred to a initial variable
        # n_removed_features = 0 that is incremented
        # in each step by the number of removed features in order to have unique indexes.
        elimination_order[ original_feature_indices[ z < threshold ][ remove_order ] ] = \
            np.arange(0, n_features_to_drop) + n_removed_features + 1
        n_removed_features += n_features_to_drop
        length -= n_features_to_drop

```

```

# Delete from X, z and original_features the selected ones
final_X = final_X[ :, z >= threshold ]
original_feature_indices = original_feature_indices[ z >= threshold ]
z = z[ z >= threshold ]

# Removing of all remaining features (features not processed)
if length > 0:
    remove_order = np.argsort(z)
    elimination_order[ original_feature_indices[ remove_order ] ] = \
        np.arange(0, length) + n_removed_features + 1

# The array is reversed so the more relevant features,
# the last ones to remove, are in the first places
# in order to ease the feature selection.
return np.argsort(-elimination_order)

```

To introduce previous knowledge to obtain the partially supervised extension of L2-AROM algorithm it's necessary to introduce a weight vector  $\beta$  according to the modified equations (6) to (8)

1. At step  $k = 0$ , initialize

$$\vec{z}_0 = \vec{\beta}$$

2. Iterate until convergence:

- a. Calculate

$$\min_{\vec{w}} \|\vec{w}\|_2^2 \text{ constrained to : } y_i(\vec{w}(\vec{x}_i * \vec{z}_k) + b) \geq 1$$

- b. With this  $\vec{w}$  set the following iteration vector:

$$\vec{z}_k * \vec{w} * \vec{\beta} \rightarrow \vec{z}_{k+1}$$

The modification of the previous algorithm is included in point 1.3.4 *Main process* in the first method **ps\_l2\_aron\_feature\_ranking**.

### 1.3 Experiments of paper 4

Reproduce the experiments reported in [4]. For this, you can make use of the associated datasets which you will find in the data folder associated to this project proposal. Note that given a particular selected subset of variables, the classifier employed should be a soft-margin linear SVM with  $C = 1$ .

We are implemented all the experiments. We are going to summarize here the interesting things in the scope of the procedure and discrepancies with the results that the authors show in the paper.

#### Preprocessing of datasets

We have three datasets from three experiments: Chandran, Singh and Welsh. All three used the same Affymetrix microarray technology but one of them a different version (Welsh), so the features do not coincide in position or often in name. There are even subtle differences between the names of the features of the two matching datasets.

The first task was to relate the features. We were not able to obtain references on the web, but a visual inspection allowed us to determine the necessary transformations between their names.

For this we implemented an intersection procedure. In the first step we modified the names of the columns of the three datasets applying a simple process that made the spurious differences disappear.

With the columns thus homogenized, we proceeded to the intersection so that we were left with new versions of the three datasets. These versions contain the same variable in each column. So in index 4, for example, the 3 datasets contain the data of feature *102\_f\_at*.

The three original datasets were reduced to 12600 feature columns plus the labels column *Y*, from an initial situation of 12626 columns in Chandran and Singh and 12627 in Welsh. This coincides with what was obtained by the authors.

Also we need to homogenize to  $-1$  the value of the negative label on Singh dataset.

### **T-test prior ranking**

To give weights to the most significant variables of the datasets we have tried to reproduce the strategy proposed by the authors, by using the t-test statistic. The variables are ordered from highest to lowest t-value. Actually it is a Welch's t-test, or unequal variances t-test. We take the absolute value of the t-statistic before proceeding to the ordering.

The rankings of the three sources are calculated before the main process. The rankings of the combined sources are also calculated for use in the multiple transfer scenario, as indicated by the authors.

Here we disagree slightly with the points where the intersection of features of two sources that we need to combine to obtain the 50 most relevant consensus features:

1. Sources 1 and 2: 262 vs 275 in the paper
2. Sources 0 and 2: 362 vs 385 in the paper
3. Sources 0 and 1: 513 vs 557 in the paper.

This could indicate discrepancies in the way of calculating the ranking via t-test that could determine the differences observed in the graphs, but we can not assure it. We have not had time to delve further into this slight discrepancy.

### **Main process**

Here we assemble four loops:

1. Iterations  $k$  from 0 to 199
2. Iterations by target (Chandran, Singh and Welsh)
3. Iterations by source that provides the weights for the vector  $\beta$  (each of the other two sources, both sources combined (multiple transfer), zero transfer (with all weights to 0), random transfer (meaning with greater weight 50 features taken randomly) These are the scenarios indicated in paper.

We have added an additional scenario that we call *none* where we randomly select the features but do not apply any ranking system.

4. Iterations for number of features: 20 values evenly spaced in a  $\log_2$  way. The authors have more, but it seems enough to compare the results.

For each instance, the BCR quality metric is calculated, as defined by the authors.

Before painting the results, the arithmetic mean of all the values in each field is computed.

We have tried to plot the results as similar as possible to the graphs of the paper.

There are a few differences with the graphs of the paper:

1. The zero transfer (all values from beta to 1) behaves better in our analysis.

2. The random transfer behaves much worse than in the paper (and better than none transfer). We find this result more reasonable than that obtained by the authors in the paper. As a check we see that random-transfer moves in parallel to none-transfer, but a bit more higher (accurate) in all extent of the three datasets. Also random-transfer performance in paper is over no transfer performance below 50 features.
3. Is it observed that the multiple transfer has greater performance than the rest? Not really, considering also that the standard errors are around one hundredth of performance, so the measurement ranges overlap in our case (we have also calculated and painted these errors for each of the scenarios). Also the no-transfer performance is not as bad as in paper.
4. Our BCR performance is greater than that obtained by the authors. It is appreciated especially in Chandran and Singh, where in the paper it moves to the height of 0.9 in a large part of the graph, while we move to the height of 0.95. We believe that the classification method used in our case (LinearSVC) of sklearn is more precise than the used by the authors. This maybe also explain that sklearn method is more sensitive to random transfers, penalizing them much more clearly in our case.

### Stability

We have calculated the stability according to the formula defined in the paper (Kuncheva index). The stability is zero in none, which makes a lot of sense (sequences obtained randomly). The stability without transfer is lower, as in the paper, but again the stability of random, in the paper is much more closer to the values that are achieved with transfers.

We agree that the maximum stability values are given for all datasets for a number of features equal to 50.

It is likely that we have calculated the random transfer in a different way than the authors or as we said, perhaps the classifier strategy, or the iterative ranking algorithm are more precise than the authors one.

### Impact of parameter B

In this point of the paper, the authors analyze the convenience of the choice of value 10 as a weight for the variables favored in the transfer of rankings from the sources to the targets. The result is perfectly reproduced that around 50 features selected the stability is directly proportional to B.

We also agree on the fact between 5 and 100, and specially between 10 and 100, the value of B does not influence stability.

The biggest difference between the graphs is that our BCR measures are again better than those obtained by the authors. While the authors fall below 0.85 in the central peak of a few tens of features, we stay above 0.9. We believe that the classification method used in our case is more precise than the one used by the authors in their day.

### Conclusion

Despite the presence of some odd results, we think that the **PS-L2-AROM** method is a very useful method, whose effectiveness can be easily increased as more prior knowledge could be incorporated. If, instead of using an univariate test, we feed feature rankings obtained by more elaborate strategies of feature selection, the improvement should be substantial. For this could be accomplished it would be necessary that the selected features and their ranking of importance be published or could be obtained easily in a broad range of relevant articles.



### 1.3.1 Imports and globals

Script 1.3.1 (python)

```
1 import warnings
2 warnings.filterwarnings("ignore")
3 import sys
4 import string
5 import numpy as np
6 import pandas as pd
7 from sklearn.feature_selection import GenericUnivariateSelect
8 from sklearn.preprocessing import StandardScaler
9 from sklearn import metrics
10 from scipy import stats
11 from sklearn.model_selection import train_test_split
12 from sklearn.metrics import confusion_matrix
13 from sklearn.svm import SVC, LinearSVC
14
15 NROWS = sys.maxsize
16 PATH_DATA = './data'
17 VERBOSE = False
18 SELECT_SAMPLES = None
19 SELECT_FEATURES_INI = 0
20 SELECT_FEATURES_FIN = -1
21 TEST_SIZE = 0.10
22 B_SIZE = 10.0 # weight to assign to favored transfered features
23 #NUM_FEATURES_SOURCE = min(50, int((SELECT_FEATURES_FIN-SELECT_FEATURES_INI)/2))
24 NUM_FEATURES_SOURCE = 50
25 NUM_FEATURES_SELECTED = 200
26 NO_TRANSFER_IDX = 3
27 DUAL_TRANSFER_IDX = 5
28 RANDOM_IDX = 4
29 NONE_IDX = 8
30 NUM_FEATURES_SOURCE = 50
31 RANDOM_STATE = 123456
32 SAMPLE_NAMES = {0:'chandran', 1:'singh', 2:'welsh', 3:'no transfer', 4:'random',
33                 5:'singh+welsh', 6:'chandran+welsh', 7:'chandran+singh', 8:'none'}
34
35 g_B = B_SIZE # weight to assign to favored transfered features
36 g_k = 0 #iteration
```

### 1.3.2 Preprocessing datasets

Script 1.3.2 (python)

```
1 def load_df(file):
2     """
3     Load sample files
4     """
5     df = pd.read_csv('./data' + '/' + file, sep=',', header=0, nrows = NROWS)
6     return df
```

```

7
8 def normalize_feature_names(features):
9     """
10     Normalize the names of the features in order to select the common features
11     """
12     features_new = []
13     for feature in features:
14         feature_new = feature.replace('/', '@').replace('-', '@').replace('_',
15         → '@').replace('.', '@').lower()
16         if feature[0] == "X":
17             features_new.append(feature_new[1:])
18         else:
19             features_new.append(feature_new)
20     return features_new
21
22 def intersect_features(df_samples):
23     """
24     Do the intersection and reorder of columns to have equivalent features at the same
25     → indexes
26     """
27     features_0 = df_samples[0].columns
28     features_1 = df_samples[1].columns
29     features_2 = df_samples[2].columns
30     norm_features_0 = np.array(normalize_feature_names(features_0))
31     norm_features_1 = np.array(normalize_feature_names(features_1))
32     norm_features_2 = np.array(normalize_feature_names(features_2))
33     intersect_0 = np.array([], dtype=int)
34     intersect_1 = np.array([], dtype=int)
35     intersect_2 = np.array([], dtype=int)
36     for idx_0, feature_0 in enumerate(norm_features_0):
37         idx_1 = np.where(norm_features_1 == feature_0)
38         idx_2 = np.where(norm_features_2 == feature_0)
39         if idx_1[0].size == 1 and idx_2[0].size == 1:
40             intersect_0 = np.append(intersect_0, idx_0)
41             intersect_1 = np.append(intersect_1, idx_1[0][0])
42             intersect_2 = np.append(intersect_2, idx_2[0][0])
43         else:
44             print("UnMatch", idx_0, feature_0)
45     print(intersect_0.shape)
46     print(intersect_0)
47     print(intersect_1)
48     print(intersect_2)
49     df_samples_norm = []
50     df_samples_norm.append(df_samples[0].iloc[:, intersect_0])
51     df_samples_norm.append(df_samples[1].iloc[:, intersect_1])
52     df_samples_norm.append(df_samples[2].iloc[:, intersect_2])
53     return df_samples_norm
54
55 # Homogeneization of datasets
56 df_samples = []
57 for file in ['chandran.csv', 'singh.csv', 'welsh.csv']:

```

```

57     df_samples.append(load_df(file))
58     display(df_samples[-1].head())
59
60 df_samples_norm = intersect_features(df_samples)
61
62 # Standardize the 0 label as -1 in dataset 1
63 mask = df_samples_norm[1]["Y"] == 0
64 df_samples_norm[1].loc[mask, "Y"] = -1
65
66 for i in range(3):
67     display(df_samples_norm[i].head())

```

	X100_g_at	X1000_at	X1001_at	X1002_f_at	X1003_s_at	X1004_at	X1005_at	\
0	7.234793	6.494211	4.853264	3.527822	5.575283	5.630715	7.070994	
1	6.967237	6.632175	4.320490	3.535030	5.505270	5.173343	7.826527	
2	7.026961	6.510959	4.267634	3.387379	5.906008	5.321219	7.857653	
3	7.123875	6.155900	4.114608	3.380995	5.891499	5.602339	8.285221	
4	7.182206	6.237578	4.194653	3.380361	5.511587	5.383889	8.941296	

	X1006_at	X1007_s_at	X1008_f_at	...	AFFX.ThrX.5_at	AFFX.ThrX.M_at	\
0	3.586507	8.607721	8.376150	...	4.124928	3.130851	
1	3.470474	6.871599	8.732676	...	4.089809	3.030838	
2	3.292397	7.521978	8.636165	...	3.693827	2.755653	
3	3.636381	8.148127	8.472201	...	4.345752	3.122182	
4	3.331588	8.257033	8.700136	...	4.016990	2.956002	

	AFFX.TrpnX.3_at	AFFX.TrpnX.5_at	AFFX.TrpnX.M_at	AFFX.YEL002c.WBP1_at	\
0	2.983105	3.286748	3.632831	3.200749	
1	2.710369	3.204168	3.721313	3.080551	
2	2.526112	3.254250	3.362329	2.862432	
3	2.656120	3.530544	3.515947	3.026449	
4	2.622684	3.263552	3.606437	3.035578	

	AFFX.YEL018w._at	AFFX.YEL021w.URA3_at	AFFX.YEL024w.RIP1_at	Y
0	3.157482	3.572550	3.201209	1
1	2.908750	2.980353	3.264706	1
2	3.048200	3.247433	3.061890	1
3	3.231532	3.762868	3.354885	1
4	2.938062	3.156967	3.055146	1

[5 rows x 12626 columns]

	100_g_at	1000_at	1001_at	1002_f_at	1003_s_at	1004_at	1005_at	\
0	6.927460	7.391657	3.812922	3.453385	6.070151	5.527153	5.812353	
1	7.222432	7.329050	3.958028	3.407226	5.921265	5.376464	7.303408	
2	6.776402	7.664007	3.783702	3.152019	5.452293	5.111794	7.207638	
3	6.919134	7.469634	4.004581	3.341170	6.070925	5.296108	8.744059	

4	7.113561	7.322408	4.242724	3.489324	6.141657	5.628390	6.825370
---	----------	----------	----------	----------	----------	----------	----------

	1006_at	1007_s_at	1008_f_at	...	AFFX-ThrX-5_at	AFFX-ThrX-M_at	\
0	3.167275	7.354981	9.419909	...	3.770583	2.884436	
1	3.108708	7.391872	10.539579	...	3.190759	2.460119	
2	3.077360	7.488371	6.833428	...	3.325183	2.603014	
3	3.117104	7.203028	10.400557	...	3.625057	2.765521	
4	3.794904	7.403024	10.240322	...	3.698067	3.026876	

	AFFX-TrpnX-3_at	AFFX-TrpnX-5_at	AFFX-TrpnX-M_at	AFFX-YEL002c/WBP1_at	\
0	2.730025	3.126168	2.870161	3.082210	
1	2.696578	2.675271	2.940032	3.126269	
2	2.469759	2.615746	2.510172	2.730814	
3	2.681757	3.310741	3.197177	3.414182	
4	2.691670	3.236030	3.003906	3.081497	

	AFFX-YEL018w/_at	AFFX-YEL021w/URA3_at	AFFX-YEL024w/RIP1_at	Y
0	2.747289	3.226588	3.480196	0
1	3.013745	3.517859	3.428752	1
2	2.613696	2.823436	3.049716	0
3	3.193867	3.353537	3.567482	0
4	2.963307	3.472050	3.598103	1

[5 rows x 12626 columns]

	AFFX.MurIL2_at	AFFX.MurIL10_at	AFFX.MurIL4_at	AFFX.MurFAS_at	\
0	-12	16	37	40	
1	6	8	46	46	
2	-55	33	14	44	
3	-26	3	-10	39	
4	-27	1	1	18	

	AFFX.BioB.5_at	AFFX.BioB.M_at	AFFX.BioB.3_at	AFFX.BioC.5_at	\
0	269	209	197	695	
1	261	215	153	676	
2	570	535	378	1362	
3	273	249	177	632	
4	261	251	193	654	

	AFFX.BioC.3_at	AFFX.BioDn.5_at	...	X101_at	X102_at	X103_at	X104_at	\
0	748	816	...	56	21	228	63	
1	658	804	...	36	27	93	79	
2	1400	1640	...	39	20	56	86	
3	672	844	...	100	19	78	61	
4	711	788	...	74	34	26	38	

X105_at	X106_at	X107_at	X108_g_at	X109_at	Y
---------	---------	---------	-----------	---------	---

0	64	-23	-94	-99	248	1
1	52	14	-70	-179	129	1
2	90	-15	-102	-89	117	1
3	9	16	-117	-64	153	1
4	7	23	-53	-66	141	1

[5 rows x 12627 columns]

## Output

```

UnMatch 651 160020@at
UnMatch 652 160021@r@at
UnMatch 653 160022@at
UnMatch 654 160023@at
UnMatch 655 160024@at
UnMatch 656 160025@at
UnMatch 657 160026@at
UnMatch 658 160027@s@at
UnMatch 659 160028@s@at
UnMatch 660 160029@at
UnMatch 661 160030@at
UnMatch 662 160031@at
UnMatch 663 160032@at
UnMatch 664 160033@s@at
UnMatch 665 160034@s@at
UnMatch 666 160035@at
UnMatch 667 160036@at
UnMatch 668 160037@at
UnMatch 669 160038@s@at
UnMatch 670 160039@at
UnMatch 671 160040@at
UnMatch 672 160041@at
UnMatch 673 160042@s@at
UnMatch 674 160043@at
UnMatch 675 160044@g@at
(12601,)
[ 0 1 2 ... 12623 12624 12625]
[ 0 1 2 ... 12623 12624 12625]
[12616 11737 11738 ... 66 65 12626]

```

	X100_g_at	X1000_at	X1001_at	X1002_f_at	X1003_s_at	X1004_at	X1005_at	\
0	7.234793	6.494211	4.853264	3.527822	5.575283	5.630715	7.070994	
1	6.967237	6.632175	4.320490	3.535030	5.505270	5.173343	7.826527	
2	7.026961	6.510959	4.267634	3.387379	5.906008	5.321219	7.857653	
3	7.123875	6.155900	4.114608	3.380995	5.891499	5.602339	8.285221	
4	7.182206	6.237578	4.194653	3.380361	5.511587	5.383889	8.941296	

	X1006_at	X1007_s_at	X1008_f_at	...	AFFX.ThrX.5_at	AFFX.ThrX.M_at	\
0	3.586507	8.607721	8.376150	...	4.124928	3.130851	

1	3.470474	6.871599	8.732676	...	4.089809	3.030838
2	3.292397	7.521978	8.636165	...	3.693827	2.755653
3	3.636381	8.148127	8.472201	...	4.345752	3.122182
4	3.331588	8.257033	8.700136	...	4.016990	2.956002

	AFFX.TrpnX.3_at	AFFX.TrpnX.5_at	AFFX.TrpnX.M_at	AFFX.YEL002c.WBP1_at	\
0	2.983105	3.286748	3.632831	3.200749	
1	2.710369	3.204168	3.721313	3.080551	
2	2.526112	3.254250	3.362329	2.862432	
3	2.656120	3.530544	3.515947	3.026449	
4	2.622684	3.263552	3.606437	3.035578	

	AFFX.YEL018w._at	AFFX.YEL021w.URA3_at	AFFX.YEL024w.RIP1_at	Y
0	3.157482	3.572550	3.201209	1
1	2.908750	2.980353	3.264706	1
2	3.048200	3.247433	3.061890	1
3	3.231532	3.762868	3.354885	1
4	2.938062	3.156967	3.055146	1

[5 rows x 12601 columns]

	100_g_at	1000_at	1001_at	1002_f_at	1003_s_at	1004_at	1005_at	\
0	6.927460	7.391657	3.812922	3.453385	6.070151	5.527153	5.812353	
1	7.222432	7.329050	3.958028	3.407226	5.921265	5.376464	7.303408	
2	6.776402	7.664007	3.783702	3.152019	5.452293	5.111794	7.207638	
3	6.919134	7.469634	4.004581	3.341170	6.070925	5.296108	8.744059	
4	7.113561	7.322408	4.242724	3.489324	6.141657	5.628390	6.825370	

	1006_at	1007_s_at	1008_f_at	...	AFFX-ThrX-5_at	AFFX-ThrX-M_at	\
0	3.167275	7.354981	9.419909	...	3.770583	2.884436	
1	3.108708	7.391872	10.539579	...	3.190759	2.460119	
2	3.077360	7.488371	6.833428	...	3.325183	2.603014	
3	3.117104	7.203028	10.400557	...	3.625057	2.765521	
4	3.794904	7.403024	10.240322	...	3.698067	3.026876	

	AFFX-TrpnX-3_at	AFFX-TrpnX-5_at	AFFX-TrpnX-M_at	AFFX-YEL002c/WBP1_at	\
0	2.730025	3.126168	2.870161	3.082210	
1	2.696578	2.675271	2.940032	3.126269	
2	2.469759	2.615746	2.510172	2.730814	
3	2.681757	3.310741	3.197177	3.414182	
4	2.691670	3.236030	3.003906	3.081497	

	AFFX-YEL018w/_at	AFFX-YEL021w/URA3_at	AFFX-YEL024w/RIP1_at	Y
0	2.747289	3.226588	3.480196	-1
1	3.013745	3.517859	3.428752	1
2	2.613696	2.823436	3.049716	-1
3	3.193867	3.353537	3.567482	-1

4                    2.963307                    3.472050                    3.598103    1

[5 rows x 12601 columns]

	X100_g_at	X1000_at	X1001_at	X1002_f_at	X1003_s_at	X1004_at	X1005_at	\
0	232	269	46	68	-11	-67	2059	
1	188	245	45	18	-15	44	1885	
2	205	310	24	93	-30	-8	652	
3	198	328	13	41	16	38	2536	
4	187	359	40	13	-1	42	3845	

	X1006_at	X1007_s_at	X1008_f_at	...	AFFX.ThrX.5_at	AFFX.ThrX.M_at	\
0	43	1425	1073	...	873	613	
1	25	1313	1521	...	908	700	
2	-52	1648	1561	...	1450	1102	
3	-35	1006	1307	...	853	604	
4	-18	1009	1156	...	931	664	

	AFFX.TrpnX.3_at	AFFX.TrpnX.5_at	AFFX.TrpnX.M_at	AFFX.YELO02c.WBP1_at	\
0	-2	41	-26	5	
1	-8	13	-26	14	
2	9	27	-7	34	
3	-4	8	-35	-4	
4	-3	21	-16	5	

	AFFX.YELO18w._at	AFFX.YELO21w.URA3_at	AFFX.YELO24w.RIP1_at	Y
0	-15	75	16	1
1	-9	137	5	1
2	-4	67	16	1
3	-15	70	18	1
4	1	43	12	1

[5 rows x 12601 columns]

### 1.3.3 Calculate prior rankings

#### Script 1.3.3 (python)

```

1 def split_data(df, test_size=TEST_SIZE, select_samples=SELECT_SAMPLES):
2     """
3     Split data into train and set
4     """
5     global g_k
6
7     #print("K", g_k)
8

```

```

9     if select_samples == None:
10         labels = df.iloc[:, -1]
11         features = df.iloc[:, :-1]
12     else:
13         labels = np.concatenate([df.iloc[:select_samples, -1],
14                                   df.iloc[-select_samples:, -1]], axis = 0)
15
16         features = np.concatenate([df.iloc[:select_samples,
17                                           ↳ SELECT_FEATURES_INI:SELECT_FEATURES_FIN],
18                                   df.iloc[-select_samples:,
19                                           ↳ SELECT_FEATURES_INI:SELECT_FEATURES_FIN]], axis = 0)
18
19     X_train, X_test, y_train, y_test = train_test_split(features, labels,
20                                                         ↳ test_size=test_size,\
21                                                         random_state=RANDOM_STATE + g_k)
22     #print("@@@@@", test_size, X_train.shape)
23     return X_train, X_test, y_train, y_test
24
25 def ttest(X, y):
26     """
27     Score statistic function for transformer GenericUnivariate
28     """
29     t, _ = stats.ttest_ind(X[y==1] , X[y==-1], equal_var=False)
30     return abs(t)
31
32 def ranking_ttest(X, y):
33     """
34     Ranking the features by t-statistic
35     """
36     ttest_scores = ttest(X, y)
37     feature_indexes = np.argsort(ttest_scores)[::-1]
38     #feature_indexes = np.argsort(ttest_scores)
39     return feature_indexes
40
41 def select_combined_features(idx_source1, idx_source2, feature_rankings,
42                               ↳ num_features=NUM_FEATURES_SOURCE):
43     """
44     Select the features for the multiple transfer
45     """
46     #275 1 y 2
47     #385 0 y 2
48     #557 0 y 1
49     for p in range(51,4000):
50         feature_indexes = np.intersect1d(feature_rankings[idx_source1][:p],
51                                           ↳ feature_rankings[idx_source2][:p])
52         if len(feature_indexes) >= num_features:
53             print("p", p, len(feature_indexes))
54             break
55     return feature_indexes
56
57 def calculate_prior_rankings(df_samples_norm):
58     """

```



```

56     Calculate prior rankings
57     """
58     feature_rankings = []
59     for idx_source in range(3):
60         X1, _, y1, _ = split_data(df_samples_norm[idx_source], test_size=0)
61         feature_rankings.append(ranking_ttest(X1, y1))
62
63     feature_rankings_2sources = []
64     feature_rankings_2sources.append(select_combined_features(1, 2, feature_rankings))
65     feature_rankings_2sources.append(select_combined_features(0, 2, feature_rankings))
66     feature_rankings_2sources.append(select_combined_features(0, 1, feature_rankings))
67
68     return feature_rankings, feature_rankings_2sources
69
70 feature_rankings, feature_rankings_2sources = calculate_prior_rankings(df_samples_norm)

```

## Output

```

p 262 50
p 362 50
p 513 50

```

### 1.3.4 Main process

#### Script 1.3.4 (python)

```

1 def ps_l2_arom_feature_ranking(X, Y, C=1, b=None, threshold=1e-10):
2     """
3     # X is numpy array witht the data (rows are data instances)
4     # Y is a numpy vector with the class labels (-1 or 1)
5     # C is the regularization coefficient of the SVM
6     # b is the relevance vector
7     # threshold is the threshold value to drop features in L2AROM
8
9     # At step k = 0, initialize z = b (relevance vector)
10    # Relevance vector b:
11    #   Prior relevance of feature j encoded in b_j .
12    #   The more (a priori) relevant feature j, the higher b_j. If no information on j, b_j
13    → = 1.
14    """
15    global g_K
16    # Preserve X input
17    final_X = X.copy()
18    # Initialice w_k = (1,...,1)
19    # At step k = 0, initialize z = (1, ..., 1) /b
20    z = b.copy()
21    w_new = b.copy()
22    # Number of attributes
23    length = z.shape[0]

```

```

24     # Array that stores the elimination order, being the higher number the first attribute
25     # that is eliminated and 0 the last one
26     elimination_order = np.zeros(length, dtype = int)
27     original_feature_indices = np.arange(0, length, dtype = int)
28     clf = SVC(kernel = "linear", C = C, random_state = g_k + RANDOM_STATE)
29     iter_without_dropping = 0
30     n_removed_features = 0
31
32     # Iterate until convergence
33     while iter_without_dropping < 20 and length > 10:
34         clf.fit(final_X * np.outer(np.ones(X.shape[ 0 ]), w_new), Y)
35         # w = coef_ is the solution so z_new <- z*w*b
36         # z = np.abs(clf.coef_[0])*b # In absolute value
37         # print(clf.coef_)
38         w_new *= clf.coef_[0]*b
39         z = abs(w_new)
40         n_features_to_drop = np.sum(z < threshold)
41         if n_features_to_drop == 0:
42             iter_without_dropping += 1
43         else:
44             iter_without_dropping = 0
45             remove_order = np.argsort(z[ z < threshold ])
46             elimination_order[ original_feature_indices[ z < threshold ][ remove_order ] ] = \
47                 np.arange(0, n_features_to_drop) + n_removed_features + 1
48             n_removed_features += n_features_to_drop
49             length -= n_features_to_drop
50             # Delete from X, z and original_features the selected attributes
51             final_X = final_X[ :, z >= threshold ]
52             original_feature_indices = original_feature_indices[ z >= threshold ]
53             b = b[ z >= threshold ]
54             w_new = w_new[ z >= threshold ]
55             z = z[ z >= threshold ]
56
57     # We remove all remaining features
58     if length > 0:
59         remove_order = np.argsort(z)
60         elimination_order[ original_feature_indices[ remove_order ] ] = \
61             np.arange(0, length) + n_removed_features + 1
62     # ranking of features for more to less significance
63     return np.argsort(-elimination_order) # So array starts at 0 (python indexing)
64
65 def linearsvc_bcr(X_train_scaled_target, y_train_target, X_test_scaled_target, y_test_target, \
66                 num_features_selected=NUM_FEATURES_SELECTED, transfer_indexes=[]):
67     """
68     Perform linear SVC
69     """
70     global g_B
71
72     # print("Shape", X_train_scaled_target.shape)
73     b = np.ones(X_train_scaled_target.shape[1])
74     b[transfer_indexes] = g_B
75     # print("Beta vector", b, X_train_scaled_target.shape[0])

```

```

76     #print("Selected features on target", num_features_selected)
77     feature_ranking = ps_l2_arom_feature_ranking(X_train_scaled_target, y_train_target, C=1,
    ↪     b=b)
78
79     if VERBOSE: print("Ranking by PS-L2-AROM", feature_ranking)
80     ranking_selected = feature_ranking[:num_features_selected]
81
82     # Perform
83     X_train_feature_reduction = X_train_scaled_target[:, ranking_selected]
84     X_test_feature_reduction = X_test_scaled_target[:, ranking_selected]
85     #print(X_train_feature_reduction)
86     #print(y_train)
87     lin_clf = LinearSVC(C=1.0, random_state=RANDOM_STATE)
88     lin_clf.fit(X_train_feature_reduction, y_train_target)
89
90     predicted = lin_clf.predict(X_test_feature_reduction)
91     if VERBOSE: print("Predicted", predicted)
92     #accuracy = metrics.accuracy_score(y_test_target, predicted)
93     bcr = metrics.balanced_accuracy_score(y_test_target, predicted)
94     if VERBOSE: print("Accuracy", accuracy)
95     return bcr, ranking_selected
96
97 def linearsvc_bcr_none(X_train_scaled_target, y_train_target, X_test_scaled_target,
    ↪ y_test_target, \
98                        num_features_selected=NUM_FEATURES_SELECTED, transfer_indexes=[]):
99     """
100     Perform linear SVC for none transfer
101     """
102     ranking_selected = transfer_indexes[:num_features_selected]
103     #print("@Selected features on target(none)", len(transfer_indexes),
    ↪     len(ranking_selected))
104
105     # Perform
106     X_train_feature_reduction = X_train_scaled_target[:, ranking_selected]
107     X_test_feature_reduction = X_test_scaled_target[:, ranking_selected]
108     #print(X_train_feature_reduction)
109     #print(y_train)
110     lin_clf = LinearSVC(C=1.0, random_state=RANDOM_STATE)
111     lin_clf.fit(X_train_feature_reduction, y_train_target)
112
113     predicted = lin_clf.predict(X_test_feature_reduction)
114     if VERBOSE: print("Predicted", predicted)
115     #accuracy = metrics.accuracy_score(y_test_target, predicted)
116     bcr = metrics.balanced_accuracy_score(y_test_target, predicted)
117     if VERBOSE: print("Accuracy", accuracy)
118     return bcr, ranking_selected
119
120 def compute_transfer(X_train_scaled_target, X_test_scaled_target, y_train_target,
    ↪ y_test_target, \
121                    idx_source, num_features_selected):
122     """
123     Main method for compute or the transfer strategies

```

```

124     """
125     if idx_source == NO_TRANSFER_IDX: #no transfer
126         indexes = []
127     elif idx_source == RANDOM_IDX:
128         indexes = np.arange(X_train_scaled_target.shape[1])
129         np.random.shuffle(indexes)
130         indexes = indexes[:NUM_FEATURES_SOURCE]
131     elif idx_source == NONE_IDX:
132         indexes = np.arange(X_train_scaled_target.shape[1])
133         np.random.shuffle(indexes)
134         indexes = indexes
135     elif idx_source >= DUAL_TRANSFER_IDX:
136         indexes = feature_rankings_2sources[idx_source -
137             ↪ DUAL_TRANSFER_IDX][:NUM_FEATURES_SOURCE]
138     else:
139         indexes = feature_rankings[idx_source][:NUM_FEATURES_SOURCE]
140         if VERBOSE: print("Indexes from source", y_train_target.shape[0], len(indexes))
141
142     if idx_source == NONE_IDX:
143         bcr, ranking_selected = linearsvc_bcr_none(X_train_scaled_target, y_train_target,
144             ↪ X_test_scaled_target, y_test_target, \
145                 num_features_selected, transfer_indexes=indexes)
146     else:
147         bcr, ranking_selected = linearsvc_bcr(X_train_scaled_target, y_train_target,
148             ↪ X_test_scaled_target, y_test_target, \
149                 num_features_selected, transfer_indexes=indexes)
150
151     return bcr, ranking_selected
152
153 def get_target_data_sets(df_samples_norm, idx_target):
154     """
155     """
156     X_train_target, X_test_target, y_train_target, y_test_target =
157         ↪ split_data(df_samples_norm[idx_target])
158     #features =
159     ↪ df_samples_norm[idx_target].columns[SELECT_FEATURES_INI:SELECT_FEATURES_FIN].values
160     scaler_target = StandardScaler(with_mean=False, with_std=False)
161     scaler_target.fit(X_train_target)
162     X_train_scaled_target = scaler_target.transform(X_train_target)
163     X_test_scaled_target = scaler_target.transform(X_test_target)
164     return X_train_scaled_target, X_test_scaled_target, y_train_target, y_test_target
165
166 print("Num features to feed from sources", NUM_FEATURES_SOURCE )
167
168 feature_rankings, feature_rankings_2sources = calculate_prior_rankings(df_samples_norm)
169
170 FILTER_SOURCES = [0,1,2,3,4,8]
171 FILTER_TARGETS = [0,1,2]
172 features_to_select = np.unique(np.logspace(1, 12.5, num=20, endpoint=True, base=2.0,
173     ↪ dtype=int))
174 #features_to_select = [2,4,16,64,256,1024,4096]
175 bcr_list = []

```

```

170 for g_k in range(0, 200):
171     for idx_target in FILTER_TARGETS:
172         #print("TARGET", SAMPLE_NAMES[idx_target])
173         X_train_scaled_target, X_test_scaled_target, y_train_target, y_test_target = \
174         get_target_data_sets(df_samples_norm, idx_target)
175         for idx_source in [0,1,2,3,4, DUAL_TRANSFER_IDX + idx_target, 8]:
176             #if idx_source in FILTER_SOURCES and idx_source!= idx_target:
177             if idx_source!= idx_target:
178                 print("k", g_k, "TARGET", SAMPLE_NAMES[idx_target], "SOURCE",
179                     ↪ SAMPLE_NAMES[idx_source])
180                 for features_selected in features_to_select:
181                     #print("Features", features_selected)
182                     bcr, ranking_selected = compute_transfer(X_train_scaled_target,
183                     ↪ X_test_scaled_target, y_train_target, y_test_target, \
184                     ↪ idx_source=idx_source,
185                     ↪ num_features_selected=features_selected)
186                     bcr_list.append([SAMPLE_NAMES[idx_target], SAMPLE_NAMES[idx_source], \
187                     ↪ features_selected, bcr, ranking_selected])
188                 if VERBOSE: print("Target", idx_target, "Source", idx_source,
189                 ↪ "#Features", \
190                     ↪ features_selected, "BCR", bcr)
191
192 df_bcr = pd.DataFrame(bcr_list, columns=['target', 'source', 'num features', 'BCR', 'S'])
193 df_bcr.head()

```

### 1.3.5 Plot BCR

#### Script 1.3.5 (python)

```

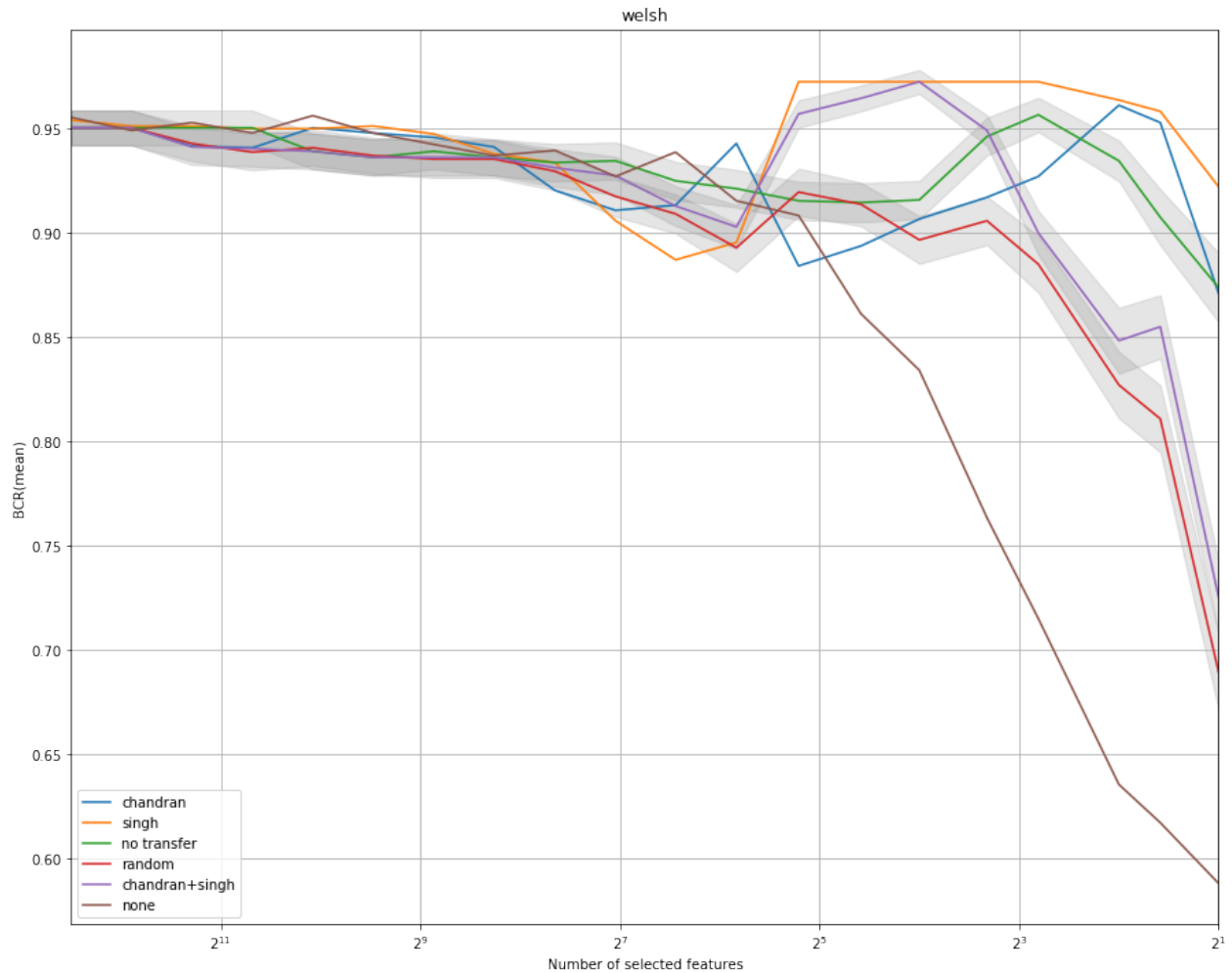
1 import matplotlib.pyplot as plt
2 %matplotlib inline
3
4 idx_target = 0
5 df_bcr_mean = pd.DataFrame(df_bcr.groupby(['target', 'source', 'num
6     ↪ features'])['BCR'].mean()).reset_index()
7 df_bcr_sem = pd.DataFrame(df_bcr.groupby(['target', 'source', 'num
8     ↪ features'])['BCR'].sem()).reset_index()
9 for idx_target in [2,0,1]:
10     target = SAMPLE_NAMES[idx_target]
11     df_target = df_bcr_mean.loc[df_bcr_mean['target'] == target]
12     df_target_sem = df_bcr_sem.loc[df_bcr_sem['target'] == target]
13     plt.figure(figsize=(15,12))
14     plt.xscale('log', basex=2)
15     for idx_source in [0,1,2,3,4, DUAL_TRANSFER_IDX + idx_target, 8]:
16         #if idx_source in FILTER_SOURCES and idx_source!= idx_target:
17         if idx_source!= idx_target:
18             label = SAMPLE_NAMES[idx_source]
19             df_source = df_target[df_target['source'] == label]
20             plt.xlim(max(df_source['num features']), min(df_source['num features']))
21             plt.plot(df_source['num features'], df_source['BCR'], label=label)
22     # Plot sem interval

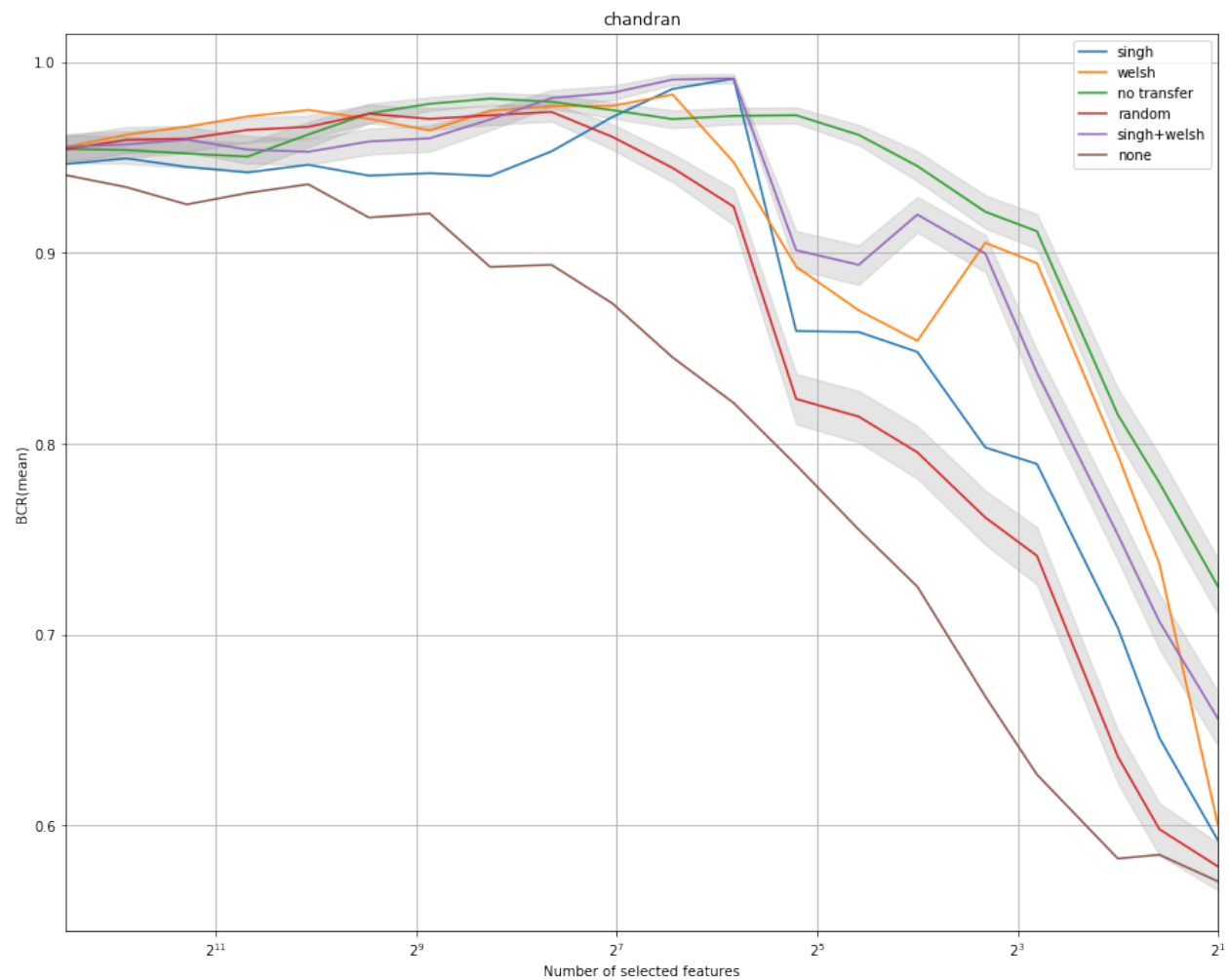
```

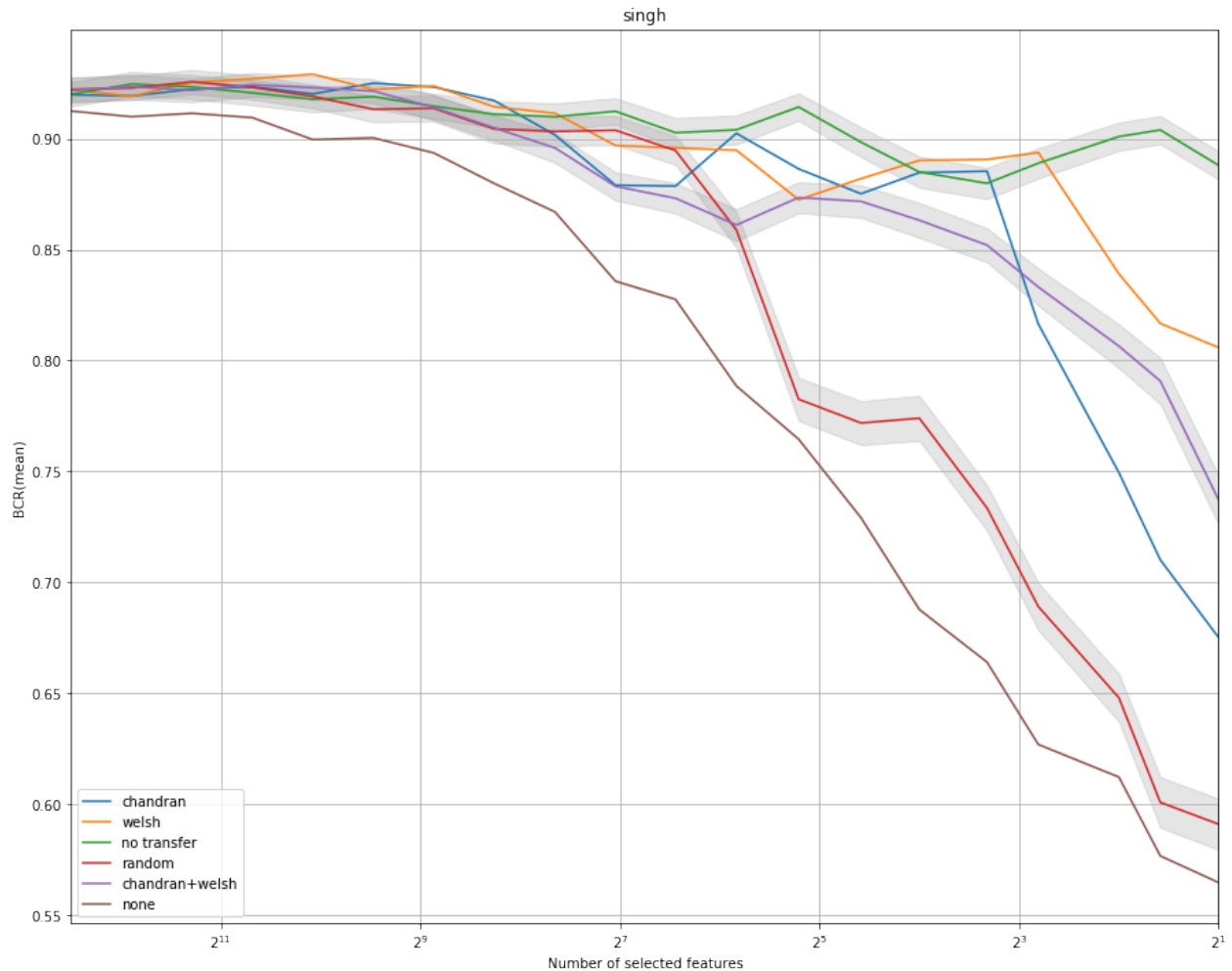
```

21     if idx_source in [DUAL_TRANSFER_IDX + idx_target, 3, RANDOM_IDX]:
22         df_source_sem = df_target_sem[df_target_sem['source'] == label]
23         plt.fill_between(df_source['num features'], df_source['BCR'] -
24             ↪ df_source_sem['BCR'],
25                         df_source['BCR'] + df_source_sem['BCR'], color='gray', alpha=0.)
26
27 2)
28 plt.title(target)
29 plt.xlabel("Number of selected features")
30 #plt.xlim(100,400)
31 #plt.xticks(df_source['num features'])
32 plt.ylabel("BCR(mean)")
33 plt.legend(loc = "best")
34 plt.grid()
35 plt.show()

```







### 1.3.6 Plot BCR (standard error)

Standard error is relatively high and could weaken in a high amount the conclusions of this statistical experiment. It's necessary to increase the iteration number to see if we can reduce this metric.

#### Script 1.3.6 (python)

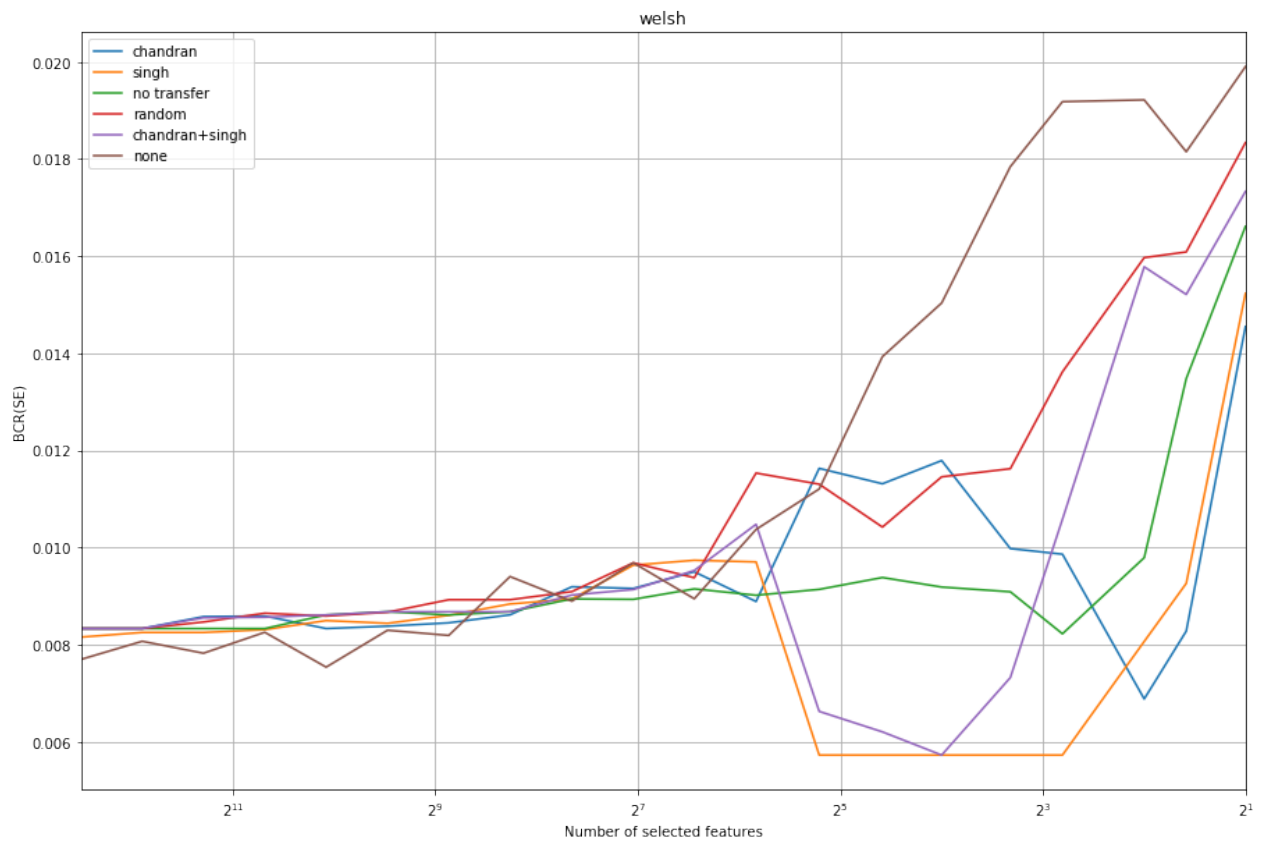
```
1 idx_target = 0
2 df_bcr_sem = pd.DataFrame(df_bcr.groupby(['target', 'source', 'num
   ↳ features'])['BCR'].sem()).reset_index()
3 for idx_target in [2,0,1]:
4     target = SAMPLE_NAMES[idx_target]
5     df_target = df_bcr_sem.loc[df_bcr_sem['target'] == target]
6     plt.figure(figsize=(15,10))
7     plt.xscale('log', base=2)
8     for idx_source in [0,1,2,3,4, DUAL_TRANSFER_IDX + idx_target, 8]:
9         #if idx_source in FILTER_SOURCES and idx_source!= idx_target:
```

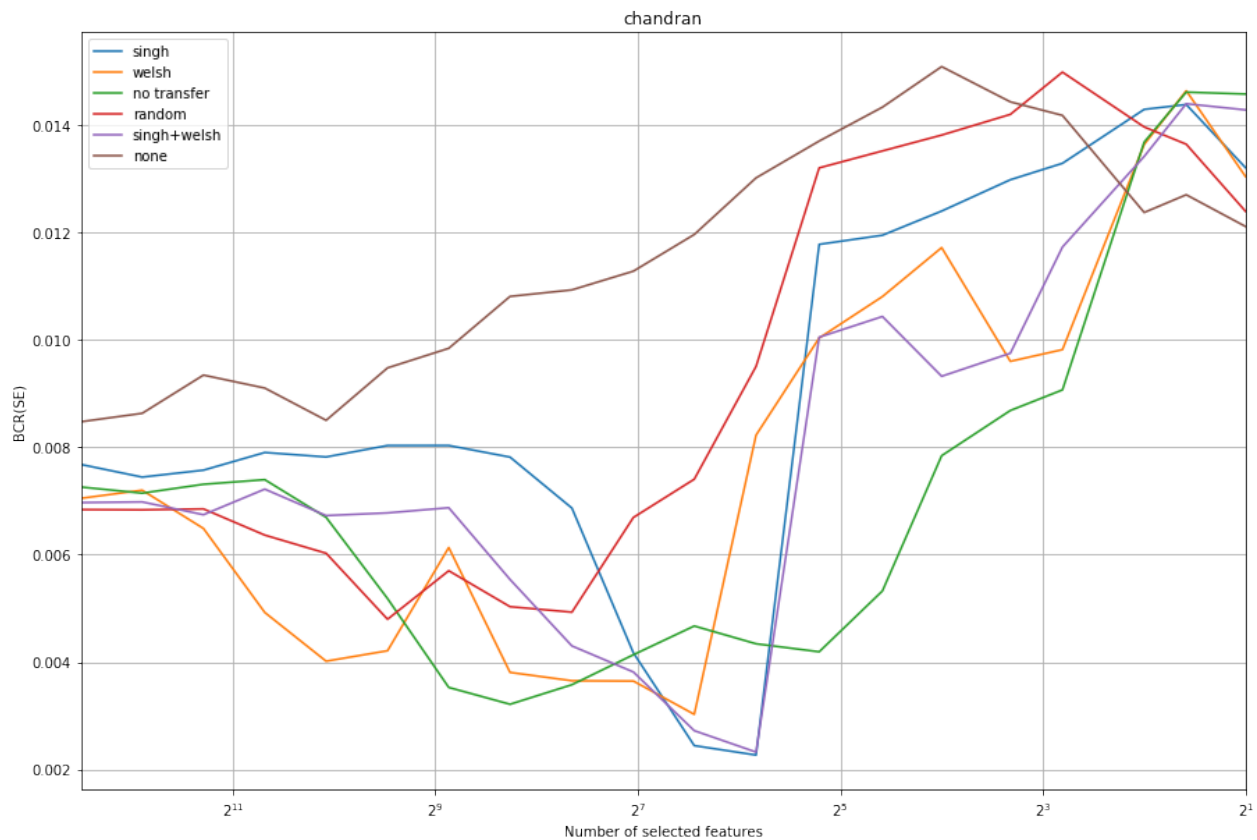


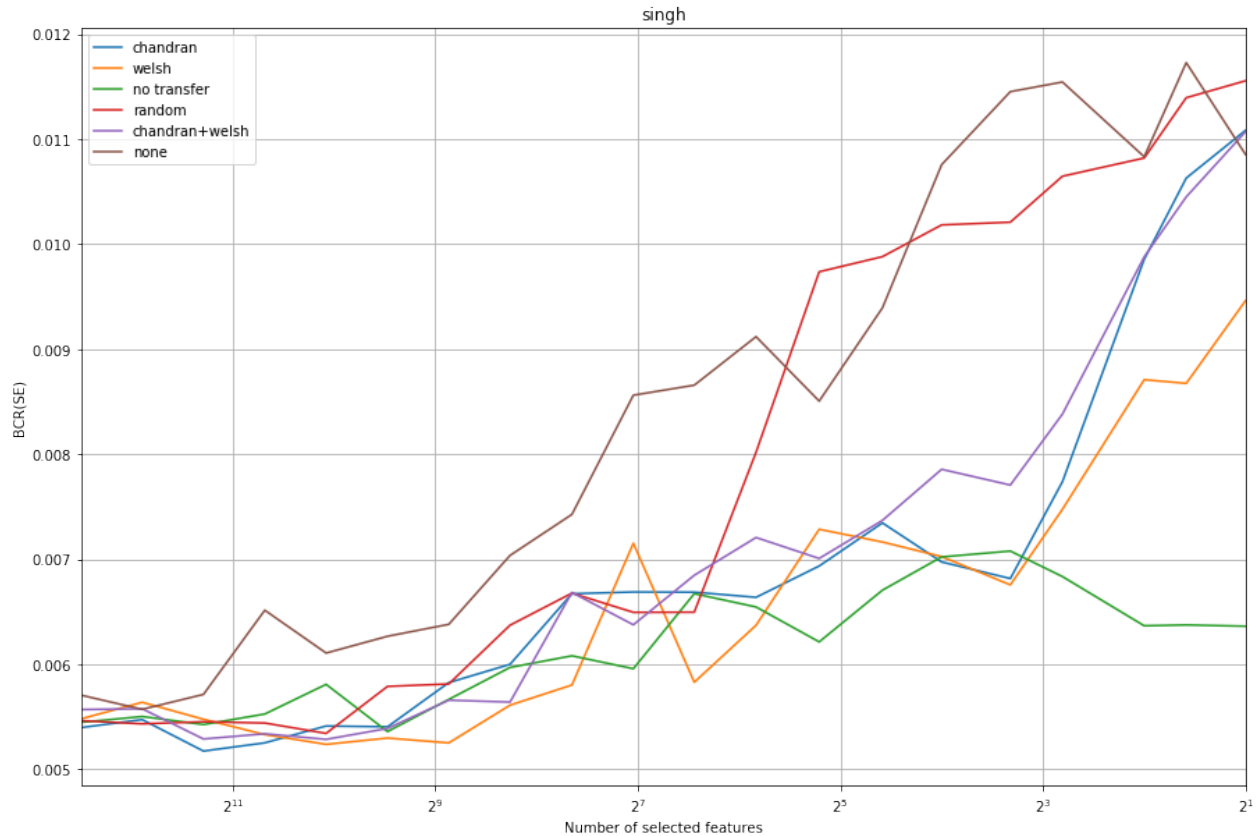
```

10     if idx_source != idx_target:
11         label = SAMPLE_NAMES[idx_source]
12         df_source = df_target[df_target['source'] == label]
13         plt.xlim(max(df_source['num features']), min(df_source['num features']))
14         plt.plot(df_source['num features'], df_source['BCR'], label=label)
15
16     plt.title(target)
17     plt.xlabel("Number of selected features")
18     #plt.xlim(100,400)
19     #plt.xticks(df_source['num features'])
20     plt.ylabel("BCR(SE)")
21     plt.legend(loc = "best")
22     plt.grid()
23     plt.show()

```







### 1.3.7 Calculate stability

Script 1.3.7 (python)

```

1  stability = []
2  for idx_target in FILTER_TARGETS:
3      target = SAMPLE_NAMES[idx_target]
4      df_target = df_bcr.loc[df_bcr['target'] == target]
5      for idx_source in [0,1,2,3,4, DUAL_TRANSFER_IDX + idx_target, 8]:
6          if idx_source != idx_target:
7              source = SAMPLE_NAMES[idx_source]
8              df_source = df_target[df_target['source'] == source]
9              n_features = np.unique(df_source['num features'])
10             #print(n_features)
11             for num_features in n_features:
12                 df_num_features = df_source[df_source['num features'] == num_features]
13                 # Calculate stability
14                 s = num_features
15                 s2 = s**2
16                 n = 12600
17                 s2_n = s2/n
18                 den = s - s2_n

```

```

19     list_S = list(df_num_features['S'])
20     stab = 0
21     count = 0
22     k = len(list_S)
23     for i in range(k):
24         for j in range(i+1, k):
25             Si_Sj = np.intersect1d(list_S[i], list_S[j])
26             stab += (len(Si_Sj) - s2_n) / den
27             count += 1
28     stability.append([target, source, num_features, stab/count])
29     #print(1/count, 2/(k*(k-1)), stability[-1], 2*stab/(k*(k-1)))
30
31 df_stab = pd.DataFrame(stability, columns=['target', 'source', 'num features', 'stability'])
32 df_stab.head()

```

### Display output

	target	source	num features	stability
0	chandran	singh	2	0.334769
1	chandran	singh	3	0.369247
2	chandran	singh	4	0.456360
3	chandran	singh	7	0.590038
4	chandran	singh	10	0.726602

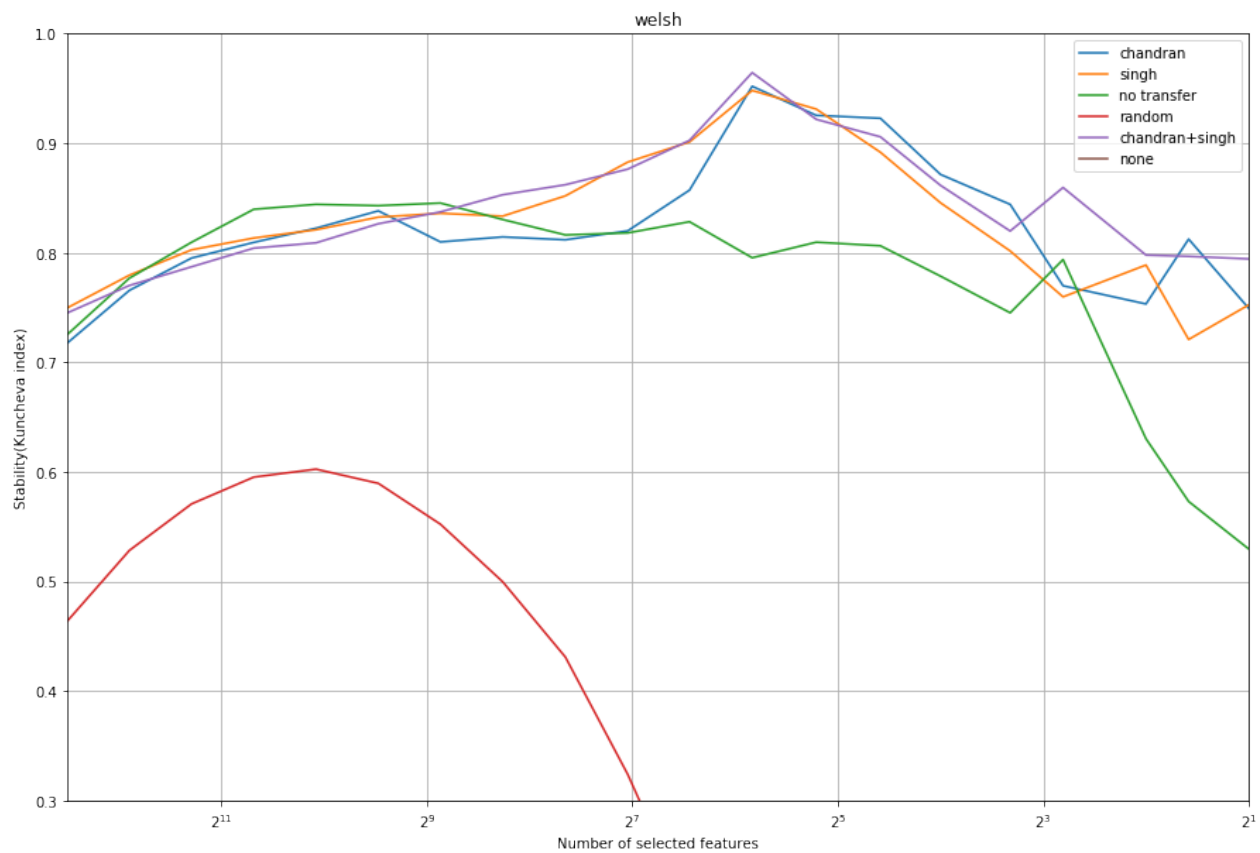
### 1.3.8 Plot stability

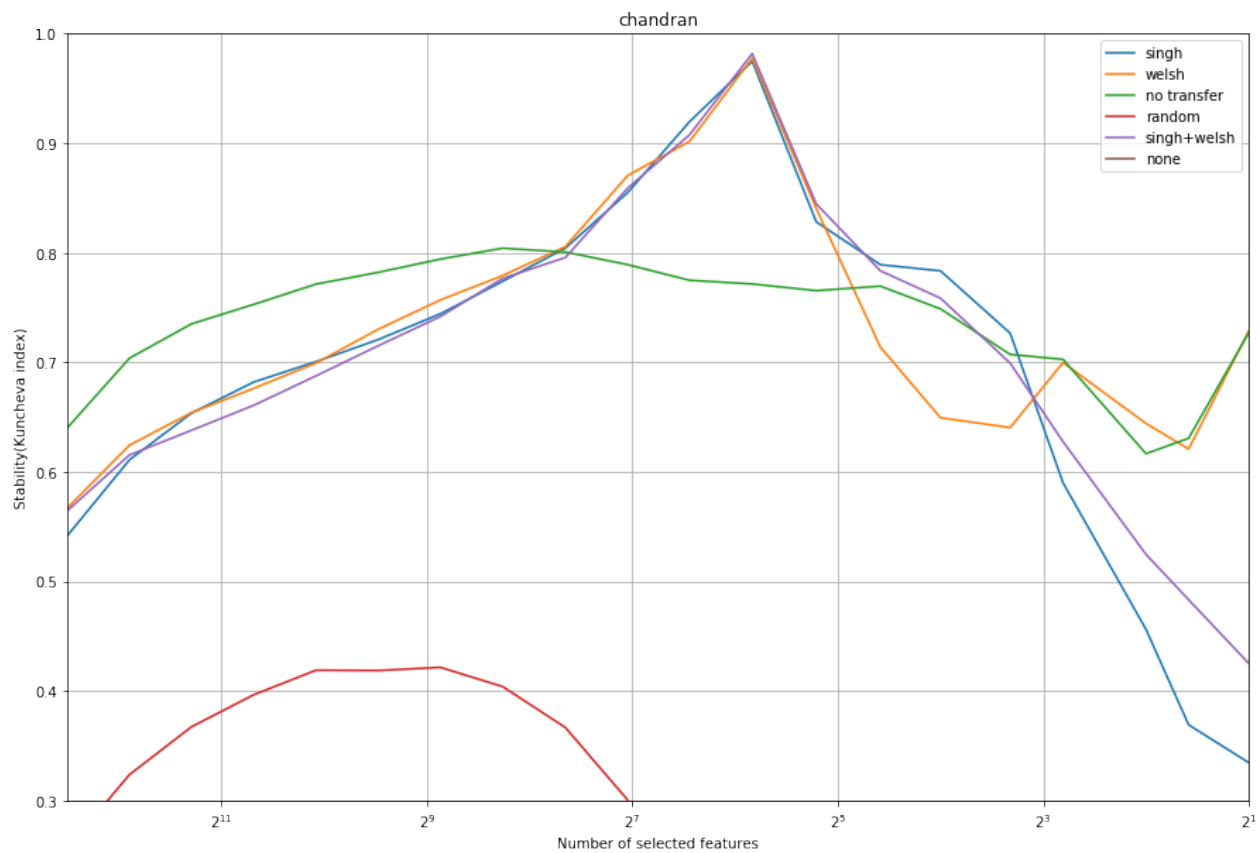
#### Script 1.3.8 (python)

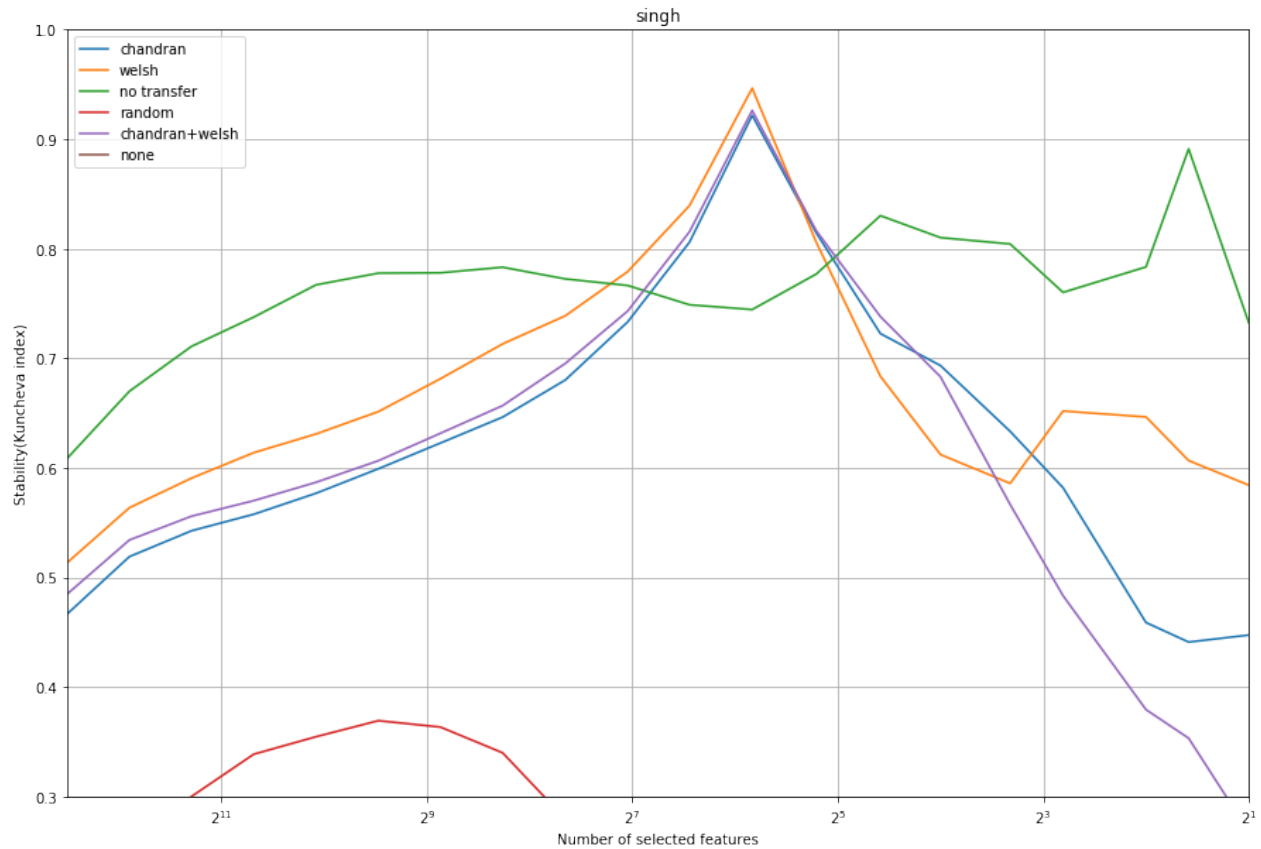
```

1  idx_target = 0
2  for idx_target in [2,0,1]:
3      target = SAMPLE_NAMES[idx_target]
4      df_target = df_stab.loc[df_stab['target'] == target]
5      plt.figure(figsize=(15,10))
6      plt.xscale('log', basex=2)
7      for idx_source in [0,1,2,3,4, DUAL_TRANSFER_IDX + idx_target, 8]:
8          #if idx_source in FILTER_SOURCES and idx_source!= idx_target:
9          if idx_source!= idx_target:
10             label = SAMPLE_NAMES[idx_source]
11             df_source = df_target[df_target['source'] == label]
12             plt.xlim(max(df_source['num features']), min(df_source['num features']))
13             plt.plot(df_source['num features'], df_source['stability'], label=label)
14
15     plt.title(target)
16     plt.xlabel("Number of selected features")
17     plt.ylim(0.3, 1)
18     #plt.xticks(df_source['num features'])
19     plt.ylabel("Stability(Kuncheva index)")
20     plt.legend(loc = "best")
21     plt.grid()
22     plt.show()

```







### 1.3.9 Impact of B

#### BCR

##### Script 1.3.9 (python)

```

1 FILTER_TARGETS = [2] #welsh
2 #features_to_select = np.unique(np.logspace(2, 12.5, num=50, endpoint=True, base=2.0,
  ↳ dtype=int))
3 bcr_list = []
4 B_values = [1,2,5,10,100,1000]
5 for g_B in B_values:
6     for g_k in range(0,200):
7         for idx_target in FILTER_TARGETS:
8             #print("TARGET", SAMPLE_NAMES[idx_target])
9             X_train_scaled_target, X_test_scaled_target, y_train_target, y_test_target = \
10             get_target_data_sets(df_samples_norm, idx_target)
11             for idx_source in [DUAL_TRANSFER_IDX + idx_target]:
12                 print("k", g_k, "TARGET", SAMPLE_NAMES[idx_target], "SOURCE",
  ↳ SAMPLE_NAMES[idx_source])
13             for features_selected in features_to_select:
14                 #print("Features", features_selected)

```

```

15         bcr, ranking_selected = compute_transfer(X_train_scaled_target,
16           ↪ X_test_scaled_target, y_train_target, y_test_target,\
17             idx_source=idx_source,
18             ↪ num_features_selected=features_selected)
19         bcr_list.append([g_B, features_selected, bcr, ranking_selected])
20         if VERBOSE: print("Target", idx_target, "Source", idx_source,
21           ↪ "#Features",\
22             features_selected, "BCR", bcr)
23
24 df_bcr_B = pd.DataFrame(bcr_list, columns=['B', 'num features', 'BCR', 'S'])
25 df_bcr_B.head()

```

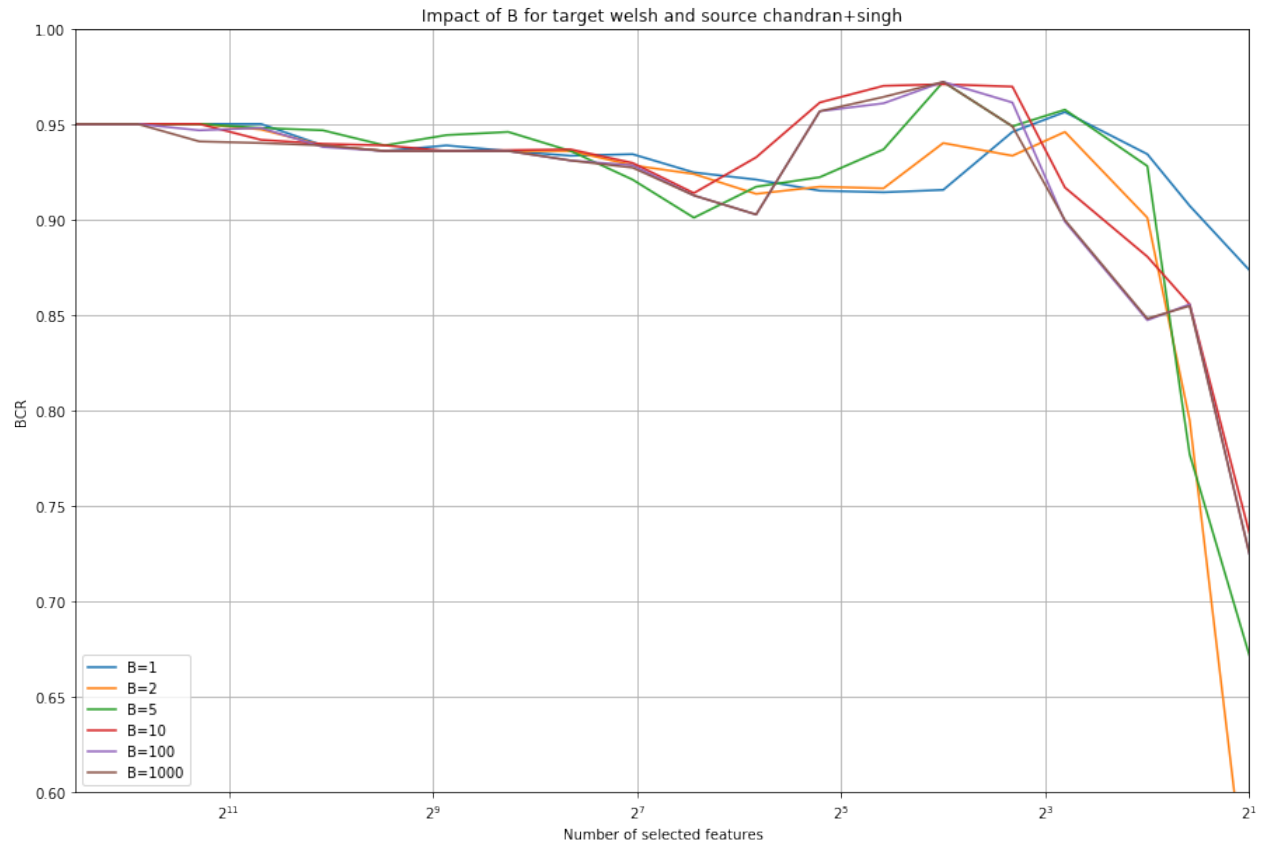
### Script 1.3.10 (python)

```

1  idx_target = 2
2  df_bcr_mean = pd.DataFrame(df_bcr_B.groupby(['B', 'num
   ↪ features'])['BCR'].mean()).reset_index()
3
4  target = SAMPLE_NAMES[2]
5  source = SAMPLE_NAMES[DUAL_TRANSFER_IDX + idx_target]
6  plt.figure(figsize=(15,10))
7  plt.xscale('log', basex=2)
8  for idx_B in B_values:
9      df_B = df_bcr_mean.loc[df_bcr_mean['B'] == idx_B]
10     plt.xlim(max(df_B['num features']), min(df_B['num features']))
11     plt.plot(df_B['num features'], df_B['BCR'], label='B=' + str(idx_B))
12 plt.title("Impact of B for target " + target + " and source " + source)
13 plt.xlabel("Number of selected features")
14 #plt.xlim(100,400)
15 #plt.xticks(df_source['num features'])
16 plt.ylim(0.6, 1.0)
17 plt.ylabel("BCR")
18 plt.legend(loc = "best")
19 plt.grid()
20 plt.show()

```





## Stability

Script 1.3.11 (python)

```

1  stability = []
2  for idx_B in B_values:
3      df_B = df_bcr_B.loc[df_bcr_B['B'] == idx_B]
4      n_features = np.unique(df_bcr['num features'])
5      #print(n_features)
6      for num_features in n_features:
7          df_num_features = df_B[df_B['num features'] == num_features]
8          # Calculate stability
9          s = num_features
10         s2 = s**2
11         n = 12600
12         s2_n = s2/n
13         den = s - s2_n
14         list_S = list(df_num_features['S'])
15         stab = 0
16         count = 0
17         k = len(list_S)
18         for i in range(k):

```

```

19         for j in range(i+1, k):
20             Si_Sj = np.intersect1d(list_S[i], list_S[j])
21             stab += (len(Si_Sj) - s2_n) / den
22             count += 1
23         stability.append([idx_B, num_features, stab/count])
24         #print(1/count, 2/(k*(k-1)), stability[-1], 2*stab/(k*(k-1)))
25
26 df_stab_B = pd.DataFrame(stability, columns=['B', 'num features', 'stability'])
27 df_stab_B.head()

```

### Display output

	B	num features	stability
0	1	2	0.529699
1	1	3	0.573081
2	1	4	0.630297
3	1	7	0.793791
4	1	10	0.745220

### Script 1.3.12 (python)

```

1 target = SAMPLE_NAMES[idx_target]
2 source = SAMPLE_NAMES[DUAL_TRANSFER_IDX + idx_target]
3 plt.figure(figsize=(15,10))
4 plt.xscale('log', basex=2)
5 for idx_B in B_values:
6     df_B = df_stab_B.loc[df_stab_B['B'] == idx_B]
7     plt.xlim(max(df_B['num features']), min(df_B['num features']))
8     plt.plot(df_B['num features'], df_B['stability'], label='B=' + str(idx_B))
9 plt.title("Impact of B for target " + target + " and source " + source)
10 plt.xlabel("Number of selected features")
11 #plt.xlim(100,400)
12 #plt.xticks(df_source['num features'])
13 plt.ylabel("Stability (Kuncheva index)")
14 plt.legend(loc = "best")
15 plt.grid()
16 plt.show()

```

