

3. Find the Kth Smallest Sum of a Matrix With Sorted Rows

You are given an $m \times n$ matrix `mat` that has its rows sorted in non-decreasing order and an integer `k`.

You are allowed to choose exactly one element from each row to form an array.

Return the `k`th smallest array sum among all possible arrays.

Code:

```
import heapq

def kthSmallest(mat,k):
    m,n=len(mat),len(mat[0])
    min_heap=[]
    initial_tuple=(sum(row[0] for row in mat), [0] * m)
    heapq.heappush(min_heap, initial_tuple)
    visited=set()
    visited.add(tuple([0]*m))
    for _ in range(k-1):
        current_sum,indices=heapq.heappop(min_heap)
        for i in range(m):
            if indices[i]+1<n:
                new_indices=indices[:]
                new_indices[i]+= 1
                new_sum=current_sum-mat[i][indices[i]]+mat[i][new_indices[i]]
                new_tuple=(new_sum, new_indices)
                if tuple(new_indices) not in visited:
                    heapq.heappush(min_heap,new_tuple)
                    visited.add(tuple(new_indices))
    return heapq.heappop(min_heap)[0]

mat=[[1, 3, 11],
     [2, 4, 6]]
k=5
print(kthSmallest(mat,k))
mat=[[1, 3, 11],
     [2, 4, 6],
```

[5, 6, 7]]

k=6

print(kthSmallest(mat,k))

output:

```
PS C:\Users\karth>
PS C:\Users\karth> & c:/Users/karth/AppData/Local/Programs/Python/Python312/python.exe c:/Users/karth/OneDrive/Desktop/daa.py
7
11
PS C:\Users\karth> █
```

Time complexity:

$F(n) = O(km \log n)$