

1. 143. You are given a cost matrix where each element `cost[i][j]` represents the cost of assigning worker `i` to task `j`. Develop a program that utilizes exhaustive search to solve the assignment problem. The program should Define a function `total_cost(assignment, cost_matrix)` that takes an assignment (list representing worker-task pairings) and the cost matrix as input. It iterates through the assignment and calculates the total cost by summing the corresponding costs from the cost matrix Implement a function `assignment_problem(cost_matrix)` that takes the cost matrix as input and performs the following Generate all possible permutations of worker indices (excluding repetitions).

**Test Cases:**

**Input**

1. **Simple Case:** Cost Matrix:

```
[[3, 10, 7],  
 [8, 5, 12],  
 [4, 6, 9]]
```

Code:

```
def total_cost(assignment, cost_matrix):  
    total = 0  
    for worker, task in enumerate(assignment):  
        total += cost_matrix[worker][task]  
    return total  
  
from itertools import permutations  
  
def assignment_problem(cost_matrix):  
    num_workers = len(cost_matrix)  
    all_permutations = permutations(range(num_workers))  
  
    min_cost = float('inf')  
    best_assignment = None  
  
    for perm in all_permutations:  
        current_cost = total_cost(perm, cost_matrix)  
        if current_cost < min_cost:  
            min_cost = current_cost  
            best_assignment = perm  
  
    return best_assignment, min_cost  
  
# Example input  
cost_matrix = [  
    [3, 10, 7],  
    [8, 5, 12],  
    [4, 6, 9]  
]  
  
# Solve the assignment problem  
best_assignment, min_cost = assignment_problem(cost_matrix)  
print("Best Assignment:", best_assignment)  
print("Minimum Cost:", min_cost)
```

output:

```
PS C:\Users\karth>
PS C:\Users\karth> & c:/Users/karth/AppData/Local/Programs/Python/Python312/python.exe c:/Users/karth/OneDrive/Documents/OriginLab/problems.py
Best Assignment: (2, 1, 0)
Minimum Cost: 16
PS C:\Users\karth> □
```

Time complexity: $f(n)=O(n\log n)$