

First-principles Studies of Strongly-Correlated States in Spin Defects in Diamond

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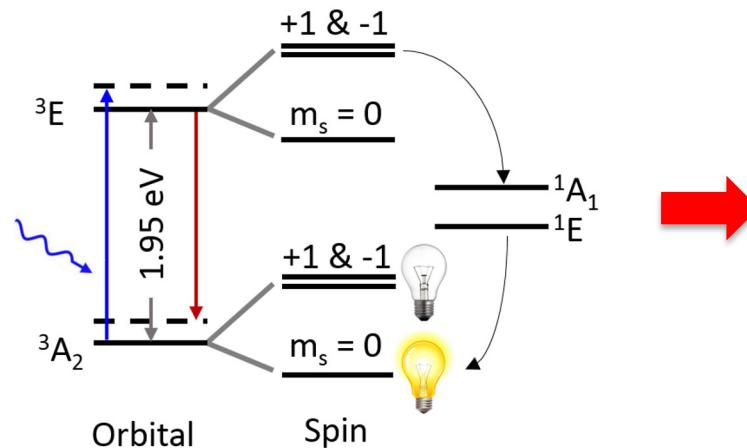
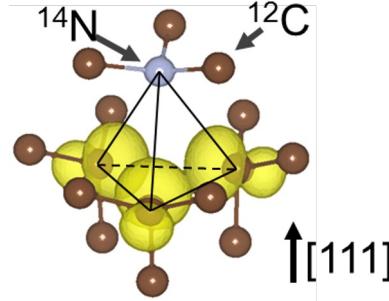
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- Strongly-correlated states in spin defects
- Quantum embedding theory
- Quantum embedding theory applied to spin defects

Strongly-correlated states in spin defects used as qubits



Example: 2 electrons in 2 degenerate orbitals

Spin singlet state:
 $S = 0$

$$\frac{1}{\sqrt{2}} \left(\begin{array}{c} \uparrow \\ \downarrow \end{array} - \begin{array}{c} \downarrow \\ \uparrow \end{array} \right)$$

Spin triplet states:
 $S = 1$

$$\frac{1}{\sqrt{3}} \left(\begin{array}{c} \uparrow \\ \uparrow \\ \downarrow \end{array} + \begin{array}{c} \uparrow \\ \downarrow \\ \uparrow \end{array} + \begin{array}{c} \downarrow \\ \uparrow \\ \uparrow \end{array} \right)$$

Strongly-correlated states: important for the initialization and read-out of spins, yet challenging for mean-field theories such as Kohn-Sham Density Functional Theory (DFT)

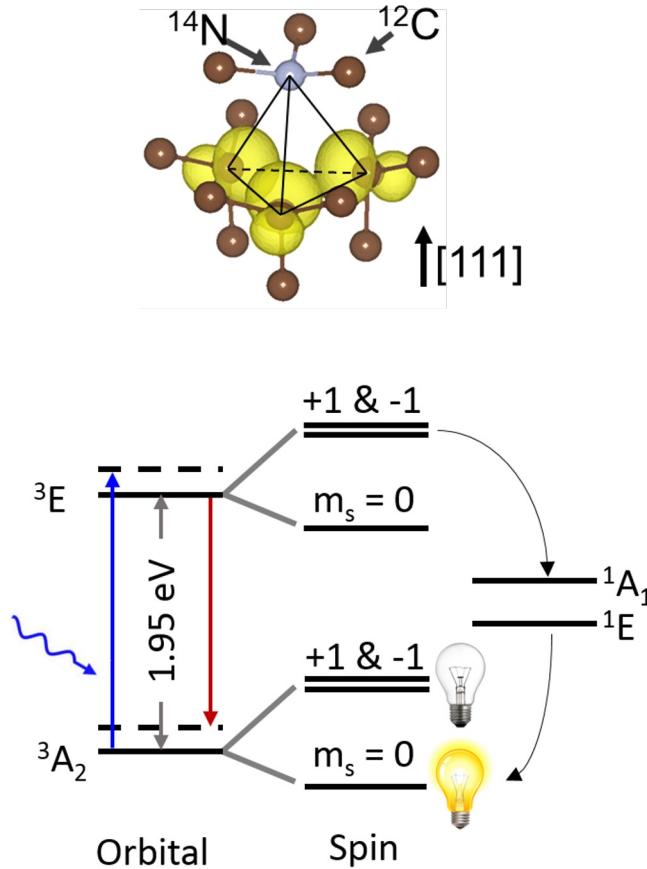
Most existing methods to describe strongly correlated states are computationally **very expensive** (limited to tens of electrons):

- Dynamical mean-field theory
- Quantum Monte-Carlo
- Multi-reference quantum chemistry methods

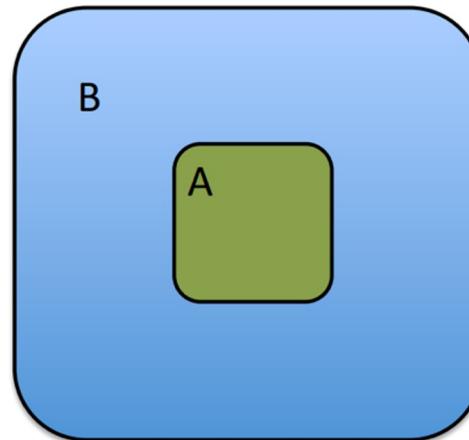
From dielectric screening to quantum embedding



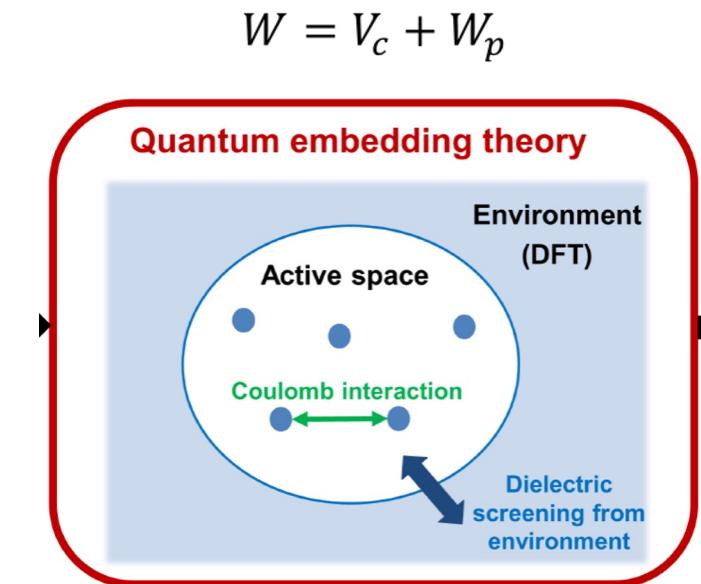
For the use of spin defects to realize qubits, electronic states should be **localized** in well defined regions of space and separated in energy from the levels of the host solid



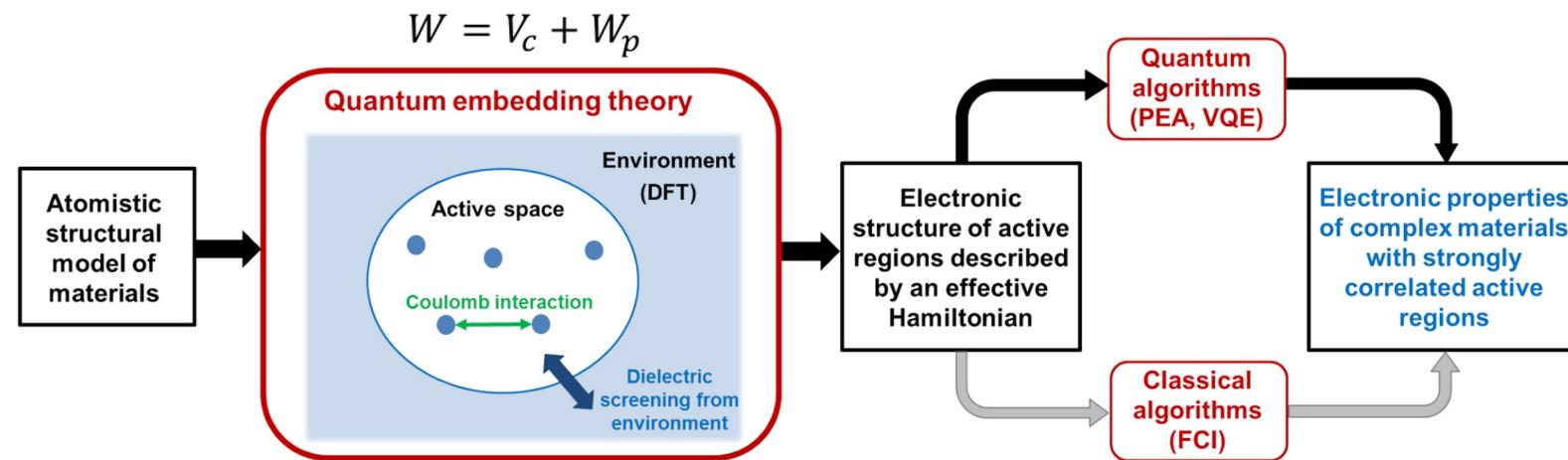
Multi-level description



A – higher level theory
B – lower level theory



Quantum embedding theory



Features of the embedding theory:

- Based on **many body perturbation theory** (the **GW** method)
- No explicit summation over **empty electronic states** ↗ scalable to large systems
- Dielectric screening is computed including **exchange-correlation effects**, thus going beyond the random phase approximation (RPA)
- The use of hybrid functions, for example, **dielectric-dependent hybrid functional (DDH)**, is straightforward and yields improved results over GGA (PBE)

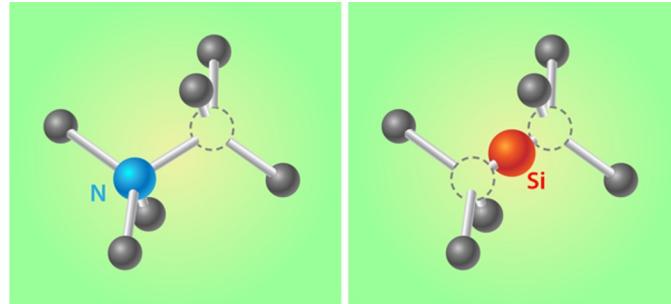
Ma, H., Govoni, M. & Galli, G. npj Comput Mater 6, 85 (2020)

Ma, H., **Sheng, N.**, Govoni, M. & Galli, G. J. Chem. Theory Comput., accepted (2021)

Quantum embedding theory applied to spin-defects

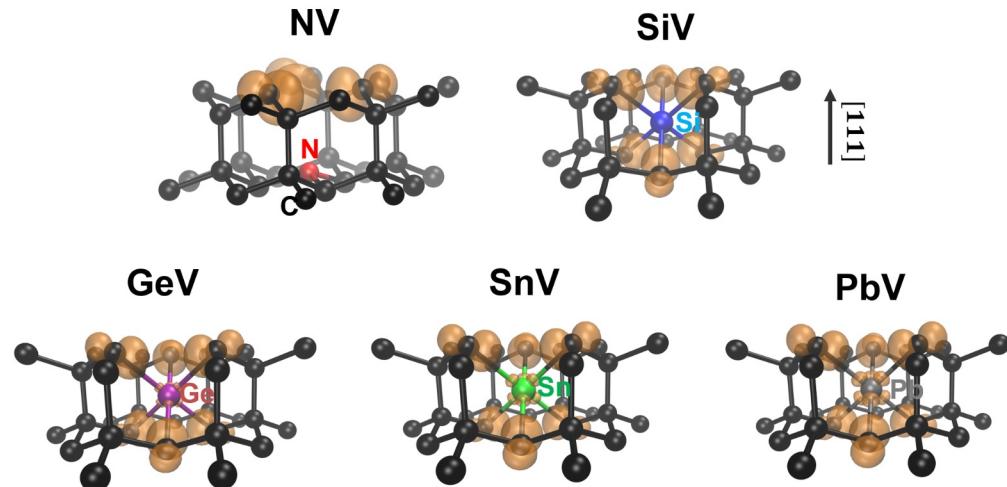


We applied the quantum embedding theory to study NV⁻ in diamond & group-IV⁰ defects in diamond. We choose active spaces to include defect levels and band edge states



Spin polarization density

$$\Delta\rho = \rho_\alpha - \rho_\beta$$



Computational setup:

- Dielectric dependent hybrid functional
- 50 Ry Ecut; ONCV PP
- 3*3*3 supercell for diamond; Γ -point sampling
- Finite-field calculation of exchange-correlation kernel



[https://quantum-
espresso.org/](https://quantum-espresso.org/)



<http://west->



<http://qboxcode.org/>

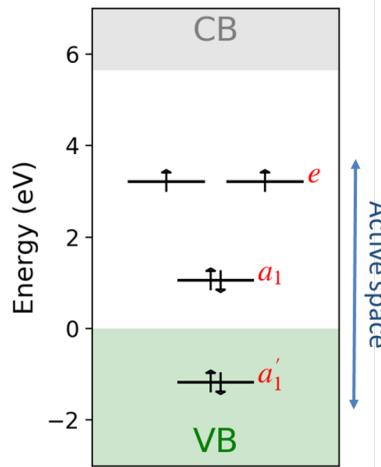


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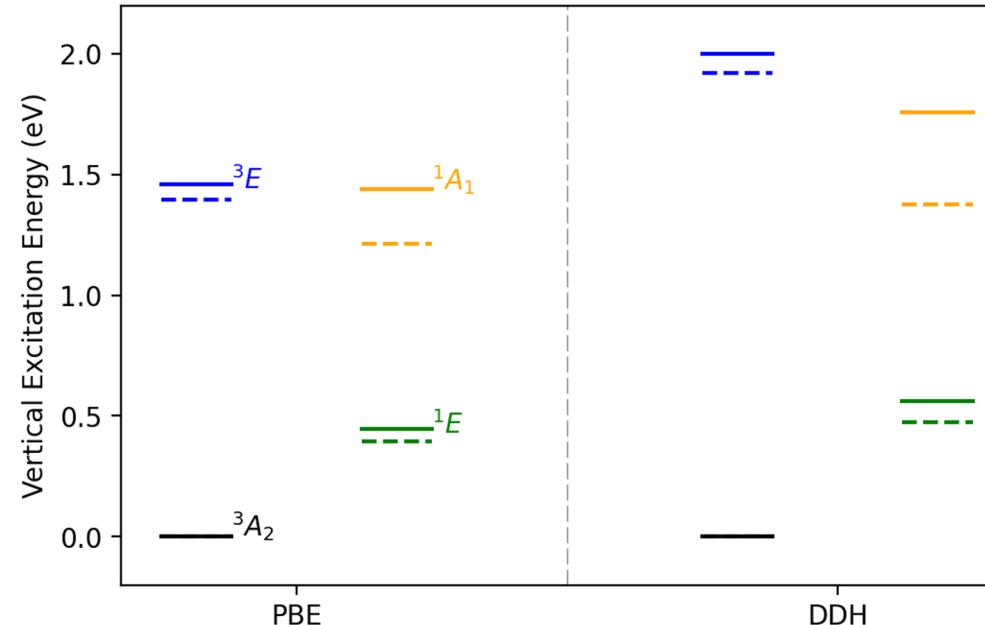
Electronic structure of NV⁻ in diamond



Single-electron levels
(DFT)



Many-electron
states
(embedding theory)



Vertical excitation energies (eV)

Excitation	RPA	Beyond -RPA	Exp.
	1.921	2.001	2.180*
	0.900	1.198	1.190**

*1.945 eV ZPL + 0.235 eV Stokes energy; **ZPL

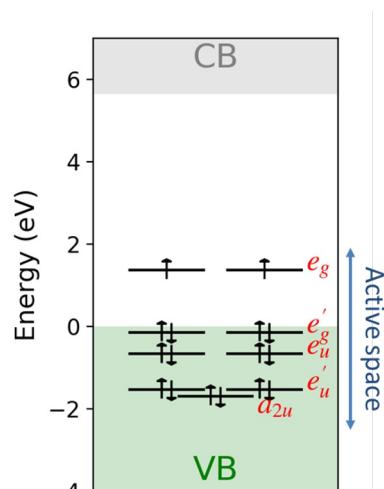
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Rogers, L. J., Armstrong, S., Sellars, M. J. & Manson, N. B. New J. Phys. 10, 103024 (2008).

- Ordering and symmetry of low-lying states are correctly reproduced
- We obtained better agreement with experiments by computing dielectric screening beyond the RPA

Electronic structure of group-IV⁰ defects in diamond

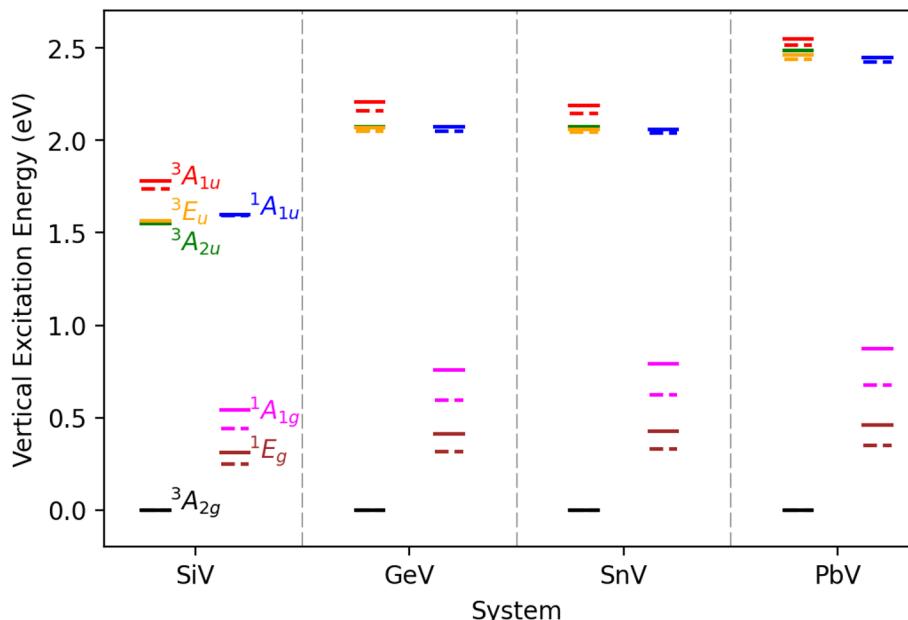


Single-electron levels
(DFT)



Many-electron
states

DDH



Vertical excitation energies of SiV⁰ (eV):

Excitation	Beyond-RPA	Exp
	1.594	1.568*
	0.011	0.007**

*1.31 eV ZPL + 0.258 eV Stokes energy

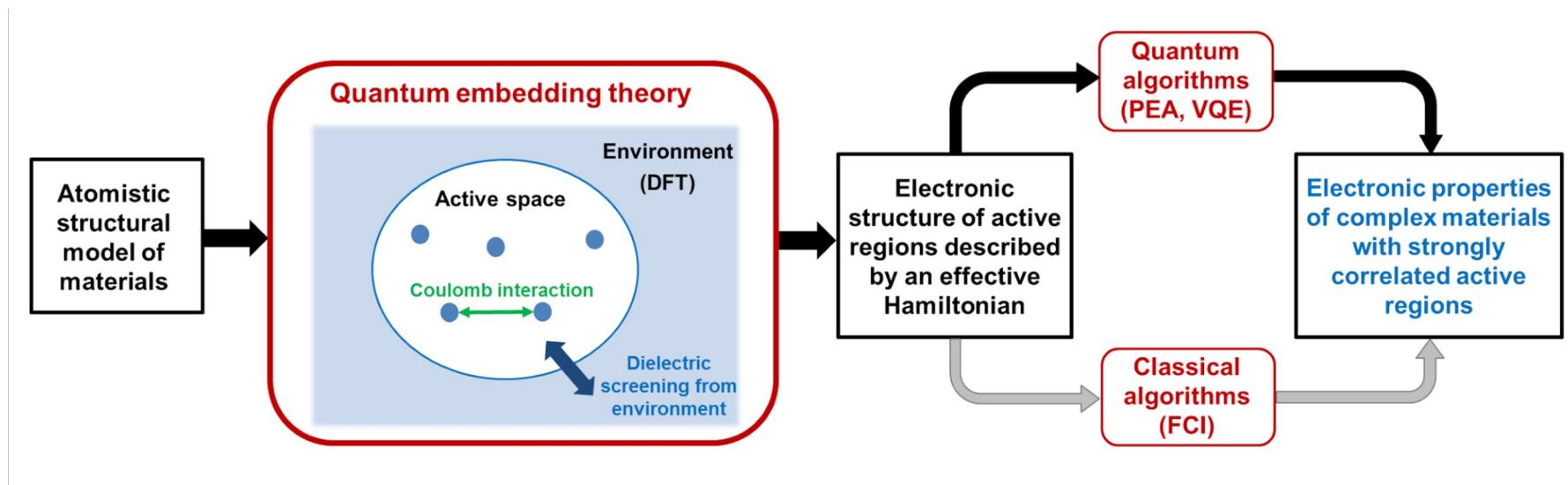
Thiering, G. & Gali, A. npj Comput. Mater. 5, 18 (2019).

** Green, B. L. et al. Phys. Rev. B 99, 161112 (2019).

- We confirmed the existence of the $^3A_{2u}/^3E_u$ manifold proposed by experimental studies
- Our results on singlet states provide a possible explanation for the experimental difficulty to perform optical spin polarization of SiV⁰
- Possible **intersystem crossing** in SnV⁰ and PbV⁰
- Spin-orbit coupling effects are negligible on defect states

Ma, H., Sheng, N., Govoni, M., & Galli, G. Phys. Chem. Chem. Phys. (2020)

Conclusions



- We used a quantum embedding theory (QET) to **investigate and predict strongly-correlated electronic states**, e.g. singlet states for spin defects in diamond. These states cannot be described with DFT. Our results may help the experimental design of qubits.
- The QET used here is scalable to large systems.
- Going **beyond the RPA** in the calculation of dielectric screening of the environment provides results more accurate than those at the RPA level.

Ma, H., Govoni, M. & Galli, G. *npj Comput Mater* 6, 85 (2020)

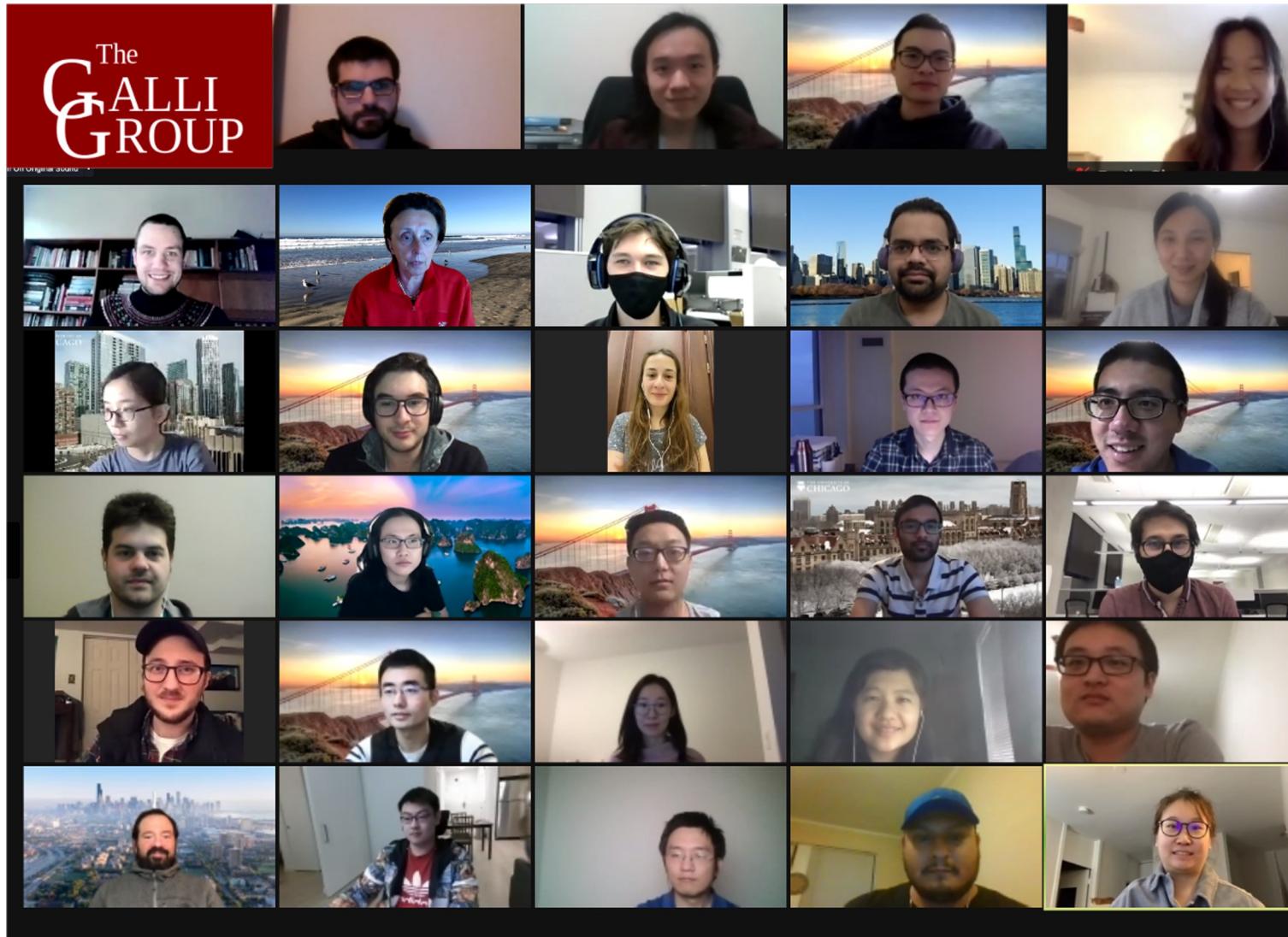
Ma, H., **Sheng, N.**, Govoni, M., & Galli, G. *Phys. Chem. Chem. Phys.* (2020)

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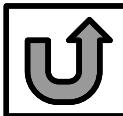
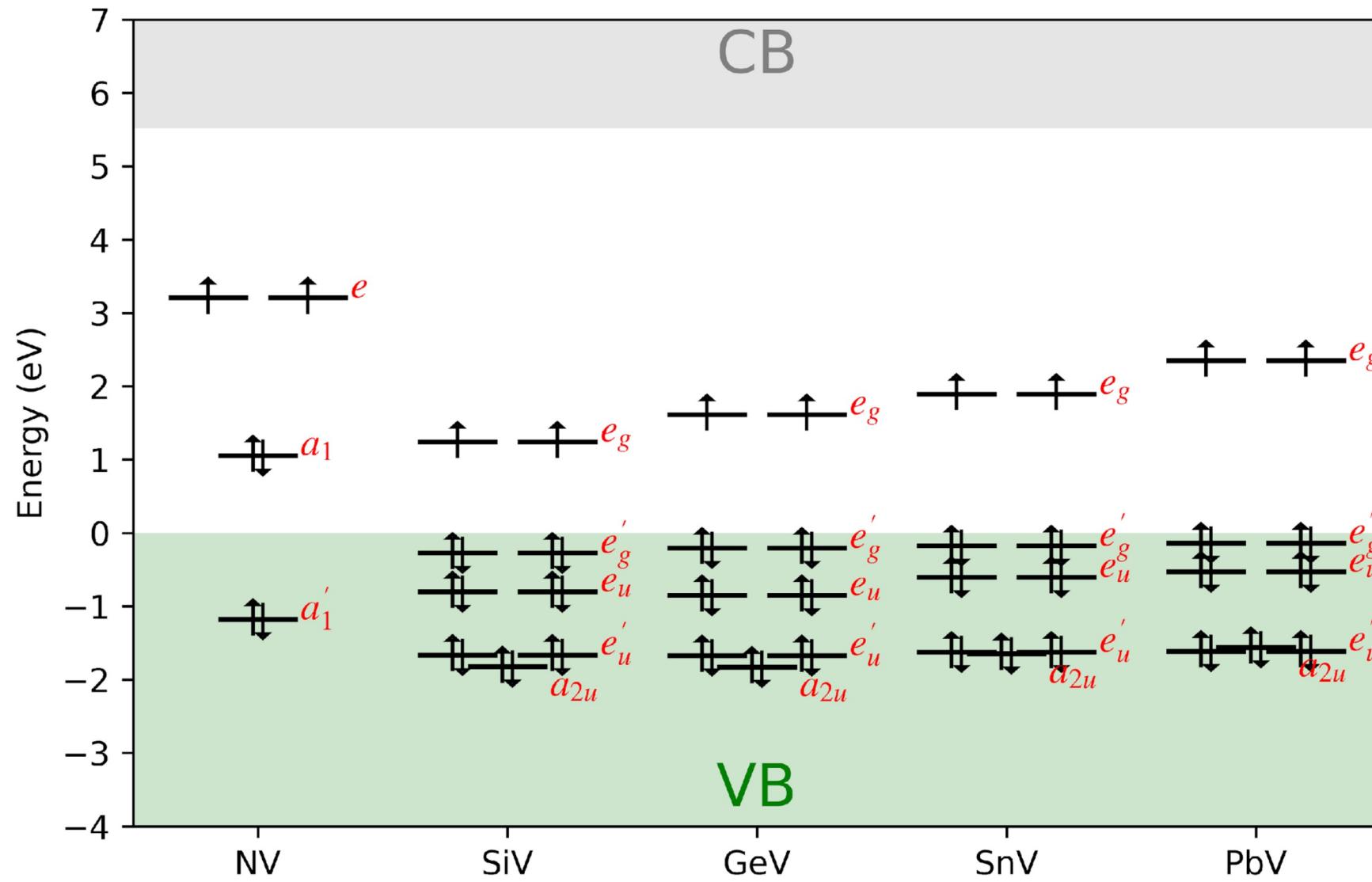


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DFT defect orbitals



DFT defect orbitals



Minimum model of NV⁻

a'_1

a_1

e_x

e_y

Minimum model of SiV⁰

a_{2u}

e'_{ux}

e'_{uy}

e_{ux}

e_{uy}

e'_{gx}

e'_{gy}

e_{gx}

e_{gy}

