─── MODULE *Sailfish* ───

Specification of the *Sailfish* consensus algorithm at a high level of abstraction.

We use a number of abstractions and simplifiying assumptions in order to expose the high-level principles of the algorithm clearly and in order to make model-checking of interesting configiations tractable :

1) Nodes read and write a global DAG. Each round, each node gets to see an arbitrary quorum of vertices from the previous round (and, after GST, this quorum must include all correct vertices).

2) We do not model timeouts. Instead, before GST, nodes can non-deterministically increase their round number (inluding skipping rounds entirely); after GST, correct nodes can only increment their round number and only do so after acting upon a superset of the correct vertices of the previous round.

3) We do not model the DAG ordering procedure. Instead, we check that for every two committed vertices, there is a path in the DAG from the one with the higher round to the one with the lower round. Moreover, we define committed vertices using the global DAG and it is plausible that local DAG views would contain fewer committed vertices; so there is a potential for missing safety or liveness violations because of this.

4) We model *Byzantine* nodes explicitly by assigning them an algorithm. This algorithm should allow *Byzantine* nodes to do the worst possible, but there is no guarantee that this is the case. A more realistic model would allow *Byzantine* nodes to send completely arbitrary messages at any time, but this would make model-checking too hard.

5) We do model committing based on $2f + 1$ first RBC messages.

This version of the algorithm does not use "*no_vote*" messages.

EXTENDS *DomainModel*

CONSTANT
  GST the first synchronous round (all later rounds are synchronous)

 --algorithm *Sailfish***{**
  variables
   $vs = \{\}$, the vertices of the DAG
   $es = \{\}$ **;** the edges of the DAG
  define {
   $LeaderVertice(r) \triangleq \langle Leader(r), r \rangle$
   $ValidVertexQuorums(r) \triangleq$
    Quorums of valid vertices of round r
    $\{ VQ \in$ SUBSET $vs :$ LET $NQ \triangleq \{Node(v) : v \in VQ\}$ IN
     $\wedge\ NQ \in Quorum$
     $\wedge\ \forall v \in VQ :$
      $\wedge\ Round(v) = r$
      the leader vertex, if included, must be valid (*i.e.* if it does not point to the previous leader vertice, t
      $\wedge\ \vee\ \neg(r > 0 \wedge v = LeaderVertice(r) \wedge \langle v, LeaderVertice(r-1) \rangle \notin es)$
       $\vee\ \exists VQ2 \in$ SUBSET $VQ :$
        $\wedge\ VQ2 \in Quorum$
        $\wedge\ \forall v2 \in VQ2 : \langle v2, LeaderVertice(r-1) \rangle \notin es\}$

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$$VerticeQuorums(r) \triangleq$$

Quorums of vertices of round r; included leader vertex may be invalid (*i.e.* does not point to the previous lea

$$\{VQ \in \text{SUBSET } vs : \text{LET } NQ \triangleq \{Node(v) : v \in VQ\}\text{IN}$$
$$\wedge\ NQ \in Quorum$$
$$\wedge\ \forall\, v \in VQ : Round(v) = r\}$$

}

process ($correctNode \in N \setminus F$ **)**

    variables $round = 0$ **;**   current round

{

*l*0:   **while (** TRUE **)**

    either with ($v = \langle self,\, round \rangle$ **) {**

        add a new vertex to the DAG and go to the next round

        $vs := vs \cup \{v\}$ **;**

        if ($round > 0$ **)**

        with ($VQ \in ValidVerticeQuorums(round - 1)$ **) {**

          from GST onwards, each node receives all correct vertices of the previous round:

          when $round \geq GST \Rightarrow (N \setminus F) \subseteq \{Node(v2) : v2 \in VQ\}$ **;**

          if ($Leader(round) = self$ **) {**

            we must either include the previous leader vertice,

            or a quorum of vertices not voting for the previous leader vertice

            when

              $\vee\ LeaderVertice(round - 1) \in VQ$

              $\vee\ \exists\, Q \in Quorum : \forall\, n \quad\quad \in Q \setminus \{self\} : \text{LET } vn \triangleq \langle n,\, round \rangle \text{IN}$

                $\wedge\ \ vn \in vs$

                $\wedge\ \langle vn,\, LeaderVertice(round - 1) \rangle \notin es$ **;**

          } ;

          $es := es \cup \{\langle v,\, pv \rangle : pv \in VQ\}$ **;**   add the edges

        } ;

        $round := round + 1$

    }

    or with ($r \in \{r \in R : r > round\}$ **) {**

        go to a higher round

        when $r \leq GST$ **;**   from GST onwards, correct nodes do not skip rounds

        $round := r$

    }

}

Next comes our model of *Byzantine* nodes. Because the real protocol disseminates DAG vertices using reliable broadcast, *Byzantine* nodes cannot equivocate and cannot deviate much from the protocol (lest their messages be ignored). Also note that creating a round-r vertice commutes to the left of actions of rounds greater than r and to the right of actions of rounds smaller than R, so we can, without loss of generality, schedule *Byzantine* nodes in the same "round-by-round" manner as other nodes.

process ($byzantineNode \in F$ **)**

    variables $round_- = 0$ **;**

{

```
l0:     while ( TRUE ) {
              maybe add a vertices to the DAG:
              either with ( v = ⟨self, round_⟩ ) {
                  vs := vs ∪ {v} ;
                  if ( round_ > 0 )
                  with ( vq ∈ VerticeQuorums(round_ − 1) ) {
                      es := es ∪ {⟨v, pv⟩ : pv ∈ vq}
                    }
                } or skip ;
                go to the next round:
                round_ := round_ + 1
          }
      }
 }
```

Next we define the safety and liveness properties

$Committed(v) \triangleq$
    $\wedge\ v \in vs$
    $\wedge\ Node(v) = Leader(Round(v))$
    $\wedge\ \exists\, Bl \in Blocking : Bl \subseteq \{Node(pv) : pv \in Parents(v,\, es)\}$
    $\wedge\ \vee\ Round(v) = 0$
       $\vee\ LeaderVertice(Round(v) − 1) \in Children(v,\, es)$
       $\vee\ \exists\, Q \in Quorum : \forall\, n \in Q : \text{LET } vn \triangleq \langle n,\, Round(v)\rangle \text{ IN}$
          $\wedge\ vn \in vs$
          $\wedge\ \langle vn,\, LeaderVertice(Round(v) − 1)\rangle \notin es$

$Safety \triangleq \forall\, v1,\, v2 \in vs :$
    $\wedge\ Committed(v1)$
    $\wedge\ Committed(v2)$
    $\wedge\ Round(v1) \leq Round(v2)$
    $\Rightarrow Reachable(v2,\, v1,\, es)$

$Liveness \triangleq \forall\, r \in R :$
    $\wedge\ r \geq GST$
    $\wedge\ Leader(r) \notin F$
    all correct $round − (r + 1)$ vertices are created:
    $\wedge\ \forall\, n \in N \setminus F : round[n] > r + 1$
    $\Rightarrow Committed(LeaderVertice(r))$

Finally we make a few auxiliary definitions used for model-checking with *TLC*

$Quorum1 \triangleq \{Q \in \text{SUBSET } N : Cardinality(Q) \geq Cardinality(N) − Cardinality(F)\}$
$Blocking1 \triangleq \{Q \in \text{SUBSET } N : Cardinality(Q) > Cardinality(F)\}$

 The round of a node, whether *Byzantine* or not
$Round\_(n) \triangleq \text{IF } n \in F \text{ THEN } round\_[n] \text{ ELSE } round[n]$

Basic typing invariant:

$TypeOK \triangleq$
$\quad \wedge\ \forall\, v \in vs : Node(v) \in N \wedge Round(v) \in Nat$
$\quad \wedge\ \forall\, e \in es :$
$\qquad \wedge\ e = \langle e[1],\ e[2]\rangle$
$\qquad \wedge\ \{e[1],\ e[2]\} \subseteq vs$
$\qquad \wedge\ Round(e[1]) > Round(e[2])$
$\quad \wedge\ \forall\, n \in N : Round\_(n) \in Nat$

Sequentialization constraints, which enforce a particular ordering of the actions. Because of how actions commute, the set of reachable states remains unchanged. Essentially, we schedule all nodes "round-by-round" and in lock-steps, with the leader last. This speeds up model-checking a lot.

Note that we must always schedule the leader last because, due to its use of other nodes's vertices, its action does not commute to the left of the actions of other nodes.

$SeqConstraints(n) \triangleq$
$\quad$ wait for all nodes to finish previous rounds:
$\quad \wedge\, (Round\_(n) > 0 \Rightarrow \forall\, n2 \in N : Round\_(n2) \geq Round\_(n))$
$\qquad$ wait for all nodes with lower index to leave the round (leader index is always last):
$\quad \wedge\, \forall\, n2 \in N : NodeIndexLeaderLast(n2, Round\_(n)) < NodeIndexLeaderLast(n, Round\_(n)) \Rightarrow Round$

$SeqNext \triangleq (\exists\, self \in N \setminus F : SeqConstraints(self) \wedge correctNode(self))$
$\qquad\qquad \vee\, (\exists\, self \in F : SeqConstraints(self) \wedge byzantineNode(self))$
$SeqSpec \triangleq Init \wedge \square[SeqNext]_{vars}$

$\quad$ Example assignment of leaders to rounds:
$ModLeader(r) \triangleq NodeSeq[(r\% Cardinality(N)) + 1]$

$\quad$ Constraint to stop the model checker:
$StateConstraint \triangleq$
$\quad$ LET $Max(S) \triangleq$ CHOOSE $x \in S : \forall\, y \in S : y \leq x$ IN
$\qquad \forall\, n \in N : Round\_(n) \in 0\, ..\, (Max(R) + 1)$

$\quad$ Some properties we expect to be violated (useful to get the model-checker to print interesting executions):

$Falsy1 \triangleq \neg($
$\quad \wedge\, Committed(\langle Leader(1),\ 1\rangle)$
$)$

$Falsy2 \triangleq \neg($
$\quad \wedge\, Committed(\langle Leader(0),\ 0\rangle)$
$\quad \wedge\, \neg Committed(\langle Leader(1),\ 1\rangle)$
$\quad \wedge\, \neg Committed(\langle Leader(2),\ 2\rangle)$
$\quad \wedge\, Committed(\langle Leader(3),\ 3\rangle)$
$)$