Specification of the Sailfish consensus algorithm at a high level of abstraction.

We use a number of abstractions and simplifying assumptions in order to expose the high-level principles of the algorithm clearly and in order to make model-checking of interesting configuations tractable :

- 1) Nodes read and write a global DAG. Each round, each node gets to see an arbitrary quorum of vertices from the previous round (and, after GST, this quorum must include all correct vertices).
- 2) We do not model timeouts. Instead, we assume that, every round r after GST, correct nodes always rbc-deliver all correct vertices of round r-1 before entering round r. TODO: is this an acceptable assumption? Should it be just f+1 correct vertices?
- 4) We model *Byzantine* nodes explicitly by assigning them an algorithm. This algorithm should allow the worst attacks possible, but, while the author thinks this is true, there is no formal guarantee that this is the case. A more realistic model would allow *Byzantine* nodes to send completely arbitrary messages at any time, but this would make model-checking too hard.
- 5) We do not explicitly model committing based on 2f + 1 first RBC messages.

This version of the algorithm does not use "no_vote" messages.

EXTENDS DomainModel

CONSTANT

GST the first synchronous round (all later rounds are synchronous)

```
--algorithm Sailfish {
   variables
        vs = \{\}, the vertices of the DAG
        es = \{\}; the edges of the DAG
        LeaderVertice(r) \stackrel{\Delta}{=} \langle Leader(r), r \rangle
        ValidVerticeQuorums(r) \stackrel{\triangle}{=} Quorums of valid vertices of round r
             \{\, VQ \in \text{SUBSET} \,\, vs : \text{LET} \,\, NQ \,\, \stackrel{\Delta}{=} \,\, \{Node(v) : v \in \, VQ\} \text{IN}
                     \land NQ \in Quorum
                     \land \forall v \in VQ:
                         \land Round(v) = r
                          the leader vertice, if included, must be valid (i.e. if it does not point
                           to the previous leader vertice, then a quorum of votes must justify that):
                         \land \lor \neg (r > 0 \land v = LeaderVertice(r) \land \langle v, LeaderVertice(r-1) \rangle \notin es)
                               \lor \exists VQ2 \in \text{Subset } VQ:
                                    \land \quad VQ2 \in \mathit{Quorum}
                                    \land \ \forall \, v2 \in \mathit{VQ2} : \langle v2, \, \mathit{LeaderVertice}(r-1) \rangle \notin \mathit{es} \}
    }
  process ( correctNode \in N \setminus F )
        variables
             round = 0, current round
             log = \langle \rangle; delivered log
```

```
while (TRUE)
         with ( v = \langle self, round \rangle ) {
              complete a round: add the new DAG vertice v, and maybe commit new leader vertice
             vs := vs \cup \{v\};
             if (round > 0)
             with ( VQ \in ValidVerticeQuorums(round - 1) ) {
                   from GST onwards, each node receives all correct vertices of the previous round:
                  when round \geq GST \Rightarrow (N \setminus F) \subseteq \{Node(v2) : v2 \in VQ\};
                 if ( Leader(round) = self ) {
                         we must either include the previous leader vertice,
                        or we must have seen a quorum of vertices not voting for the previous leader vertice
                       when
                            \lor LeaderVertice(round - 1) \in VQ
                                                           \in Q \setminus \{self\} : \text{LET } vn \stackrel{\triangle}{=} \langle n, round \rangle \text{IN}
                            \lor \exists Q \in Quorum : \forall n
                                \land \langle vn, LeaderVertice(round - 1) \rangle \notin es;
                  es := es \cup \{\langle v, pv \rangle : pv \in VQ\}; add v's edges
                   possibly commit the leader vertice of round r-2:
                  if (round > 1)
                       with ( votesForLeader = \{pv \in VQ : \langle pv, LeaderVertice(round - 2) \rangle \in es\} )
                       if ( \{Node(pv) : pv \in votesForLeader\} \in Quorum )
                            log := OrderDAG(es, [i \in 1 ... (round - 2) \mapsto LeaderVertice(i)])
              } ;
             round := round + 1
         }
     }
Next comes our model of Byzantine nodes. Because the real protocol disseminates DAG vertices
```

Next comes our model of Byzantine nodes. Because the real protocol disseminates DAG vertices using reliable broadcast, Byzantine nodes cannot equivocate and cannot deviate much from the protocol (lest their messages be ignored). Also note that creating a round-r vertice commutes to the left of actions of rounds greater than r and to the right of actions of rounds smaller than R, so we can, without loss of generality, schedule Byzantine nodes in the same "round-by-round" manner as other nodes.

```
\begin{array}{l} \mathbf{process} \; (\; byzantineNode \in F \; ) \\ \qquad \mathbf{variables} \; round_- = 0 \; ; \\ \{ \\ l0: \quad \mathbf{while} \; (\; \mathsf{TRUE} \; ) \; \{ \\ \qquad \qquad \mathbf{maybe} \; \mathrm{add} \; \mathrm{a} \; \mathrm{vertices} \; \mathrm{to} \; \mathrm{the} \; \mathit{DAG} \colon \\ \qquad \mathbf{either} \; \mathbf{with} \; (\; v = \langle self, \; round_- \rangle \; ) \; \{ \\ \qquad \qquad vs := vs \cup \{v\} \; ; \\ \qquad \mathbf{if} \; (\; round_- > 0 \; ) \\ \qquad \mathbf{with} \; (\; vq \in \mathit{ValidVerticeQuorums}(round_- - 1) \; ) \; \{ \\ \qquad \qquad es := es \cup \{\langle v, \; pv \rangle : pv \in vq \} \\ \qquad \qquad \} \end{array}
```

```
} or skip;
                   go to the next round:
                 round_{-} := round_{-} + 1
             }
       }
 }
Next we define the safety and liveness properties
Committed(v, view) \stackrel{\Delta}{=} view intended to be a sub-DAG of the DAG es
       \land v \in view
       \land Node(v) = Leader(Round(v))
       \land \exists Bl \in Blocking : Bl \subseteq \{Node(pv) : pv \in Parents(v, es) \cap view\}
       \land \lor Round(v) = 0
            \lor LeaderVertice(Round(v) - 1) \in Children(v, es)
            \lor \exists Q \in Quorum : \forall n \in Q : \text{LET } vn \stackrel{\triangle}{=} \langle n, Round(v) \rangle \text{IN}
                 \land vn \in view
                  \land \langle vn, LeaderVertice(Round(v) - 1) \rangle \notin es
Safety \triangleq \forall n1, n2 \in N \setminus F:
      Compatible(log[n1], log[n2])
  TODO: update Livenes to use local logs
Liveness \stackrel{\triangle}{=} \forall r \in R:
       \land r \geq GST
       \land Leader(r) \notin F
        all correct round - (r + 1) vertices are created:
       \land \forall n \in N \setminus F : round[n] > r + 1
       \Rightarrow Committed(LeaderVertice(r), vs)
Finally we make a few auxiliary definitions used for model-checking with \,TLC\,
\begin{array}{ll} \textit{Quorum1} \; \stackrel{\triangle}{=} \; \{\textit{Q} \in \texttt{SUBSET} \; \textit{N} : \textit{Cardinality}(\textit{Q}) \geq \textit{Cardinality}(\textit{N}) - \textit{Cardinality}(\textit{F})\} \\ \textit{Blocking1} \; \stackrel{\triangle}{=} \; \{\textit{Q} \in \texttt{SUBSET} \; \textit{N} : \textit{Cardinality}(\textit{Q}) > \textit{Cardinality}(\textit{F})\} \end{array}
 The round of a node, whether Byzantine or not
Round_{-}(n) \stackrel{\triangle}{=} \text{ if } n \in F \text{ THEN } round_{-}[n] \text{ ELSE } round[n]
 Basic typing invariant:
TypeOK \triangleq
       \land \forall v \in vs : Node(v) \in N \land Round(v) \in Nat
       \land \forall e \in es:
                \land e = \langle e[1], e[2] \rangle
                \land \{e[1], e[2]\} \subseteq vs
                \land Round(e[1]) > Round(e[2])
       \land \forall n \in N : Round_{-}(n) \in Nat
```

Sequentialization constraints, which enforce a particular ordering of the actions. Because of how actions commute, the set of reachable states remains unchanged. Essentially, we schedule all nodes "round-by-round" and in lock-steps, with the leader last. This speeds up model-checking a lot.

Note that we must always schedule the leader last because, due to its use of other nodes's vertices, its action does not commute to the left of the actions of other nodes.

```
SeqConstraints(n) \triangleq
      wait for all nodes to finish previous rounds:
      \land (Round_{-}(n) > 0 \Rightarrow \forall n2 \in N : Round_{-}(n2) \geq Round_{-}(n))
      wait for all nodes with lower index to leave the round (leader index is always last):
      \land \forall n \in N : NodeIndexLeaderLast(n, Round_n) < NodeIndexLeaderLast(n, Round_n) \Rightarrow Round_n
SeqNext \triangleq (\exists self \in N \setminus F : SeqConstraints(self) \land correctNode(self))
                 \lor (\exists self \in F : SeqConstraints(self) \land byzantineNode(self))
SegSpec \triangleq Init \wedge \Box [SegNext]_{vars}
 Example assignment of leaders to rounds:
ModLeader(r) \triangleq NodeSeq[(r\%Cardinality(N)) + 1]
 Constraint to stop the model checker:
StateConstraint \triangleq
     LET Max(S) \stackrel{\triangle}{=} \text{ CHOOSE } x \in S : \forall y \in S : y \leq x \text{IN}
           \forall n \in N : Round_{-}(n) \in 0 \dots (Max(R) + 1)
 Some properties we expect to be violated (useful to get the model-checker to print interesting executions):
Falsy1 \stackrel{\triangle}{=} \neg (\text{ we commit something in round } 1
     \exists n \in N \setminus F : log[n] \neq \langle \rangle \land Round(log[n][Len(log[n])]) \neq 0
Falsy2 \stackrel{\triangle}{=} \neg (
     \land Committed(\langle Leader(0), 0 \rangle, vs)
     \land \neg Committed(\langle Leader(1), 1 \rangle, vs)
     \land Committed(\langle Leader(2), 2 \rangle, vs)
       \land Committed(\langle Leader(3), 3 \rangle, vs)
)
```