

Tests for *BlockDag* operators using small concrete *DAGs*.

EXTENDS *FiniteSets*, *Sequences*, *Integers*, *TLC*

$N \triangleq \{1, 2\}$
 $R \triangleq 1 \dots 3$
 $Leader(r) \triangleq \text{CASE}$
 $r = 1 \rightarrow 1$
 $\square \quad r = 2 \rightarrow 2$
 $\square \quad r = 3 \rightarrow 1$

INSTANCE *BlockDag* WITH $N \leftarrow N$, $R \leftarrow R$, $Leader \leftarrow Leader$

$v11 \triangleq \langle 1, 1 \rangle$ leader
 $v21 \triangleq \langle 2, 1 \rangle$
 $v12 \triangleq \langle 1, 2 \rangle$
 $v22 \triangleq \langle 2, 2 \rangle$ leader
 $v13 \triangleq \langle 1, 3 \rangle$ leader
 $v23 \triangleq \langle 2, 3 \rangle$

ASSUME $TestNodeRound \triangleq Node(v12) = 1 \wedge Round(v12) = 2$

ASSUME $TestLeaderVertex \triangleq$
 $\wedge \quad LeaderVertex(1) = v11$
 $\wedge \quad LeaderVertex(2) = v22$
 $\wedge \quad LeaderVertex(3) = v13$

ASSUME $TestOrderSetPermutation \triangleq$
 LET $SeqToSet(seq) \triangleq \{seq[i] : i \in \text{DOMAIN } seq\}$
 $IsPermutation(seq, s) \triangleq SeqToSet(seq) = s \wedge Len(seq) = Cardinality(s)$
 IN $IsPermutation(OrderSet(\{v11, v21\}), \{v11, v21\})$

$dag1 \triangleq$
 $\langle \{Genesis, v11, v21, v12, v22, v13, v23\},$
 $\{ \langle v11, Genesis \rangle, \langle v21, Genesis \rangle,$
 $\langle v12, v21 \rangle, \langle v22, v11 \rangle, \langle v13, v22 \rangle,$
 $\langle v13, v21 \rangle, \langle v13, v12 \rangle, \langle v23, v22 \rangle \} \rangle$

ASSUME $TestPreviousLeader1 \triangleq PreviousLeader(dag1, 3) = v22$
 ASSUME $TestPreviousLeader2 \triangleq PreviousLeader(dag1, 2) = v11$
 ASSUME $TestPreviousLeaderBase \triangleq PreviousLeader(dag1, 1) = \langle \rangle$

ASSUME $TestLinearize \triangleq Linearize(dag1, v13) =$
 $\langle \langle 1, 1 \rangle, \langle 2, 2 \rangle \rangle \circ OrderSet(\{ \langle 2, 1 \rangle, \langle 1, 2 \rangle \}) \circ \langle \langle 1, 3 \rangle \rangle$