
 MODULE *BlockDagTest*

Tests for *BlockDag* operators using small concrete *DAGs*.

EXTENDS *FiniteSets*, *Sequences*, *Integers*, *TLC*

$$\begin{aligned} N &\triangleq \{1, 2\} \\ R &\triangleq 1..3 \\ Leader(r) &\triangleq \text{CASE} \\ &\quad r = 1 \rightarrow 1 \\ \square &\quad r = 2 \rightarrow 2 \\ \square &\quad r = 3 \rightarrow 1 \end{aligned}$$

INSTANCE *BlockDag* WITH $N \leftarrow N$, $R \leftarrow R$, $Leader \leftarrow Leader$

$$\begin{aligned} v11 &\triangleq \langle 1, 1 \rangle \text{ leader} \\ v21 &\triangleq \langle 2, 1 \rangle \\ v12 &\triangleq \langle 1, 2 \rangle \\ v22 &\triangleq \langle 2, 2 \rangle \text{ leader} \\ v13 &\triangleq \langle 1, 3 \rangle \text{ leader} \\ v23 &\triangleq \langle 2, 3 \rangle \end{aligned}$$

ASSUME $TestNodeRound \triangleq Node(v12) = 1 \wedge Round(v12) = 2$

$$\begin{aligned} \text{ASSUME } TestLeaderVertice &\triangleq \\ &\wedge LeaderVertex(1) = v11 \\ &\wedge LeaderVertex(2) = v22 \\ &\wedge LeaderVertex(3) = v13 \end{aligned}$$

$$\begin{aligned} \text{ASSUME } TestOrderSetPermutation &\triangleq \\ \text{LET } SeqToSet(seq) &\triangleq \{seq[i] : i \in \text{DOMAIN } seq\} \\ \text{IN } IsPermutation(seq, s) &\triangleq SeqToSet(seq) = s \wedge \text{Len}(seq) = \text{Cardinality}(s) \\ &\text{IN } IsPermutation(OrderSet(\{v11, v21\}), \{v11, v21\}) \end{aligned}$$

$$\begin{aligned} dag1 &\triangleq \\ &\langle \{Genesis, v11, v21, v12, v22, v13, v23\}, \\ &\quad \{\langle v11, Genesis \rangle, \langle v21, Genesis \rangle, \\ &\quad \langle v12, v21 \rangle, \langle v22, v11 \rangle, \langle v13, v22 \rangle, \\ &\quad \langle v13, v21 \rangle, \langle v13, v12 \rangle, \langle v23, v22 \rangle\} \rangle \end{aligned}$$

ASSUME $TestPreviousLeader1 \triangleq PreviousLeader(dag1, 3) = v22$

ASSUME $TestPreviousLeader2 \triangleq PreviousLeader(dag1, 2) = v11$

ASSUME $TestPreviousLeaderBase \triangleq PreviousLeader(dag1, 1) = \langle \rangle$

$$\begin{aligned} \text{ASSUME } TestLinearize &\triangleq Linearize(dag1, v13) = \\ &\langle \langle 1, 1 \rangle, \langle 2, 2 \rangle \rangle \circ OrderSet(\{\langle 2, 1 \rangle, \langle 1, 2 \rangle\}) \circ \langle \langle 1, 3 \rangle \rangle \end{aligned}$$
