Specification of the Sailfish consensus algorithm at a high level of abstraction.

We use a number of abstractions and simplifying assumptions in order to expose the high-level principles of the algorithm clearly and in order to make model-checking of interesting configuations tractable :

- 1) Nodes read and write a global DAG. Each round, each node gets to see an arbitrary quorum of vertices from the previous round (and, after GST, this quorum must include all correct vertices).
- 2) We do not model timeouts. Instead, before GST, nodes can non-deterministically increase their round number (inluding skipping rounds entirely); after GST, correct nodes can only increment their round number and only do so after acting upon a superset of the correct vertices of the previous round.
- 3) We do not model the DAG ordering procedure. Instead, we check that for every two committed vertices, there is a path in the DAG from the one with the higher round to the one with the lower round. Moreover, we define committed vertices using the global DAG and it is plausible that local DAG views would contain fewer committed vertices; so there is a potential for missing safety or liveness violations because of this.
- 4) We model *Byzantine* nodes explicitly by assigning them an algorithm. This algorithm should allow *Byzantine* nodes to do the worst possible, but there is no guarantee that this is the case. A more realistic model would allow *Byzantine* nodes to send completely arbitrary messages at any time, but this would make model-checking too hard.
- 5) We do model committing based on 2f + 1 first RBC messages.

This version of the algorithm does not use " $no\_vote$ " messages.

## EXTENDS DomainModel

--algorithm Sailfish {

## CONSTANT

GST the first synchronous round (all later rounds are synchronous)

```
 vs = \{\}, \quad \text{the vertices of the } DAG \\ es = \{\}; \quad \text{the edges of the } DAG \\ \textbf{define } \{ \\ Leader Vertice(r) \triangleq \langle Leader(r), r \rangle \\ Valid Vertice Quorums(r) \triangleq \\ \text{Quorums of valid vertices of round } r \\ \{ VQ \in \text{SUBSET } vs : \text{LET } NQ \triangleq \{ Node(v) : v \in VQ \} \text{IN} \\ \land NQ \in Quorum \\ \land \forall v \in VQ : \\ \land Round(v) = r \\ \text{the leader vertice, if included, must be valid } (i.e. \text{ if it does not point to the previous leader vertice, } r \\ \land \lor \neg (r > 0 \land v = Leader Vertice(r) \land \langle v, Leader Vertice(r - 1) \rangle \notin es) \\ \lor \exists VQ2 \in \text{SUBSET } VQ : \\ \land VQ2 \in Quorum \\ \land \forall v2 \in VQ2 : \langle v2, Leader Vertice(r - 1) \rangle \notin es \}
```

```
}
    process ( correctNode \in N \setminus F )
         variables round = 0; current round
l0:
         while (TRUE)
         either with ( v = \langle self, round \rangle ) {
              add a new vertex to the DAG and go to the next round
             vs := vs \cup \{v\};
             if (round > 0)
             with ( VQ \in ValidVerticeQuorums(round - 1) ) {
                   from GST onwards, each node receives all correct vertices of the previous round:
                  when round \geq GST \Rightarrow (N \setminus F) \subseteq \{Node(v2) : v2 \in VQ\};
                 if ( Leader(round) = self ) {
                        we must either include the previous leader vertice,
                        or a quorum of vertices not voting for the previous leader vertice
                            \lor LeaderVertice(round - 1) \in VQ
                                                           \in Q \setminus \{self\} : \text{LET } vn \stackrel{\Delta}{=} \langle n, round \rangle \text{IN}
                            \lor \exists Q \in Quorum : \forall n
                                \land vn \in vs
                                \land \langle vn, LeaderVertice(round - 1) \rangle \notin es;
                 es := es \cup \{\langle v, pv \rangle : pv \in VQ\}; add the edges
             round := round + 1
         }
        or with (r \in \{r \in R : r > round\})
               go to a higher round
             when r \leq GST; from GST onwards, correct nodes do not skip rounds
             round := r
          }
     }
```

Next comes our model of Byzantine nodes. Because the real protocol disseminates DAG vertices using reliable broadcast, Byzantine nodes cannot equivocate and cannot deviate much from the protocol (lest their messages be ignored). Also note that creating a round-r vertice commutes to the left of actions of rounds greater than r and to the right of actions of rounds smaller than R, so we can, without loss of generality, schedule Byzantine nodes in the same "round-by-round" manner as other nodes.

```
process ( byzantineNode \in F )
variables round_- = 0;
{
0: while ( TRUE ) {
maybe add a vertices to the DAG:
either with ( v = \langle self, round_- \rangle ) {
vs := vs \cup \{v\};
if ( round_- > 0 )
```

```
with ( vq \in ValidVerticeQuorums(round_- - 1) ) {
                         es := es \cup \{\langle v, pv \rangle : pv \in vq\}
                     }
                } or skip;
                go to the next round:
               round_{-} := round_{-} + 1
           }
      }
 }
Next we define the safety and liveness properties
Committed(v) \stackrel{\Delta}{=}
     \land v \in vs
     \land Node(v) = Leader(Round(v))
     \land \exists Bl \in Blocking : Bl \subseteq \{Node(pv) : pv \in Parents(v, es)\}
     \land \lor Round(v) = 0
          \lor LeaderVertice(Round(v) - 1) \in Children(v, es)
          \lor \exists Q \in Quorum : \forall n \in Q : \text{LET } vn \stackrel{\Delta}{=} \langle n, Round(v) \rangle \text{IN}
               \land vn \in vs
               \land \langle vn, LeaderVertice(Round(v) - 1) \rangle \notin es
Safety \triangleq \forall v1, v2 \in vs:
     \land Committed(v1)
     \land Committed(v2)
     \land Round(v1) \leq Round(v2)
      \Rightarrow Reachable(v2, v1, es)
Liveness \stackrel{\triangle}{=} \forall r \in R:
     \land r \geq GST
     \land Leader(r) \notin F
      all correct round - (r + 1) vertices are created:
     \land \forall n \in N \setminus F : round[n] > r + 1
      \Rightarrow Committed(LeaderVertice(r))
Finally we make a few auxiliary definitions used for model-checking with TLC
Quorum1 \triangleq \{Q \in SUBSET \ N : Cardinality(Q) \geq Cardinality(N) - Cardinality(F)\}
Blocking1 \triangleq \{Q \in SUBSET \ N : Cardinality(Q) > Cardinality(F)\}
 The round of a node, whether {\it Byzantine} or not
Round_{-}(n) \stackrel{\triangle}{=} \text{ if } n \in F \text{ THEN } round_{-}[n] \text{ ELSE } round[n]
 Basic typing invariant:
TypeOK \triangleq
     \land \ \forall \, v \in \mathit{vs} : Node(v) \in \mathit{N} \land \mathit{Round}(v) \in \mathit{Nat}
     \land \forall e \in es:
```

Sequentialization constraints, which enforce a particular ordering of the actions. Because of how actions commute, the set of reachable states remains unchanged. Essentially, we schedule all nodes "round-by-round" and in lock-steps, with the leader last. This speeds up model-checking a lot.

Note that we must always schedule the leader last because, due to its use of other nodes's vertices, its action does not commute to the left of the actions of other nodes.

```
SegConstraints(n) \triangleq
       wait for all nodes to finish previous rounds:
      \land (Round_{-}(n) > 0 \Rightarrow \forall n2 \in N : Round_{-}(n2) > Round_{-}(n))
       wait for all nodes with lower index to leave the round (leader index is always last):
      \land \forall n \in N : NodeIndexLeaderLast(n, Round_n) < NodeIndexLeaderLast(n, Round_n) \Rightarrow Round_n
SeqNext \triangleq (\exists self \in N \setminus F : SeqConstraints(self) \land correctNode(self))
                  \lor (\exists \mathit{self} \in \mathit{F} : \mathit{SeqConstraints}(\mathit{self}) \land \mathit{byzantineNode}(\mathit{self}))
SeqSpec \stackrel{\triangle}{=} Init \wedge \Box [SeqNext]_{vars}
 Example assignment of leaders to rounds:
ModLeader(r) \triangleq NodeSeq[(r\%Cardinality(N)) + 1]
 Constraint to stop the model checker:
StateConstraint \triangleq
     LET Max(S) \triangleq \text{CHOOSE } x \in S : \forall y \in S : y \leq x \text{IN}
           \forall n \in N : Round_{-}(n) \in 0 .. (Max(R) + 1)
 Some properties we expect to be violated (useful to get the model-checker to print interesting executions):
Falsy1 \stackrel{\triangle}{=} \neg (
     \land Committed(\langle Leader(1), 1 \rangle)
Falsy2 \stackrel{\triangle}{=} \neg (
      \land Committed(\langle Leader(0), 0 \rangle)
      \land \neg Committed(\langle Leader(1), 1 \rangle)
      \land \neg Committed(\langle Leader(2), 2 \rangle)
      \land Committed(\langle Leader(3), 3 \rangle)
```