



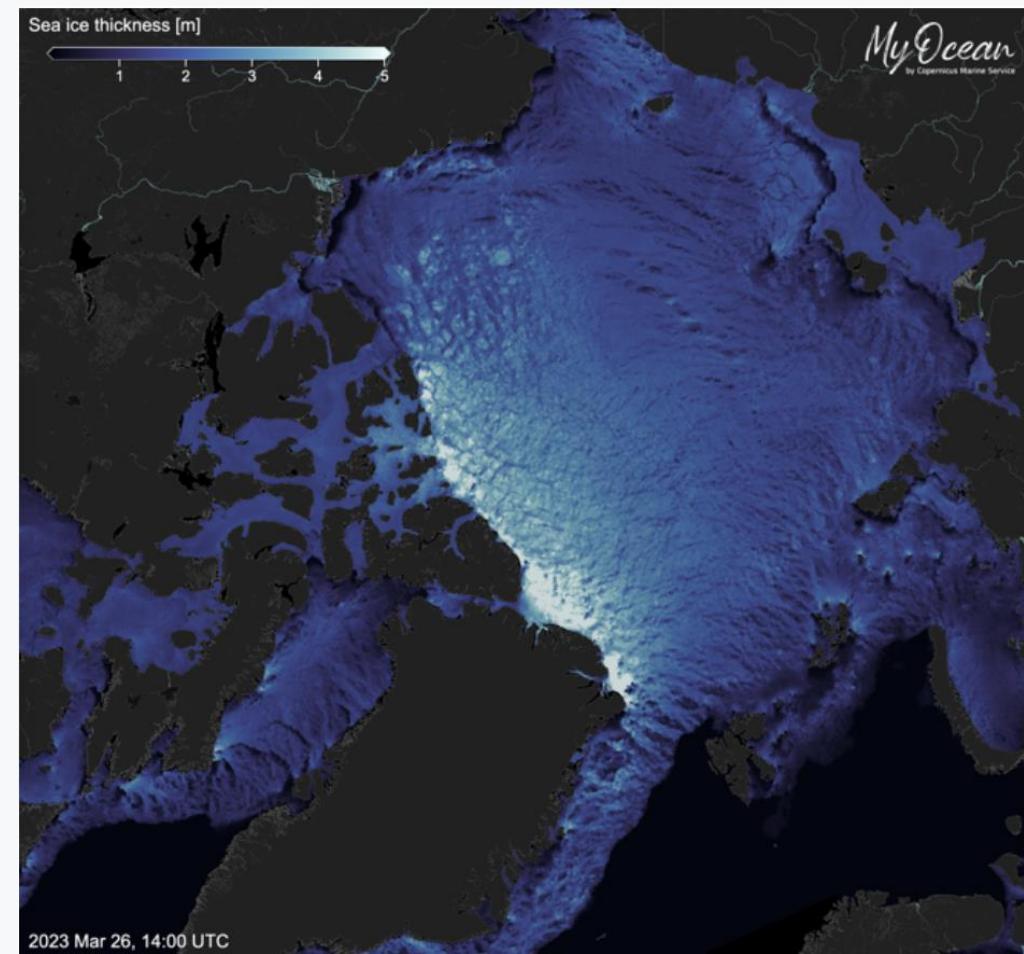
Super-resolution of satellite observations of sea ice thickness using diffusion models and physical modeling

Julien Brajard, Anton Korosov, Fabio Mangini, Adrien Perrin, Richard Davy, and Yiguo Wang

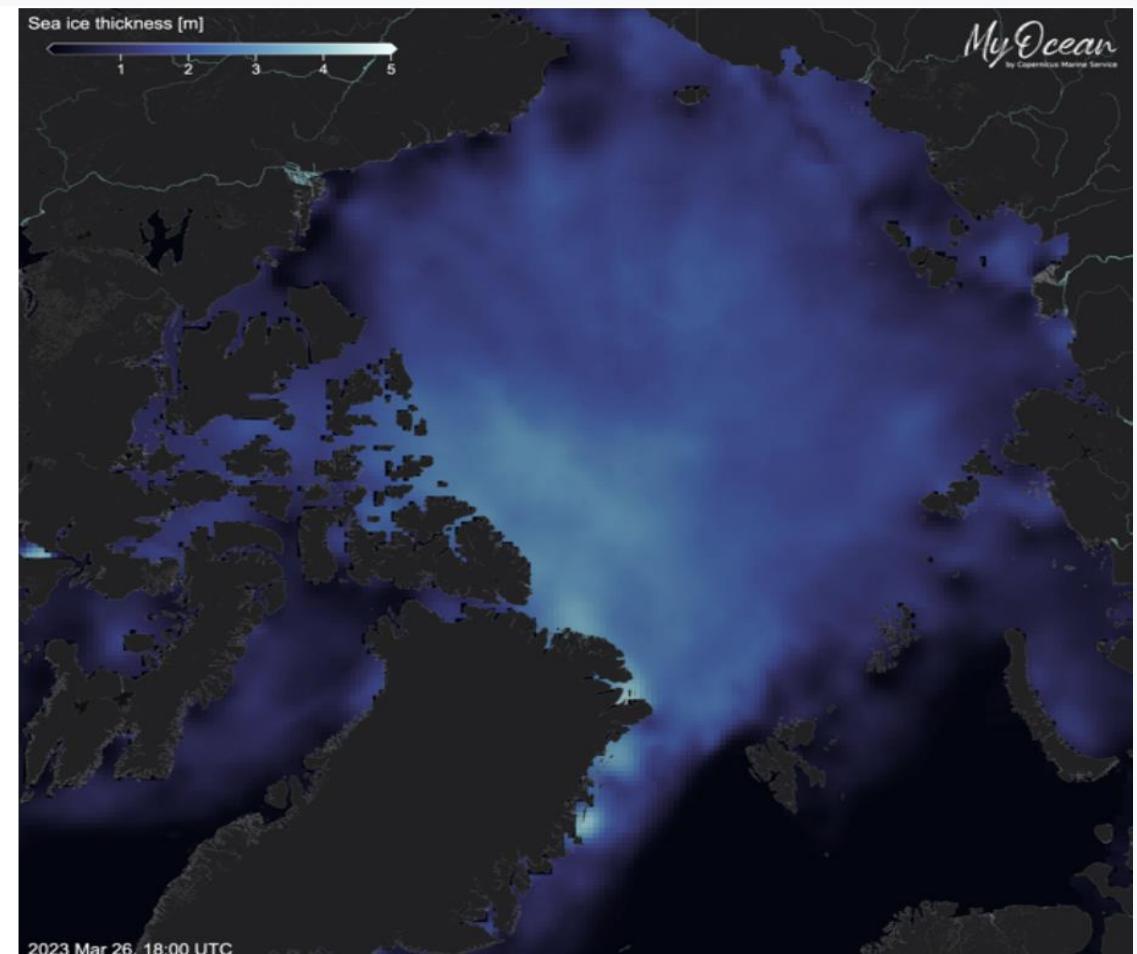


Context

High-resolution model simulation of Sea ice thickness
in the Arctic
(3 km resolution)

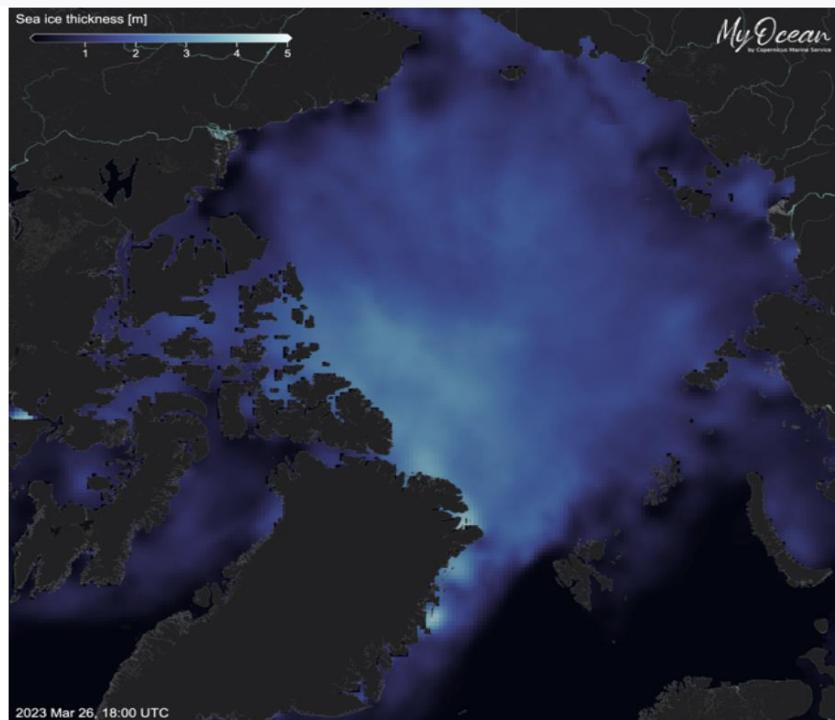


The resolution we can observe
(~90 km resolution)



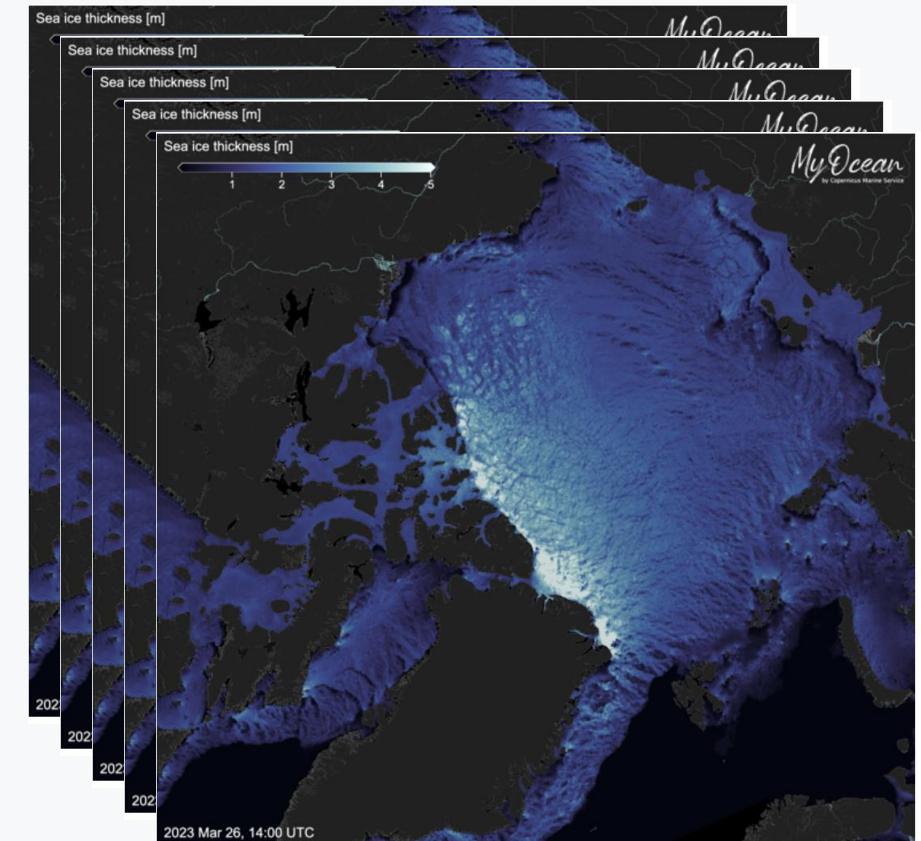
Objective of SuperIce

Low resolution image of sea ice thickness



Neural Networks

High-resolution images





We use **diffusion models** to generate an ensemble of high-resolution sea ice thickness.

Good **accuracy** and **realism** of the generated fields.

Please visit my poster for more details **#13**

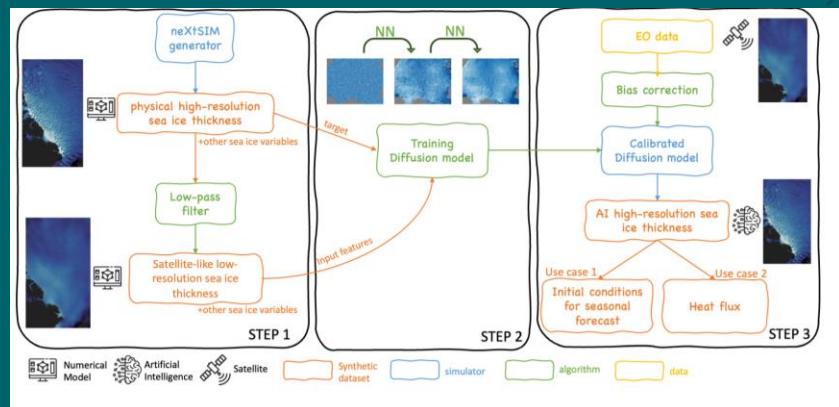


Super-resolution

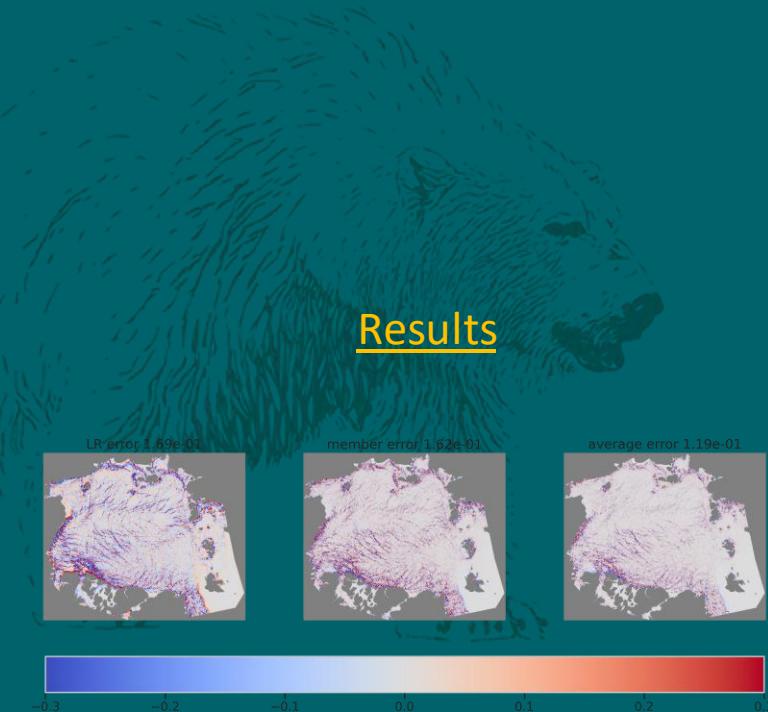
Motivation



Sketch of the project

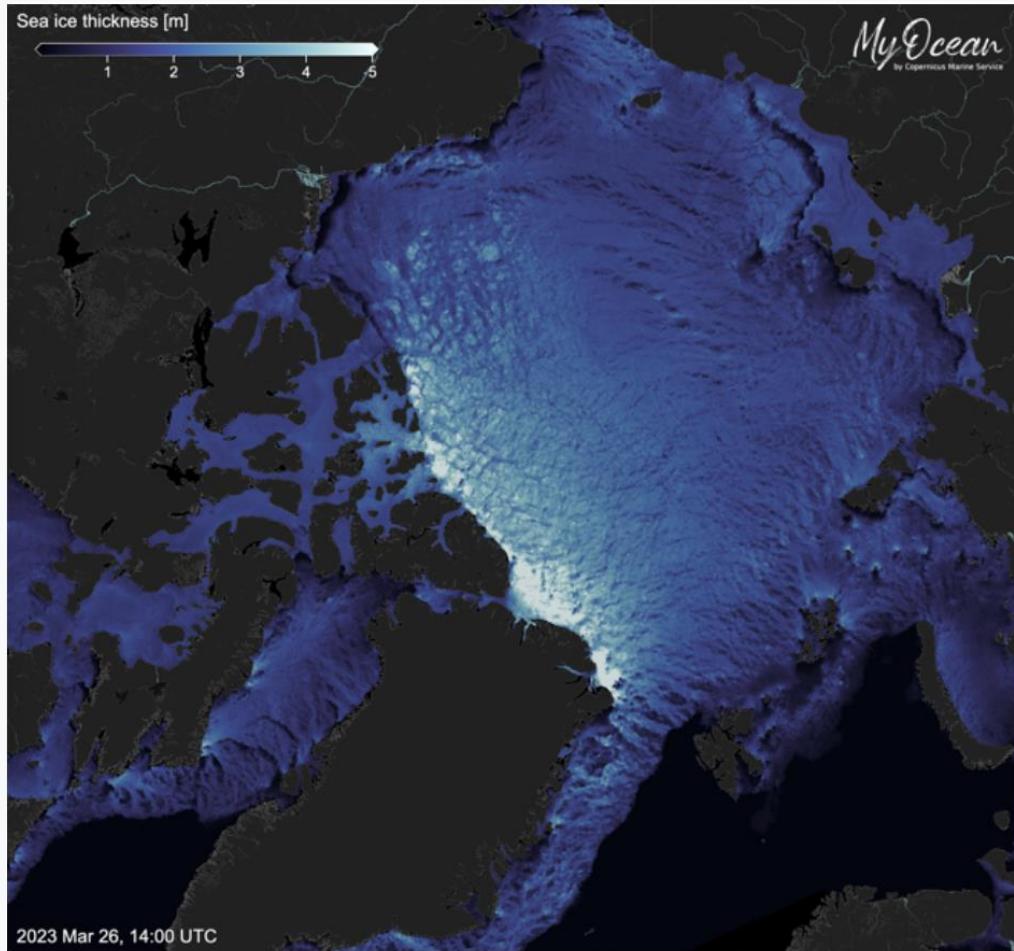


Results

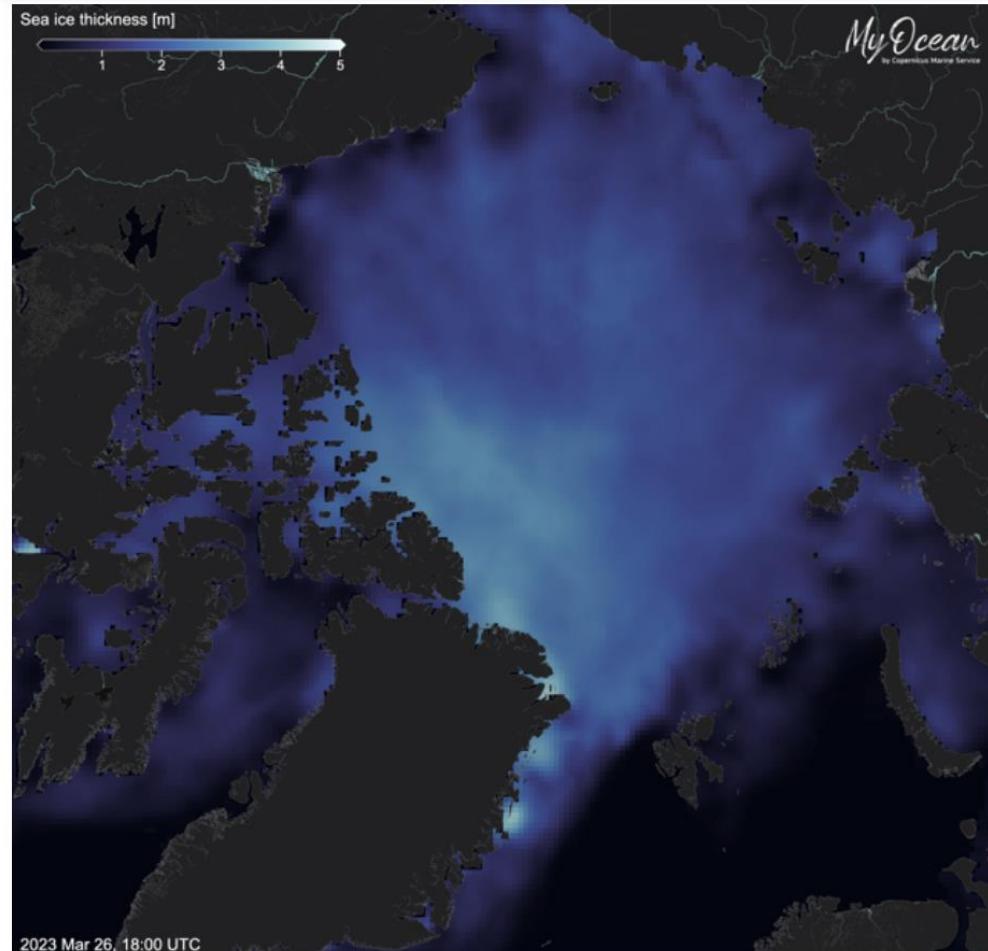


Motivation

Physical model (NeXtSIM) forecast



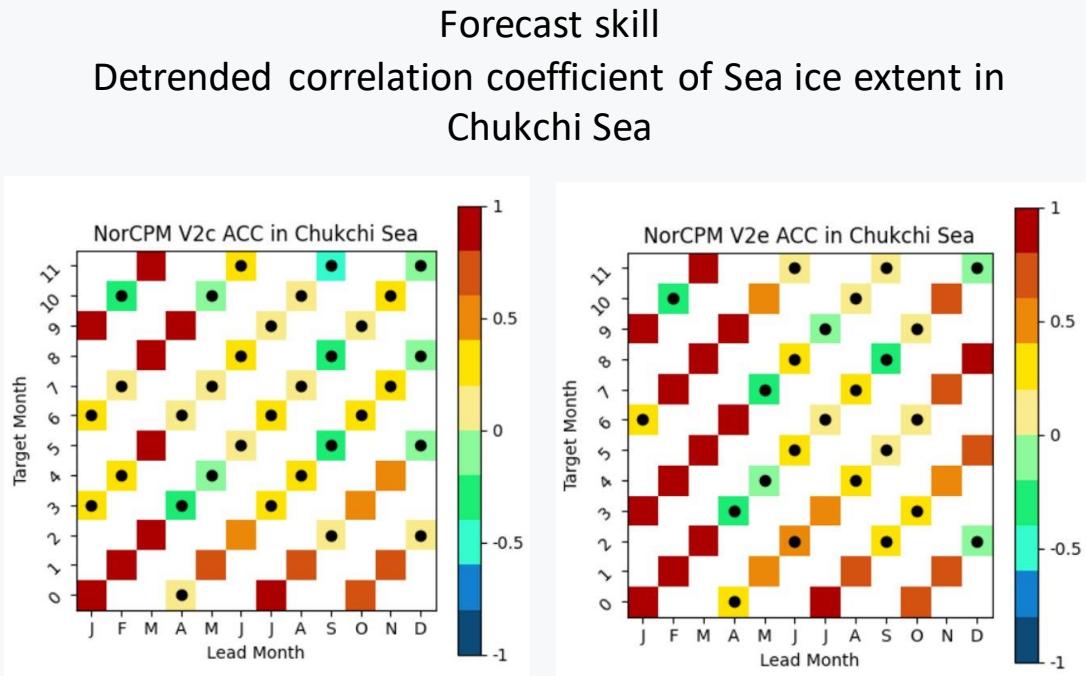
Satellite observation product (CS2SMOS)



Satellite product does not resolve small scales in sea ice thickness (e.g. leads)

Why is it important?

Case 1: Predictability



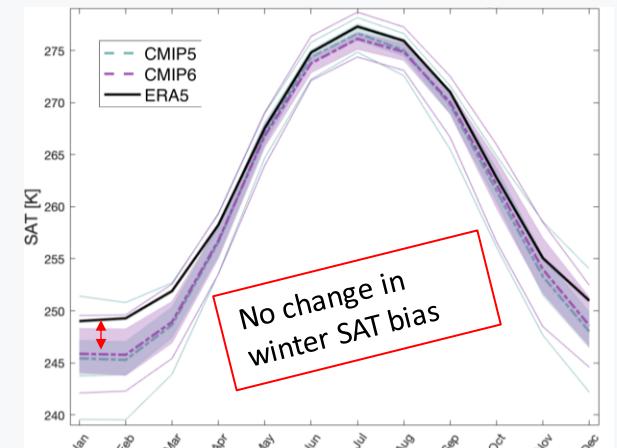
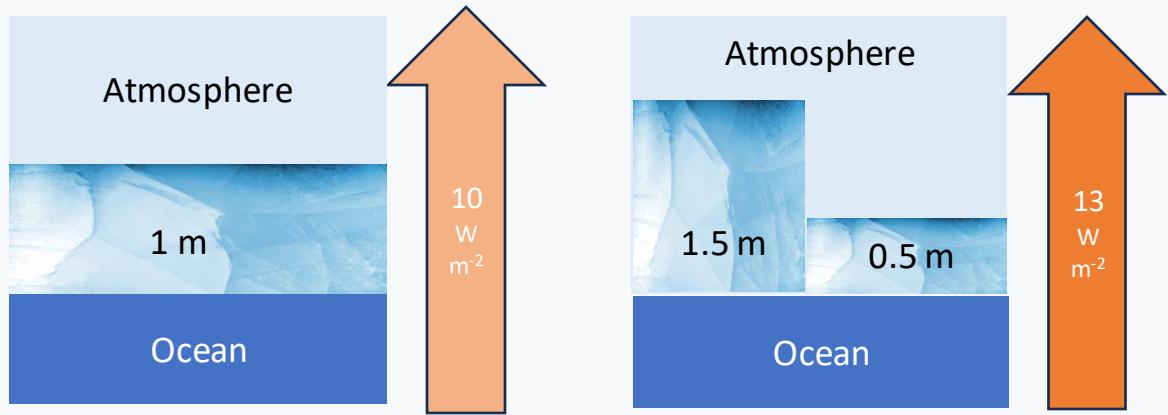
Initialization using Sea ice concentration observations only

Initialization using Sea ice concentration observations + Sea ice thickness only

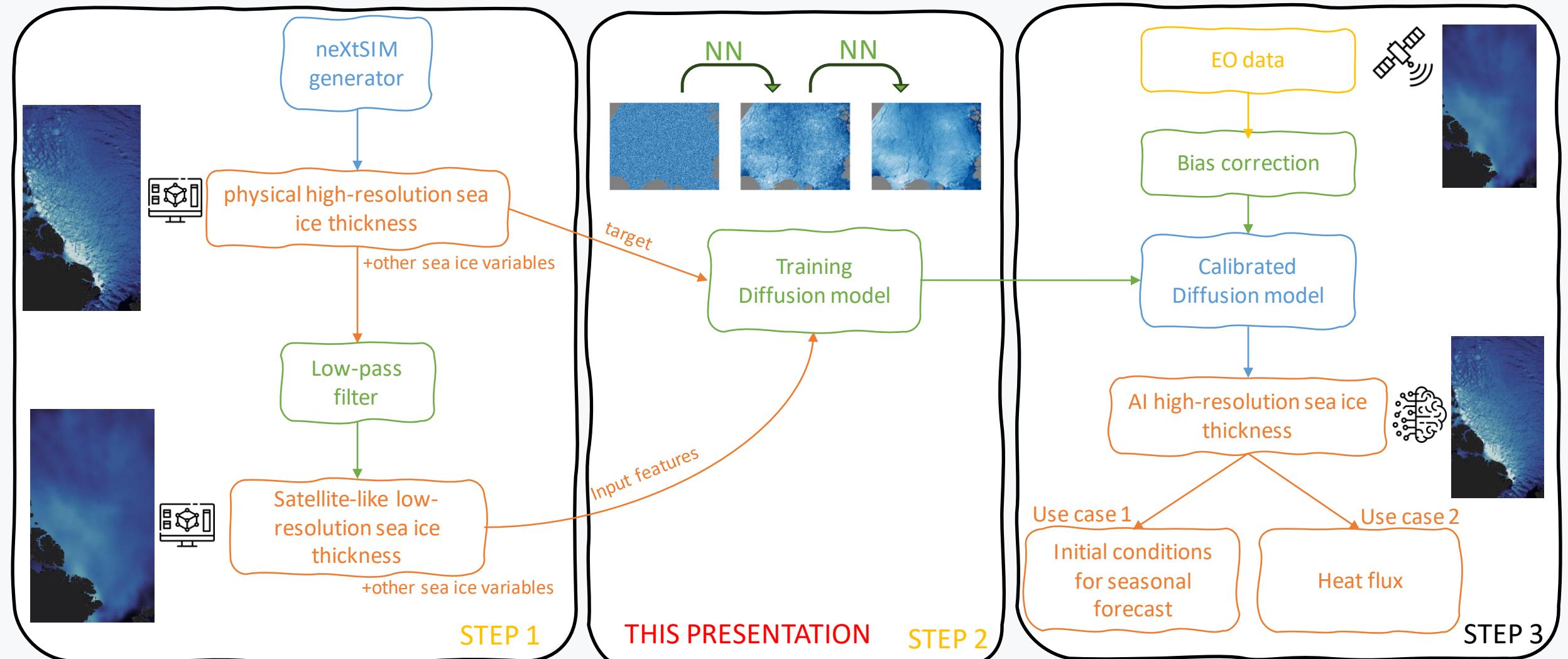
Black dot means not significant

Courtesy of N. Williams

Case 2: Surface fluxes



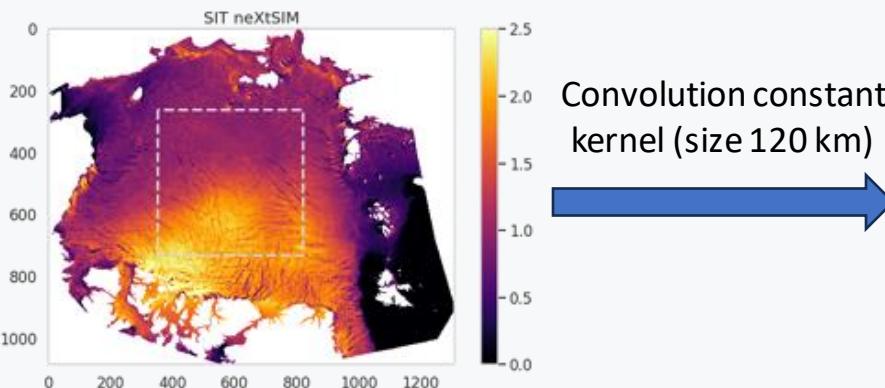
Overview of the project



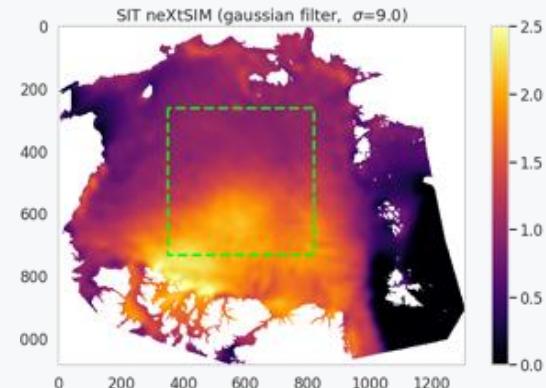
Step 1: Dataset constitution

Principle: Filtering of NeXtSIM simulations

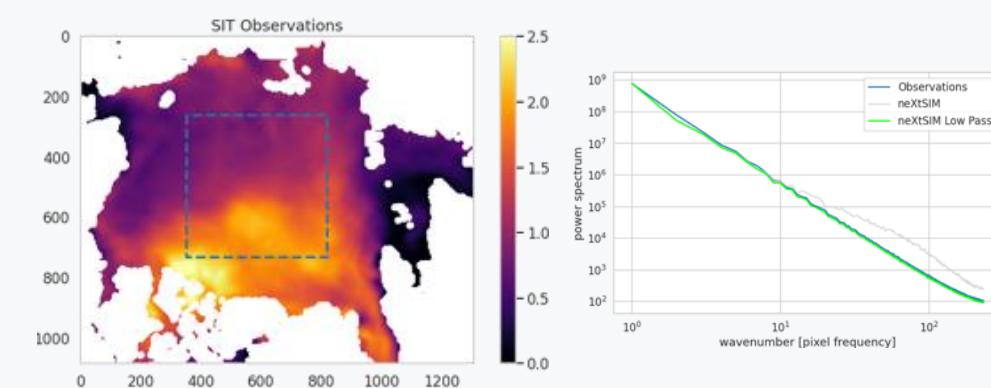
NeXtSIM sea ice thickness
01-01-2021 (res 3km)



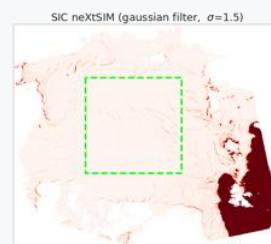
Filtered sea ice thickness
(res \sim 90 km)



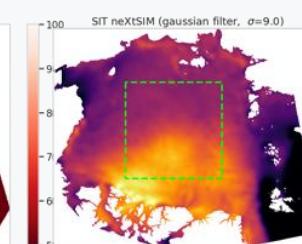
Observation product (CS2SMOS)
01-01-2021



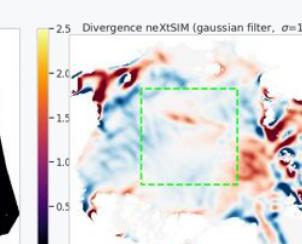
Concentration
(res \sim 15km)



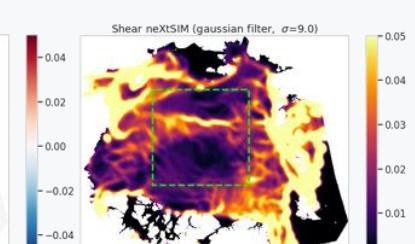
Thickness
(res \sim 90km)



Divergence
(res \sim 120km)



Shear
(res \sim 90km)



+ land mask
(res \sim 3km, no smoothing)

Dataset:

- 5 input features (low-pass filtered) 1086x1308
- 529 samples, from 18-10-2013 to 15-04-2023 (Only Oct-Apr)
- Training: 2013-> Apr. 2020 (1157 samples)
- Validation/test Oct. Oct. 2020-> 2023 (540 samples)

Apply diffusion model to sea ice thickness super-resolution

Used for AI image generator (Ex: Midjourney)

A prompt

“man walking dog at dusk --ar 4:3”

Generative
diffusion model



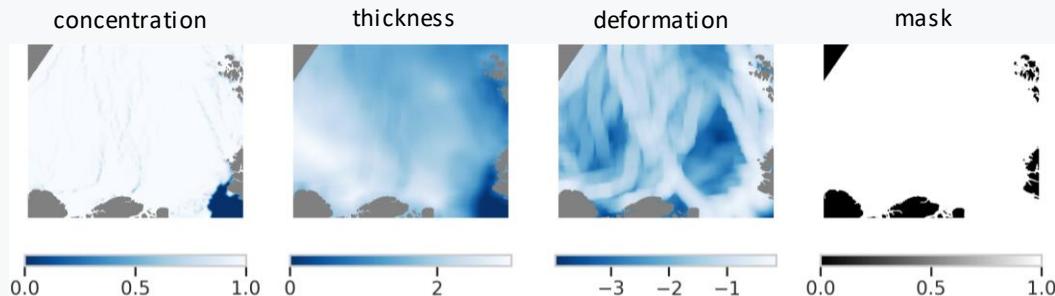
A generated image



Apply diffusion model to sea ice thickness super-resolution

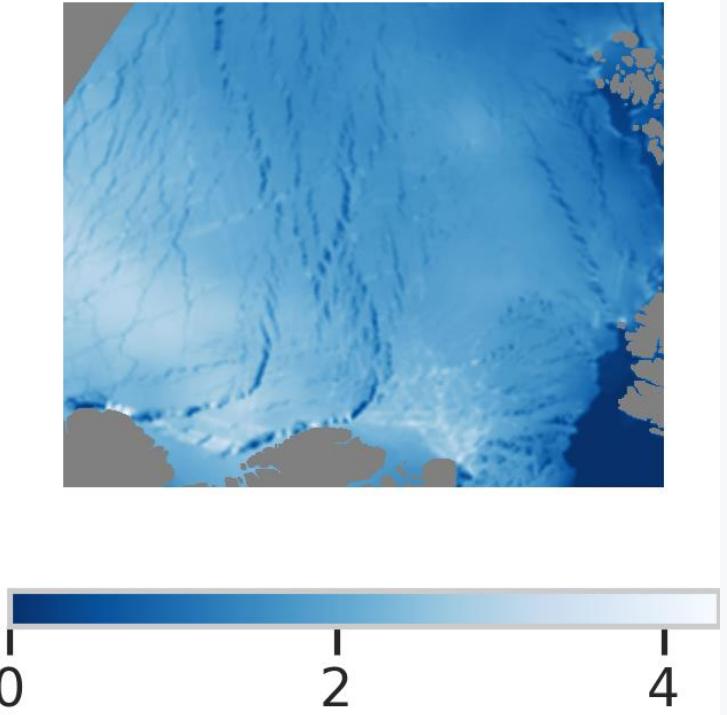
Used for AI image generator (Ex: Midjourney)

Observable low-resolution images

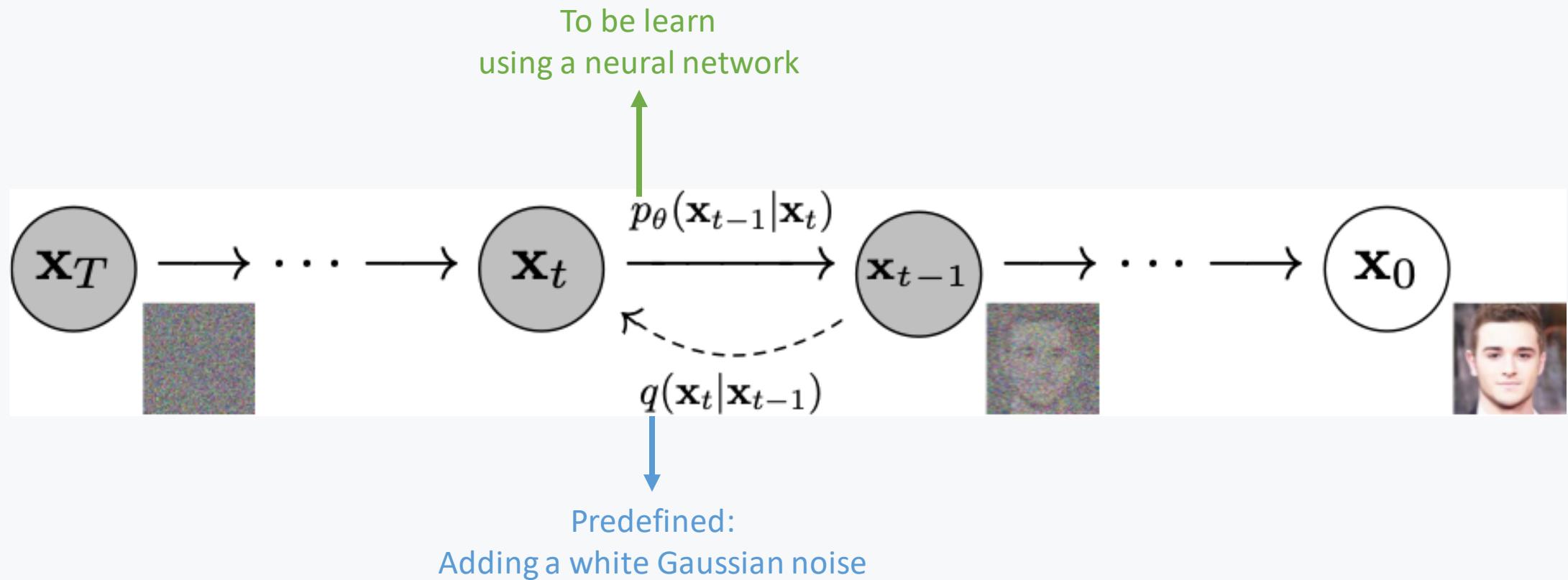


Generative
diffusion model

A generated high-resolution image

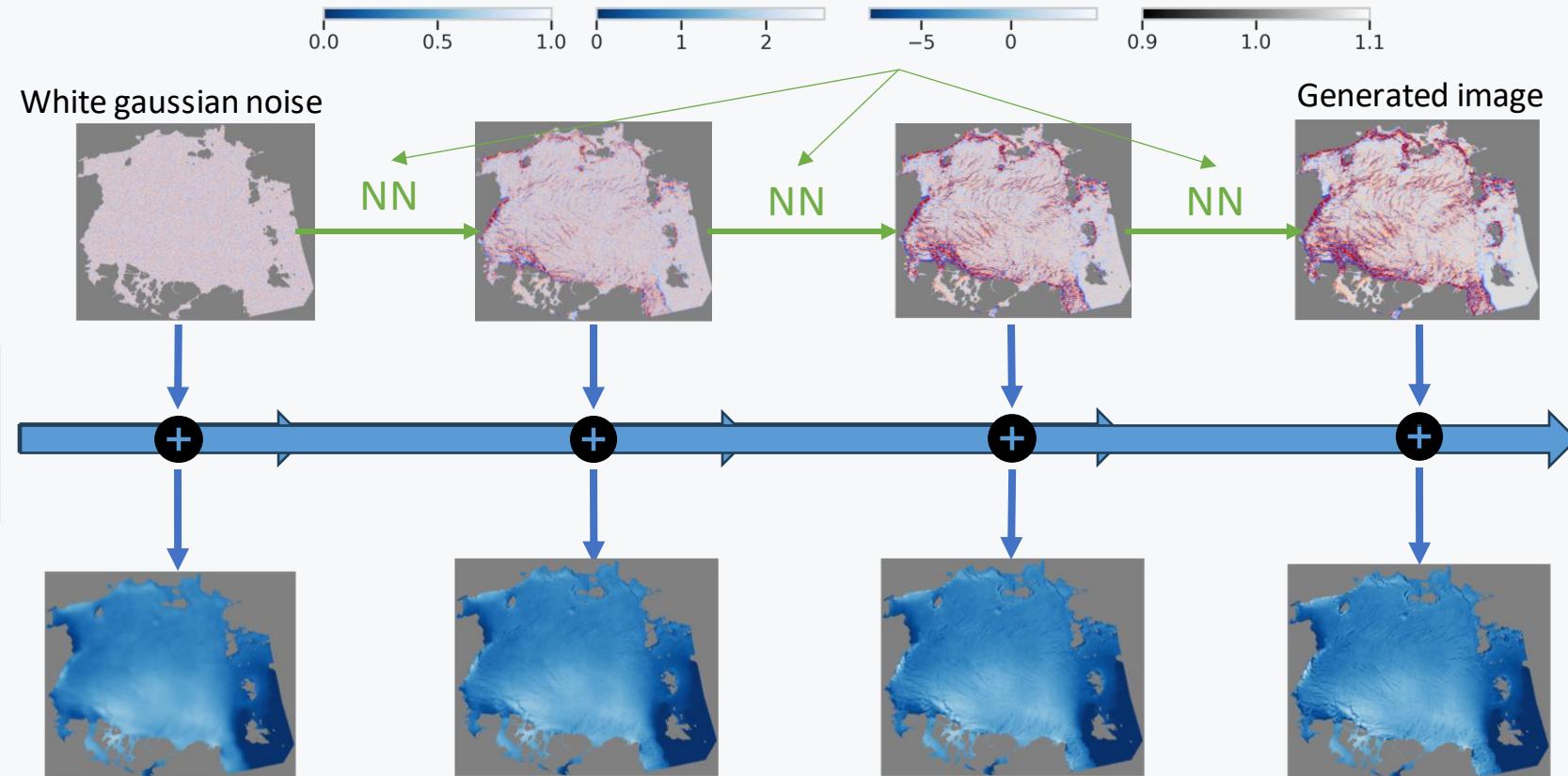
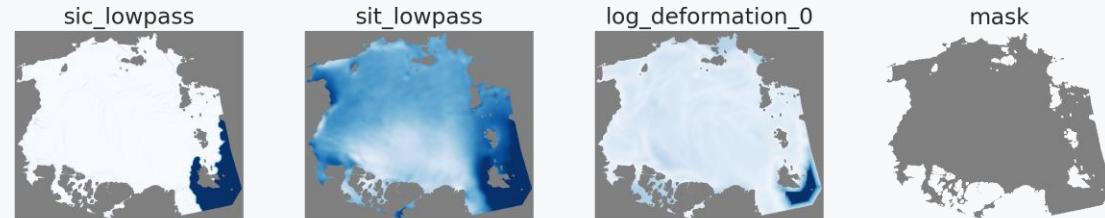


Principle of the diffusion model

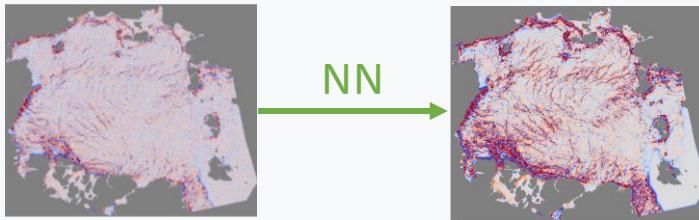


Principle of the diffusion model in SuperIce

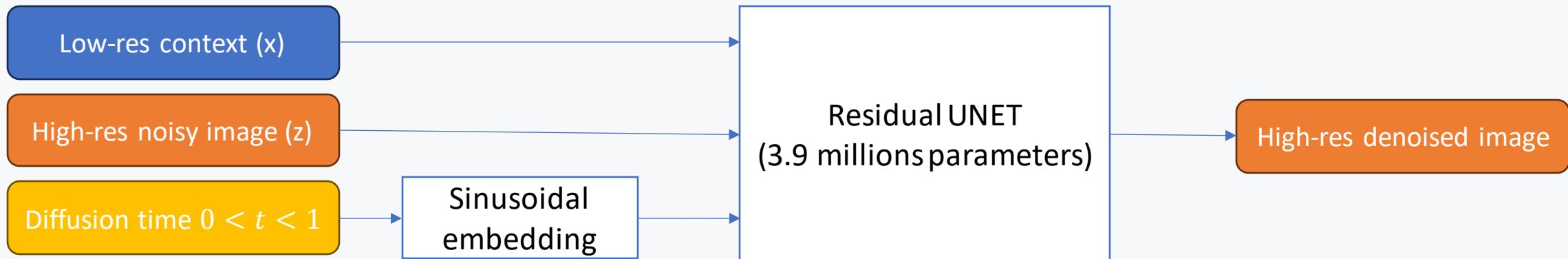
The low-resolution “context”
(low-resolution fields)



Implementation details



Model Residual Neural network $f(x,z,t)$



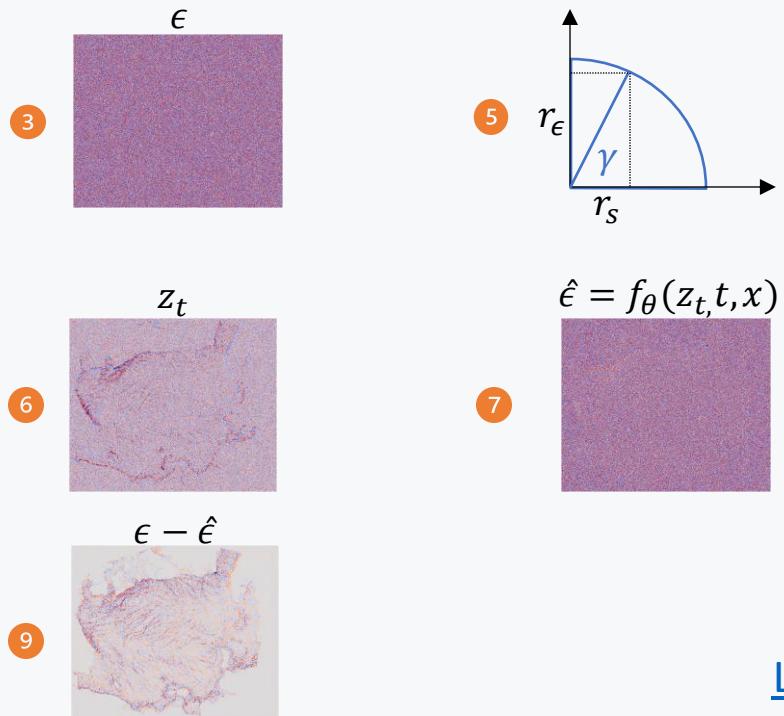
Training algorithm



$\tau \epsilon$

For one sample

1. Draw a HR image y and a LR context x in the training set
2. Draw a diffusion time t between 0 (full signal) and 1 (full noise)
3. Draw a white Gaussian noise ϵ
4. Compute diffusion angle: $\gamma = \gamma_{min} + t \cdot (\gamma_{max} - \gamma_{min})$
5. Compute the signal and noise rate: $r_s = \cos \gamma, r_\epsilon = \sin \gamma$
6. Compute the noisy image: $z_t = r_s \cdot y + r_\epsilon \cdot \epsilon$
7. Predict the noise by the NN: $\hat{\epsilon} = f_\theta(z_t, t, x)$
8. Predict the image: $\hat{z}_{t-1} = (z_t - r_\epsilon \cdot \hat{\epsilon}) / r_s$
9. Compute the loss on the noise: $L(\theta) = \|\epsilon - \hat{\epsilon}\|^2$
10. Minimize L



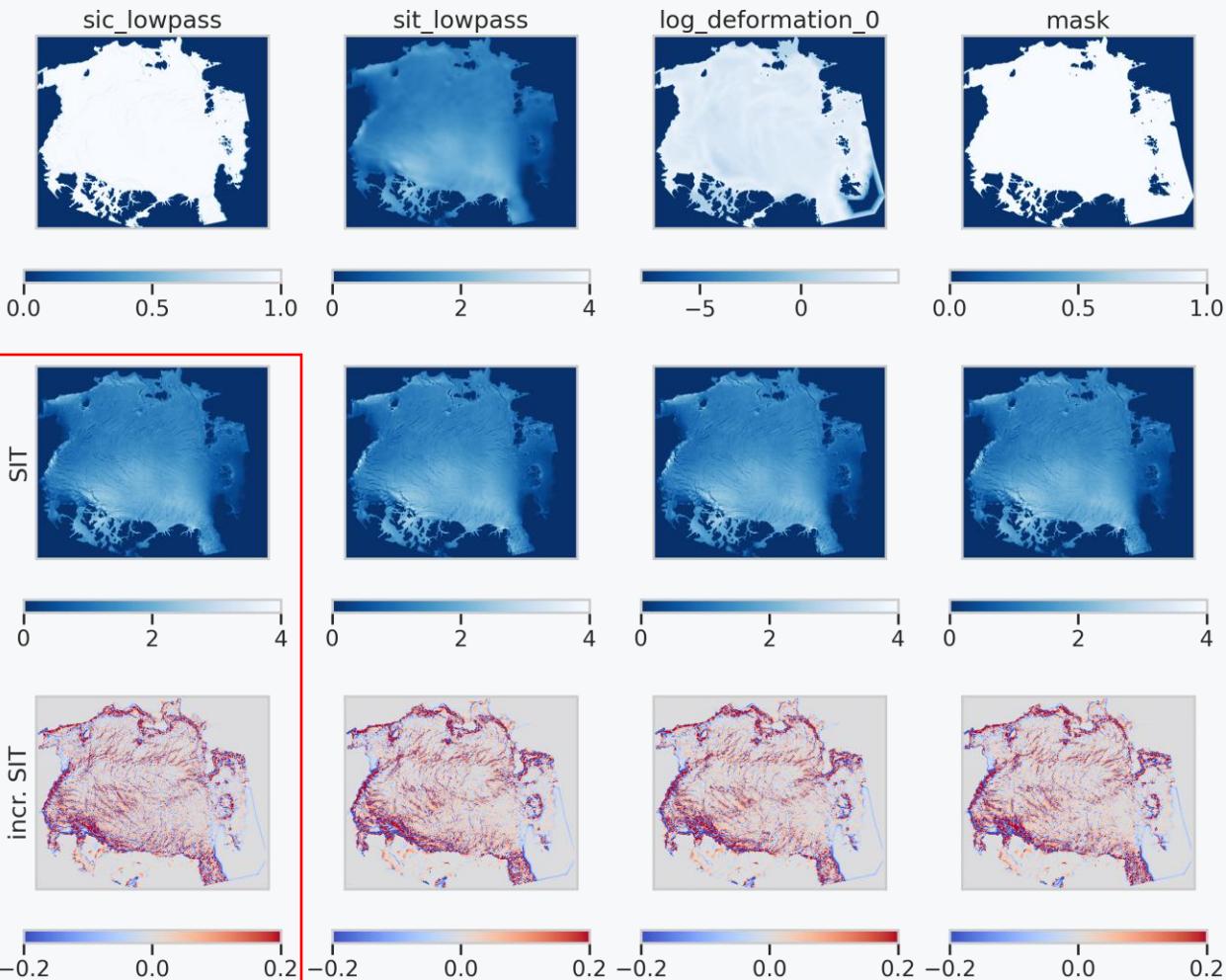
Learning curve

Results

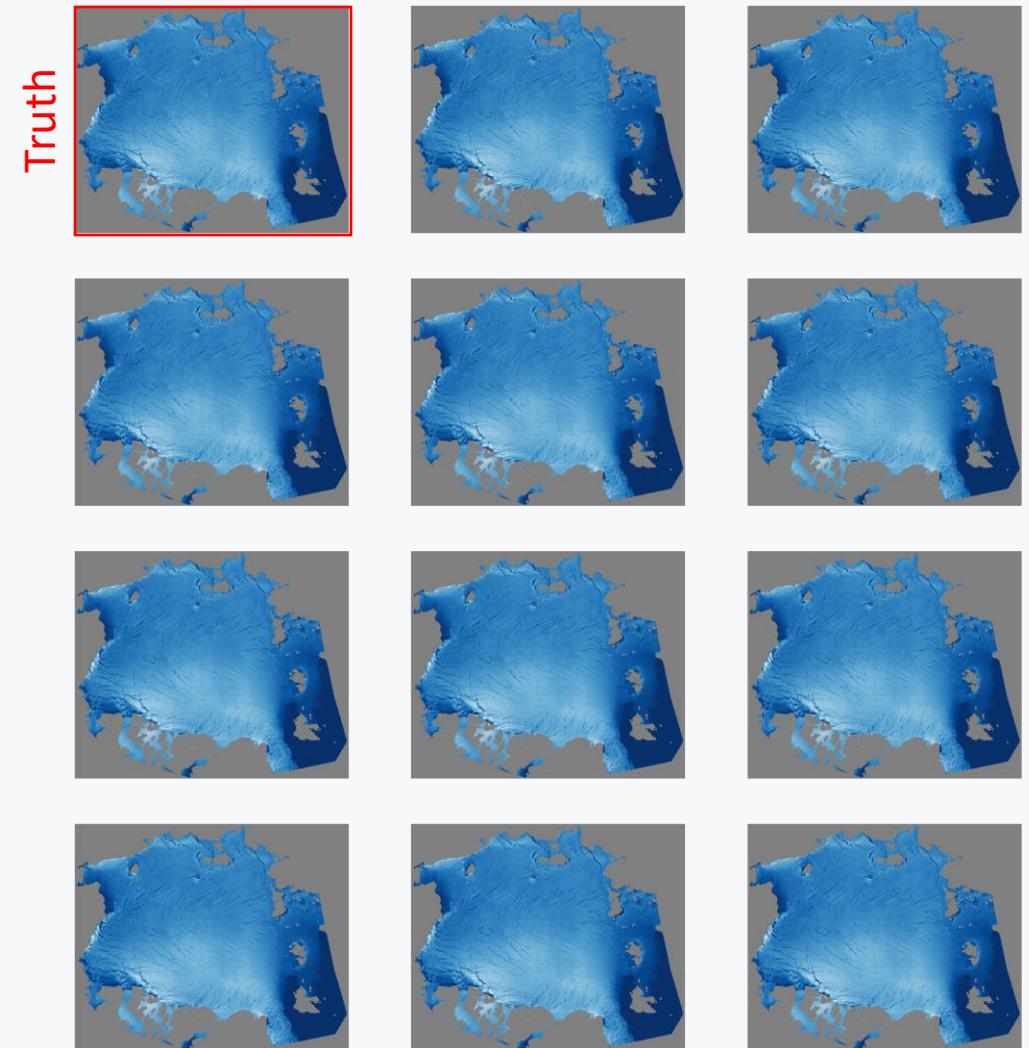
- ✓ Results of the 10 January 2021
- ✓ Results of the 23 October 2020
- ✓ Global results

Results of 26 January 2021

Generation of high-res SIT and residuals

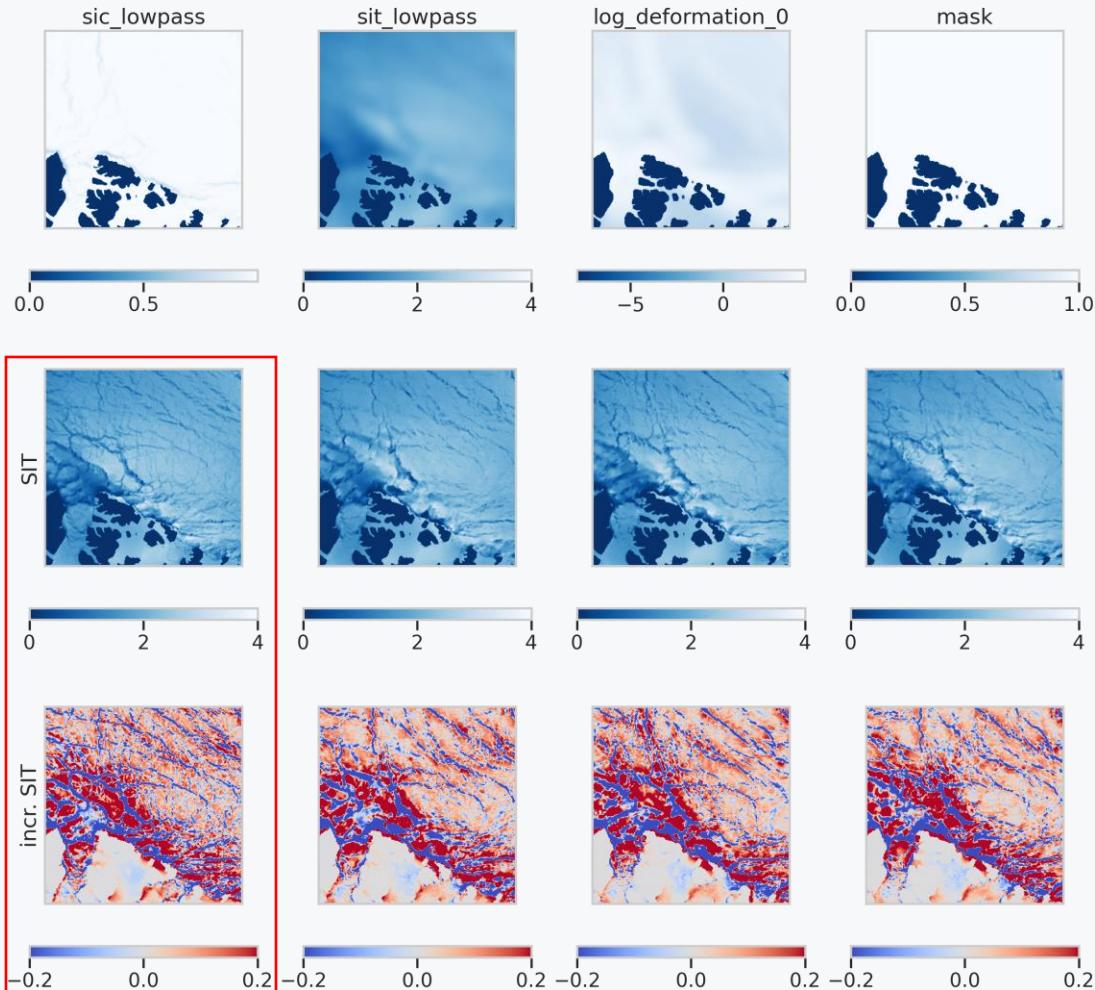


Generation of an ensemble

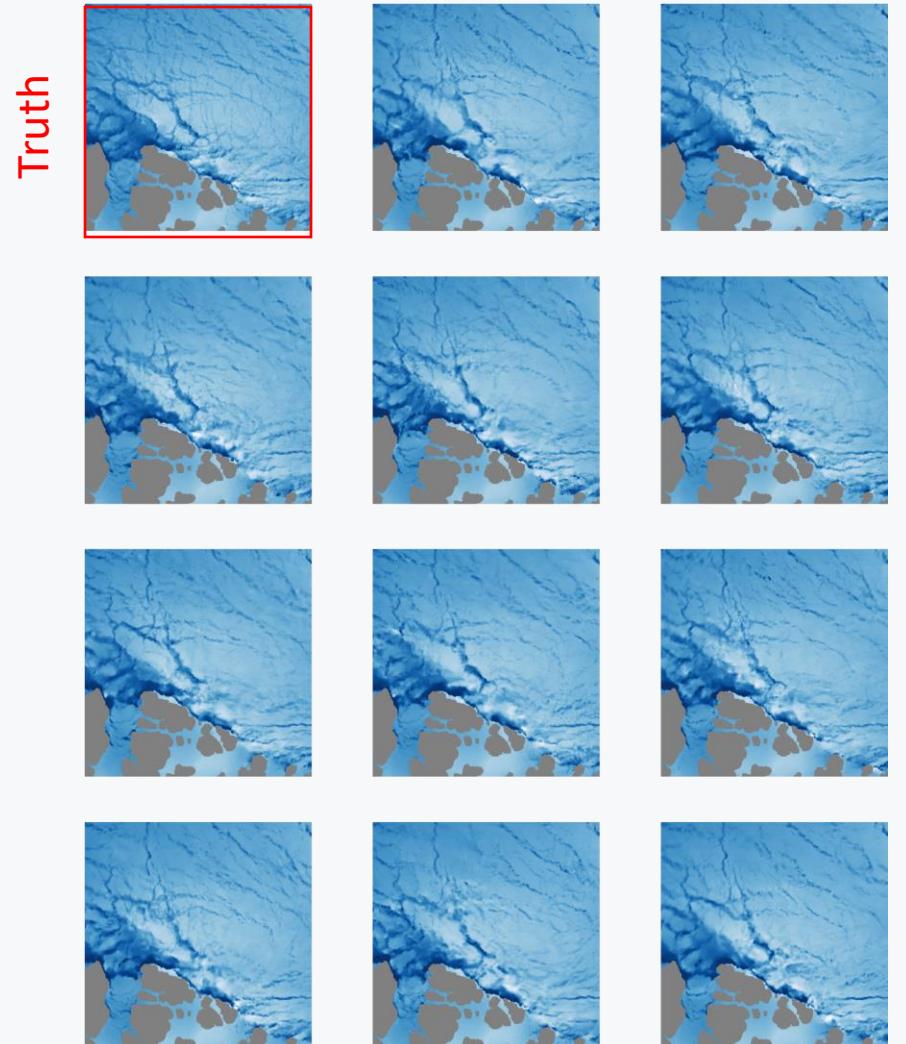


Results of 26 January 2021 (zoom)

Generation of high-res SIT and residuals

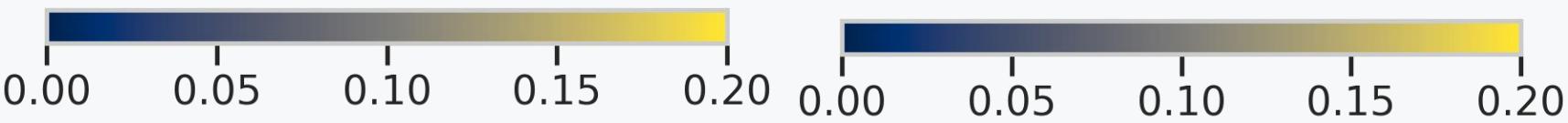
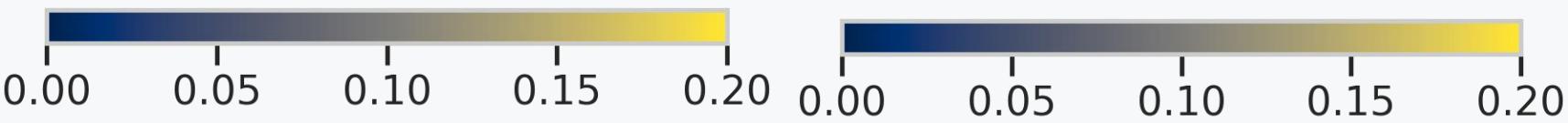
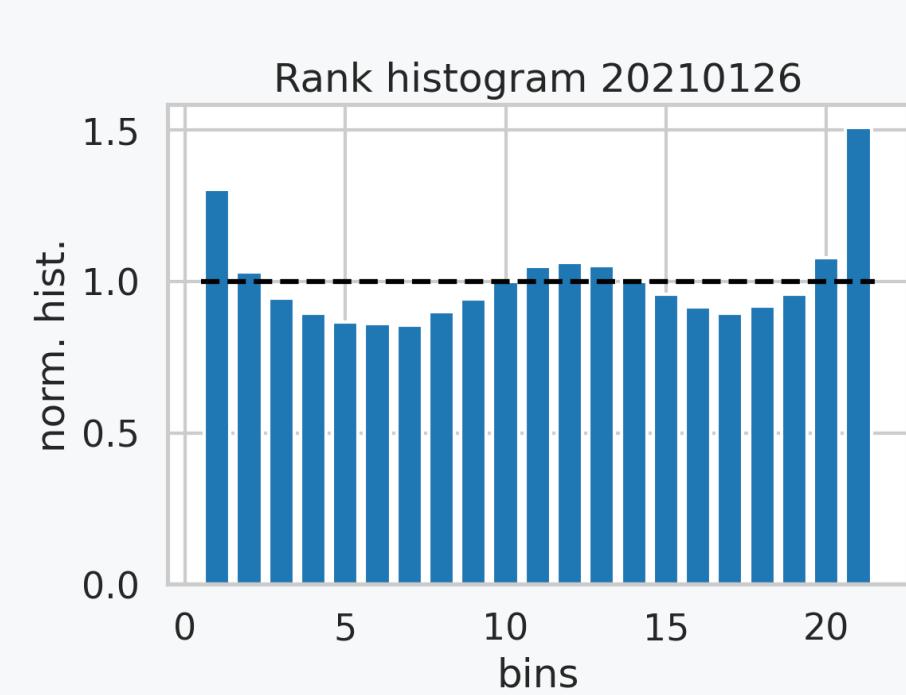
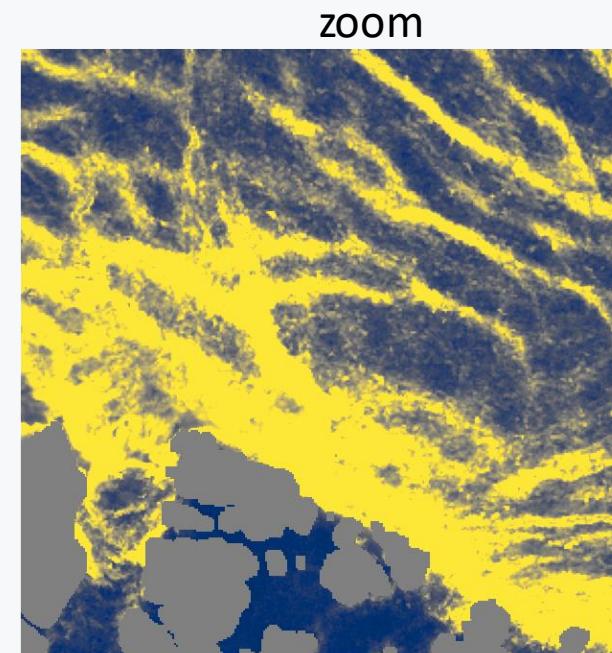
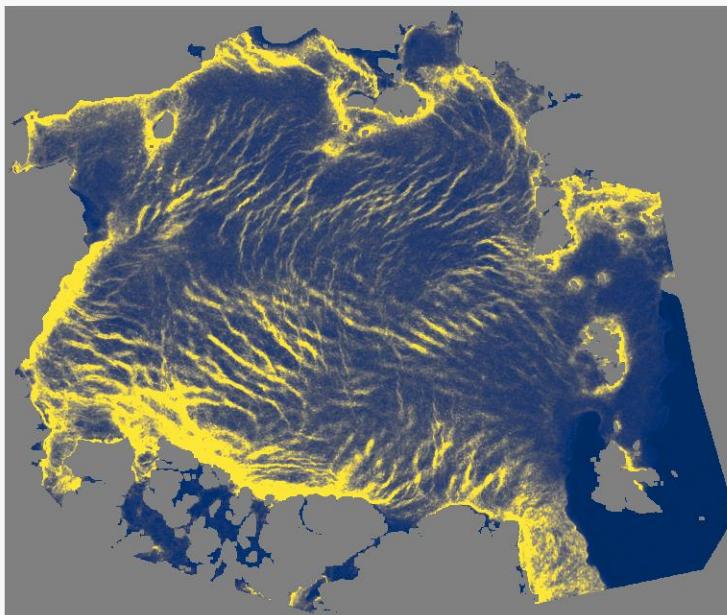


Generation of an ensemble



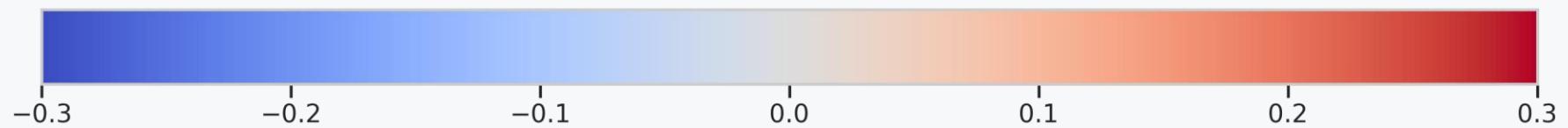
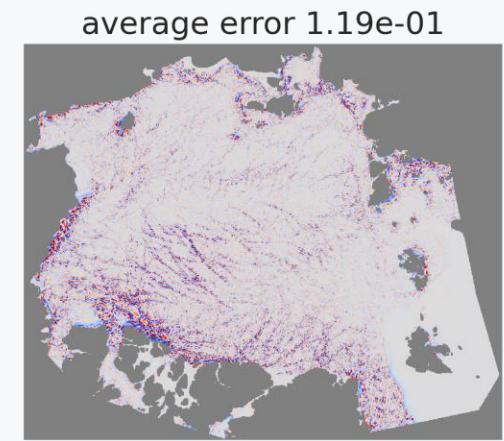
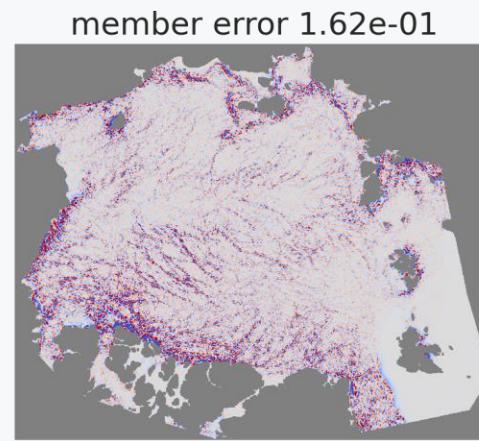
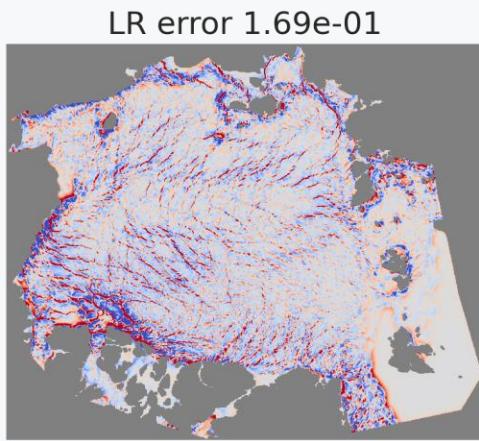
Results of 26 January 2021

Spread and reliability

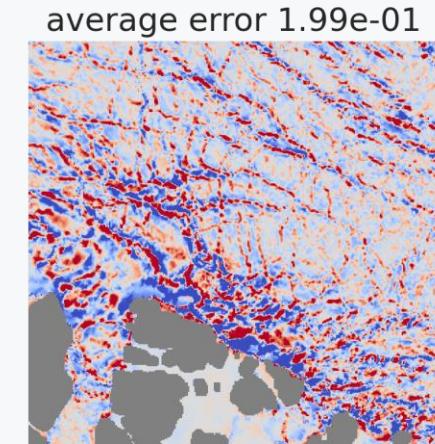
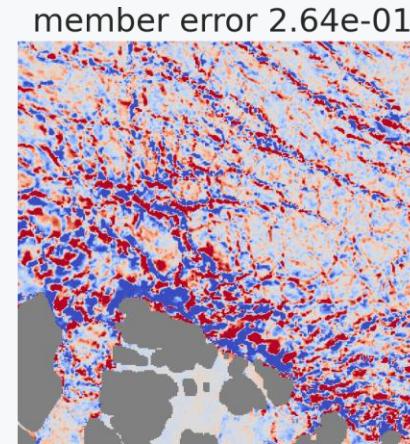
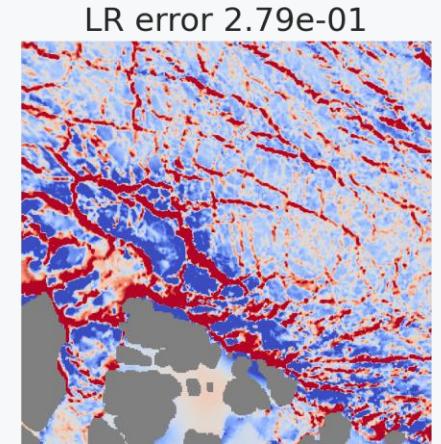


Results of 26 January 2021

Accuracy

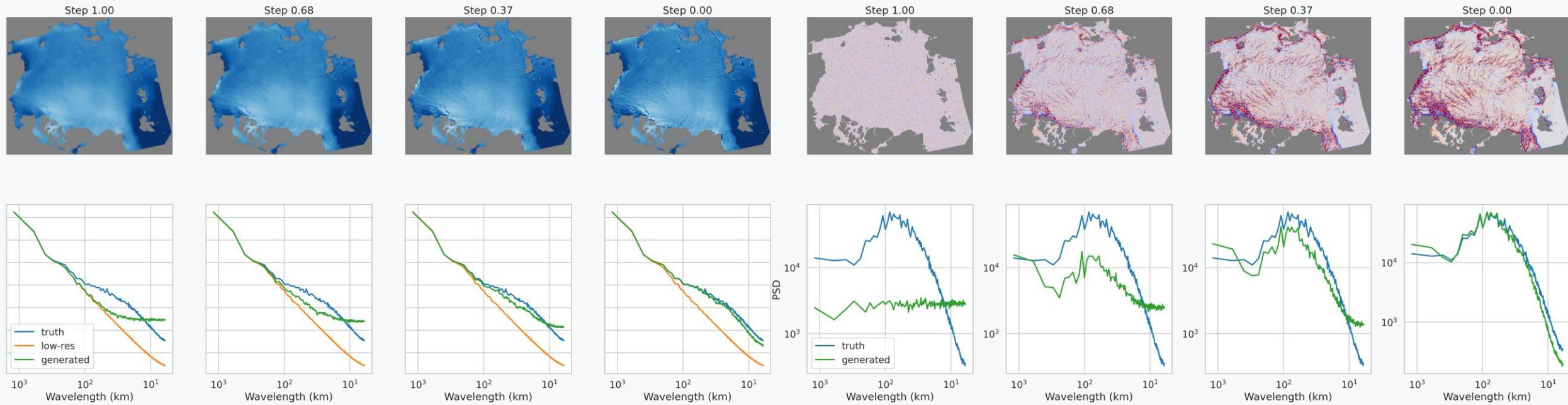


zoom



Spectrum 26 January 2021

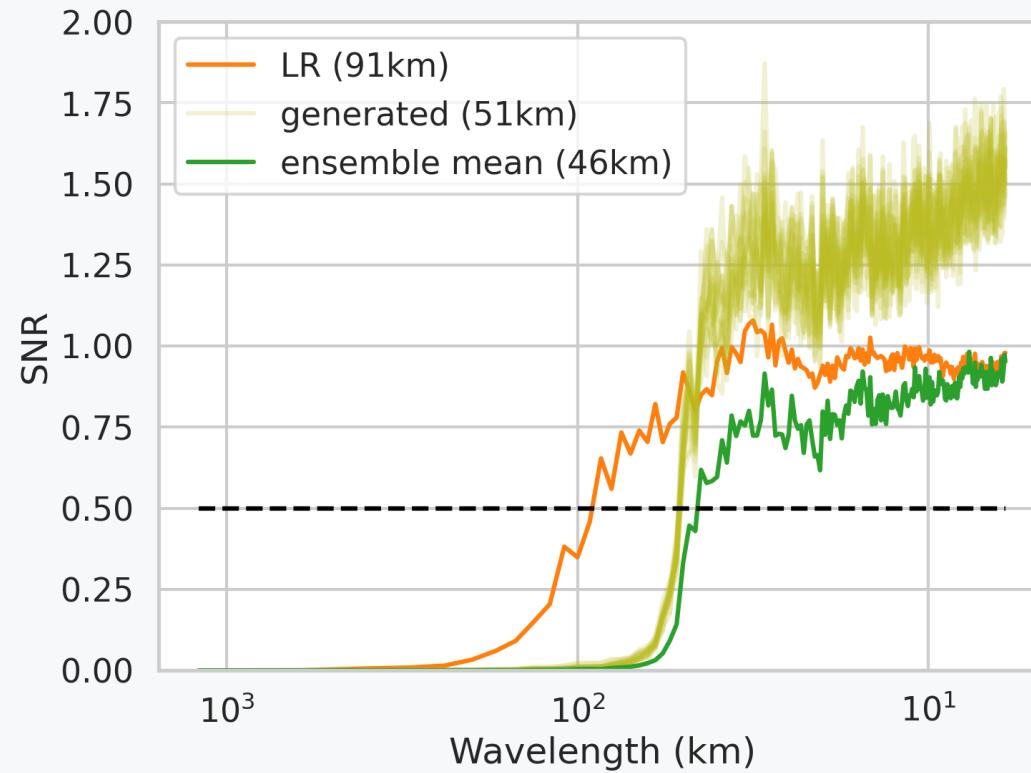
Power Spectrum Density as a function of the diffusion time (Step)



Spectrum

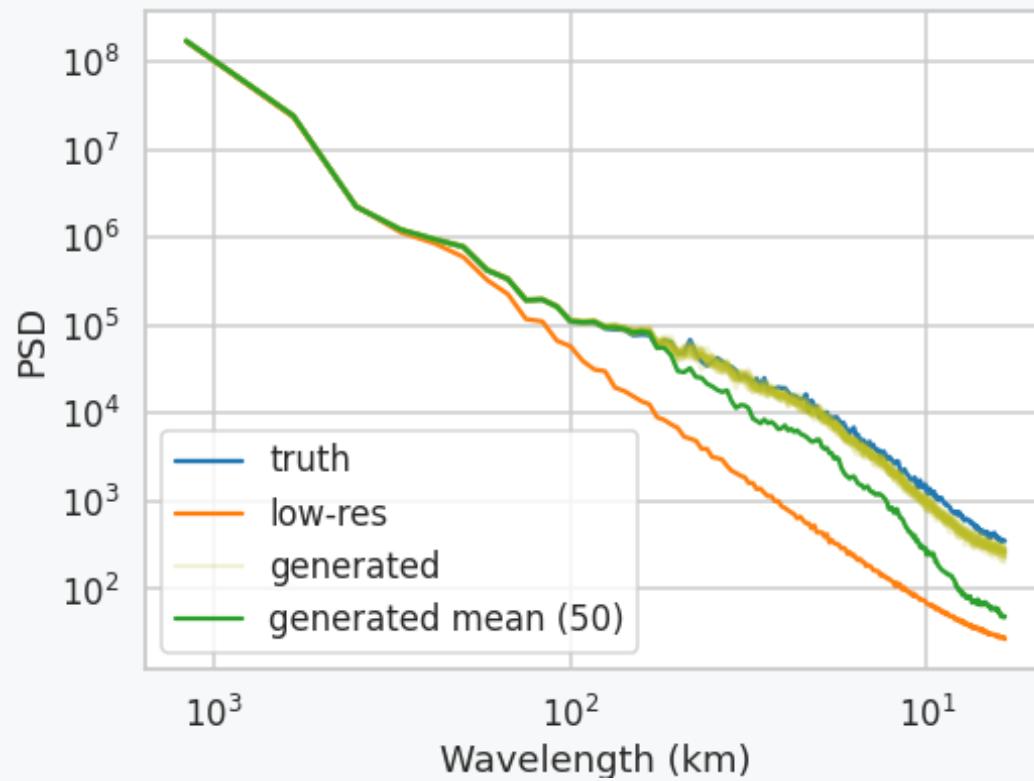
Signal to noise

Spectral ratio = PSD (reconstruction-truth) / PSD(truth)

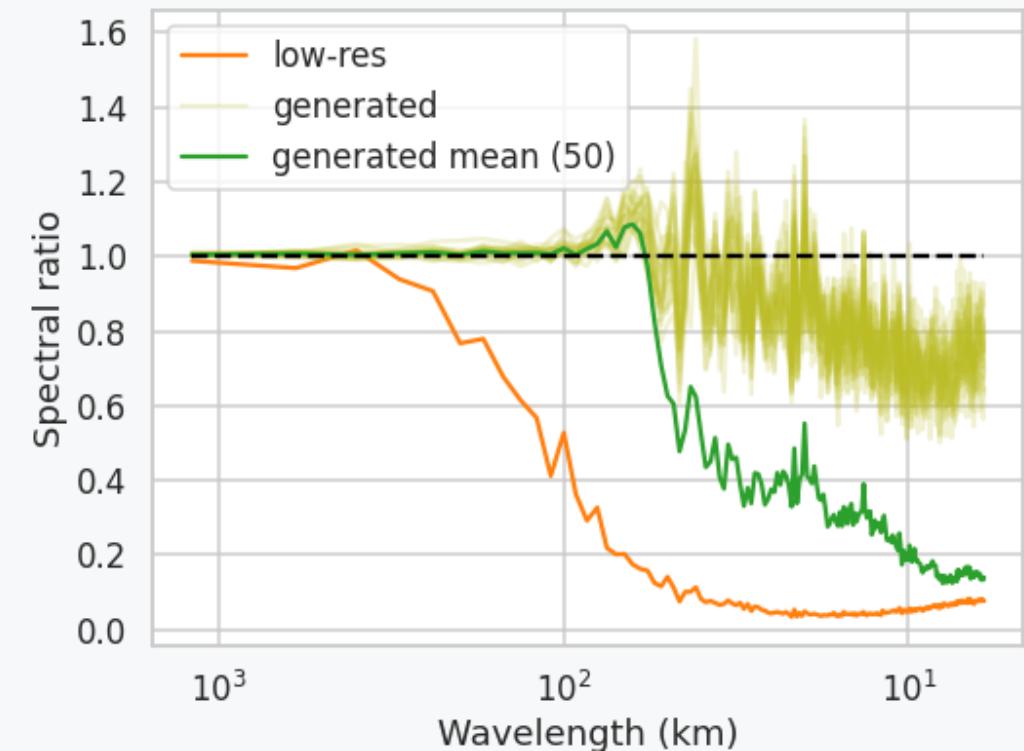


Spectrum

Power Spectrum Density

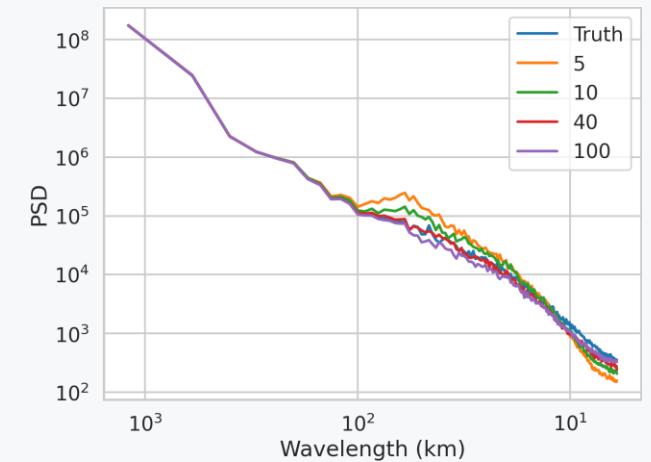
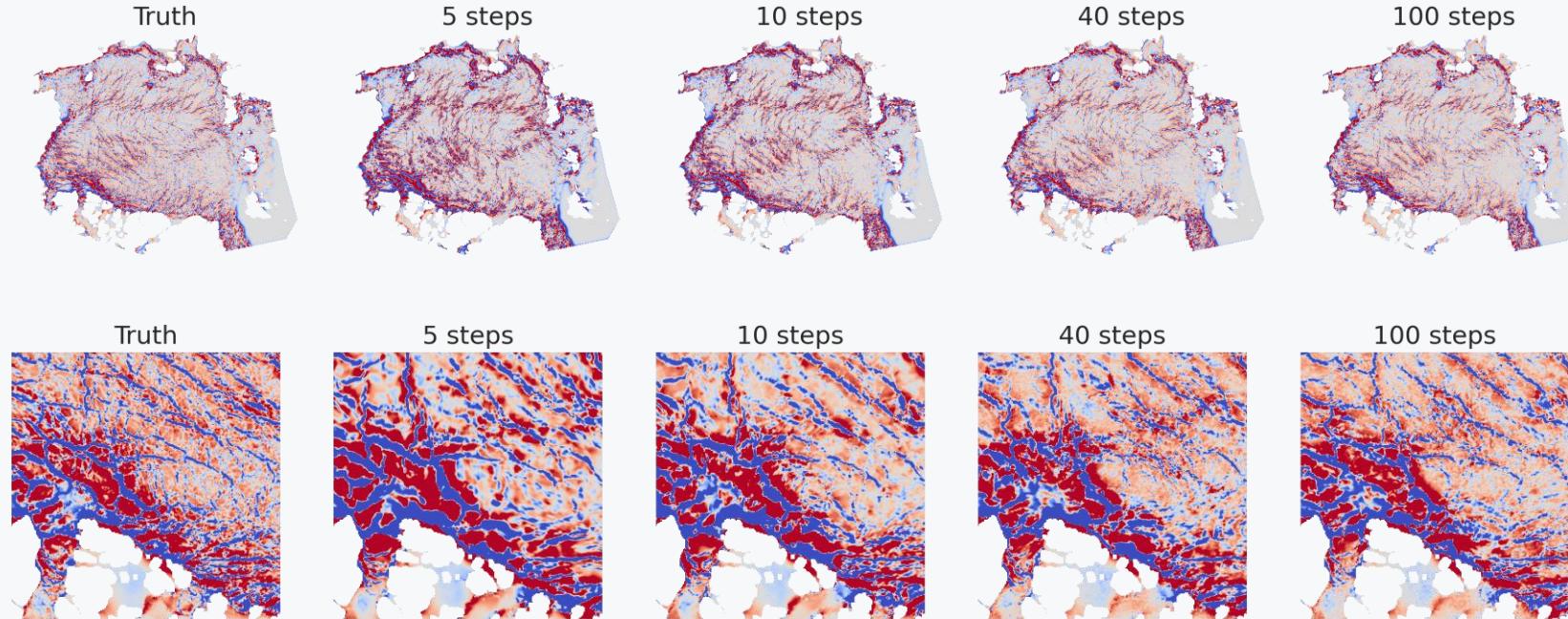


Spectral ratio = PSD-reconstruction / PSD-truth



Sensitivity to the number of diffusion steps

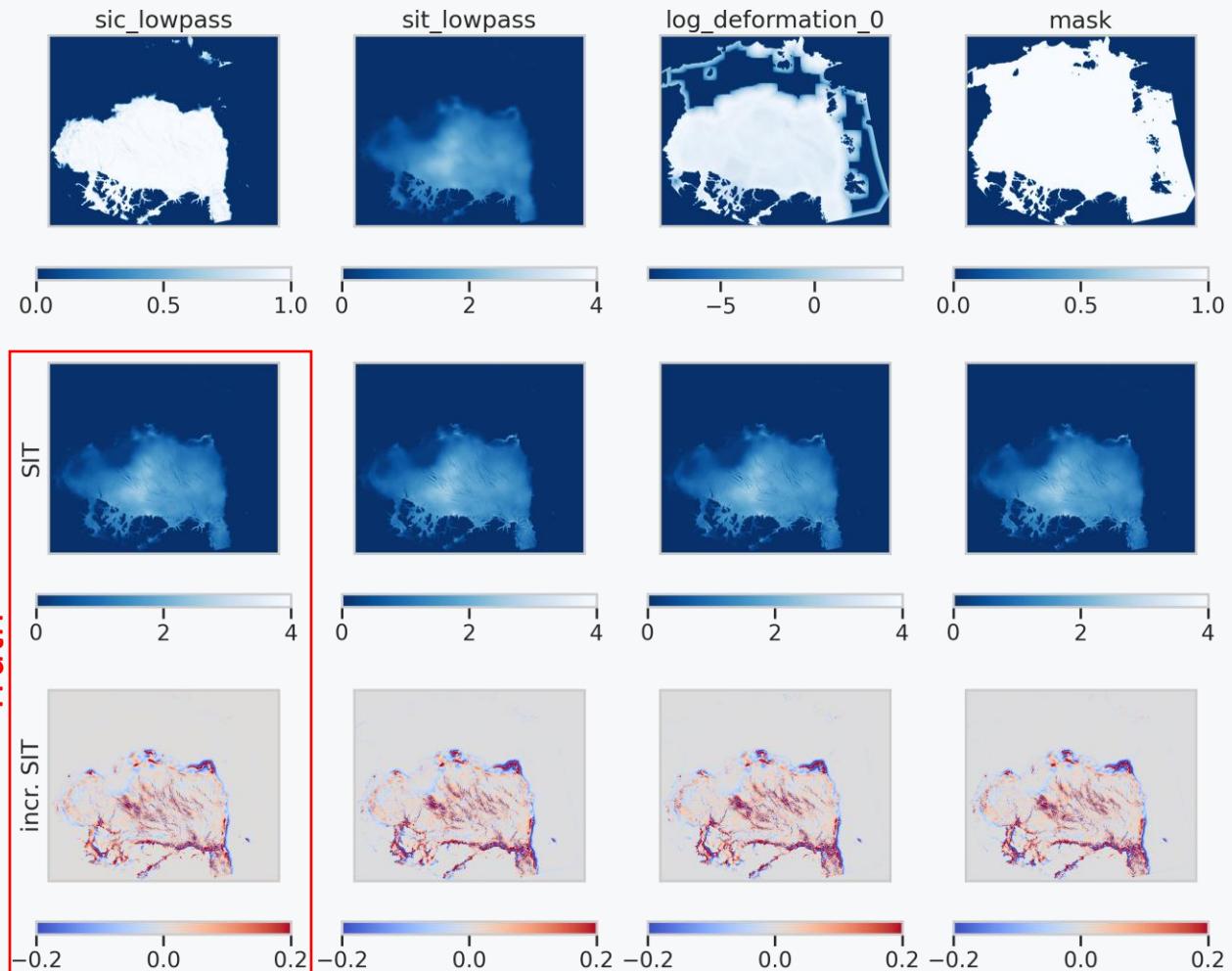
Zoom



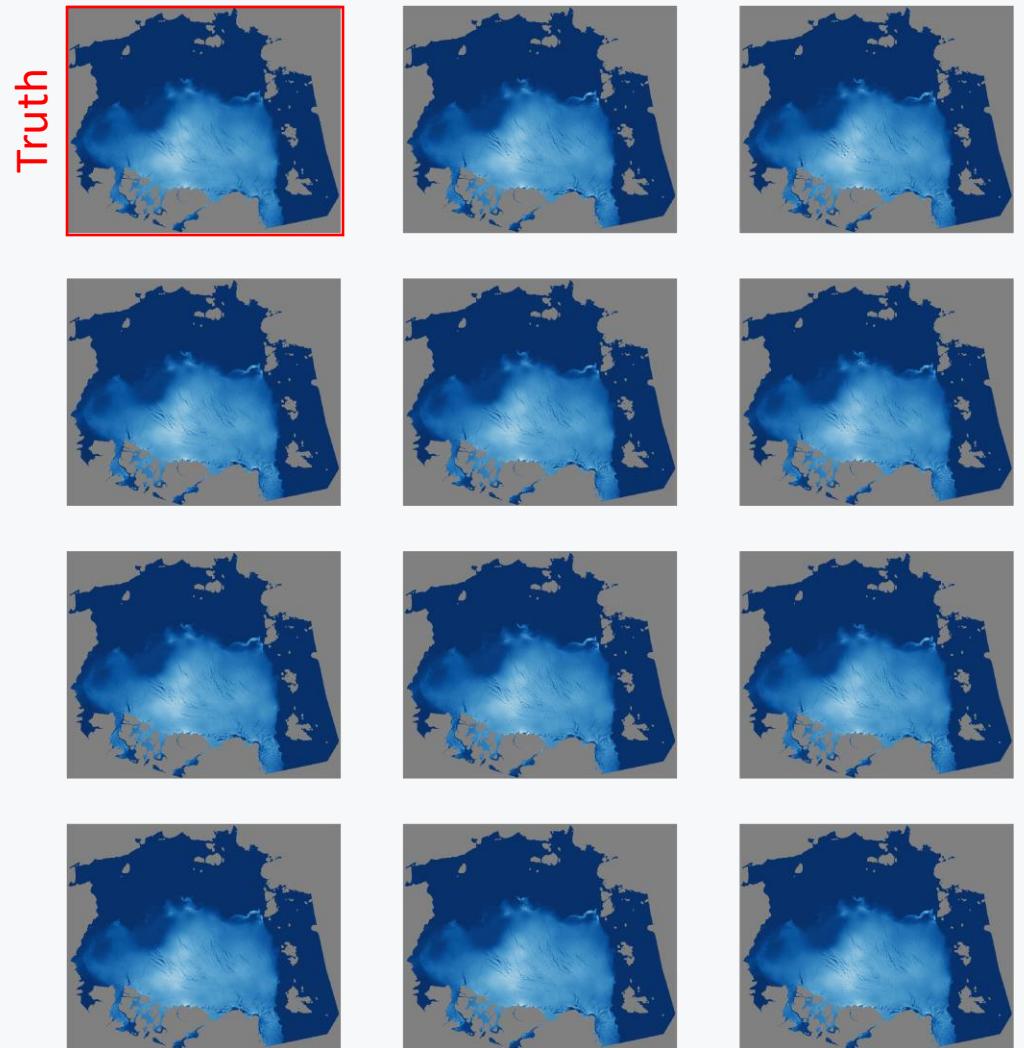
In the other sections, 40 steps are used

Results of 23 October 2020

Generation of high-res SIT and residuals

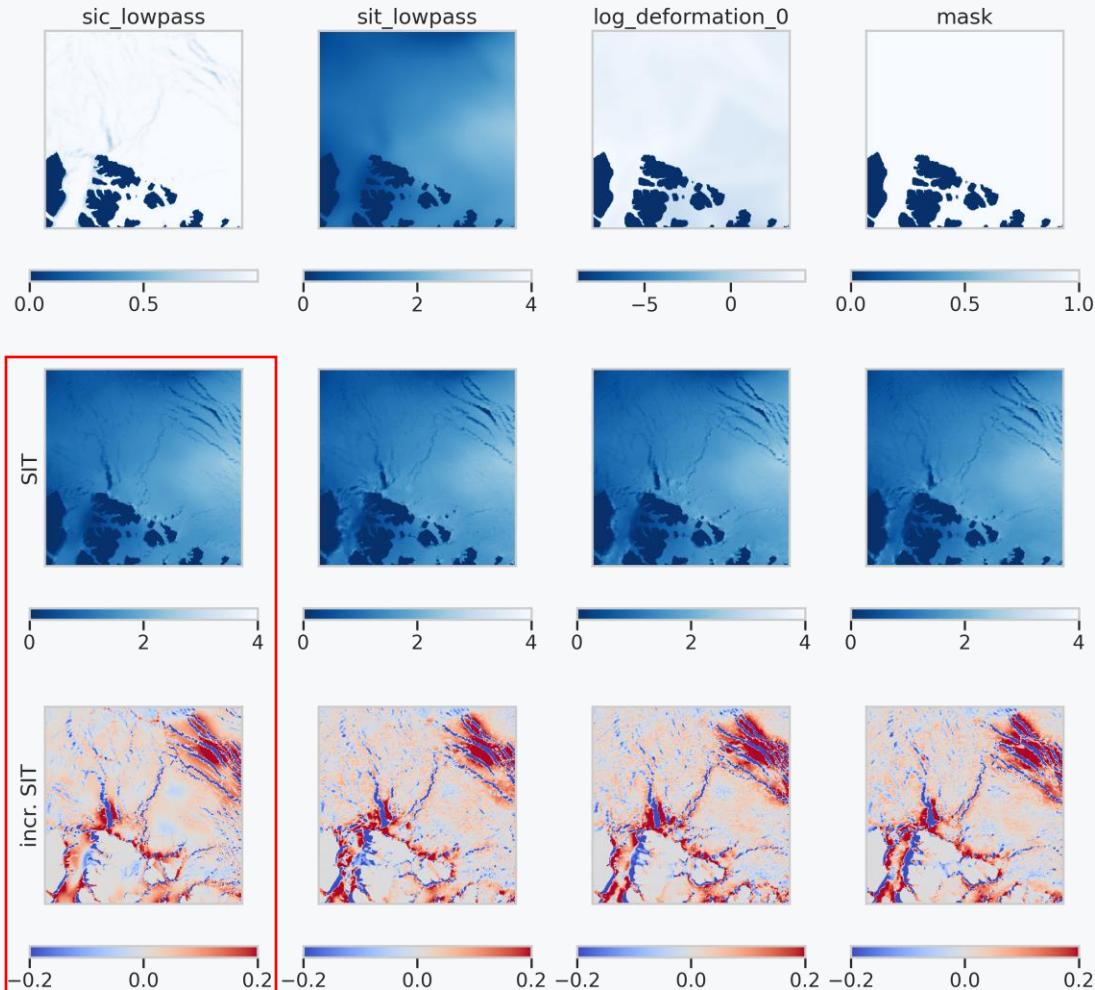


Generation of an ensemble

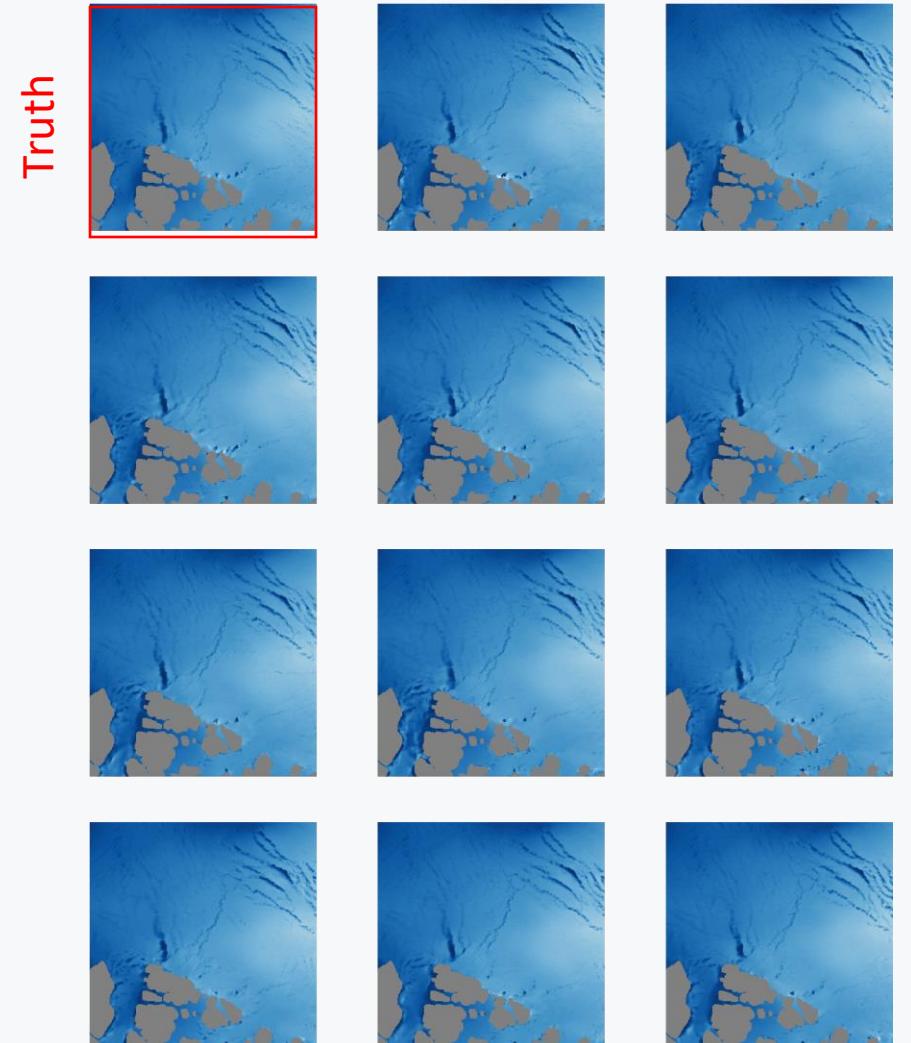


Results of 23 October 2020 (zoom)

Generation of high-res SIT and residuals

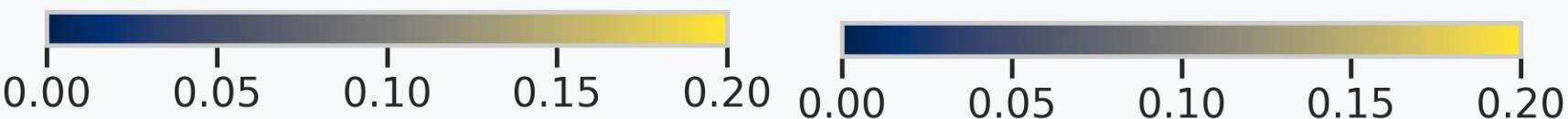
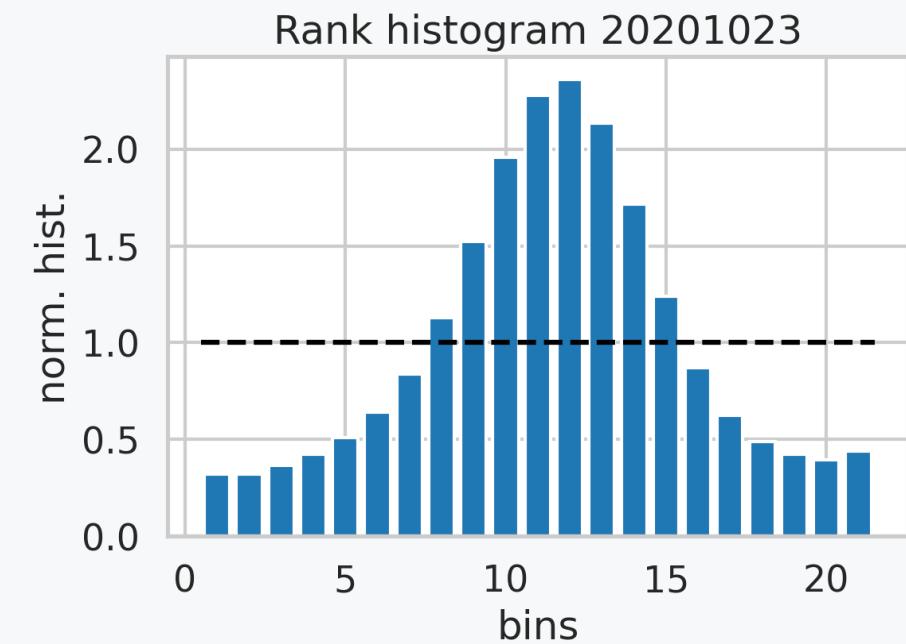
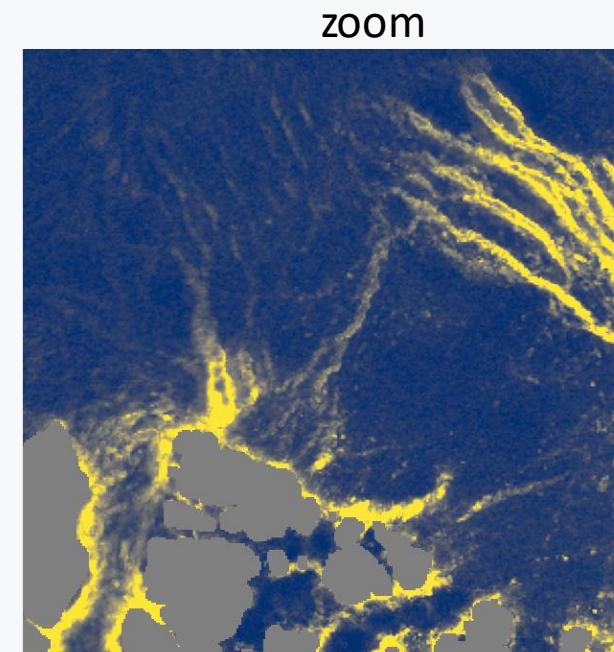
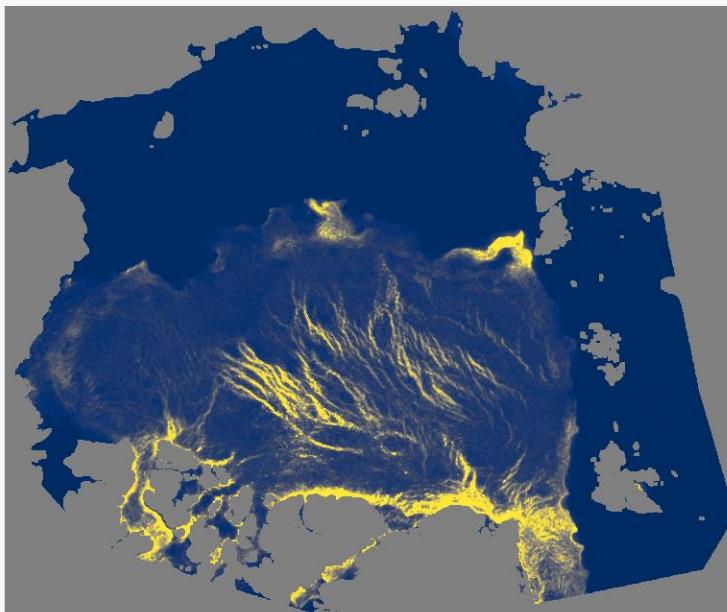


Generation of an ensemble



Results of 23 October 2020

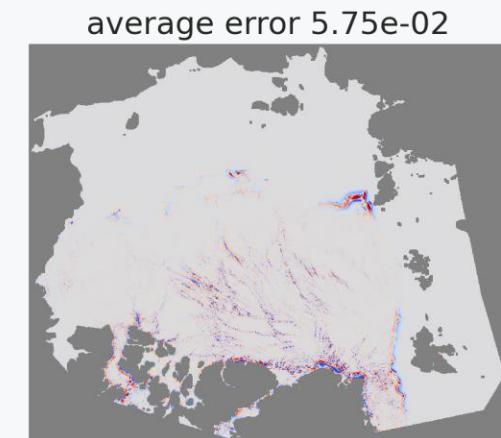
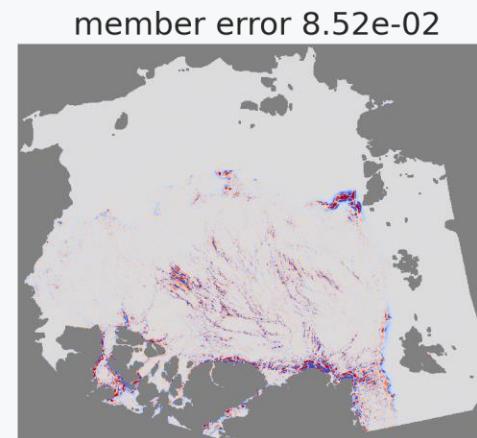
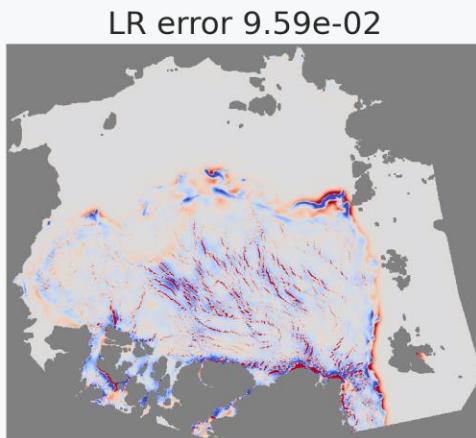
Spread and reliability



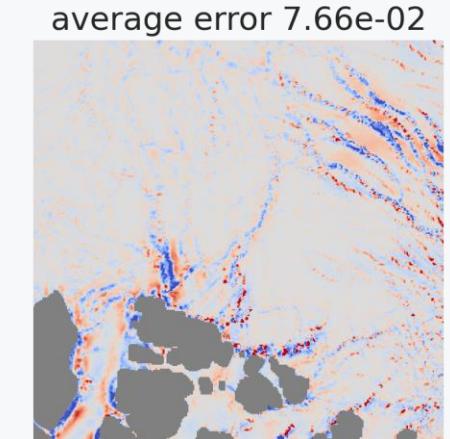
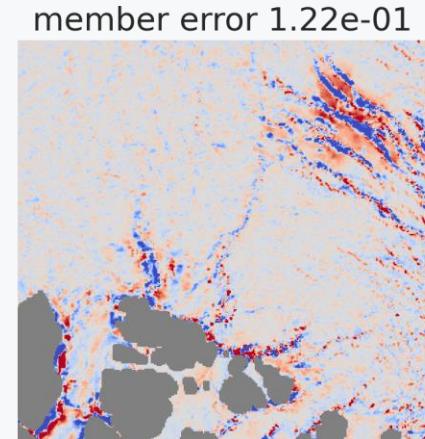
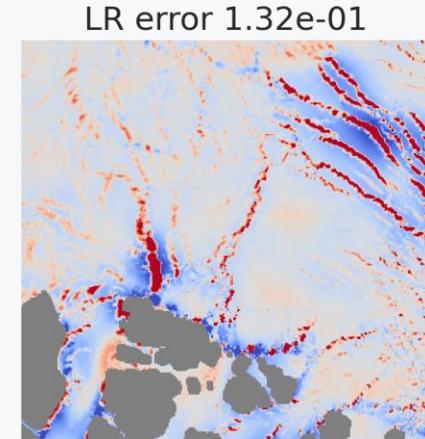
Ensemble over-dispersive

Results of 23 October 2020

Accuracy

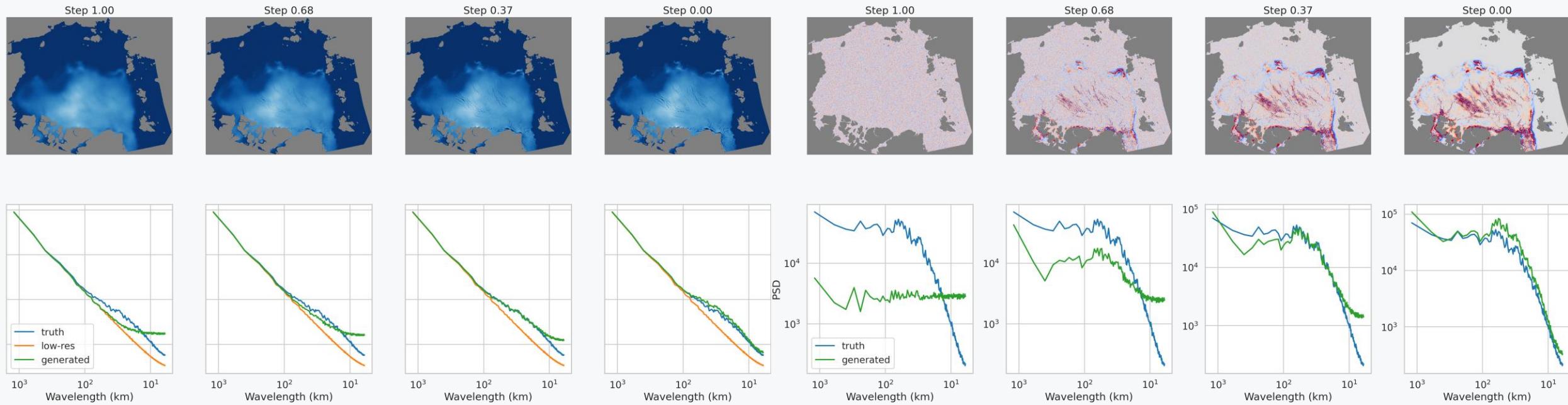


zoom



Spectrum 23 October 2020

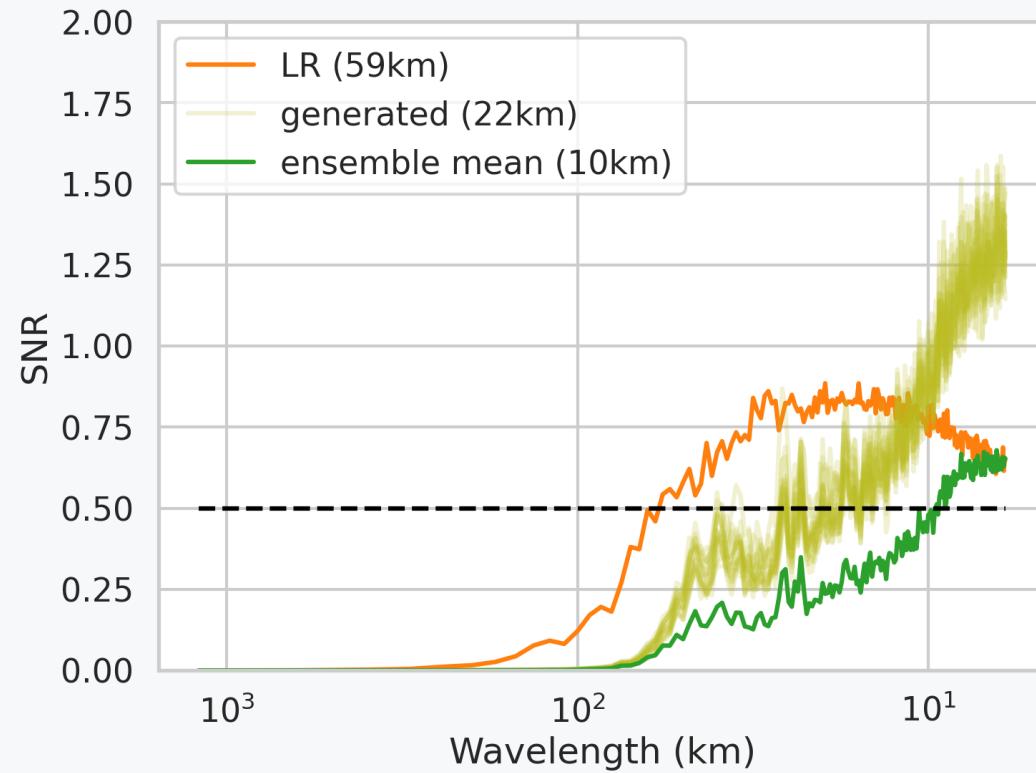
Power Spectrum Density as a function of the diffusion time (Step)



Spectrum

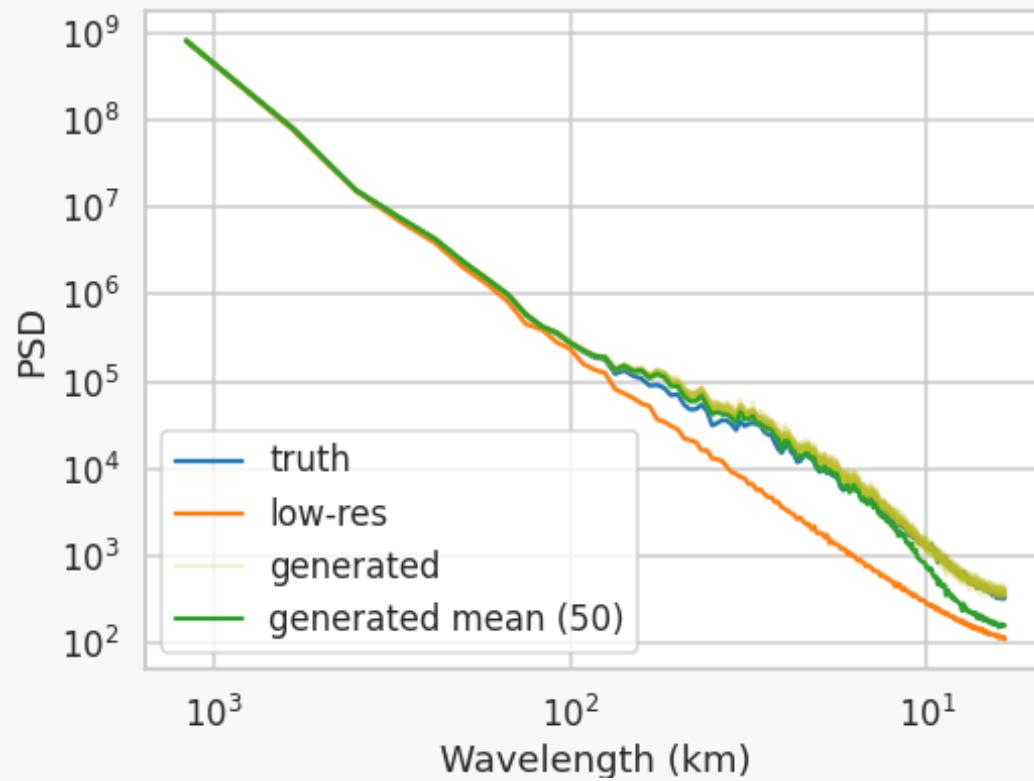
Signal to noise

Spectral ration = PSD (reconstruction-truth) / PSD(truth)

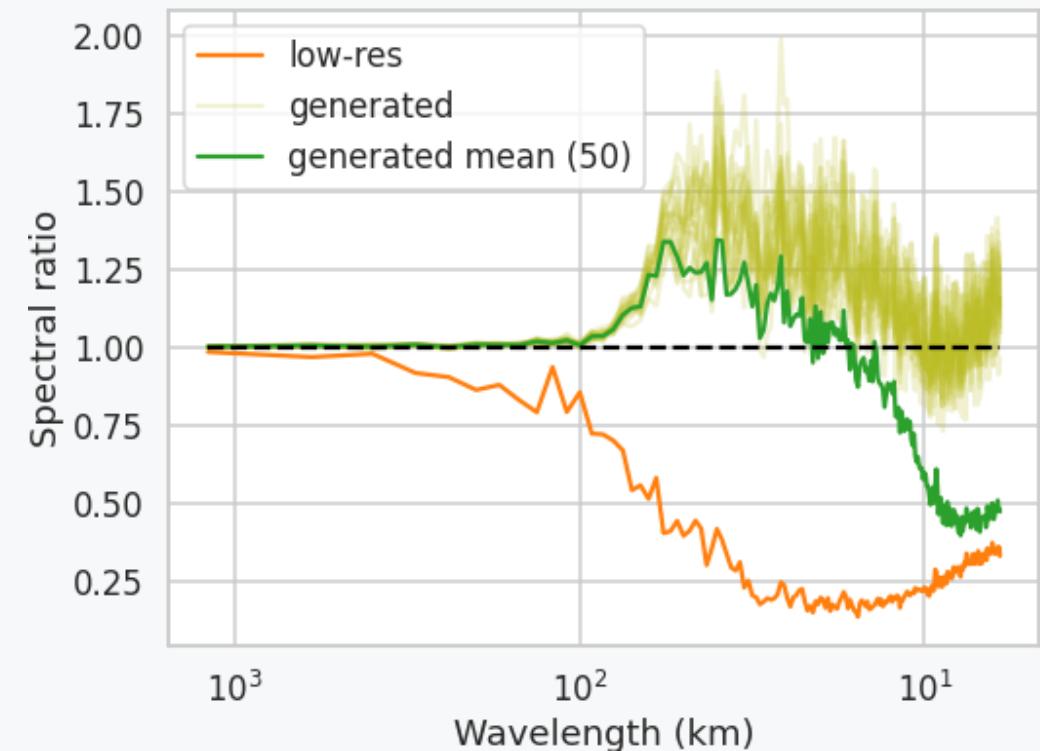


Spectrum

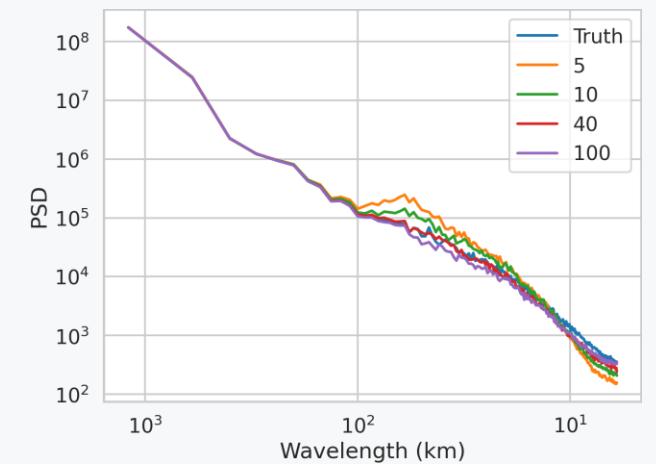
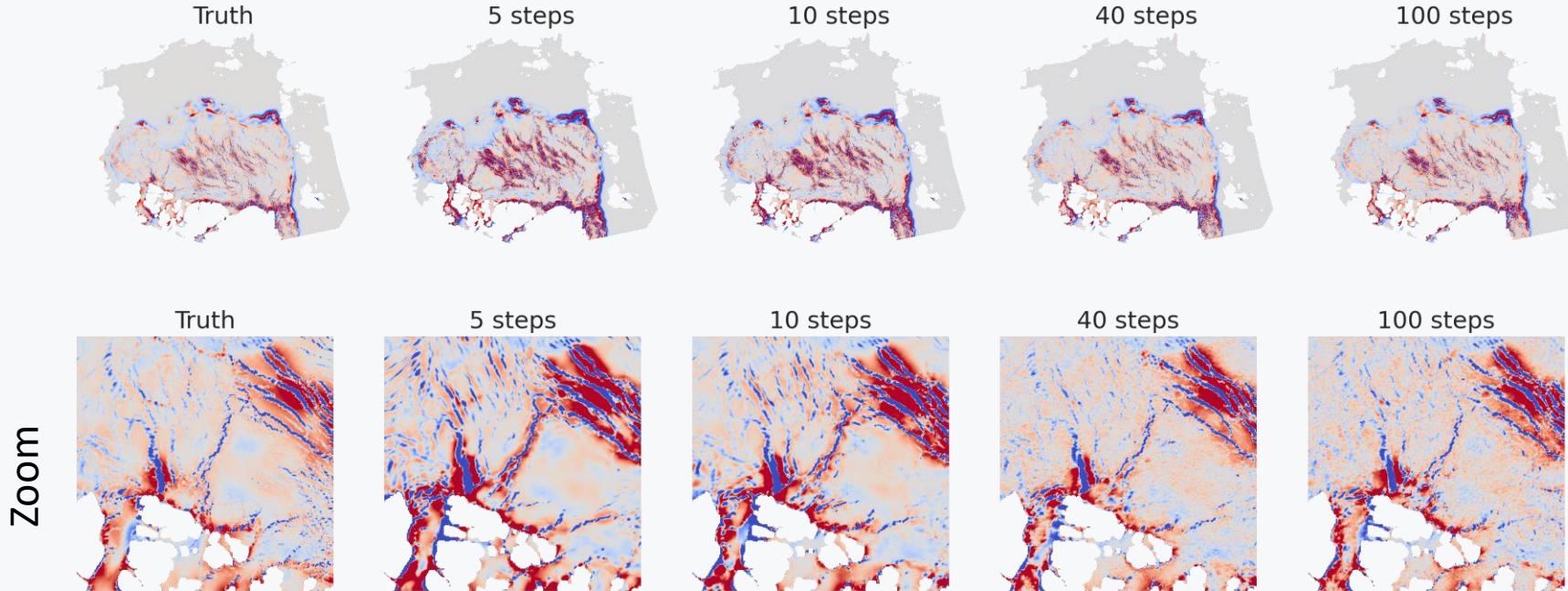
Power Spectrum Density



Spectral ratio = PSD-reconstruction / PSD-truth



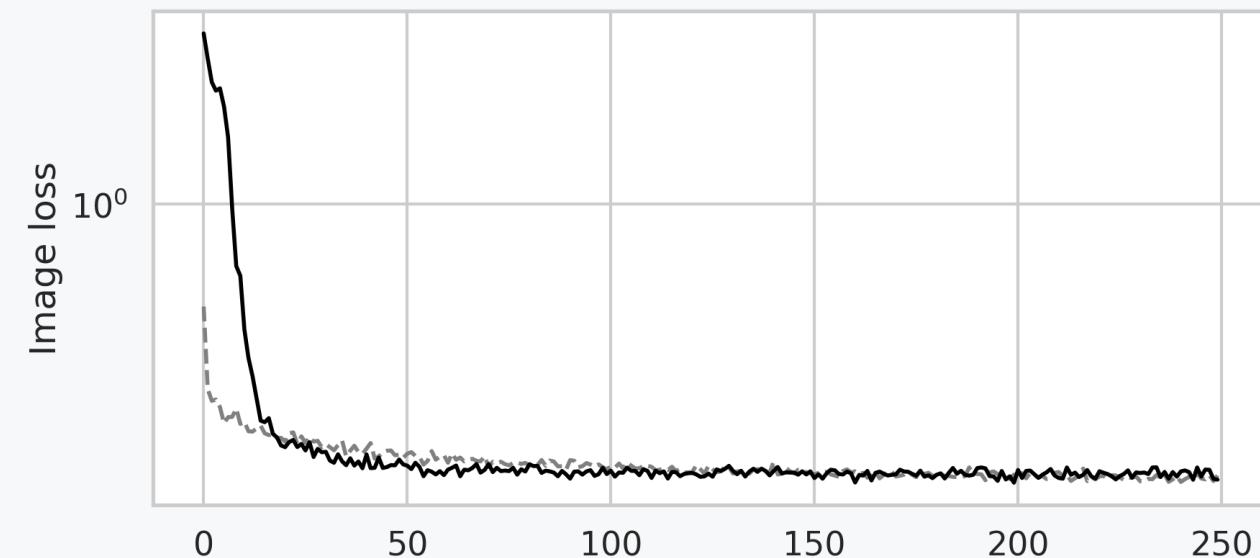
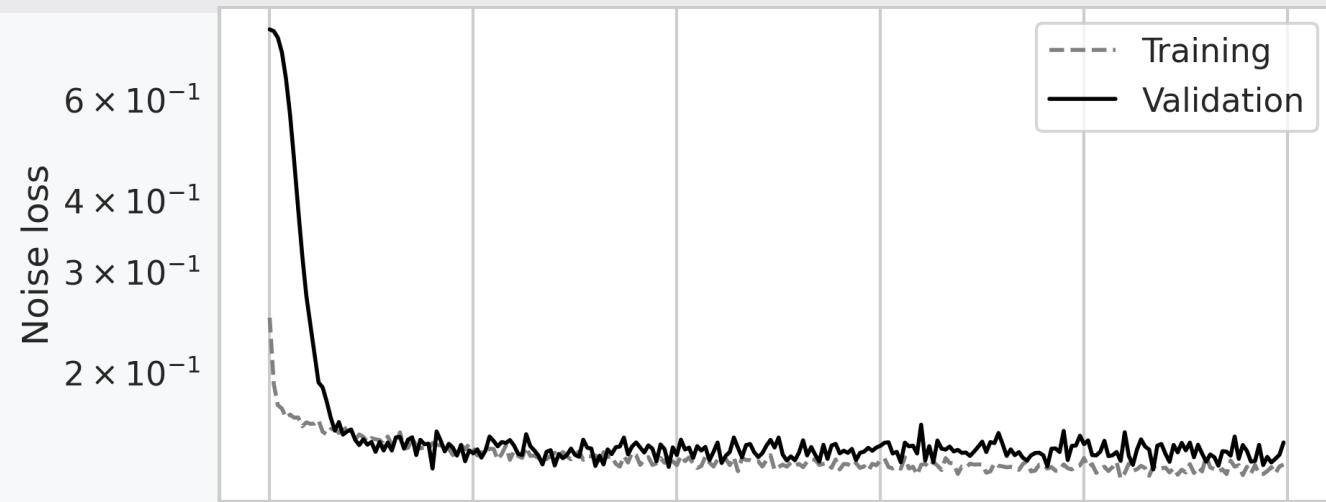
Sensitivity to the number of diffusion steps



In the other sections, 40 steps are used

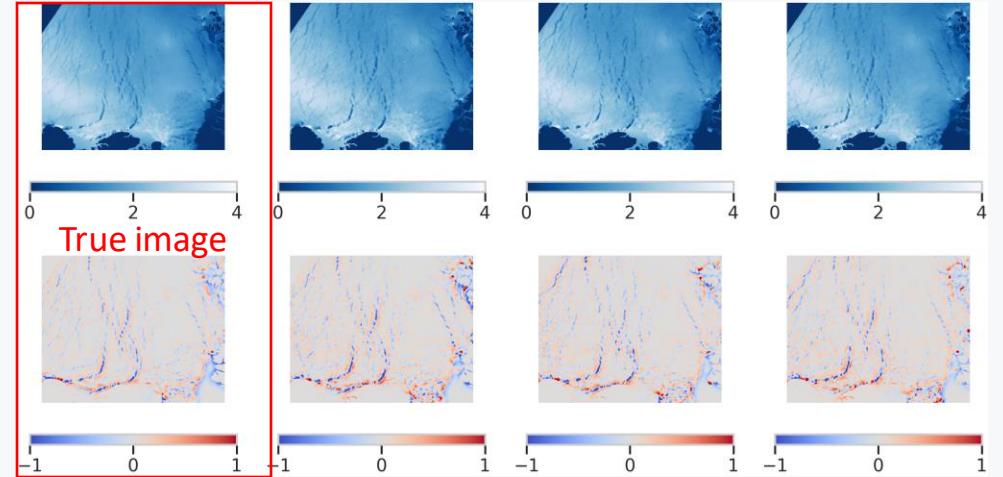
Globals results

Learning curve

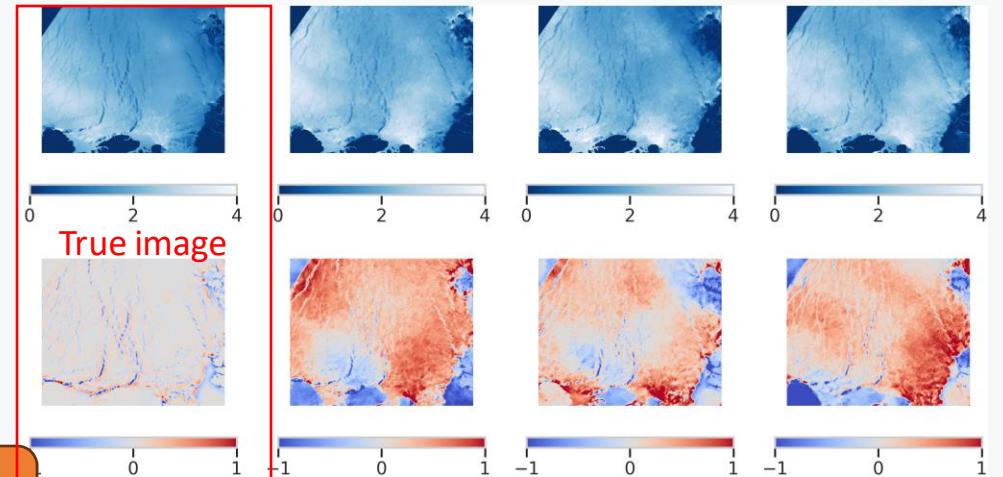


Residual Vs full field generation

Residual generation



Full-field generation



Full-field induces large-scale biases