

Decision analysis of toy NAO

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Abstract

Abstract TK

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1 Model

Hypotheses: $H \in \{\text{threat}, \text{not-threat}\}$

Data stream: $\{X_1, X_2, \dots\}$.

Likelihood function: $p(x|h)$

Loss function:

$$L_i = \begin{array}{cc} & \begin{array}{cc} \text{not-threat} & \text{threat} \end{array} \\ \begin{array}{c} \text{flag} \\ \text{wait} \end{array} & \begin{array}{cc} c & 0 \\ L_{i+1} & d + L_{i+1} \end{array} \end{array} \quad (1)$$

Threshold posterior: $p_{\text{thresh}} = \operatorname{argmin}_{p_t} \mathbb{E} \{L_0(p_t)\}$

Prior: $p_0 = \mathbb{P} \{H = \text{threat}\}$

Posterior: $P_i = \mathbb{P} \{H = \text{threat} | X_1, X_2, \dots, X_i\}$

Updates:

$$P_{i+1} = \frac{P_i}{2} \quad (2)$$

2 Expected losses

3 Optimal decision threshold

4 Discussion