

Design analysis and algorithm

Lab 10

Divide And Conquer Nearest Neighbour

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Course code: CSE3004

Nearest Neighbour:

```
import math
import copy
class Point():
    def __init__(self, x, y):
        self.x = x
        self.y = y
def dist(p1, p2):
    return math.sqrt((p1.x - p2.x) *
                     (p1.x - p2.x) +
                     (p1.y - p2.y) *
                     (p1.y - p2.y))
def bruteForce(P, n):
    min_val = float('inf')
    for i in range(n):
        for j in range(i + 1, n):
            if dist(P[i], P[j]) < min_val:
                min_val = dist(P[i], P[j])

    return min_val
def stripClosest(strip, size, d):
    min_val = d
    for i in range(size):
        j = i + 1
        while j < size and (strip[j].y -
                           strip[i].y) < min_val:
            min_val = dist(strip[i], strip[j])
            j += 1

    return min_val
def closestUtil(P, Q, n):
    if n <= 3:
        return bruteForce(P, n)
    mid = n // 2
    midPoint = P[mid]
    P1 = P[:mid]
    Pr = P[mid:]
    dl = closestUtil(P1, Q, mid)
    dr = closestUtil(Pr, Q, n - mid)

    d = min(dl, dr)
    stripP = []
    stripQ = []
    lr = P1 + Pr
    for i in range(n):
        if abs(lr[i].x - midPoint.x) < d:
```

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        stripP.append(lr[i])
        if abs(Q[i].x - midPoint.x) < d:
            stripQ.append(Q[i])

    stripP.sort(key = lambda point: point.y)
    min_a = min(d, stripClosest(stripP, len(stripP), d))
    min_b = min(d, stripClosest(stripQ, len(stripQ), d))

    return min(min_a,min_b)
def closest(P, n):
    P.sort(key = lambda point: point.x)
    Q = copy.deepcopy(P)
    Q.sort(key = lambda point: point.y)
    return closestUtil(P, Q, n)

P = [Point(2, 3), Point(12, 30),
     Point(40, 50), Point(5, 1),
     Point(12, 10), Point(3, 4)]
n = len(P)
print("The smallest distance is",closest(P, n))

```

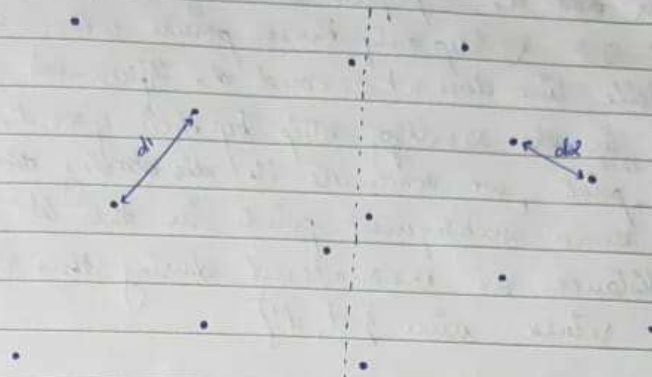
Output:

The smallest distance is 2.23606797749979

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Analysis:

### Nearest Neighbour:

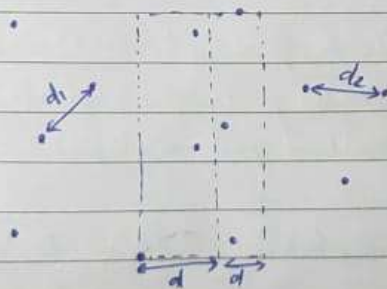


To solve this we first split the given 'n' points by an appropriately chosen vertical line into 2 halves  $S_1$  &  $S_2$  of size  $n/2$ .

By making 2 recursive calls for the sets  $S_1$  &  $S_2$ , we find the minimum distances  $d_1$  &  $d_2$  in these subsets.

$$\text{let } d = \min\{d_1, d_2\}$$

but this way takes a lot of time thus not providing us the goal. What we do is, part the strip into  $d \times d$  squares & show that each such square contains at most four input points.



then we sort n points by their x-coordinate & then split the resulting sorted list into 2 halves  $S_1$  &  $S_2$  of size  $n/2$ .

Calculate  $\min$  of  $d_1$  &  $d_2$  distances & check whether it is

Smaller than  $d$ . To perform such a check, we filter the initial point set & keep only those points whose  $x$ -distance to the middle line does not exceed  $d$ . Afterwards we sort the set of points in the resulting strip by their  $y$ -coordinates & scan the list. For <sup>each</sup> point, we compute its ~~distance to the~~ distance to the scan subsequent points in this list of points. For ~~the~~ distance we encountered during this scan, Afterwards, we return  $\min \{d, d'\}$ .

The running time of algorithm satisfies the recurrence relation,

$$T(n) = 2T(n/2) + O(n \log n)$$

The  $O(n \log n)$  term comes from sorting the points in the strip by their  $y$ -coordinates at every iteration.