

# Incremental Visual-Inertial 3D Mesh Generation with Structural Regularities

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## Introduce

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deal map represent:

- lightweight to compute and store
- describes the topology of the environment
- couples state estimation and mapping, improve each other

So proposed a method use 3D mesh represent

## Framework

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consider a stereo visual-inertial system and adopt a keyframe-based approach

### Front-end

- 3D Mesh Generation

it is difficult to create a 3D mesh

- 3D positions of the landmarks are noisy
- the density of the point cloud is highly irregular
- points are being removed (marginalized) and added

perform a 2D Delaunay triangulation only over the tracked keypoints in the latest frame

Delaunay triangulation maximizes the minimum angle of all the angles of the triangles in the triangulation

- 3D Mesh Propagation

maintain a mesh over the receding horizon of the fixed-lag smoothing optimization problem

- Temporal

we re-compute a 2D Delaunay triangulation from scratch over the keypoints of the current frame

- Spatial

add: merging new local 3D mesh, ensuring no duplicated 3D faces

remove: remove any face in the 3D mesh that has the landmark as a vertex

- Regularity Detection

extract the geometry in the scene in a non-iterative way (unlike RANSAC approaches).

interested in co-planarity regularities between landmarks(ground and wall)

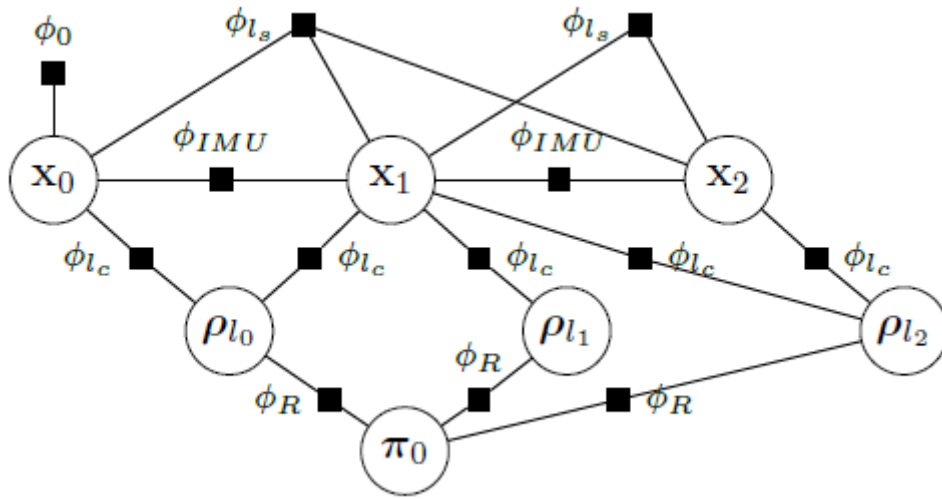
- detect planes that are horizontal (i.e. floor, tables)
- cluster the faces of the mesh with vertical normals
- build a 1D histogram of the height of the vertices
- smoothing the histogram with a Gaussian filter
- take the candidates with the most inliers (above 20 faces).

## Back-end

- Factor Graph Formulation

estimate the posterior probability

$$p(\mathcal{X}_t | \mathcal{Z}_t) \stackrel{(a)}{\propto} p(\mathcal{X}_t) p(\mathcal{Z}_t | \mathcal{X}_t)$$



- MAP Estimation  
calculate the maximum a posteriori (MAP) estimator
- Regularity Constraints

$$\mathbf{n} \cdot \boldsymbol{\rho}_{l_c} - d.$$

will lead to a singular information matrix

To avoid this problem, we optimize in the tangent space

$$S^2 \doteq \{\mathbf{n} = (n_x, n_y, n_z)^T \mid \|\mathbf{n}\| = 1\}$$

$$\mathcal{R}_{\mathbf{n}}(v) : T_{\mathbf{n}}S^2 \in \mathbb{R}^2$$

$$\mathbf{r}_R(v, d) = \mathcal{R}_{\mathbf{n}}(v)^T \cdot \boldsymbol{\rho} - d$$

## Result

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a(2D Delaunay triangulation), b(3D Mesh)

green(wall), blue(ground)

