README for ssd_solidangle.cpp

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This is a script to 1. Calculate the α detection efficiency of the beam profile monitor and 2. Find the optimum geometry parameters z_0 and x_0 that maximizes the detection efficiency. Here, "detection efficiency" is defined as the percentage of particles that hit the SSD which are emitted from the surface of the MCP/mesh. In the general literature, "detection efficiency" would be defined as the fraction of α particles that generate a detectable signal at the Si detector out of the number of Fr ions that reached the surface of the MCP/mesh. In our particular case, this efficiency ε_{tot} could be factorized in the following way:

$$\varepsilon_{tot} = \varepsilon_{mesh} \varepsilon_{decay} \varepsilon_{direction} \varepsilon_{geometry} \varepsilon_{detection}$$

where ε_{mesh} is the probability that the incoming Fr ion is captured on the mesh surface, ε_{decay} is the average ratio of Fr ions that decay and emit an α particle, $\varepsilon_{direction} = \frac{1}{2}$ is the ratio of α particles that are emitted in the beamline upstream direction rather than the downstream direction which would be undetectable with the SSD, $\varepsilon_{geometry}$ is the ratio of α particles that enter the SSD holder/box out of the ones that were emitted in the upstream direction, and $\varepsilon_{detection}$ is the ratio of α particles that generate a signal which depends on the detector characteristics. In the script ssd_solidangle.cpp, only $\varepsilon_{geometry}$ is calculated. This is nearly equivalent to the solid angle Ω of the hole opened on the lid of the SSD holder/box observed from the center of the MCP. Since the hole is off-axis with respect to the MCP center, it is approximated with $\Omega = 2\pi(1-\cos\theta)$, $\cos\theta \approx \frac{\sqrt{z_0^2+x_0^2}}{\sqrt{\left(\frac{R_{SSD}}{\sqrt{2}}\right)^2+z_0^2+x_0^2}}$. The factor $\sqrt{2}$ for the R_{SSD} is

used to approximate the off-axis solid angle with a 45 degree tilt. The meaning of each parameter is to be referenced below.

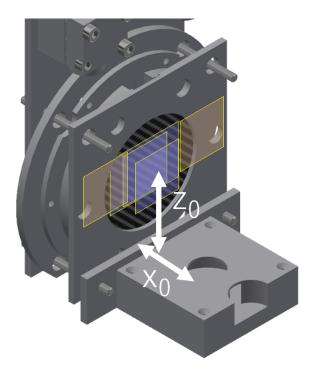


Figure 1: The planned design for the beam profile monitor.

Figure 1 depicts the design of the beam profile monitor. The plate in the center (height M_H and width M_W) is the topmost plate holding the MCP. A metal mesh covers this plate which catches the incoming Fr beam. The α particles emitted from the Fr are assumed to emerge from the surface of the plate $\left\{(x_M,\ y_M,\ z_M)\mid x_M=0,\ -\frac{M_W}{2}\leq y_M\leq \frac{M_W}{2},\ z_0-\frac{M_H}{2}\leq z_M\leq z_0+\frac{M_H}{2}\right\}$ following the quasi-Gaussian distribution $(X_c,Y_c,\sigma_x,\sigma_y)$ on the MCP coordinates given by the beam simulations. Here, z_0 is the distance between the center of the mesh and the lower surface of the lid of the box holding the SSD. The α particle is assumed to be emitted in random directions $a_M=(a_x,\ a_y,\ a_z),\ a_x\geq 0$ from the surface, following a uniform half-sphere direction distribution.

The SSD is placed inside the box in the lower right corner in figure 1. A hole of diameter $2R_{\rm SSD}$ in the lid of thickness z_l is the entrance for α rays to be detected by the SSD. In the current coordinates, the upper surface of the lid is defined as $\{(x_{lu}, y_{lu}, z_{lu}) \mid z_{lu} = z_l, (x_lu - x_0)^2 + y_lu^2 > R_{\rm SSD}^2\}$ and the lower surface as $\{(x_{ll}, y_{ll}, z_{ll}) \mid z_{ll} = 0, (x_{ll} - x_0)^2 + y_{ll}^2 > R_{\rm SSD}^2\}$. Here x_0 is the distance between the mesh and the center of the hole in the lid.

In this setup, the geometrical parameters z_0 and x_0 can be adjusted to yield the maximum detection efficiency. In order to analyze this, a method of calculating the detection efficiency is developed in the following way. Note that this method only considers the α particles emitted from the surface of the mesh in the direction of the incoming beam, and enters the SSD box. It does not consider the efficiency of the Fr ions being captured at the mesh, and the detection efficiency of the detector for the α particles that entered the box.

For each particle:

- 1. Set point $\vec{P}=(0,\ y_M,\ z_M)$ following a Gaussian random distribution $(X_c,\ Y_c,\ \sigma_X,\ \sigma_Y)$ as $y_M\sim N(X_c,\ \sigma_X)$ and $z_M\sim N(z_0+Y_c,\ \sigma_Y)$, constrained within $-\frac{M_W}{2}\leq y_M\leq \frac{M_W}{2}$ and $z_0-\frac{M_H}{2}\leq z_M\leq z_0+\frac{M_H}{2}$ as starting point of the α particle.
- 2. Set direction of α particle as $\vec{a_M} = (a_x, a_y, a_z)$ with a_x as a non-negative random number, and a_y and a_z as random numbers.
- 3. Define $t_u = \frac{z_l z_M}{a_z}$ so that $\vec{P} + t_u \vec{a_M}$ is on the surface $z = z_l$ i.e. the upper surface of the lid of the SSD box. Similarly, define $t_l = -\frac{z_M}{a_z}$ so that $\vec{P} + t_l \vec{a_M}$ is on the surface z = 0 i. e. the lower surface of the lid.
- 4. Define $x_{lu} = t_u a_x$, $y_{lu} = y_M + t_u a_y$, $x_{ll} = t_l a_x$, and $y_{ll} = y_M + t_l a_y$. The α particle passes the upper surface of the lid at point (x_{lu}, y_{lu}, z_l) and the lower surface of the lid at point $(x_{ll}, y_{ll}, 0)$.
- 5. If $(x_{lu} x_0)^2 + y_{lu}^2 > R_{\rm SSD}^2$, the α particle hits the upper lid and does not reach the SSD. Similarly, if $(x_{ll} x_0)^2 + y_{ll}^2 > R_{\rm SSD}^2$, the α particle hits the lid and does not reach the SSD.

Repeat for all the N_{Fr} particles defined and count the number $N_{Detected}$ of them that reached the SSD. The detection efficiency ε_i for this set i of N_{Fr} particles is defined as $\varepsilon_i = \frac{N_{Detected}}{N_{Fr}}$. This value is expected to be sample-dependent, since the particle positions and directions are randomly selected. In order to obtain a more reliable value, the average of $N_{Average}$ samples is calculated as the final detection efficiency: $\varepsilon = \sum_{i=1}^{N_{Average}} \varepsilon_i$.

In the code, the value of ε is calculated for various combinations of z_0 and x_0 . For the TOF-BPM at CYRIC, $z_0 = 29$ mm and $x_0 = 33$ mm.