

ALGEBRA II
HOMEWORK #1-5
USING STRUCTURE TO FACTOR

1. The expression $x^2(x+2) - 1(x+2)$ is equivalent to

1) x^2
2) $x^2 - 1$

$(x+2)(x^2-1)$
 $(x+2)(x+1)(x-1)$

3) $x^3 + 2x^2 - x + 2$
4) $(x+1)(x-1)(x+2)$

2. When factored completely, the expression $3x^3 - 5x^2 - 48x + 80$ is equivalent to

1) $(x^2 - 16)(3x - 5)$
2) $(x^2 + 16)(3x - 5)(3x + 5)$

$x^2(3x-5) - 16(3x-5)$
 $(3x-5)(x^2-16)$
 $(3x-5)(x+4)(x-4)$

3) $(x+4)(x-4)(3x-5)$
4) $(x+4)(x-4)(3x-5)(3x-5)$

3. Factor completely: $x^4 - 9x^2 + x^3 - 9x - 6x^2 + 54$

$x^2(x^2-9) + x(x^2-9) - 6(x^2-9)$
 $(x^2-9)(x^2+x-6)$
 $(x+3)(x-3)(x+3)(x-2)$

OR

$(x+3)^2(x-3)(x-2)$

$\begin{array}{r} -6 \\ 3 \times 2 \\ 1 \end{array}$

4. Factor completely: $x^2 + 6x + 6 + 5x + 5x^2 + x^3$

$x^3 + x^2 + 5x^2 + 5x + 6x + 6$
 $x^2(x+1) + 5x(x+1) + 6(x+1)$
 $(x+1)(x^2+5x+6)$
 $(x+1)(x+2)(x+3)$

$\begin{array}{r} 6 \\ 2 \times 3 \\ 5 \end{array}$



$$\text{GCF} = 3x(2x^2 + 9)$$

5. Factor completely: $9x^3(2x^2 + 9) - 3x(2x^2 + 9)^2$

$$3x(2x^2 + 9)(3x^2 - (2x^2 + 9))$$

$$3x(2x^2 + 9)(3x^2 - 2x^2 - 9)$$

$$3x(2x^2 + 9)(x^2 - 9)$$

$$\boxed{3x(2x^2 + 9)(x + 3)(x - 3)}$$

6. Factor completely: $1 - x^3 = \boxed{(1 - x)(1 + x + x^2)}$

$$a = 1 \quad b = x$$

7. Factor completely: $y^4 + 2y^2 - 3$

$$(y^2 + 3)(y^2 - 1) \quad \begin{matrix} \swarrow \text{Diffs} \\ 3 \quad \begin{matrix} -3 \\ 2 \end{matrix} \quad -1 \end{matrix}$$

$$\boxed{(y^2 + 3)(y + 1)(y - 1)}$$