

ALGEBRA II
HOMEWORK #1-7
SIMPLIFYING RATIONAL EXPRESSIONS

Simplify each of the following expressions.

$$1) \frac{12x^2 - 32x}{3x - 8} = \frac{\cancel{4x}(\cancel{3x-8})}{\cancel{3x-8}} = \boxed{4x}$$

$$2) \frac{125 - 5x^2}{x^2 + 4x - 45} = \frac{5(5+x)(\cancel{5-x})}{(\cancel{x-5})(x+9)} \quad \text{①}$$

$$= \frac{-5(5+x)}{x+9}$$

$$\begin{array}{l} 12x^2 - 32x \\ 4x(3x - 8) \end{array}$$

$$\begin{array}{ll} 125 - 5x^2 & x^2 + 4x - 45 \\ 5(25 - x^2) & (x-5)(x+9) \\ 5(5+x)(5-x) & \end{array}$$

$$3) \frac{x^2 - 4}{3x^2 - 2x - 8} = \frac{(x+2)(\cancel{x-2})}{(\cancel{x-2})(3x+4)} = \boxed{\frac{x+2}{3x+4}}$$

$$4) \frac{x^3 + 3x^2 - 2x - 6}{x^2 - 9} = \frac{(\cancel{x+3})(x^2 - 2)}{(\cancel{x+3})(x-3)}$$

$$= \frac{x^2 - 2}{x-3}$$

$$\begin{array}{l} x^2 - 4 \\ (x+2)(x-2) \end{array}$$

$$\begin{array}{r} \text{M 24} \\ 3x^2 - 2x - 8 \\ 3x^2 - 6x \\ \hline 3x(x-2) \\ 3x(x-2) \\ \hline 3x(x-2) + 4(x-2) \\ (x-2)(3x+4) \end{array}$$

$$\begin{array}{ll} x^3 + 3x^2 - 2x - 6 & x^2 - 9 \\ x^2(x+3) - 2(x+3) & (x+3)(x-3) \\ \hline (x+3)(x^2 - 2) & \end{array}$$

*** SKIP**

Re-write each of the following rational expressions into quotient-remainder form.

5) $\frac{x^3+7}{x^3+4}$

$$\frac{x^3+4+3}{x^3+4}$$

$$\frac{x^3+4}{x^3+4} + \frac{3}{x^3+4}$$

$$1 + \frac{3}{x^3+4}$$

6) $\frac{2x^2+3x-1}{2x^2+3x+5}$

$$\frac{2x^2+3x+5-6}{2x^2+3x+5}$$

$$\frac{2x^2+3x+5}{2x^2+3x+5} - \frac{6}{2x^2+3x+5}$$

$$1 - \frac{6}{2x^2+3x+5}$$

Factor each of the following.

7) $27x^3 + 1$

$a = 3x$

$b = 1$

$$(3x + 1)(9x^2 - 3x + 1)$$

8) $x^3y^6 - 64$

$a = xy^2$

$b = 4$

$$(xy^2 - 4)(x^2y^4 + 4xy^2 + 16)$$

Self-Reflection...

☐ I got

☐ I almost got it...

☐ I need more practice...

☐ I don't get it... Help!