

Simplifying Rational Expressions

A **rational expression** is an expression that is the ratio of two polynomials. Simply put, a **rational expression** is nothing more than a fraction in which the numerator and/or the denominator are polynomials

Steps to simplify rational expressions:

1. Factor both the numerator and the denominator.
2. Then reduce any common factors.
3. What you have left is your answer!

Simplify each rational expression.

$$1.) \frac{3x^2 + 5x - 2}{x^3 + 2x^2} = \frac{(x+2)(3x-1)}{x^2(x+2)} = \boxed{\frac{3x-1}{x^2}}$$

$$\begin{array}{l} \text{M-6} \\ \text{A} \\ 3x^2 + 5x - 2 \\ 3x^2 + 6x - 1x - 2 \\ 3x(x+2) - 1(x+2) \\ (x+2)(3x-1) \end{array} \quad \begin{array}{l} \text{M-6} \\ \text{A} \\ x^3 + 2x^2 \\ x^2(x+2) \end{array}$$

$$2.) \frac{16x - 8x^2}{x^3 - 4x^2 + 4x} = \frac{8x(2-x)}{x(x-2)(x-2)} = \frac{-8}{(x-2)}$$

$$\begin{array}{l} 16x - 8x^2 \\ 8x(2-x) \end{array} \quad \begin{array}{l} x^3 - 4x^2 + 4x \\ x(x^2 - 4x + 4) \\ x(x^2 - 2x - 2x + 4) \\ x(x(x-2) - 2(x-2)) \\ x(x-2)(x-2) \end{array} \quad \begin{array}{l} 4 \\ -2 \quad -2 \\ -4 \end{array}$$

UNDEFINED RATIONAL EXPRESSIONS

A rational expression is undefined when the denominator is equal to zero.

3.) Which value(s) of x make the expression $\frac{x^2 - 9}{x^2 + 7x + 10}$ undefined?

can't have a zero in the denominator!

↳ Set = 0

$$x^2 + 7x + 10 = 0$$

$$\begin{array}{r} 10 \\ 5 \times 2 \\ 7 \end{array}$$

$$(x+5)(x+2) = 0$$

$$\begin{array}{r} x+5=0 \\ -5 \quad -5 \\ \hline \end{array}$$

$$\begin{array}{r} x+2=0 \\ -2 \quad -2 \\ \hline \end{array}$$

$$x = -5$$

$$x = -2$$

RE-WRITING RATIONAL EXPRESSIONS

Re-write each of the following rational expressions so that they are expressed in quotient-remainder form.

4.) $\frac{x^2 + 4}{x^2 + 3}$

$$\frac{x^2 + 3 + 1}{x^2 + 3}$$

$$\frac{x^2 + 3}{x^2 + 3} + \frac{1}{x^2 + 3}$$

$$1 + \frac{1}{x^2 + 3}$$

5.) $\frac{2x^2 + 5x - 3}{2x^2 + 5x + 6}$

$$\frac{2x^2 + 5x + 6 - 9}{2x^2 + 5x + 6}$$

$$\frac{2x^2 + 5x + 6}{2x^2 + 5x + 6} - \frac{9}{2x^2 + 5x + 6}$$

$$1 - \frac{9}{2x^2 + 5x + 6}$$

Name _____
Algebra II

Date: _____
Lesson 1-7

SIMPLIFYING RATIONAL EXPRESSIONS PRACTICE TASK CARDS

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1.

Answers are
on the
Task Cards!
😊

2.

3.

4.