## EE24BTECH11063 - Y.Harsha Vardhan Reddy

## **Question:**

Using integration, find the area of the region bounded by the parabolas  $y^2 = 4x$  and  $x^2 = 4y$ .

Solution: The parameters of the conics are

Variable	Description
$V_1, u_1, f_1$	Parameters of Parabola
$V_2, u_2, f_2$	Parameters of Parabola
$P_{1}, P_{2}$	Points of intersection
A	Area between the conics

TABLE 0: Variables Used

$$V_1 = \begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix}, \ u_1 = \begin{pmatrix} -2 \\ 0 \end{pmatrix}, \ f_1 = 0$$
 (0.1)

$$V_2 = \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix}, \ u_2 = \begin{pmatrix} 0 \\ -2 \end{pmatrix}, \ f_2 = 0$$
 (0.2)

The intersection of two conics with parameters  $V_i$ ,  $u_i$ ,  $f_i$ , i = 1, 2 is defined as

$$x^{T}(V_{1} + \mu V_{2})x + 2(u_{1} + \mu u_{2})^{T}x + (f_{1} + \mu f_{2}) = 0$$
(0.3)

Solving this the points of intersection are

$$\begin{pmatrix} 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 4 \\ 4 \end{pmatrix} \tag{0.4}$$

Area between the curves is,

$$\int_0^4 \left(\sqrt{4x} - \frac{x^2}{4}\right) dx \tag{0.5}$$

By solving the integration, we get area is equal to 5.33 sq.units

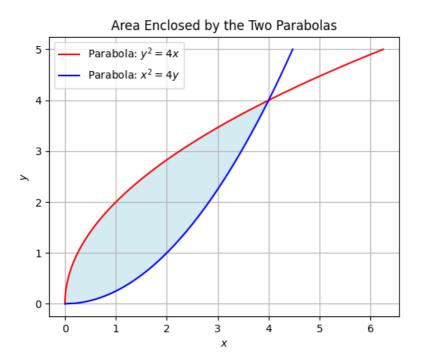


Fig. 0.1