# matrix project

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#### February 2019

## 1 Question

Find the product of perpendiculars drawn from the foci of ellipse  $(x^2/9) + (y^2/25) = 1$  upon the tangent to it at point  $(3/2, 5\sqrt{3}/2)$ .

### Answer

Given equation of ellipse can be written in matrices as

$$x^T \begin{bmatrix} 25 & 0 \\ 0 & 9 \end{bmatrix} x = 225....(1)$$

A conic can be expressed in the form of

$$x^T V x + 2u^T x + F = 0....(2)$$

By comparing (1) and (2), we can say

$$V = \begin{bmatrix} 25 & 0 \\ 0 & 9 \end{bmatrix}, u = 0, F = -225....(3)$$

If x is the some vector then

$$(p^TV + u^T)x + p^Tu + F = 0....(4)$$

becomes tangent vector of ellipse

$$(\begin{bmatrix} 3/2 & 5\sqrt{3}/2 \end{bmatrix} \begin{bmatrix} 25 & 0 \\ 0 & 9 \end{bmatrix})x + 0 = 225$$

$$([75/2 \quad 45\sqrt{3}/2])x = 225$$

$$\Rightarrow T : n^T x = 225$$

$$n = \begin{bmatrix} 5/2 \\ 3\sqrt{3}/2 \end{bmatrix}$$

$$e = \sqrt{1 - a^2/b^2}$$

$$e = 4/5$$

$$foci = (0, be), (0, -be)$$

$$\Rightarrow foci = (0, 4), (0, -4)$$

Tangent of vector :

$$\begin{bmatrix} 10 & 6 \end{bmatrix} \begin{bmatrix} a \\ b \end{bmatrix} - 225 = 0$$

let dist1 be the perpendicular distance from s1 and dist2 be the perpendicular distance from s2

$$A = \begin{bmatrix} 10 & 6\sqrt{3} \end{bmatrix} \begin{bmatrix} 0 \\ 4 \end{bmatrix}$$

$$B = \begin{bmatrix} 10 & 6\sqrt{3} \end{bmatrix} \begin{bmatrix} 0 \\ -4 \end{bmatrix}$$

$$C = \begin{bmatrix} 10 & 6\sqrt{3} \end{bmatrix} \begin{bmatrix} 3/2 \\ 5\sqrt{3}/2 \end{bmatrix}$$

$$D = \sqrt{a^2 + b^2}$$

$$dist1 = \frac{A - C}{D}$$

$$dist2 = \frac{B - C}{D}$$

product of distances(D) = dist1 \* dist2

$$D = 9$$