

Assignment 2

Sachinkumar Dubey

Download all python codes from

<https://github.com/sachinomdubey/Matrix-theory/Assignment2/codes>

and latex-tikz codes from

<https://github.com/sachinomdubey/Matrix-theory/Assignment2>

Q no. 73. Find the angle between the following pair of lines.

1)

$$L_1 : \mathbf{x} = \begin{pmatrix} 2 \\ -5 \\ 1 \end{pmatrix} + \lambda_1 \begin{pmatrix} 3 \\ 2 \\ 6 \end{pmatrix} \quad (0.0.1)$$

$$L_2 : \mathbf{x} = \begin{pmatrix} 7 \\ -6 \\ 0 \end{pmatrix} + \lambda_2 \begin{pmatrix} 1 \\ 2 \\ 2 \end{pmatrix} \quad (0.0.2)$$

2)

$$L_1 : \mathbf{x} = \begin{pmatrix} 3 \\ 1 \\ -2 \end{pmatrix} + \lambda_1 \begin{pmatrix} 1 \\ -1 \\ -2 \end{pmatrix} \quad (0.0.3)$$

$$L_2 : \mathbf{x} = \begin{pmatrix} 2 \\ -1 \\ -56 \end{pmatrix} + \lambda_2 \begin{pmatrix} 3 \\ -5 \\ -4 \end{pmatrix} \quad (0.0.4)$$

Explanation :

The given equations are in the form:

$$\mathbf{x} = \mathbf{p}_1 + \lambda_1 \mathbf{m}_1 \quad (0.0.5)$$

$$\mathbf{x} = \mathbf{p}_2 + \lambda_2 \mathbf{m}_2 \quad (0.0.6)$$

Finding the angle between the lines :

The angle between the lines can be found by substituting the values of the direction vectors \mathbf{m}_1 and \mathbf{m}_2 in dot product formula:

$$\cos \theta = \frac{\mathbf{m}_1^T \mathbf{m}_2}{\|\mathbf{m}_1\| \|\mathbf{m}_2\|} \quad (0.0.7)$$

Solution :

Problem 1:

The direction vectors of the lines are $\mathbf{m}_1 = \begin{pmatrix} 3 \\ 2 \\ 6 \end{pmatrix}$ and

$$\mathbf{m}_2 = \begin{pmatrix} 1 \\ 2 \\ 2 \end{pmatrix}.$$

Thus, the angle θ between two vectors is given by

$$\cos \theta = \frac{\mathbf{m}_1^T \mathbf{m}_2}{\|\mathbf{m}_1\| \|\mathbf{m}_2\|} \quad (0.0.8)$$

$$= \frac{19}{3 \times 7} \quad (0.0.9)$$

$$\Rightarrow \theta = 25.21^\circ \quad (0.0.10)$$

Problem 2:

The direction vectors of the lines are $\mathbf{m}_1 = \begin{pmatrix} 1 \\ -1 \\ -2 \end{pmatrix}$ and

$$\mathbf{m}_2 = \begin{pmatrix} 3 \\ -5 \\ -4 \end{pmatrix}.$$

Thus, the angle θ between two vectors is given by

$$\cos \theta = \frac{\mathbf{m}_1^T \mathbf{m}_2}{\|\mathbf{m}_1\| \|\mathbf{m}_2\|} \quad (0.0.11)$$

$$= \frac{16}{\sqrt{6} \times \sqrt{50}} \quad (0.0.12)$$

$$\Rightarrow \theta = 22.52^\circ \quad (0.0.13)$$