# Synchronous Shopping



Problem

Submissions

Leaderboard

Discussions

Your submission will run against only preliminary test cases. Full test cases will run at the end of the day.

Bitville is a seaside city that has N shopping centers connected via M bidirectional roads. Each road connects exactly two distinct shopping centers and has a travel time associated with it.

There are K different types of fish sold in Bitville. Historically, any shopping center has a fishmonger selling certain types of fish. Buying any amount of fish from any fishmonger takes no time.

Our heroes, Big Cat and Little Cat, are standing at Bitville shopping center number 1. They have a list of the types of fish sold at each fishmonger, and they want to collectively purchase all K types of fish in a minimal amount of time. To do this, they decide to split the shopping between themselves in the following way:

- ullet Both cats choose their own paths, starting at shopping center 1 and ending at shopping center N. It should be noted that Little Cat's path is not necessarily the same as Big Cat's.
- While traveling their respective paths, each cat will buy certain types of fish at certain shops.
- ullet When the cats reach shopping center N, they must have collectively purchased all K types of fish in a minimal amount of time.
- ullet If one cat finishes shopping before the other, he waits at shopping center N for his partner to finish; this means that the total shopping time is the maximum of Little and Big Cats' respective shopping times.

It is to be noted that any of the cats can visit the shopping center N in between, but they both have to finish their paths at the shopping center N.

Given the layout for Bitville and the list of fish types sold at each fishmonger, what is the minimum amount of time it will take for Big and Little Cat to purchase all K types of fish and meet up at shopping center N?

## **Input Format**

The first line contains 3 space-separated integers: N (the number of shopping centers), M (the number of roads), and K (the number of types of fish sold in Bitville), respectively.

Each line i of the N subsequent lines ( $1 \le i \le n$ ) describes a shopping center as a line of spaceseparated integers. Each line takes the following form:

- The first integer,  $T_i$ , denotes the number of types of fish that are sold by the fishmonger at the  $i^{th}$ shopping center.
- ullet Each of the  $T_i$  subsequent integers on the line describes a type of fish sold by that fishmonger. Which is denoted by  $A_{i,j}$ .

Each line j of the M subsequent lines ( $1 \leq j \leq m$ ) contains 3 space-separated integers describing a road. The first two integers,  $X_j$  and  $Y_j$ , describe the two cities it connects. The third integer,  $Z_j$ , denotes the amount of time it takes to travel the road (i.e., travel time).

### Constraints

- $2 \le N \le 10^3$
- $1 \le M \le 2 \times 10^3$
- $1 \le K \le 10$
- $0 \leq T_i \leq K$
- $1 \le A_{i,j} \le K$
- All  $A_{i,j}$  are different for every fixed i.

Submissions: 270

Max Score: 40

Difficulty: Moderate

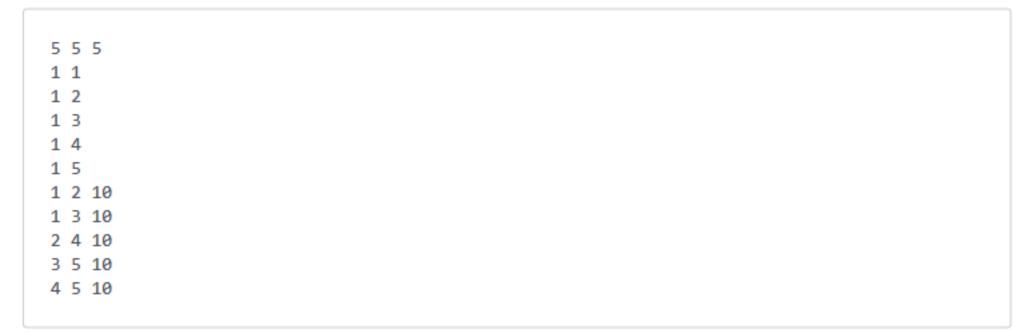
More

- $1 \leq X_j, Y_j \leq N$
- $1 \le Z_j \le 10^4$
- Each road connectes 2 distinct shopping centers (i.e., no road connects a shopping center to itself).
- Each pair of shopping centers is directly connected by no more than 1 road.
- It is possible to get to any shopping center from any other shopping center.
- Each type of fish is always sold by at least one fishmonger.

#### **Output Format**

Print the minimum amount of time it will take for the cats to collectively purchase all K fish and meet up at shopping center N.

#### Sample Input



#### **Sample Output**

30

#### **Explanation**

Big Cat can choose the following route:  $1 \to 2 \to 4 \to 5$ , and buy fish at all of the shopping centers on his way.

Little Cat can choose the following route: 1 o 3 o 5, and buy fish from the fishmonger at the  $3^{rd}$  shopping center only.

