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%Code to apply Shannon Fano coding to a grayscale image
clc;
clear all;
close all;
I=imread("C:\Users\hp\Downloads\images.jpg");
if size(I,3)==3
    I=rgb2gray(I);
end
figure
imshow(I);
counts=imhist(I); %Finding frequency of each gray level intensity.
p=counts/sum(counts); %Normalizing histogram counts into
probabilities.
symbols=find(p>0)-1; %Extracting only those intensity values that
appear.
p=p(p>0); %Removing all zero probability gray levels.
[p_sorted,idx]=sort(p,'descend'); %Sorting probabilities from highest
to lowest.
symbols_sorted=symbols(idx); %Rearranging symbols in the same sorted
order.
codes=strings(1,length(symbols_sorted));
%Creating an empty string array to store Shannon-Fano binary codes.
codes=shannon_fano(symbols_sorted,p_sorted,codes,1,length(p_sorted));
%Calling the recursive function that generates Shannon-Fano codes.
disp("Top 20 Shannon-Fano Codes for Image Symbols:");
disp("GrayLevel Probability Code");
disp("-----");
for i=1:min(20,length(symbols_sorted))
    fprintf("%3d %.6f %s\n", ...
    symbols_sorted(i),p_sorted(i),codes(i));
end
%Displaying only the most frequent gray levels and their corresponding
codes.
Lavg=0;
for i=1:length(p_sorted)
    Lavg=Lavg+p_sorted(i)*strlength(codes(i));
end
%Computing the average code length using probability weighted sum.
H=0;
for i=1:length(p_sorted)
    H=H-p_sorted(i)*log2(p_sorted(i));
end
%Applying Shannon entropy formula  $H=-\sum p_i \log_2(p_i)$  for binary coding. 1
disp("-----");
fprintf("Entropy(H)=%.4f bits/pixel\n",H);
fprintf("AverageCodeLength(Lavg)=%.4f bits/pixel\n",Lavg);
fprintf("CodingEfficiency=%.2f %%\n", (H/Lavg)*100);
%Efficiency indicates how close coding is to the theoretical entropy
limit.
function codes=shannon_fano(symbols,p,codes,startIdx,endIdx) %shannon
fano recursive function
if startIdx>=endIdx

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    return;
end
%Stopping recursion when only one symbol remains.
totalProb=sum(p(startIdx:endIdx));
%Calculating total probability of the current symbol group.
runningSum=0;
splitIdx=startIdx;
for i=startIdx:endIdx
    runningSum=runningSum+p(i);
    %Finding cumulative probability until it reaches half of total.
    if runningSum>=totalProb/2
        splitIdx=i;
        break;
    end
end
for i=startIdx:splitIdx
    codes(i)=codes(i)+"0";
end
%Assigning binary 0 to the first probability subset.
for i=splitIdx+1:endIdx
    codes(i)=codes(i)+"1";
end
%Assigning binary 1 to the second probability subset.
codes=shannon_fano(symbols,p,codes,startIdx,splitIdx);
codes=shannon_fano(symbols,p,codes,splitIdx+1,endIdx);
%Recursively repeating the splitting until all symbols get a unique
code.
end

```

Top 20 Shannon-Fano Codes for Image Symbols:

GrayLevel Probability Code

```

254 0.033403 000000
253 0.029786 000001
252 0.026110 00001
251 0.022295 00010
21 0.019116 00011
19 0.019056 001000
20 0.017804 001001
18 0.017387 001010
250 0.016036 001011
22 0.014943 001100
249 0.014446 001101
17 0.012817 001110
243 0.012022 001111
248 0.011704 0100000
245 0.010591 0100001
247 0.010094 0100010
23 0.009240 0100011
16 0.009160 0100100
246 0.008743 0100101
244 0.008544 010011

```

Entropy(H)=7.5065 bits/pixel

*AverageCodeLength(L_{avg})=7.5887 bits/pixel
CodingEfficiency=98.92 %*



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