

eg. A car company believes that the percentage of residents in city ABC that owns a vehicle is 60% or less. A sales manager disagrees with this. He conducts a hypothesis testing surveying 250 residents and found that 170 responded yes to owning a vehicle.

- state the null & alternate hypothesis.
- At 10% significance level, is there enough evidence to support the idea that vehicle ownership in city ABC is 60% or less.

⇒ Soln

$$H_0 \Rightarrow \leq 60\% \quad (\text{Null Hypothesis})$$

$$H_1 \Rightarrow > 60\% \quad (\text{Alternate Hypothesis})$$

$$n \Rightarrow 250 \quad \bar{x} \Rightarrow 170 \quad \alpha \Rightarrow 0.1$$

$$p_0 \Rightarrow 0.6 \quad \hat{p} = \frac{\bar{x}}{n} \Rightarrow \frac{170}{250} \Rightarrow 0.68$$

$$q_0 \Rightarrow 0.4$$

$$Z \text{ test with prop} \Rightarrow \frac{\hat{p} - p_0}{\sqrt{\frac{p_0 q_0}{n}}} \Rightarrow \frac{0.68 - 0.6}{\sqrt{\frac{0.6 \times 0.4}{250}}}$$

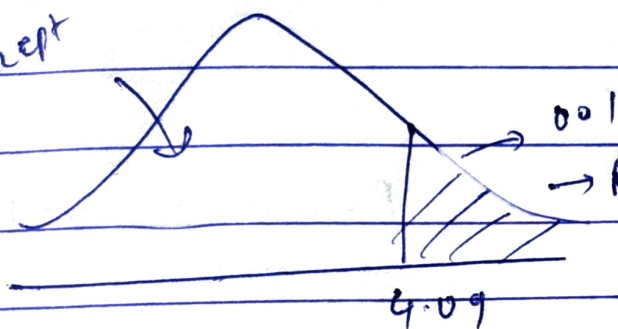
$$\Rightarrow \frac{0.08}{0.031} \Rightarrow \boxed{2.58} \Rightarrow \frac{0.08}{0.031}$$

$$\Rightarrow 0.00494$$

$$p\text{value} < \alpha$$

Reject the Null Hypothesis

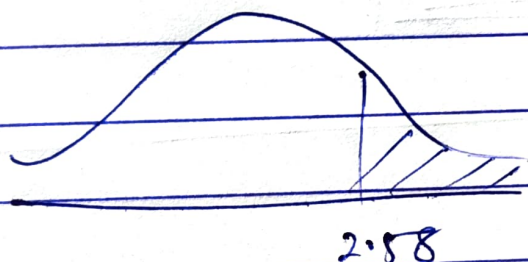
Accept



\rightarrow Reject

$$2.58 < 4.09$$

Accept the hypothesis.



$$p\text{value} \approx 0.99506$$

$$p\text{value} > \alpha$$

$$0.99506 > \alpha$$