

①

Pair class

Custom class

(name, iurr)

two value

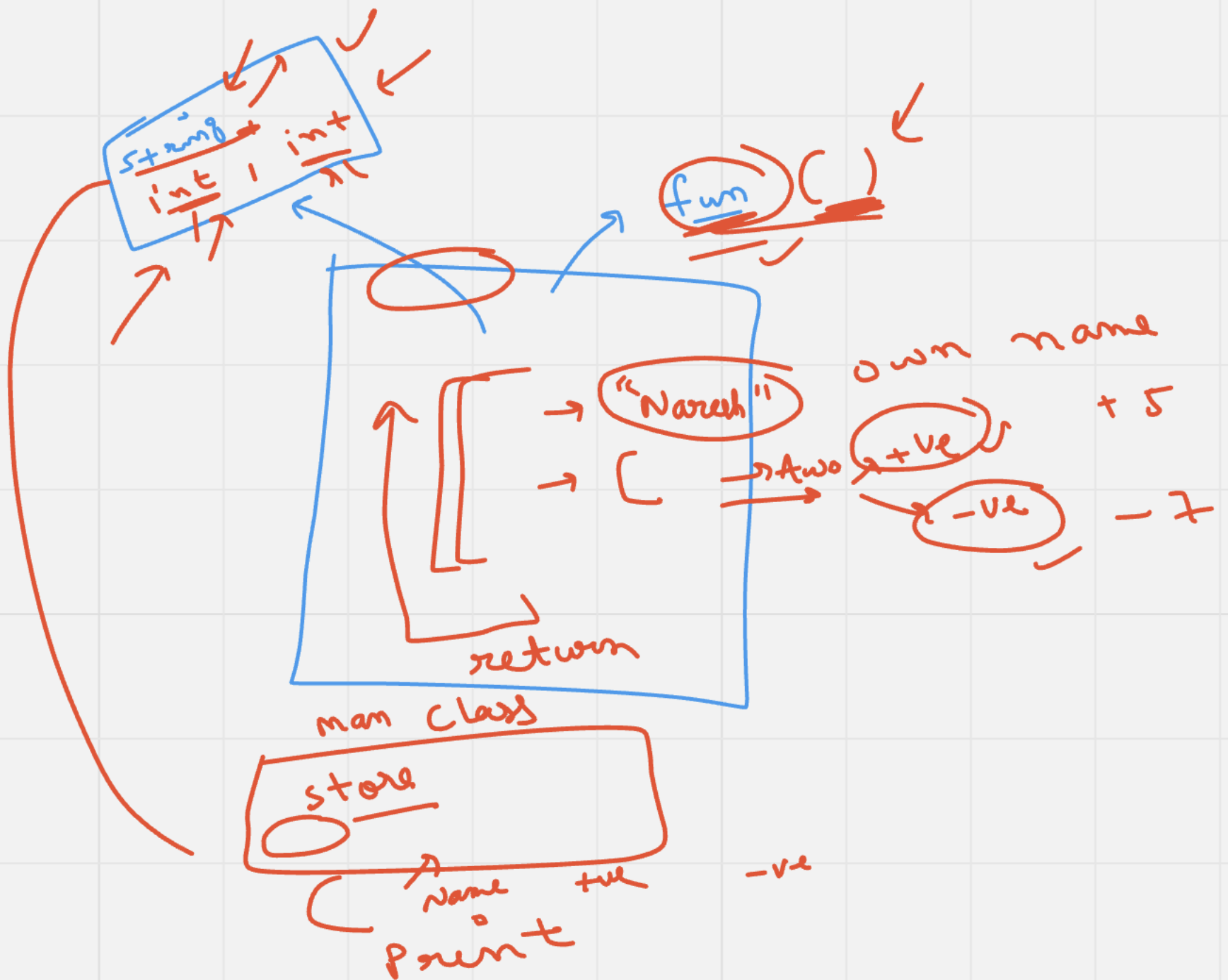
[int, string]

function

class

int  
float  
string  
arr()  
...





three

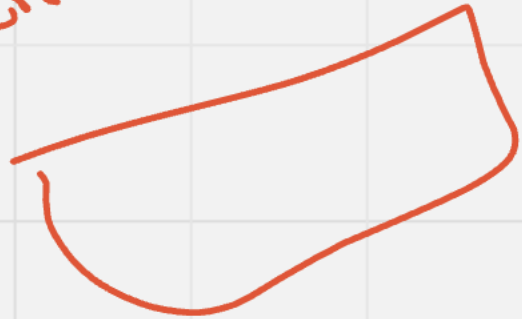
Tuplet

f string name;

int a,

int b;

const.



3

Complex Number

✓ ✓  
 $2 + 5i$

✓  
 $3$   
x

✓  
 $-5$   
x

$a + b$   
 $3$   $+ i$   
 $0 + i$

3

Complex Number

Natural No.

Real

+img

$\infty \dots -2 -1 0$   $1 2 3 \dots \infty$

$\frac{3}{2}$   $\frac{4}{5}$   $-\frac{6}{2}$   $\frac{1}{7}$

f.n

Real + imag i

Complex

```
int real  
int imag  
Print
```

$$c3 = c1 + c2$$

$$c1 = \underline{1} + \underline{2i}$$

$$c2 = \underline{3} + \underline{4i}$$

$$\underline{4} + \underline{6i}$$

*this == c1*

```
public Complex add(Complex other) {
```

```
    Complex out = new Complex(0, 0);
```

*c1. real    c2. real*

```
    out.real = this.real + other.real;
```

```
    out.imag = this.imag + other.imag;
```

```
    return out;
```

```
}
```

```
Complex c3 = c1.add(c2);
```



c1

c2



Mult Two Complex

$$C_1 = 1 + 2i$$

$$C_2 = 3 + 4i$$

$$C_1 * C_2 = (1 + 2i)(3 + 4i)$$
$$= 1*3 + 6i + 4i + 8i^2$$

$$4$$

$$= -4 + 10i$$

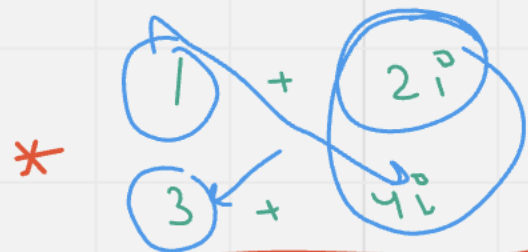
real

real

imag

$$(C_1 \cdot \text{real} * C_2 \cdot \text{real}) - (C_1 \cdot \text{imag} * C_2 \cdot \text{imag})$$
$$(C_1 \cdot \text{real} * C_2 \cdot \text{imag}) + (C_2 \cdot \text{real} * C_1 \cdot \text{imag})$$





$$(1 + 2i)(3 + 4i)$$

$$3 + 6i + 4i + 8i^2$$

$$3 + 10i - 8$$

$$\boxed{-5 + 10i}$$

Real

$$C1.\text{real} * C2.\text{real}$$

$$= C1.\text{img} * C2.\text{img}$$

Image

$$C1.\text{real} * C2.\text{img}$$

$$+ C1.\text{img} + C2.\text{real}$$

```
public Complex mult(Complex other) {
```

```
    Complex out = new Complex(0, 0);
```

```
    out.real = this.real * other.real - this.imag * other.imag;
```

```
    out.imag = this.real * other.imag - this.imag * other.real;
```

```
    return out;
```

```
}
```

Handwritten calculation for complex multiplication:

$$(1 + 2i) * (3 + 4i)$$

Result:  $-5 + 10i$

Calculation steps:

$$\begin{aligned} 1 * 3 &= 3 \\ 1 * 4 &= 4 \\ 2 * 3 &= 6 \\ 2 * 4 &= 8 \end{aligned}$$

Final result:  $3 - 8 + 4i + 6i = -5 + 10i$

Annotations: real, imag, div

# fraction

✓ numerator

←  $\frac{1}{2}$

✓ denominator

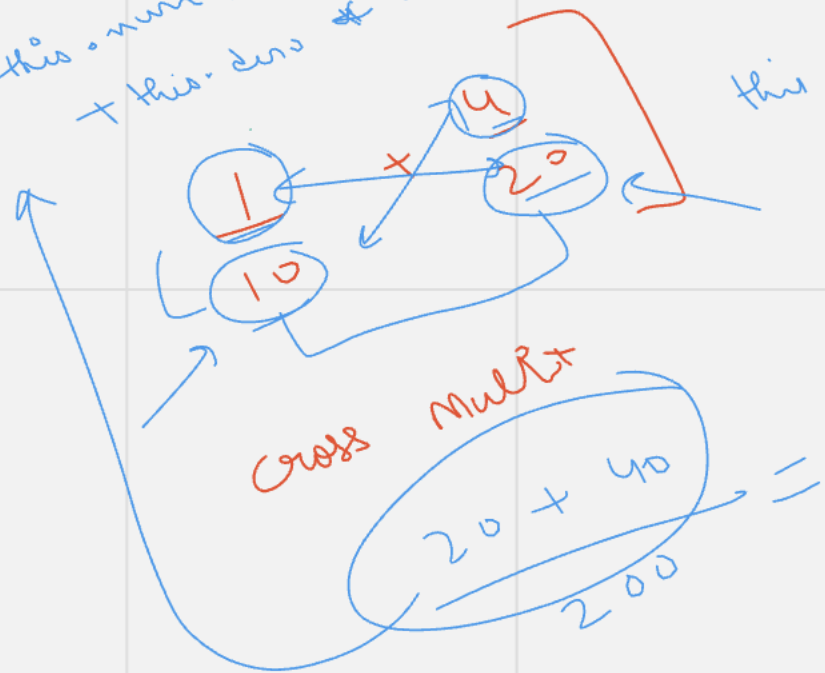
$\frac{3}{4}$

$\frac{6}{7}$

int	<u>num</u>
ind	<u>denom</u>

this num \* other deno  
+ this deno \* other num

this deno \* other num



HCM (60, 200)

3/10

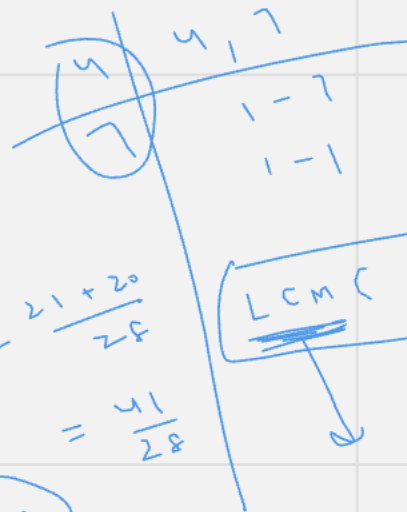
setter  
setter



add

$$\frac{3 \times 7}{28} + \frac{5 \times 4}{28} = \frac{21 + 20}{28} = \frac{41}{28}$$

LCM



LCM (a, b)

Lowest com

$$\frac{1}{10} + \frac{5}{20} \quad \text{gross}$$

$$\frac{20 + 40}{200}$$

$$= \frac{60}{200}$$

$$\frac{1}{20}$$

$$\frac{3}{10} \quad \text{opt}$$

$$\frac{3}{10}$$

$$\left( \frac{3}{60}, \frac{10}{200} \right)$$

HFF

$$\cancel{20}$$



3 ~~60~~  
10 ~~200~~

HCF (60, 200)

Highest Common multiple

highest value from which  
both number are  
divisible

60 (W)

