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## 1 Theorem 1.19

Wilson's theorem in short:

$\mathbb{Z}_p$  is a field so all  $x \in \mathbb{Z}_p^* = \mathbb{Z}_p \setminus \{0\}$  is a unit  $\implies \bar{2} \cdot \overline{p-2} = \bar{1}$

$$\begin{aligned}(p-1)! &\equiv (p-1)(p-2)! \pmod{p} \\ &\equiv -1 \cdot 1 \pmod{p}\end{aligned}$$

See also Pinter, 23G.

## 2 Lemma 1.28

The only units in  $\mathbb{Z}[i]$  are  $\pm 1, \pm i$ .