

# Assignment: Implement Elliptic Curve Algorithms

1. Find modular square root
2. Find order of elliptic curve
3. Add points on an elliptic curve (scalar multiplication)
4. Find order of a point on an elliptic curve

Example (for testing/debugging the implementation):

$$E : y^2 \equiv x^3 + 7x + 15 \pmod{3571}$$

Order of elliptic curve  $\#E=3645$

Sample points on the curve:

$\{6,62\}$

$\{6,3509\}$

$\{9,1194\}$

$\{9,2377\}$

$\{11,1285\}$   
 $\{11,2286\}$   
 $\{13,620\}$   
 $\{13,2951\}$   
 $\{14,987\}$   
 $\{14,2584\}$   
 $\{16,475\}$   
 $\{16,3096\}$

Point multiplication:

$$150 * \{16,3096\} = \{3309, 2985\}$$

$$173 * \{14,987\} = \{1878, 2295\}$$

Order of points:

$$\#(\{6,62\}) = 135$$

$$\#(\{9,2377\}) = 405$$

$$\#(\{2288, 1585\}) = 1215$$