

MathematicalFunctions

5.1

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Chapter 1

Module Index

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Chapter 2

Namespace Index

2.1 Namespace List

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Chapter 3

Data Structure Index

3.1 Data Structures

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File Index

4.1 File List

Here is a list of all files with brief descriptions:

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Chapter 5

Module Documentation

5.1 Models

Modules

- [Utils](#)

5.1.1 Detailed Description

5.2 Utils

Modules

- [Math](#)

5.2.1 Detailed Description

5.3 Math

Files

- file [gauss_quadrature.hh](#)
Gauss Quadrature implementation.
- file [math_messages.hh](#)
Define the class MathMessages.
- file [matrix3x3.hh](#)
Matrix math inline functions.
- file [matrix3x3_inline.hh](#)
Matrix math inline functions.
- file [numerical.hh](#)
Miscellaneous math inline functions.
- file [numerical_inline.hh](#)
Vector math inline functions.
- file [vector3.hh](#)
Vector math inline functions.
- file [vector3_inline.hh](#)
Vector math inline functions.
- file [dm_invert.cc](#)
Define Matrix3x3::invert.
- file [dm_invert_symm.cc](#)
Define Matrix3x3::invert_symmetric.
- file [gauss_quadrature.cc](#)
Define Gauss Quadrature functionality.
- file [math_messages.cc](#)
Implement the class MathMessages.

Namespaces

- [jeod](#)
Namespace jeod.

Macros

- `#define MAKE_MATH_MESSAGE_CODE(id) JEOD_MAKE_MESSAGE_CODE(MathMessages, "utils/math/", id)`

5.3.1 Detailed Description

5.3.2 Macro Definition Documentation

5.3.2.1 MAKE_MATH_MESSAGE_CODE

```
#define MAKE_MATH_MESSAGE_CODE(  
    id ) JEOD_MAKE_MESSAGE_CODE(MathMessages, "utils/math/", id)
```

Definition at line 34 of file `math_messages.cc`.

Chapter 6

Namespace Documentation

6.1 jeod Namespace Reference

Namespace jeod.

Data Structures

- class [GaussQuadrature](#)
- class [MathMessages](#)
Specifies the message IDs used in the math model.
- class [Matrix3x3](#)
Provides static methods for operations that involve 3x3 matrices.
- class [Numerical](#)
Provides miscellaneous numerical functions.
- class [Vector3](#)
Provides static methods for operations that involve 3-vectors.

Variables

- static constexpr double [SQRT_DBL_MIN](#) {1.4916681462400413e-154}

6.1.1 Detailed Description

Namespace jeod.

6.1.2 Variable Documentation

6.1.2.1 SQRT_DBL_MIN

```
constexpr double jeod::SQRT_DBL_MIN {1.4916681462400413e-154} [static]
```

Definition at line 66 of file `numerical_inline.hh`.

Referenced by `jeod::Numerical::square()`, and `jeod::Numerical::square_incr()`.

Chapter 7

Data Structure Documentation

7.1 jeod::GaussQuadrature Class Reference

```
#include <gauss_quadrature.hh>
```

Static Public Attributes

- static const int [max_order](#) = 8
- static const double [gauss_weights](#) [[max_order](#)+1][[max_order](#)]
- static const double [gauss_xvalues](#) [[max_order](#)+1][[max_order](#)]

7.1.1 Detailed Description

Definition at line 69 of file gauss_quadrature.hh.

7.1.2 Field Documentation

7.1.2.1 gauss_weights

```
const double jeod::GaussQuadrature::gauss_weights [static]
```

Initial value:

```
= {  
    {0.0000000, 0.0000000, 0.0000000, 0.0000000, 0.0000000, 0.0000000, 0.0000000, 0.0000000},  
    {2.0000000, 0.0000000, 0.0000000, 0.0000000, 0.0000000, 0.0000000, 0.0000000, 0.0000000},  
    {1.0000000, 1.0000000, 0.0000000, 0.0000000, 0.0000000, 0.0000000, 0.0000000, 0.0000000},  
    {0.5555556, 0.8888889, 0.5555556, 0.0000000, 0.0000000, 0.0000000, 0.0000000, 0.0000000},  
    {0.3478548, 0.6521452, 0.6521452, 0.3478548, 0.0000000, 0.0000000, 0.0000000, 0.0000000},  
    {0.2369269, 0.4786287, 0.5688889, 0.4786287, 0.2369269, 0.0000000, 0.0000000, 0.0000000},  
    {0.1713245, 0.3607616, 0.4679139, 0.4679139, 0.3607616, 0.1713245, 0.0000000, 0.0000000},  
    {0.1294850, 0.2797054, 0.3818301, 0.4179592, 0.3818301, 0.2797054, 0.1294850, 0.0000000},  
    {0.1012285, 0.2223810, 0.3137067, 0.3626838, 0.3626838, 0.3137067, 0.2223810, 0.1012285}  
}
```

Definition at line 73 of file gauss_quadrature.hh.

7.1.2.2 gauss_xvalues

```
const double jeod::GaussQuadrature::gauss_xvalues [static]
```

Initial value:

```
= {
  { 0.0000000, 0.0000000, 0.0000000, 0.0000000, 0.0000000, 0.0000000, 0.0000000, 0.0000000},
  { 0.0000000, 0.0000000, 0.0000000, 0.0000000, 0.0000000, 0.0000000, 0.0000000, 0.0000000},
  {-0.5773503, 0.5773503, 0.0000000, 0.0000000, 0.0000000, 0.0000000, 0.0000000, 0.0000000},
  {-0.7745967, 0.0000000, 0.7745967, 0.0000000, 0.0000000, 0.0000000, 0.0000000, 0.0000000},
  {-0.8611363, -0.3399810, 0.3399810, 0.8611363, 0.0000000, 0.0000000, 0.0000000, 0.0000000},
  {-0.9061798, -0.5384693, 0.0000000, 0.5384693, 0.9061798, 0.0000000, 0.0000000, 0.0000000},
  {-0.9324695, -0.6612094, -0.2386192, 0.2386192, 0.6612094, 0.9324695, 0.0000000, 0.0000000},
  {-0.9491079, -0.7415312, -0.4058452, 0.0000000, 0.4058452, 0.7415312, 0.9491079, 0.0000000},
  {-0.9602899, -0.7966665, -0.5255324, -0.1834346, 0.1834346, 0.5255324, 0.7966665, 0.9602899}
}
```

Definition at line 74 of file gauss_quadrature.hh.

7.1.2.3 max_order

```
const int jeod::GaussQuadrature::max_order = 8 [static]
```

Definition at line 72 of file gauss_quadrature.hh.

The documentation for this class was generated from the following files:

- [gauss_quadrature.hh](#)
- [gauss_quadrature.cc](#)

7.2 jeod::MathMessages Class Reference

Specifies the message IDs used in the math model.

```
#include <math_messages.hh>
```

Public Member Functions

- [MathMessages](#) ()=delete
- [MathMessages](#) (const [MathMessages](#) &)=delete
- [MathMessages](#) & [operator=](#) (const [MathMessages](#) &)=delete

Static Public Attributes

- static const char * [ill_conditioned](#) = "utils/math/" "ill_conditioned"
Error issued when an ill-conditioned matrix is detected.

7.2.1 Detailed Description

Specifies the message IDs used in the math model.

Definition at line 71 of file math_messages.hh.

7.2.2 Constructor & Destructor Documentation

7.2.2.1 MathMessages() [1/2]

```
jeod::MathMessages::MathMessages ( ) [delete]
```

7.2.2.2 MathMessages() [2/2]

```
jeod::MathMessages::MathMessages (
    const MathMessages & ) [delete]
```

7.2.3 Member Function Documentation

7.2.3.1 operator=()

```
MathMessages& jeod::MathMessages::operator= (
    const MathMessages & ) [delete]
```

7.2.4 Field Documentation

7.2.4.1 ill_conditioned

```
char const * jeod::MathMessages::ill_conditioned = "utils/math/" "ill_conditioned" [static]
```

Error issued when an ill-conditioned matrix is detected.

trick_units(-)

Definition at line 78 of file math_messages.hh.

Referenced by jeod::Matrix3x3::invert(), and jeod::Matrix3x3::invert_symmetric().

The documentation for this class was generated from the following files:

- [math_messages.hh](#)
- [math_messages.cc](#)

7.3 jeod::Matrix3x3 Class Reference

Provides static methods for operations that involve 3x3 matrices.

```
#include <matrix3x3.hh>
```

Static Public Member Functions

- static void [initialize](#) (double mat[3][3])
Zero-fill matrix: $mat[i][j] = 0.0$.
- static void [identity](#) (double mat[3][3])
Construct identity matrix: $mat[i][j] = \delta_{ij}$.
- static void [cross_matrix](#) (const double vec[3], double cross_mat[3][3])
Construct the skew symmetric cross product matrix: $mat[i][k] = \epsilon_{ijk} vec[j]$, ϵ_{ijk} is the Levi-Cevita symbol.
- static void [outer_product](#) (const double vec_left[3], const double vec_right[3], double prod[3][3])
*Construct the outer product of two vectors: $mat[i][j] = vec_left[i] * vec_right[j]$.*
- static void [negate](#) (double mat[3][3])
Negated matrix in-place: $mat[i][j] = -mat[i][j]$.
- static void [transpose](#) (double mat[3][3])
Transpose matrix in-place: $mat[i][j] = mat[j][i]$.
- static void [scale](#) (double scalar, double mat[3][3])
*Scale matrix in-place, $mat[i][j] = scalar * mat[i][j]$.*
- static void [incr](#) (const double addend[3][3], double mat[3][3])
Increment matrix in-place: $mat[i][j] = mat[i][j] + addend[i][j]$.
- static void [decr](#) (const double subtrahend[3][3], double mat[3][3])
Decrement matrix in-place: $mat[i][j] = mat[i][j] - subtrahend[i][j]$.
- static void [copy](#) (const double input_mat[3][3], double copy[3][3])
Copy matrix: $copy[i][j] = mat[i][j]$.
- static void [negate](#) (const double input_mat[3][3], double copy[3][3])
Negate matrix: $copy[i][j] = -mat[i][j]$.
- static void [transpose](#) (const double input_mat[3][3], double trans[3][3])
Transpose matrix: $copy[i][j] = mat[j][i]$.
- static void [scale](#) (const double mat[3][3], double scalar, double prod[3][3])
*Scale matrix: $copy[i][j] = scalar * mat[i][j]$.*
- static void [add](#) (const double augend[3][3], const double addend[3][3], double sum[3][3])
Add matrices: $sum[i][j] = augend[i][j] + addend[i][j]$.
- static void [subtract](#) (const double minuend[3][3], const double subtrahend[3][3], double diff[3][3])
Subtract matrices: $diff[i][j] = minuend[i][j] - subtrahend[i][j]$.
- static void [product](#) (const double mat_left[3][3], const double mat_right[3][3], double prod[3][3])
*Compute the matrix product $mat_left * mat_right$: $prod[i][j] = mat_left[i][k] * mat_right[k][j]$.*
- static void [product_left_transpose](#) (const double mat_left[3][3], const double mat_right[3][3], double prod[3][3])
*Compute the matrix product $mat_left^T * mat_right$: $prod[i][j] = mat_left[k][i] * mat_right[k][j]$.*
- static void [product_right_transpose](#) (const double mat_left[3][3], const double mat_right[3][3], double prod[3][3])
*Compute the matrix product $mat_left * mat_right^T$: $prod[i][j] = sum_k mat_left[i][k] * mat_right[j][k]$.*
- static void [product_transpose_transpose](#) (const double mat_left[3][3], const double mat_right[3][3], double prod[3][3])
*Compute the matrix product $mat_left^T * mat_right^T$: $prod[i][j] = sum_k mat_left[k][i] * mat_right[j][k]$.*
- static void [transform_matrix](#) (const double trans[3][3], const double mat[3][3], double prod[3][3])

- Compute the matrix product $\text{trans} * \text{mat} * \text{trans}^T$ $\text{prod}[i][j] = \text{trans}[i][k] * \text{mat}[k][l] * \text{trans}[j][l]$.

 - static void [transpose_transform_matrix](#) (const double trans[3][3], const double mat[3][3], double prod[3][3])

Compute the matrix product $\text{trans}^T * \text{mat} * \text{trans}$ $\text{prod}[i][j] = \text{trans}[k][i] * \text{mat}[k][l] * \text{trans}[l][j]$.

 - static int [invert](#) (const double matrix[3][3], double inverse[3][3])

Compute the inverse of a 3x3 matrix.

 - static int [invert_symmetric](#) (const double matrix[3][3], double inverse[3][3])

Compute the inverse of a symmetric 3x3 matrix.

 - static void [print](#) (const double mat[3][3])

Print matrix to standard error.

7.3.1 Detailed Description

Provides static methods for operations that involve 3x3 matrices.

Definition at line 71 of file matrix3x3.hh.

7.3.2 Member Function Documentation

7.3.2.1 add()

```
void jeod::Matrix3x3::add (
    const double augend[3][3],
    const double addend[3][3],
    double sum[3][3] ) [inline], [static]
```

Add matrices: $\text{sum}[i][j] = \text{augend}[i][j] + \text{addend}[i][j]$.

Parameters

in	<i>augend</i>	Matrix
in	<i>addend</i>	Matrix
out	<i>sum</i>	Sum

Definition at line 326 of file matrix3x3_inline.hh.

7.3.2.2 copy()

```
void jeod::Matrix3x3::copy (
    const double input_mat[3][3],
    double copy[3][3] ) [inline], [static]
```

Copy matrix: $\text{copy}[i][j] = \text{mat}[i][j]$.

Parameters

in	<i>input_mat</i>	Source matrix
out	<i>copy</i>	Matrix copy

Definition at line 237 of file matrix3x3_inline.hh.

Referenced by `negate()`.

7.3.2.3 cross_matrix()

```
void jeod::Matrix3x3::cross_matrix (
    const double vec[3],
    double cross_mat[3][3] ) [inline], [static]
```

Construct the skew symmetric cross product matrix: $\text{mat}[i][k] = \epsilon_{ijk} \text{vec}[j]$, ϵ_{ijk} is the Levi-Cevita symbol.

Parameters

in	<i>vec</i>	Vector
out	<i>cross_mat</i>	Cross product matrix

Definition at line 101 of file matrix3x3_inline.hh.

7.3.2.4 decr()

```
void jeod::Matrix3x3::decr (
    const double subtrahend[3][3],
    double mat[3][3] ) [inline], [static]
```

Decrement matrix in-place: $\text{mat}[i][j] = \text{mat}[i][j] - \text{subtrahend}[i][j]$.

Parameters

in	<i>subtrahend</i>	Decrement
in, out	<i>mat</i>	Decrement matrix

Definition at line 219 of file matrix3x3_inline.hh.

7.3.2.5 identity()

```
void jeod::Matrix3x3::identity (
    double mat[3][3] ) [inline], [static]
```

Construct identity matrix: $\text{mat}[i][j] = \delta_{ij}$.

Parameters

out	<i>mat</i>	Identity matrix
-----	------------	-----------------

Definition at line 86 of file matrix3x3_inline.hh.

7.3.2.6 incr()

```
void jeod::Matrix3x3::incr (
    const double addend[3][3],
    double mat[3][3] ) [inline], [static]
```

Increment matrix in-place: $\text{mat}[i][j] = \text{mat}[i][j] + \text{addend}[i][j]$.

Parameters

in	<i>addend</i>	Increment
in, out	<i>mat</i>	Incremented matrix

Definition at line 201 of file matrix3x3_inline.hh.

7.3.2.7 initialize()

```
void jeod::Matrix3x3::initialize (
    double mat[3][3] ) [inline], [static]
```

Zero-fill matrix: $\text{mat}[i][j] = 0.0$.

Parameters

out	<i>mat</i>	Zero-filled matrix
-----	------------	--------------------

Definition at line 73 of file matrix3x3_inline.hh.

7.3.2.8 invert()

```
int jeod::Matrix3x3::invert (
    const double matrix[3][3],
    double inverse[3][3] ) [static]
```

Compute the inverse of a 3x3 matrix.

Assumptions and Limitations

- Input and output matrices are distinct.
- Input matrix is well-conditioned.

Returns

0=success, non-zero=singular

Parameters

in	<i>matrix</i>	Matrix to invert
out	<i>inverse</i>	Inverse

Definition at line 72 of file dm_invert.cc.

References jeod::MathMessages::ill_conditioned.

7.3.2.9 invert_symmetric()

```
int jeod::Matrix3x3::invert_symmetric (
    const double matrix[3][3],
    double inverse[3][3] ) [static]
```

Compute the inverse of a symmetric 3x3 matrix.

Assumptions and Limitations

- Input and output matrices are distinct.
- Input matrix is symmetric.
- Determinate is non-zero.

Returns

0=success, non-zero=singular

Parameters

in	<i>matrix</i>	Symmetric matrix to invert
out	<i>inverse</i>	Inverse

Definition at line 73 of file dm_invert_symm.cc.

References jeod::MathMessages::ill_conditioned.

7.3.2.10 negate() [1/2]

```
void jeod::Matrix3x3::negate (
    double mat[3][3] ) [inline], [static]
```

Negated matrix in-place: $\text{mat}[i][j] = -\text{mat}[i][j]$.

Parameters

in, out	<i>mat</i>	Negated matrix
---------	------------	----------------

Definition at line 142 of file matrix3x3_inline.hh.

7.3.2.11 negate() [2/2]

```
void jeod::Matrix3x3::negate (
    const double input_mat[3][3],
    double copy[3][3] ) [inline], [static]
```

Negate matrix: $\text{copy}[i][j] = -\text{mat}[i][j]$.

Assumptions and Limitations

- Input and output matrices are distinct.

Parameters

in	<i>input_mat</i>	Source matrix
out	<i>copy</i>	Negated matrix

Definition at line 260 of file matrix3x3_inline.hh.

References `copy()`.

7.3.2.12 outer_product()

```
void jeod::Matrix3x3::outer_product (
    const double vec_left[3],
    const double vec_right[3],
    double prod[3][3] ) [inline], [static]
```

Construct the outer product of two vectors: $\text{mat}[i][j] = \text{vec_left}[i] * \text{vec_right}[j]$.

Parameters

in	<i>vec_left</i>	Vector
in	<i>vec_right</i>	Vector
out	<i>prod</i>	Outer product matrix

Definition at line 125 of file matrix3x3_inline.hh.

7.3.2.13 print()

```
void jeod::Matrix3x3::print (
    const double mat[3][3] ) [inline], [static]
```

Print matrix to standard error.

Parameters

in	<i>mat</i>	Matrix to print
----	------------	-----------------

Definition at line 540 of file matrix3x3_inline.hh.

7.3.2.14 product()

```
void jeod::Matrix3x3::product (
    const double mat_left[3][3],
    const double mat_right[3][3],
    double prod[3][3] ) [inline], [static]
```

Compute the matrix product $\text{mat_left} * \text{mat_right}$: $\text{prod}[i][j] = \text{mat_left}[i][k] * \text{mat_right}[k][j]$.

Assumptions and Limitations

- Input and output matrices are distinct.

Parameters

in	<i>mat_left</i>	Multiplier
in	<i>mat_right</i>	Multiplicand
out	<i>prod</i>	Product

Definition at line 368 of file matrix3x3_inline.hh.

Referenced by `transform_matrix()`, and `transpose_transform_matrix()`.

7.3.2.15 product_left_transpose()

```
void jeod::Matrix3x3::product_left_transpose (
    const double mat_left[3][3],
```



```
const double mat_right[3][3],
double prod[3][3] ) [inline], [static]
```

Compute the matrix product $\text{mat_left}^T * \text{mat_right}$: $\text{prod}[i][j] = \text{mat_left}[k][i] * \text{mat_right}[k][j]$.

Assumptions and Limitations

- Input and output matrices are distinct.

Parameters

in	<i>mat_left</i>	Multiplier
in	<i>mat_right</i>	Multiplicand
out	<i>prod</i>	Product

Definition at line 399 of file matrix3x3_inline.hh.

Referenced by transpose_transform_matrix().

7.3.2.16 product_right_transpose()

```
void jeod::Matrix3x3::product_right_transpose (
    const double mat_left[3][3],
    const double mat_right[3][3],
    double prod[3][3] ) [inline], [static]
```

Compute the matrix product $\text{mat_left} * \text{mat_right}^T$: $\text{prod}[i][j] = \sum_k \text{mat_left}[i][k] * \text{mat_right}[j][k]$.

Assumptions and Limitations

- Input and output matrices are distinct.

Parameters

in	<i>mat_left</i>	Multiplier
in	<i>mat_right</i>	Multiplicand
out	<i>prod</i>	Product

Definition at line 432 of file matrix3x3_inline.hh.

Referenced by transform_matrix().

7.3.2.17 product_transpose_transpose()

```
void jeod::Matrix3x3::product_transpose_transpose (
    const double mat_left[3][3],
```

```
const double mat_right[3][3],
double prod[3][3] ) [inline], [static]
```

Compute the matrix product $\text{mat_left}^T * \text{mat_right}^T$: $\text{prod}[i][j] = \sum_k \text{mat_left}[k][i] * \text{mat_right}[j][k]$.

Assumptions and Limitations

- Input and output matrices are distinct.

Parameters

in	<i>mat_left</i>	Multiplier
in	<i>mat_right</i>	Multiplicand
out	<i>prod</i>	Product

Definition at line 465 of file matrix3x3_inline.hh.

7.3.2.18 scale() [1/2]

```
void jeod::Matrix3x3::scale (
    double scalar,
    double mat[3][3] ) [inline], [static]
```

Scale matrix in-place, $\text{mat}[i][j] = \text{scalar} * \text{mat}[i][j]$.

Parameters

in	<i>scalar</i>	Scalar
in, out	<i>mat</i>	Scaled matrix

Definition at line 183 of file matrix3x3_inline.hh.

7.3.2.19 scale() [2/2]

```
void jeod::Matrix3x3::scale (
    const double mat[3][3],
    double scalar,
    double prod[3][3] ) [inline], [static]
```

Scale matrix: $\text{copy}[i][j] = \text{scalar} * \text{mat}[i][j]$.

Parameters

in	<i>mat</i>	Matrix
in	<i>scalar</i>	Scalar
out	<i>prod</i>	Product

Definition at line 307 of file matrix3x3_inline.hh.

7.3.2.20 subtract()

```
void jeod::Matrix3x3::subtract (
    const double minuend[3][3],
    const double subtrahend[3][3],
    double diff[3][3] ) [inline], [static]
```

Subtract matrices: $\text{diff}[i][j] = \text{minuend}[i][j] - \text{subtrahend}[i][j]$.

Parameters

in	<i>minuend</i>	Matrix
in	<i>subtrahend</i>	Matrix
out	<i>diff</i>	Difference

Definition at line 345 of file matrix3x3_inline.hh.

7.3.2.21 transform_matrix()

```
void jeod::Matrix3x3::transform_matrix (
    const double trans[3][3],
    const double mat[3][3],
    double prod[3][3] ) [inline], [static]
```

Compute the matrix product $\text{trans} * \text{mat} * \text{trans}^T$ $\text{prod}[i][j] = \text{trans}[i][k] * \text{mat}[k][l] * \text{trans}[j][l]$.

Assumptions and Limitations

- Input and output matrices are distinct.

Parameters

in	<i>trans</i>	Transformation matrix
in	<i>mat</i>	Matrix to transform
out	<i>prod</i>	Product

Definition at line 510 of file matrix3x3_inline.hh.

References [product\(\)](#), and [product_right_transpose\(\)](#).

7.3.2.22 transpose() [1/2]

```
void jeod::Matrix3x3::transpose (
    double mat[3][3] ) [inline], [static]
```

Transpose matrix in-place: $\text{mat}[i][j] = \text{mat}[j][i]$.

Parameters

in, out	<i>mat</i>	Transposed matrix
---------	------------	-------------------

Definition at line 161 of file matrix3x3_inline.hh.

7.3.2.23 transpose() [2/2]

```
void jeod::Matrix3x3::transpose (
    const double input_mat[3][3],
    double trans[3][3] ) [inline], [static]
```

Transpose matrix: $\text{copy}[i][j] = \text{mat}[j][i]$.

Assumptions and Limitations

- Input and output matrices are distinct.

Parameters

in	<i>input_mat</i>	Source matrix
out	<i>trans</i>	Matrix transpose

Definition at line 283 of file matrix3x3_inline.hh.

7.3.2.24 transpose_transform_matrix()

```
void jeod::Matrix3x3::transpose_transform_matrix (
    const double trans[3][3],
    const double mat[3][3],
    double prod[3][3] ) [inline], [static]
```

Compute the matrix product $\text{trans}^T * \text{mat} * \text{trans}$ $\text{prod}[i][j] = \text{trans}[k][i] * \text{mat}[k][l] * \text{trans}[l][j]$.

Assumptions and Limitations

- Input and output matrices are distinct.

Parameters

in	<i>trans</i>	Transformation matrix
in	<i>mat</i>	Matrix to transform
out	<i>prod</i>	Product

Definition at line 528 of file matrix3x3_inline.hh.

References `product()`, and `product_left_transpose()`.

The documentation for this class was generated from the following files:

- [matrix3x3.hh](#)
- [matrix3x3_inline.hh](#)
- [dm_invert.cc](#)
- [dm_invert_symm.cc](#)

7.4 jeod::Numerical Class Reference

Provides miscellaneous numerical functions.

```
#include <numerical.hh>
```

Static Public Member Functions

- static double [fabs](#) (double x)
Absolute value.
- static double [square](#) (double value)
Compute the square of a number, protecting against underflow.
- static double [square_incr](#) (double value, double &sum)
Add number squared to accumulator, protecting against underflow.
- static bool [compare_exact](#) (double x, double y)
Compare two doubles for exact equality.

7.4.1 Detailed Description

Provides miscellaneous numerical functions.

Definition at line 66 of file numerical.hh.

7.4.2 Member Function Documentation

7.4.2.1 `compare_exact()`

```
bool jeod::Numerical::compare_exact (
    double x,
    double y ) [inline], [static]
```

Compare two doubles for exact equality.

Returns

whether inputs are exactly the same

Parameters

in	<i>x</i>	Value1
in	<i>y</i>	Value2

Definition at line 123 of file numerical_inline.hh.

7.4.2.2 fabs()

```
double jeod::Numerical::fabs (
    double x ) [inline], [static]
```

Absolute value.

Returns

Absolute value of *x*

Parameters

in	<i>x</i>	<i>x</i>
----	----------	----------

Definition at line 73 of file numerical_inline.hh.

Referenced by square(), square_incr(), and jeod::Vector3::zero_small().

7.4.2.3 square()

```
double jeod::Numerical::square (
    double value ) [inline], [static]
```

Compute the square of a number, protecting against underflow.

Returns

value^2 or zero if too small

Parameters

in	<i>value</i>	Value
----	--------------	-------

Definition at line 90 of file numerical_inline.hh.

References fabs(), and jeod::SQRT_DBL_MIN.

7.4.2.4 square_incr()

```
double jeod::Numerical::square_incr (
    double value,
    double & sum ) [inline], [static]
```

Add number squared to accumulator, protecting against underflow.

Returns

Accumulated value

Parameters

in	value	Value
in, out	sum	Accumulator

Definition at line 108 of file numerical_inline.hh.

References fabs(), and jeod::SQRT_DBL_MIN.

The documentation for this class was generated from the following files:

- [numerical.hh](#)
- [numerical_inline.hh](#)

7.5 jeod::Vector3 Class Reference

Provides static methods for operations that involve 3-vectors.

```
#include <vector3.hh>
```

Static Public Member Functions

- static double * [initialize](#) (double vec[3])
Zero-fill vector, vec[i] = 0.0.
- static double * [unit](#) (unsigned int index, double vec[3])
Construct unit vector, vec[i] = delta_ij (delta_ij is the Kronecker delta)
- static double * [fill](#) (double scalar, double vec[3])
Construct a vector from scalar, vec[i] = scalar.
- static double * [zero_small](#) (double limit, double vec[3])
Zero-out small components of a vector, vec[i] = 0 if abs(vec[i]) < limit.
- static double * [copy](#) (const double vec[3], double copy[3])
Copy vector contents, copy[i] = vec[i].
- static double [dot](#) (const double vec2[3], const double vec1[3])
*Compute vector inner product, result = sum_i vec1[i] * vec2[i].*
- static double [vmagsq](#) (const double vec[3])
Compute square of vector magnitude, result = dot(vec,vec), but protects against underflow.
- static double [vmag](#) (const double vec[3])

- Compute vector magnitude, result = sqrt(vmagsq(vec))*

 - static double * **normalize** (double vec[3])

*Make vector a unit vector in-place, vec = vec * 1/vmag(vec)*

 - static double * **normalize** (const double vec[3], double unit_vec[3])

*Construct unit vector, unit_vec = vec * 1/vmag(vec)*

 - static double * **scale** (double scalar, double vec[3])

Scale a vector in-place, vec[i] = scalar.

 - static double * **scale** (const double vec[3], double scalar, double prod[3])

*Scale a vector, prod[i] = vec[i] * scalar.*

 - static double * **negate** (double vec[3])

Negate vector in-place, vec[i] = -vec[i].

 - static double * **negate** (const double vec[3], double copy[3])

Negate vector, copy[i] = -vec[i].

 - static double * **transform** (const double tmat[3][3], const double vec[3], double prod[3])

*Transform a column vector, prod[i] = tmat[i][j]*vec[j].*

 - static double * **transform** (const double tmat[3][3], double vec[3])

*Transform a column vector in-place, vec[i] <- tmat[i][j]*vec[j].*

 - static double * **transform_transpose** (const double tmat[3][3], const double vec[3], double prod[3])

*Transform a column vector with the transpose, prod[i] = tmat[j][i]*vec[j].*

 - static double * **transform_transpose** (const double tmat[3][3], double vec[3])

*Transform a column vector in-place with the transpose, vec[i] <- tmat[j][i]*vec[j].*

 - static double * **incr** (const double addend[3], double vec[3])

Increment a vector, vec[i] += addend[i].

 - static double * **incr** (const double addend1[3], const double addend2[3], double vec[3])

Increment a vector, vec[i] += addend1[i] + addend2[i].

 - static double * **decr** (const double subtrahend[3], double vec[3])

Decrement a vector, vec[i] -= subtrahend[i].

 - static double * **decr** (const double subtrahend1[3], const double subtrahend2[3], double vec[3])

Decrement a vector, vec[i] -= subtrahend1[i] + subtrahend2[i].

 - static double * **sum** (const double addend1[3], const double addend2[3], double vec[3])

Compute the sum of two vectors, vec[i] = addend1[i] + addend2[i].

 - static double * **sum** (const double addend1[3], const double addend2[3], const double addend3[3], double vec[3])

Compute the sum of three vectors, vec[i] = addend1[i] + addend2[i] + addend3[i].

 - static double * **diff** (const double minuend[3], const double subtrahend[3], double vec[3])

Compute the difference between two vectors, diff[i] = minuend[i] - subtrahend[i].

 - static double * **cross** (const double vec_left[3], const double vec_right[3], double prod[3])

*Compute the cross product between two vectors, prod[i] = epsilon_ijk * vec_left[j] * vec_right[k].*

 - static double * **scale_incr** (const double vec[3], double scalar, double prod[3])

*Increment a vector with a scaled vector, prod[i] += scalar*vec[i].*

 - static double * **scale_decr** (const double vec[3], double scalar, double prod[3])

*Decrement a vector with a scaled vector, prod[i] += scalar*vec[i].*

 - static double * **cross_incr** (const double vec_left[3], const double vec_right[3], double prod[3])

*Increment a vector with the the cross product between two vectors, prod[i] += epsilon_ijk * vec_left[j] * vec_right[k].*

 - static double * **cross_decr** (const double vec_left[3], const double vec_right[3], double prod[3])

*Decrement a vector with the the cross product between two vectors, prod[i] -= epsilon_ijk * vec_left[j] * vec_right[k].*

 - static double * **transform_incr** (const double tmat[3][3], const double vec[3], double prod[3])

*Increment a vector with a transformed column vector, prod[i] += tmat[i][j]*vec[j].*

 - static double * **transform_decr** (const double tmat[3][3], const double vec[3], double prod[3])

*Decrement a vector with a transformed column vector, prod[i] += tmat[i][j]*vec[j].*

 - static double * **transform_transpose_incr** (const double tmat[3][3], const double vec[3], double prod[3])

*Increment a vector with a transpose-transformed column vector, prod[i] += tmat[j][i]*vec[j].*

 - static double * **transform_transpose_decr** (const double tmat[3][3], const double vec[3], double prod[3])

*decrement a vector with a transpose-transformed column vector, prod[i] -= tmat[j][i]*vec[j]*

7.5.1 Detailed Description

Provides static methods for operations that involve 3-vectors.

Definition at line 66 of file vector3.hh.

7.5.2 Member Function Documentation

7.5.2.1 copy()

```
double * jeod::Vector3::copy (
    const double vec[3],
    double copy[3] ) [inline], [static]
```

Copy vector contents, $\text{copy}[i] = \text{vec}[i]$.

Returns

Copied vector

Parameters

in	<i>vec</i>	Source vector
out	<i>copy</i>	Copied vector

Definition at line 143 of file vector3_inline.hh.

Referenced by `negate()`, `normalize()`, `transform()`, and `transform_transpose()`.

7.5.2.2 cross()

```
double * jeod::Vector3::cross (
    const double vec_left[3],
    const double vec_right[3],
    double prod[3] ) [inline], [static]
```

Compute the cross product between two vectors, $\text{prod}[i] = \epsilon_{ijk} * \text{vec_left}[j] * \text{vec_right}[k]$.

Returns

Cross product vector

Parameters

in	<i>vec_left</i>	Left vector
in	<i>vec_right</i>	Right vector
out	<i>prod</i>	Cross product vector

Definition at line 484 of file vector3_inline.hh.

7.5.2.3 cross_decr()

```
double * jeod::Vector3::cross_decr (
    const double vec_left[3],
    const double vec_right[3],
    double prod[3] ) [inline], [static]
```

Decrement a vector with the the cross product between two vectors, $prod[i] -= \epsilon_{ijk} * vec_left[j] * vec_right[k]$.

Returns

Decrementated vector

Parameters

in	<i>vec_left</i>	Left vector
in	<i>vec_right</i>	Right vector
in, out	<i>prod</i>	Decrementated vector

Definition at line 552 of file vector3_inline.hh.

7.5.2.4 cross_incr()

```
double * jeod::Vector3::cross_incr (
    const double vec_left[3],
    const double vec_right[3],
    double prod[3] ) [inline], [static]
```

Increment a vector with the the cross product between two vectors, $prod[i] += \epsilon_{ijk} * vec_left[j] * vec_right[k]$.

Returns

Cross product vector

Parameters

in	<i>vec_left</i>	Left vector
in	<i>vec_right</i>	Right vector
in, out	<i>prod</i>	Cross product vector

Definition at line 535 of file vector3_inline.hh.

7.5.2.5 `decr()` [1/2]

```
double * jeod::Vector3::decr (
    const double subtrahend[3],
    double vec[3] ) [inline], [static]
```

Decrement a vector, $\text{vec}[i] -= \text{subtrahend}[i]$.

Returns

Decrementated vector

Parameters

<i>in</i>	<i>subtrahend</i>	Decrement
<i>in, out</i>	<i>vec</i>	Vector

Definition at line 398 of file vector3_inline.hh.

7.5.2.6 `decr()` [2/2]

```
double * jeod::Vector3::decr (
    const double subtrahend1[3],
    const double subtrahend2[3],
    double vec[3] ) [inline], [static]
```

Decrement a vector, $\text{vec}[i] -= \text{subtrahend1}[i] + \text{subtrahend2}[i]$.

Returns

Decrementated vector

Parameters

<i>in</i>	<i>subtrahend1</i>	Decrement
<i>in</i>	<i>subtrahend2</i>	Decrement
<i>in, out</i>	<i>vec</i>	Vector

Definition at line 415 of file vector3_inline.hh.

7.5.2.7 diff()

```
double * jeod::Vector3::diff (
    const double minuend[3],
    const double subtrahend[3],
    double vec[3] ) [inline], [static]
```

Compute the difference between two vectors, $\text{diff}[i] = \text{minuend}[i] - \text{subtrahend}[i]$.

Returns

Difference vector

Parameters

in	<i>minuend</i>	Minuend
in	<i>subtrahend</i>	Subtrahend
out	<i>vec</i>	Difference vector

Definition at line 467 of file vector3_inline.hh.

7.5.2.8 dot()

```
double jeod::Vector3::dot (
    const double vec2[3],
    const double vec1[3] ) [inline], [static]
```

Compute vector inner product, $\text{result} = \sum_i \text{vec1}[i] * \text{vec2}[i]$.

Returns

Inner product

Parameters

in	<i>vec2</i>	Vector 2
in	<i>vec1</i>	Vector 1

Definition at line 159 of file vector3_inline.hh.

7.5.2.9 fill()

```
double * jeod::Vector3::fill (
    double scalar,
    double vec[3] ) [inline], [static]
```

Construct a vector from scalar, $\text{vec}[i] = \text{scalar}$.

Returns

Filled vector

Parameters

in	<i>scalar</i>	Scalar
out	<i>vec</i>	Filled vector

Definition at line 103 of file vector3_inline.hh.

7.5.2.10 incr() [1/2]

```
double * jeod::Vector3::incr (
    const double addend[3],
    double vec[3] ) [inline], [static]
```

Increment a vector, *vec*[*i*] += *addend*[*i*].

Returns

Incremented vector

Parameters

in	<i>addend</i>	Increment
in, out	<i>vec</i>	Vector

Definition at line 365 of file vector3_inline.hh.

7.5.2.11 incr() [2/2]

```
double * jeod::Vector3::incr (
    const double addend1[3],
    const double addend2[3],
    double vec[3] ) [inline], [static]
```

Increment a vector, *vec*[*i*] += *addend1*[*i*] + *addend2*[*i*].

Returns

Incremented vector

Parameters

in	<i>addend1</i>	Increment
in	<i>addend2</i>	Increment
in, out	<i>vec</i>	Vector

Definition at line 382 of file vector3_inline.hh.

7.5.2.12 initialize()

```
double * jeod::Vector3::initialize (
    double vec[3] ) [inline], [static]
```

Zero-fill vector, $\text{vec}[i] = 0.0$.

Returns

Zero-filled vector

Parameters

out	vec	Zero-filled vector
-----	-----	--------------------

Definition at line 76 of file vector3_inline.hh.

Referenced by normalize().

7.5.2.13 negate() [1/2]

```
double * jeod::Vector3::negate (
    double vec[3] ) [inline], [static]
```

Negate vector in-place, $\text{vec}[i] = -\text{vec}[i]$.

Returns

Negated vector

Parameters

in, out	vec	Vector
---------	-----	--------

Definition at line 261 of file vector3_inline.hh.

7.5.2.14 negate() [2/2]

```
double * jeod::Vector3::negate (
    const double vec[3],
    double copy[3] ) [inline], [static]
```

Negate vector, $\text{copy}[i] = -\text{vec}[i]$.

Returns

Negated vector

Parameters

in	<i>vec</i>	Source vector
out	<i>copy</i>	Negated vector

Definition at line 277 of file vector3_inline.hh.

References `copy()`.

7.5.2.15 normalize() [1/2]

```
double * jeod::Vector3::normalize (
    double vec[3] ) [inline], [static]
```

Make vector a unit vector in-place, $\text{vec} = \text{vec} * 1/\text{vmag}(\text{vec})$

Returns

Normalized vector

Parameters

in, out	<i>vec</i>	Vector
---------	------------	--------

Definition at line 192 of file vector3_inline.hh.

References `initialize()`, `scale()`, and `vmag()`.

Referenced by `normalize()`.

7.5.2.16 normalize() [2/2]

```
double * jeod::Vector3::normalize (
    const double vec[3],
    double unit_vec[3] ) [inline], [static]
```

Construct unit vector, $\text{unit_vec} = \text{vec} * 1/\text{vmag}(\text{vec})$

Returns

Unit vector

Parameters

in	<i>vec</i>	Vector
out	<i>unit_vec</i>	Unit vector

Definition at line 215 of file vector3_inline.hh.

References `copy()`, and `normalize()`.

7.5.2.17 `scale()` [1/2]

```
double * jeod::Vector3::scale (
    double scalar,
    double vec[3] ) [inline], [static]
```

Scale a vector in-place, `vec[i] = scalar`.

Returns

Scaled vector

Parameters

in	<i>scalar</i>	Scalar
in, out	<i>vec</i>	Scaled vector

Definition at line 229 of file vector3_inline.hh.

Referenced by `normalize()`.

7.5.2.18 `scale()` [2/2]

```
double * jeod::Vector3::scale (
    const double vec[3],
    double scalar,
    double prod[3] ) [inline], [static]
```

Scale a vector, `prod[i] = vec[i] * scalar`.

Returns

Scaled vector

Parameters

in	<i>vec</i>	Source vector
in	<i>scalar</i>	Scalar
out	<i>prod</i>	Scaled vector

Definition at line 246 of file vector3_inline.hh.

7.5.2.19 scale_decr()

```
double * jeod::Vector3::scale_decr (
    const double vec[3],
    double scalar,
    double prod[3] ) [inline], [static]
```

Decrement a vector with a scaled vector, $\text{prod}[i] += \text{scalar} * \text{vec}[i]$.

Returns

Decrementated vector

Parameters

in	<i>vec</i>	Source vector
in	<i>scalar</i>	Scalar
in, out	<i>prod</i>	Decrementated vector

Definition at line 518 of file vector3_inline.hh.

7.5.2.20 scale_incr()

```
double * jeod::Vector3::scale_incr (
    const double vec[3],
    double scalar,
    double prod[3] ) [inline], [static]
```

Increment a vector with a scaled vector, $\text{prod}[i] += \text{scalar} * \text{vec}[i]$.

Returns

Incremented vector

Parameters

in	<i>vec</i>	Source vector
in	<i>scalar</i>	Scalar
in, out	<i>prod</i>	Incremented vector

Definition at line 501 of file vector3_inline.hh.

7.5.2.21 `sum()` [1/2]

```
double * jeod::Vector3::sum (
    const double addend1[3],
    const double addend2[3],
    double vec[3] ) [inline], [static]
```

Compute the sum of two vectors, $\text{vec}[i] = \text{addend1}[i] + \text{addend2}[i]$.

Returns

Sum vector

Parameters

in	<i>addend1</i>	Addend
in	<i>addend2</i>	Addend
out	<i>vec</i>	Sum vector

Definition at line 432 of file `vector3_inline.hh`.

7.5.2.22 `sum()` [2/2]

```
double * jeod::Vector3::sum (
    const double addend1[3],
    const double addend2[3],
    const double addend3[3],
    double vec[3] ) [inline], [static]
```

Compute the sum of three vectors, $\text{vec}[i] = \text{addend1}[i] + \text{addend2}[i] + \text{addend3}[i]$.

Returns

Sum vector

Parameters

in	<i>addend1</i>	Addend
in	<i>addend2</i>	Addend
in	<i>addend3</i>	Addend
out	<i>vec</i>	Sum vector

Definition at line 450 of file `vector3_inline.hh`.

7.5.2.23 `transform()` [1/2]

```
double * jeod::Vector3::transform (
    const double tmat[3][3],
```

```
const double vec[3],
double prod[3] ) [inline], [static]
```

Transform a column vector, $\text{prod}[i] = \text{tmat}[i][j] * \text{vec}[j]$.

Returns

Transformed vector

Parameters

in	<i>tmat</i>	Transformation matrix
in	<i>vec</i>	Source vector
out	<i>prod</i>	Transformed vector

Definition at line 294 of file vector3_inline.hh.

Referenced by transform().

7.5.2.24 transform() [2/2]

```
double * jeod::Vector3::transform (
    const double tmat[3][3],
    double vec[3] ) [inline], [static]
```

Transform a column vector in-place, $\text{vec}[i] <- \text{tmat}[i][j] * \text{vec}[j]$.

Returns

Transformed vector

Parameters

in	<i>tmat</i>	Transformation matrix
in, out	<i>vec</i>	Transformed vector

Definition at line 312 of file vector3_inline.hh.

References copy(), and transform().

7.5.2.25 transform_decr()

```
double * jeod::Vector3::transform_decr (
    const double tmat[3][3],
    const double vec[3],
    double prod[3] ) [inline], [static]
```

Decrement a vector with a transformed column vector, $\text{prod}[i] += \text{tmat}[i][j] * \text{vec}[j]$.

Returns

Decrementated vector

Parameters

<i>in</i>	<i>tmat</i>	Transformation matrix
<i>in</i>	<i>vec</i>	Source vector
<i>in, out</i>	<i>prod</i>	Decrementated vector

Definition at line 588 of file vector3_inline.hh.

7.5.2.26 transform_incr()

```
double * jeod::Vector3::transform_incr (
    const double tmat[3][3],
    const double vec[3],
    double prod[3] ) [inline], [static]
```

Increment a vector with a transformed column vector, $prod[i] += tmat[i][j]*vec[j]$.

Returns

Incremented vector

Parameters

<i>in</i>	<i>tmat</i>	Transformation matrix
<i>in</i>	<i>vec</i>	Source vector
<i>in, out</i>	<i>prod</i>	Incremented vector

Definition at line 569 of file vector3_inline.hh.

7.5.2.27 transform_transpose() [1/2]

```
double * jeod::Vector3::transform_transpose (
    const double tmat[3][3],
    const double vec[3],
    double prod[3] ) [inline], [static]
```

Transform a column vector with the transpose, $prod[i] = tmat[j][i]*vec[j]$.

Returns

Transformed vector

Parameters

in	<i>tmat</i>	Transformation matrix
in	<i>vec</i>	Source vector
out	<i>prod</i>	Transformed vector

Definition at line 330 of file vector3_inline.hh.

Referenced by transform_transpose().

7.5.2.28 transform_transpose() [2/2]

```
double * jeod::Vector3::transform_transpose (
    const double tmat[3][3],
    double vec[3] ) [inline], [static]
```

Transform a column vector in-place with the transpose, $\text{vec}[i] \leftarrow \text{tmat}[j][i] * \text{vec}[j]$.

Returns

Transformed vector

Parameters

in	<i>tmat</i>	Transformation matrix
in, out	<i>vec</i>	Transformed vector

Definition at line 348 of file vector3_inline.hh.

References copy(), and transform_transpose().

7.5.2.29 transform_transpose_decr()

```
double * jeod::Vector3::transform_transpose_decr (
    const double tmat[3][3],
    const double vec[3],
    double prod[3] ) [inline], [static]
```

decrement a vector with a transpose-transformed column vector, $\text{prod}[i] -= \text{tmat}[j][i] * \text{vec}[j]$

Returns

Decrement vector

Parameters

in	<i>tmat</i>	Transformation matrix
in	<i>vec</i>	Source vector
in, out	<i>prod</i>	Decrementated vector

Definition at line 626 of file vector3_inline.hh.

7.5.2.30 transform_transpose_incr()

```
double * jeod::Vector3::transform_transpose_incr (
    const double tmat[3][3],
    const double vec[3],
    double prod[3] ) [inline], [static]
```

Increment a vector with a transpose-transformed column vector, $prod[i] += tmat[j][i]*vec[j]$.

Returns

Incremented vector

Parameters

in	<i>tmat</i>	Transformation matrix
in	<i>vec</i>	Source vector
in, out	<i>prod</i>	Incremented vector

Definition at line 607 of file vector3_inline.hh.

7.5.2.31 unit()

```
double * jeod::Vector3::unit (
    unsigned int index,
    double vec[3] ) [inline], [static]
```

Construct unit vector, $vec[i] = \delta_{ij}$ (δ_{ij} is the Kronecker delta)

Returns

Unit vector

Parameters

in	<i>index</i>	Unit index: 0,1,2= $\hat{x}, \hat{y}, \hat{z}$
out	<i>vec</i>	Unit vector

Definition at line 89 of file vector3_inline.hh.

7.5.2.32 vmag()

```
double jeod::Vector3::vmag (
    const double vec[3] ) [inline], [static]
```

Compute vector magnitude, result = sqrt(vmagsq(vec))

Returns

Vector magnitude

Parameters

in	vec	Vector
----	-----	--------

Definition at line 181 of file vector3_inline.hh.

References vmagsq().

Referenced by normalize().

7.5.2.33 vmagsq()

```
double jeod::Vector3::vmagsq (
    const double vec[3] ) [inline], [static]
```

Compute square of vector magnitude, result = dot(vec,vec), but protects against underflow.

Returns

Inner product

Parameters

in	vec	Vector
----	-----	--------

Definition at line 170 of file vector3_inline.hh.

Referenced by vmag().

7.5.2.34 zero_small()

```
double * jeod::Vector3::zero_small (
    double limit,
    double vec[3] ) [inline], [static]
```

Zero-out small components of a vector, $\text{vec}[i] = 0$ if $\text{abs}(\text{vec}[i]) < \text{limit}$.

Returns

Truncated vector

Parameters

<i>in</i>	<i>limit</i>	Limit
<i>in, out</i>	<i>vec</i>	Truncated vector

Definition at line 116 of file vector3_inline.hh.

References `jeod::Numerical::fabs()`.

The documentation for this class was generated from the following files:

- [vector3.hh](#)
- [vector3_inline.hh](#)

Chapter 8

File Documentation

8.1 dm_invert.cc File Reference

Define Matrix3x3::invert.

```
#include <cmath>
#include "utils/message/include/message_handler.hh"
#include "../include/math_messages.hh"
#include "../include/matrix3x3.hh"
```

Namespaces

- [jeod](#)
Namespace jeod.

8.1.1 Detailed Description

Define Matrix3x3::invert.

8.2 dm_invert_symm.cc File Reference

Define Matrix3x3::invert_symmetric.

```
#include <cmath>
#include "utils/message/include/message_handler.hh"
#include "../include/math_messages.hh"
#include "../include/matrix3x3.hh"
```

Namespaces

- [jeod](#)
Namespace jeod.

8.2.1 Detailed Description

Define Matrix3x3::invert_symmetric.

8.3 gauss_quadrature.cc File Reference

Define Gauss Quadrature functionality.

```
#include "../include/gauss_quadrature.hh"
```

Namespaces

- [jeod](#)
Namespace jeod.

8.3.1 Detailed Description

Define Gauss Quadrature functionality.

8.4 gauss_quadrature.hh File Reference

Gauss Quadrature implementation.

Data Structures

- class [jeod::GaussQuadrature](#)

Namespaces

- [jeod](#)
Namespace jeod.

8.4.1 Detailed Description

Gauss Quadrature implementation.

8.5 math_messages.cc File Reference

Implement the class MathMessages.

```
#include "utils/message/include/make_message_code.hh"  
#include "../include/math_messages.hh"
```

Namespaces

- [jeod](#)
Namespace jeod.

Macros

- `#define MAKE_MATH_MESSAGE_CODE(id) JEOD_MAKE_MESSAGE_CODE(MathMessages, "utils/math/", id)`

8.5.1 Detailed Description

Implement the class MathMessages.

8.6 math_messages.hh File Reference

Define the class MathMessages.

Data Structures

- class [jeod::MathMessages](#)
Specifies the message IDs used in the math model.

Namespaces

- [jeod](#)
Namespace jeod.

8.6.1 Detailed Description

Define the class MathMessages.

8.7 matrix3x3.hh File Reference

Matrix math inline functions.

```
#include "matrix3x3_inline.hh"
```

Data Structures

- class [jeod::Matrix3x3](#)
Provides static methods for operations that involve 3x3 matrices.

Namespaces

- [jeod](#)

Namespace jeod.

Macros

- `#define` [IDENTITY](#)

8.7.1 Detailed Description

Matrix math inline functions.

8.7.2 Macro Definition Documentation

8.7.2.1 IDENTITY

```
#define IDENTITY
```

Value:

```
{1.0, 0.0, 0.0}, {0.0, 1.0, 0.0},
{
    0.0, 0.0, 1.0
}
```

Definition at line 180 of file matrix3x3.hh.

8.8 matrix3x3_inline.hh File Reference

Matrix math inline functions.

```
#include <cstdio>
#include "matrix3x3.hh"
```

Namespaces

- [jeod](#)

Namespace jeod.

8.8.1 Detailed Description

Matrix math inline functions.

8.9 numerical.hh File Reference

Miscellaneous math inline functions.

```
#include "numerical_inline.hh"
```

Data Structures

- class [jeod::Numerical](#)
Provides miscellaneous numerical functions.

Namespaces

- [jeod](#)
Namespace jeod.

8.9.1 Detailed Description

Miscellaneous math inline functions.

8.10 numerical_inline.hh File Reference

Vector math inline functions.

```
#include "numerical.hh"
```

Namespaces

- [jeod](#)
Namespace jeod.

Variables

- static constexpr double [jeod::SQRT_DBL_MIN](#) {1.4916681462400413e-154}

8.10.1 Detailed Description

Vector math inline functions.

8.11 vector3.hh File Reference

Vector math inline functions.

```
#include "vector3_inline.hh"
```

Data Structures

- class [jeod::Vector3](#)
Provides static methods for operations that involve 3-vectors.

Namespaces

- [jeod](#)
Namespace jeod.

8.11.1 Detailed Description

Vector math inline functions.

8.12 vector3_inline.hh File Reference

Vector math inline functions.

```
#include <cmath>
#include "numerical.hh"
#include "vector3.hh"
```

Namespaces

- [jeod](#)
Namespace jeod.

8.12.1 Detailed Description

Vector math inline functions.

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