

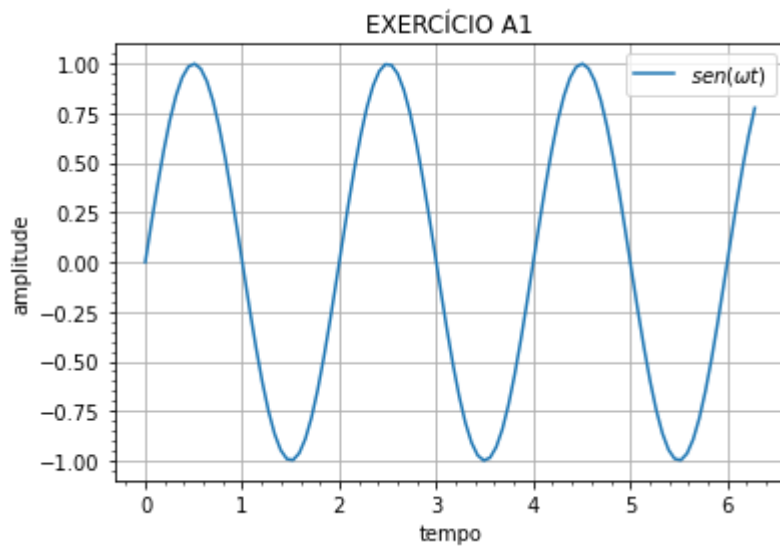


Lista 1 – Treinamento com uma linguagem de programação científica **negrito**

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In []: *# a1) Construção de gráficos x-y (intervalo 0 a 2π), atribuindo valores para ω_1 e ω_2 .*

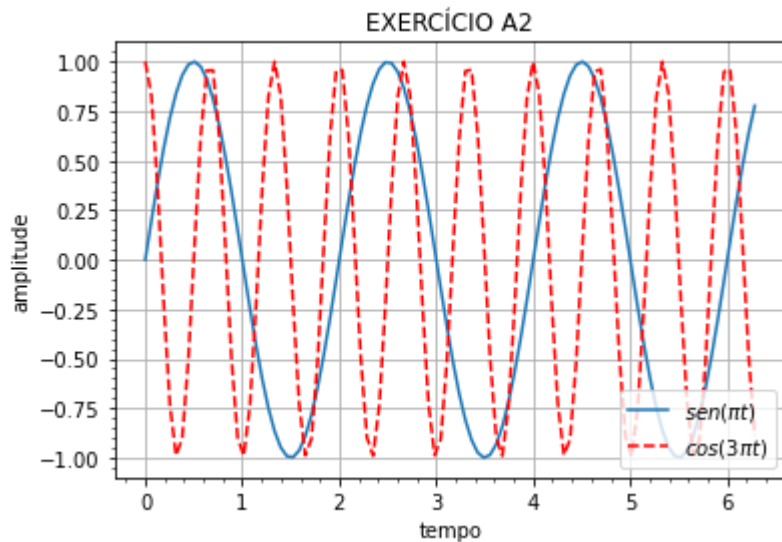
```
from pylab import *
t = linspace(0,2*pi, 100)
plot(t,sin(pi*t), label='$sen(\omega t)$')
xlabel('tempo')
ylabel('amplitude')
title("EXERCÍCIO A1")
legend()
grid()
minorticks_on()
```



In []:

In []: *# a2) Construção de gráficos x-y (intervalo 0 a 2π), atribuindo valores para ω_1 e ω_2 .*

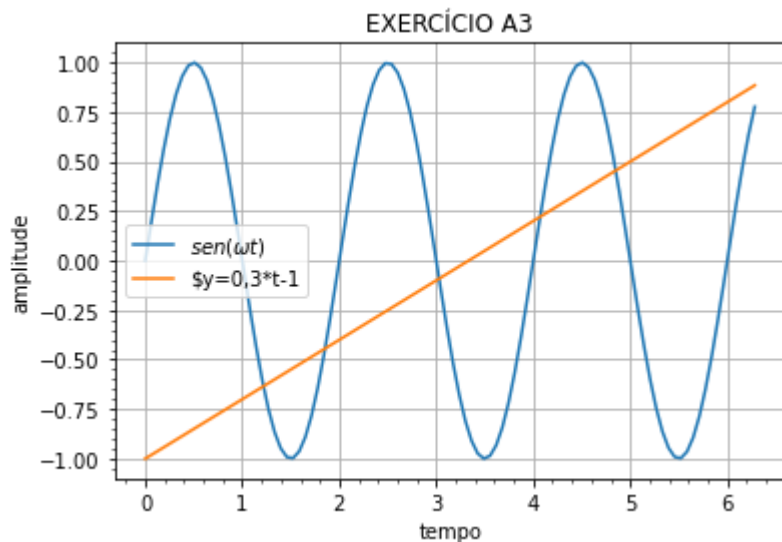
```
from pylab import *
t = linspace(0,2*pi, 100)
f1=sin(pi*t)
f2=cos(3*pi*t)
plot(t,f1, label='$sen(\pi t)$')
plot(t,f2, 'r--', label='$cos(3\pi t)$')
xlabel('tempo')
ylabel('amplitude')
title("EXERCÍCIO A2")
legend(loc='lower right')
grid()
minorticks_on()
```



In []: *# a3) Construção de gráficos x-y (intervalo 0 a 2π), atribuindo valores para ω1 e ω2.*

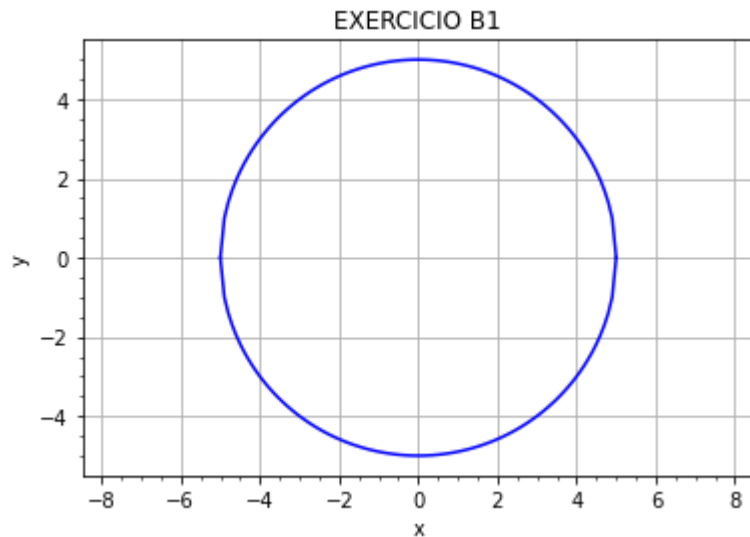
```
def y(a,b,t):
    return a*t+b

t = linspace(0,2*pi, 100)
plot(t,sin(pi*t), label='$sen(\\omega t)$')
plot(t,y(0.3,-1,t),label='$y=0,3*t-1$')
xlabel('tempo')
ylabel('amplitude')
title("EXERCÍCIO A3")
legend()
grid()
minorticks_on()
```



In []: *# b1) Construção de gráficos x-y*

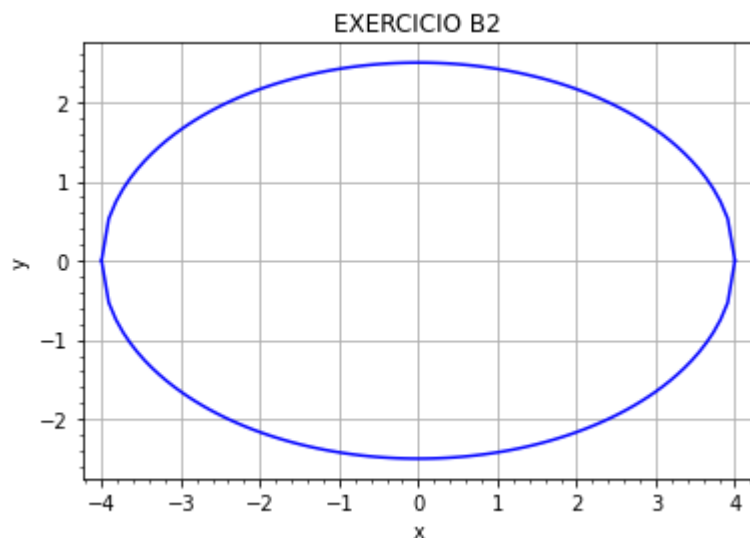
```
x=linspace(-5,5,100)
y=sqrt(5**2-x**2)
plot(x,y,'b-',label='$y^2 + x^2 = 5^2$')
plot(x,-y,'b-')
axis('equal')
xlabel('x')
ylabel('y')
title("EXERCICIO B1")
legend
grid()
minorticks_on()
```



```
In [ ]: # b2) Construção de gráficos x-y

x=linspace(-4,5,100)
y=sqrt(2.5**2*(1-x**2/4**2))
plot(x,y,'b-', label="$\\frac{x^2}{4^2}+\\frac{y^2}{2,5^2}=1$")
plot(x,-y,'b-')
axis('equal')
xlabel('x')
ylabel('y')
title("EXERCICIO B2")
legend
grid()
minorticks_on()
```

/usr/local/lib/python3.7/dist-packages/ipykernel_launcher.py:4: RuntimeWarning: invalid value encountered in sqrt
after removing the cwd from sys.path.



```
In [ ]: # c1) Zeros de funções (métodos gráficos)
```

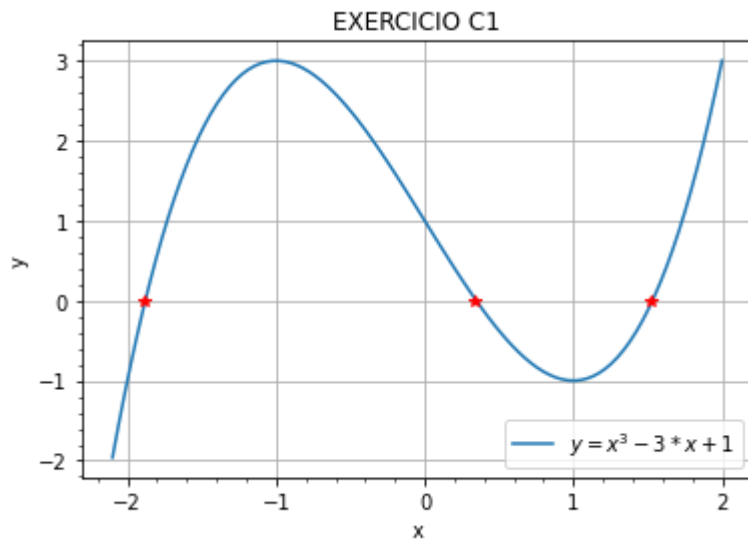
```
def y(x):
    return x**3-3*x+1
x = linspace(-2.1,2,100)
rz=[-1.89, 0.33, 1.52]
plot(x,y(x), label='$y=x^3-3*x+1$')
for i in range(len(rz)):
    plot(rz[i], 0, 'r*')
xlabel('x')
```

```

ylabel('y')
title("EXERCICIO C1")
legend()
grid()
minorticks_on()
print("As raízes são:", rz)

```

As raízes são: [-1.89, 0.33, 1.52]



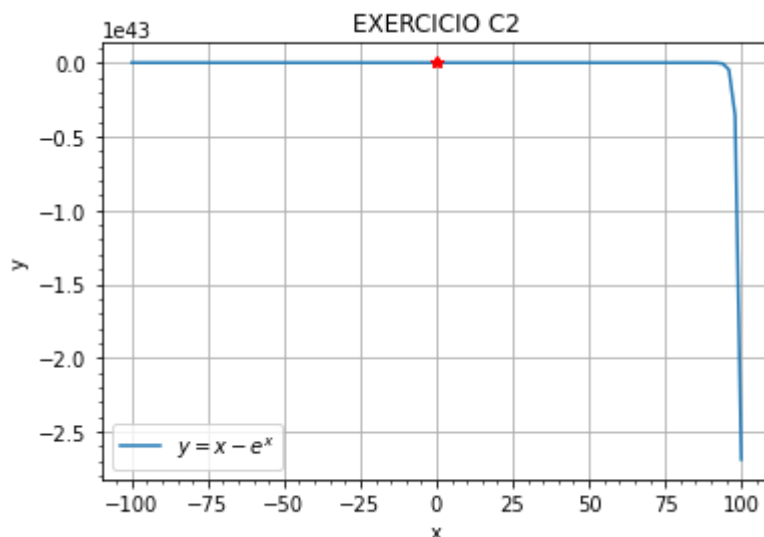
In []: # c2) Zeros de funções (métodos gráficos)

```

def y(x):
    return x-exp(x)
x = linspace(-100,100,100)
rz=[-1.89, 0.33, 1.52]
plot(x,y(x), label='$y=x-e^x$')
for i in range(len(rz)):
    plot(rz[i], 0, 'r*')
xlabel('x')
ylabel('y')
title("EXERCICIO C2")
legend()
grid()
minorticks_on()
print("As raízes são:", rz)

```

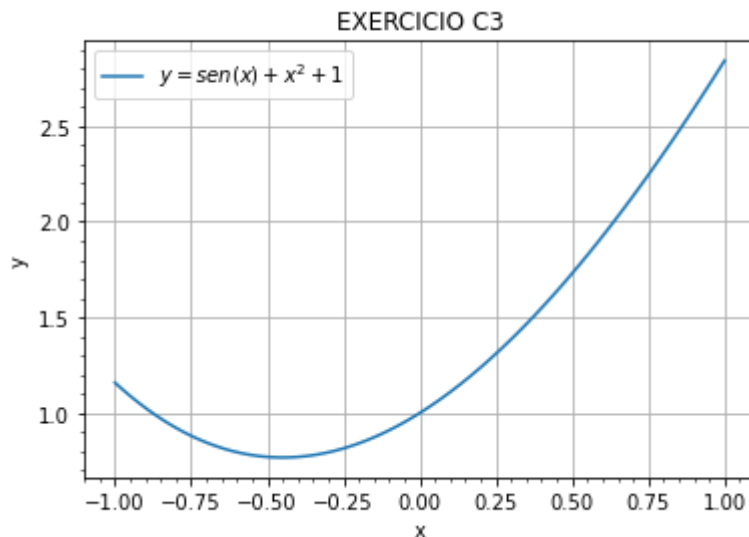
As raízes são: [-1.89, 0.33, 1.52]



In []: # c3) Zeros de funções (métodos gráficos)

```
def y(x):
    return sin(x) + x**2 + 1
x = linspace(-1,1,100)
plot(x,y(x), label='$y=sen(x)+x^2+1$')
xlabel('x')
ylabel('y')
title("EXERCICIO C3")
legend()
grid()
minorticks_on()
print("As raízes são:", rz)
```

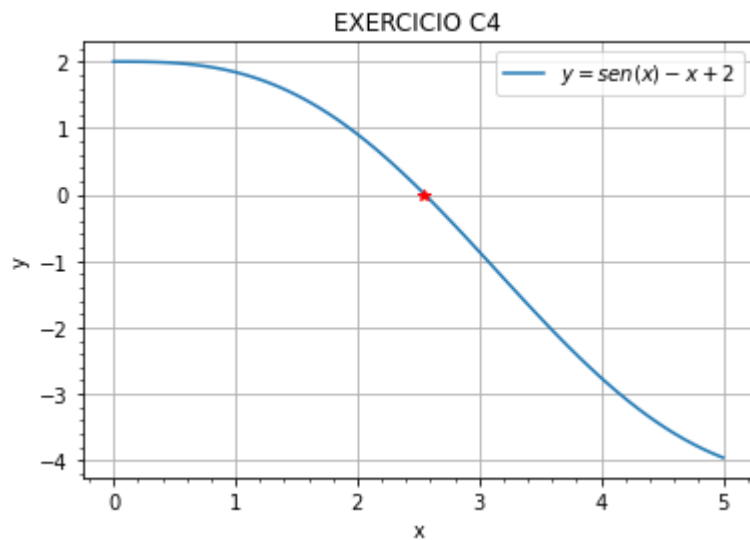
As raízes são: [2.55]



In []: # c4) Zeros de funções (métodos gráficos)

```
def y(x):
    return sin(x) - x + 2
x = linspace(0,5,100)
rz=[2.55]
plot(x,y(x), label='$y=sen(x)- x + 2$')
for i in range(len(rz)):
    plot(rz[i], 0, 'r*')
xlabel('x')
ylabel('y')
title("EXERCICIO C4")
legend()
grid()
minorticks_on()
print("As raízes são:", rz)
```

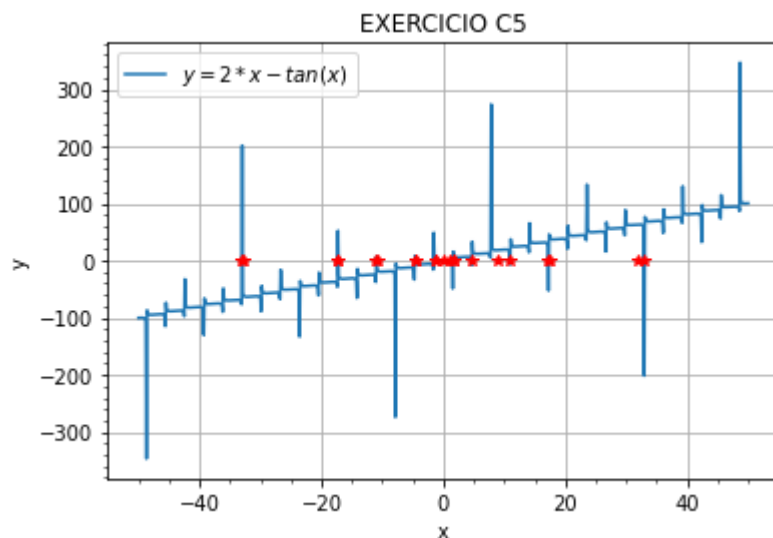
As raízes são: [2.55]



In... *# c5) Zeros de funções (métodos gráficos)*

```
def y(x):
    return 2*x-tan(x)
x = linspace(-50,50,1000)
rz=[-33.06,-32.9,-17.32,-17.2,-10.98,-10.92,-4.68,-4.58,1.62,-1.16,-1.16,0,1.16,1.62,4.58,10.92,17.2,17.32,32.9,33.06]
plot(x,y(x), label='$y=2*x-tan(x)$')
for i in range(len(rz)):
    plot(rz[i], 0, 'r*')
xlabel('x')
ylabel('y')
title("EXERCICIO C5")
legend()
grid()
minorticks_on()
print("As raízes são:", rz)
```

As raízes são: [-33.06, -32.9, -17.32, -17.2, -10.98, -10.92, -4.68, -4.58, 1.62, -1.16, -1.16, 0, 1.16, 1.62, 4.58, 10.92, 17.2, 17.32, 32.9, 33.06]



In []: *# c6) Zeros de funções (métodos gráficos)*

```
def y(x):
    return x**2+log(x)
x = linspace(0,5,100)
rz=[0.653]
plot(x,y(x), label='$y=x**2+log(x)$')
for i in range(len(rz)):
    plot(rz[i], 0, 'r*')
```

```

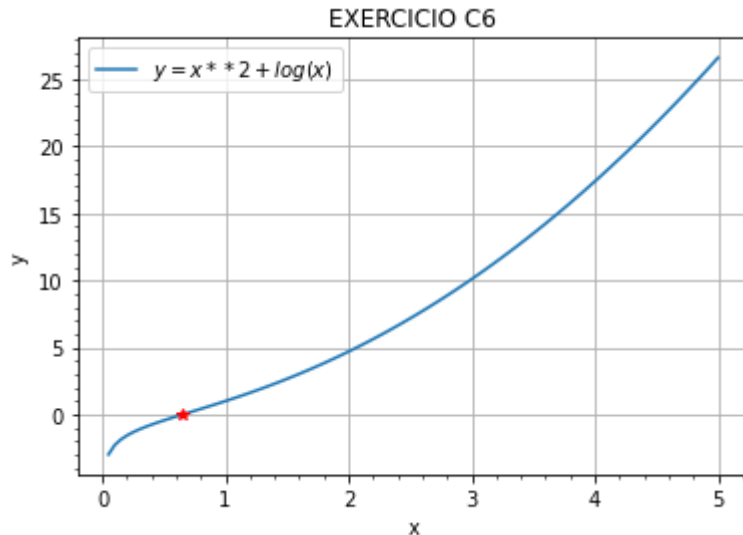
xlabel('x')
ylabel('y')
title("EXERCICIO C6")
legend()
grid()
minorticks_on()
print("As raízes são:", rz)

```

/usr/local/lib/python3.7/dist-packages/ipykernel_launcher.py:4: RuntimeWarning: divide by zero encountered in log

after removing the cwd from sys.path.

As raízes são: [0.653]



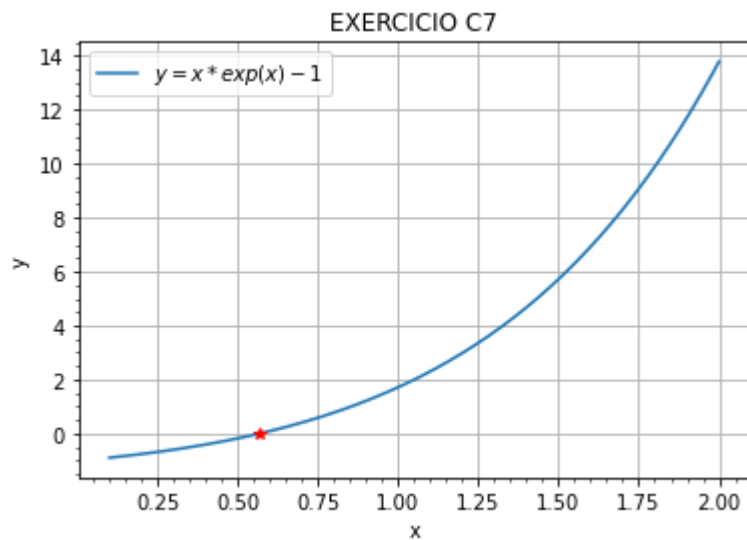
In []: # c7) Zeros de funções (métodos gráficos)

```

def y(x):
    return x*exp(x)-1
x = linspace(0.1,2,1000)
rz=[0.567]
plot(x,y(x), label='$y=x*exp(x)-1$')
for i in range(len(rz)):
    plot(rz[i], 0, 'r*')
xlabel('x')
ylabel('y')
title("EXERCICIO C7")
legend()
grid()
minorticks_on()
print("As raízes são:", rz)

```

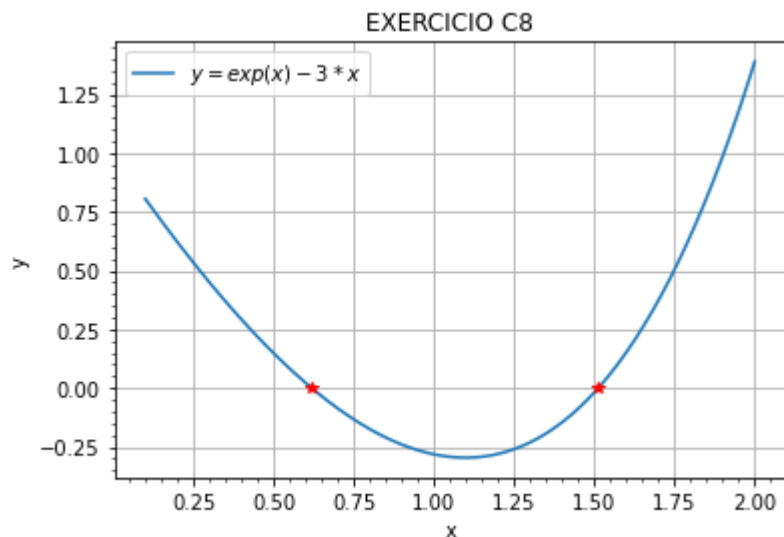
As raízes são: [0.567]



In []: *# c8) Zeros de funções (métodos gráficos)*

```
def y(x):
    return exp(x)-3*x
x = linspace(0.1,2,1000)
rz=[0.619, 1.5121]
plot(x,y(x), label='$y=exp(x)-3*x$')
for i in range(len(rz)):
    plot(rz[i], 0, 'r*')
xlabel('x')
ylabel('y')
title("EXERCICIO C8")
legend()
grid()
minorticks_on()
print("As raízes são:", rz)
```

As raízes são: [0.619, 1.5121]



In []: *# c9) Zeros de funções (métodos gráficos)*

```
def y(x):
    return x**3+cos(x)
x = linspace(-5,5,1000)
rz=[-0.866]
plot(x,y(x), label='$y=x**3+cos(x)$')
for i in range(len(rz)):
    plot(rz[i], 0, 'r*')
xlabel('x')
```

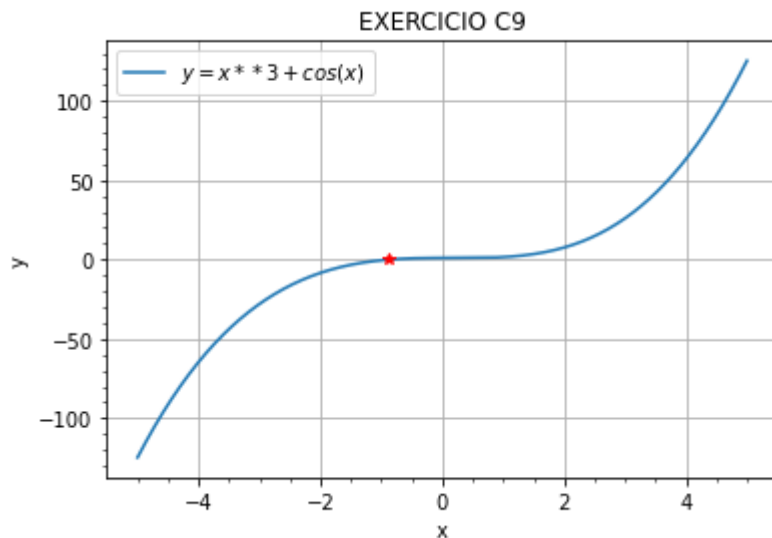


```

ylabel('y')
title("EXERCICIO C9")
legend()
grid()
minorticks_on()
print("As raízes são:", rz)

```

As raízes são: [-0.866]



In ... # d) Desenvolva um programa que, aplicando o método da bisecção, resolva as seguintes q

```

def bissecao(f,a,b,tol=1e-9,Nmax=50):
    n=1
    while n<Nmax:
        c=(b+a)/2
        #print(n, 'f(c)=', f(c))
        if f(c)==0 or ((b + a)/2)<tol:
            print('raiz=',c)
            print('erro=',f(c))
            if f(c)<=1e-2:
                return c
            elif sign(f(c)*f(a))>0:
                a=c
            else:
                b=c
        n +=1
    print('Raízes não encontradas')

```

Raízes não encontradas

In ... # d1) Desenvolva um programa que, aplicando o método da bisecção, resolva as seguintes

```

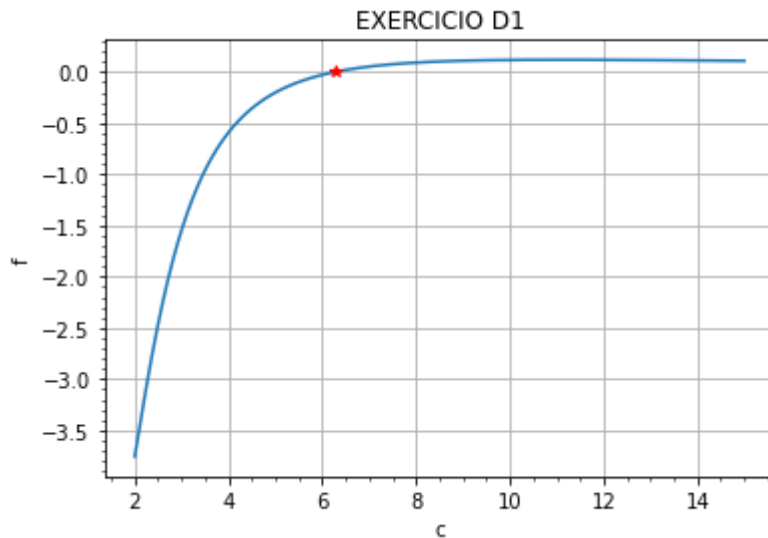
def f(R):
    return sin(8/R) - 6/R
#Verificando o intervalo de valores
x=linspace(2,15,1000)
plot(x,f(x))
xlabel('c')
ylabel('f')
title("EXERCICIO D1")
grid()
minorticks_on()

#Resolução
r=bissecao(f,a=4,b=8)
plot(6.27,0,'r*')
#Ângulo teta

```

```
th=arctan(6/6.27)
#Altura h
h=6.27*(1-cos(th))
print('A altura de', h, 'm')
```

A altura de 1.7399771127621582 m



In ... # d2) Desenvolva um programa que, aplicando o método da bisecção, resolva as seguintes

```
import matplotlib.pyplot as plt
import numpy as np

rho=1000
def f(th):
    return th-sin(th)-430*2/(9.81*rho*(0.3)**2)

#Verificando o intervalo de valores
x=linspace(0, 2*pi, 1000)
plot(x,f(x))
xlabel('th[rad]')
ylabel('f')
title("EXERCICIO D2")
grid()
minorticks_on()

#Resolução
th=bissecao(f,a=0,b=3)
h=1-cos((th/2)*100)
print('A profundidade é', h, 'm')
#plot(th,0,'r*')
```

In ... # d3) Desenvolva um programa que, aplicando o método da bisecção, resolva as seguintes

```
def f(r):
    gm_af=11.5
    gm_aq=9.96
    rho_t=60e-3
    waf=4*pi*r**3*gm_af/3
    wt=4*pi*r**2*rho_t*9.81
    waq=4*pi*r**3*gm_aq/3
    return waf-wt-waq-1300

x=linspace(0,10,1000)
plot(x,f(x))
```

```
xlabel('r')
ylabel('f')
title("EXERCICIO D3")
grid()
minorticks_on()

r=bissecao(f,a=0,b=10)
plot(r,0,'r*')
print('O diâmetro do balão deverá ser de', 2*r, 'm')
```

In ... *# d4) Desenvolva um programa que, aplicando o método da bisecção, resolva as seguintes*

```
def f(c):
    return -0.4+1.74*log(1e5*sqrt(c))-sqrt(1/c)
x=linspace(0,10,1000)
plot(x,f(x))
xlabel('c')
ylabel('f')
title("EXERCICIO D4")
grid()
minorticks_on()

c=bissecao(f,a=0.0001,b=0.1)
plot(c,0,'r*')
print('O diâmetro do balão deverá ser de', 2*r, 'm')
```