

Task 1: Ion Identification

A) For **Feature A** the atom responsible is **oxygen(833.33 Å)** .
its ionic state is (+1) [O II spectrum]

For **Feature B** the atom responsible is **Carbon(903.62 Å)** .
its ionic state is (+1) [C II spectrum]

For **Feature C** the atoms responsible are **Nitrogen(915-916Å)**
its ionic state is (+1) [N II spectrum],
Hydrogen (930-972 Å) its ionic state is (+0) [H I spectrum],
Oxygen (988 , 1025Å) its ionic state is (+0) [O I spectrum]

For **Feature D** the atom responsible is **Carbon(1036-1037Å)**
its ionic state is (+1) [C II spectrum],
oxygen atom is also in this region(**1039.230 Å**)
its ionic state is (+0) [O I spectrum],

For **Feature E** the atom responsible is **Nitrogen(1084.580Å)**
its ionic state is (+1) [N II spectrum],

For **Feature F** the atom responsible is **Hydrogen(1215Å)**
its ionic state is (+0) [H I spectrum],

For **Feature G** the atom responsible is **Oxygen(1304Å)**
its ionic state is (+0) [O I spectrum],

For **Feature H** the atom responsible is **Carbon(1329Å)**
its ionic state is (+0) [C I spectrum],
[C II spectrum] is also present in this region (**1334-1335Å**) ,
its ionic state is (+1)

B) Lyman Series:

$$1/\lambda = R_H(1 - 1/n^2)$$

Where n is a natural number greater than or equal to 2 (i.e., $n = 2, 3, 4, \dots$). λ =wavelength, $R_H = 1.0968 \times 10^{-3} \text{ \AA}^{-1}$ (Rydberg constant)

Therefore, the lines seen in the image above are the wavelengths corresponding to $n = 2$ on the right, to $n = \infty$ on the left.

The wavelengths in the Lyman series are all ultraviolet:

n	2	3	4	5	6	7	8	9	10	11	∞ , the Lym an limit
Wavelength (\AA)	1215.6701	1025.7220	972.53650	949.74287	937.80331	930.748142	926.225605	923.150275	920.963006	919.351334	911.753

In **Feature C** from right side in plot of light intensity vs wavelength in

Angstrom line started from 1025.7220 \AA where $n=3$ & continued till

911.753 \AA where $n = \infty$ There are infinitely many spectral lines, but they

become very dense as they approach $n = \infty$ (the Lyman Limit), so only some of the first lines and the last one appear.

The photon is emitted with the electron moving from a **higher energy level** to a

lower energy level. Here at near 911 \AA lines become very dense & emitted

photon energy of certain wavelength is absorbed by certain gaseous atom. As

large no of atoms are absorbing photon energy the intensity of light decreases

abruptly & reaches to near about 0.1

So the Plunge is created near 911 Å.

Task 2: Astrophysical Absorption Line Exercise

1) The intensity (I) of a given wavelength (λ) is given by the equation

$$I(\lambda) = \exp[-\alpha(\nu) \times d] \quad [\text{here } d = \text{thickness of slab}, \alpha(\nu) = \text{absorption co-efficient}]$$

$$n_H = 0.1, x = 0.1, \nu_0 = 2.46607 \times 10^{15}, \\ \Gamma = 6.265 \times 10^8, f = 0.4164, g_0 = 2, Z = 2.00$$

$$\begin{aligned} \text{A) } \nu &= c/\lambda \quad \text{here } \nu_0 = 2.46607 \times 10^{15} \\ \lambda &= 1/\nu_0 = 1/2.46607 \times 10^{15} = 0.4 \times 10^{-15} \\ \nu &= (3 \times 10^{10}) / 0.4 \times 10^{-15} = 7.5 \times 10^{25} \end{aligned}$$

$$\alpha(\nu) = (e^2 \times f \times n_H \times (1-x) \times g_0 \times \Gamma) / ((4 \times \pi \times m_e \times c \times Z)((\nu - \nu_0)^2 + (\Gamma/4\pi)^2))$$

After putting all values we get $\alpha(\nu) = 0.028 \times 10^{-46}$

Now spectrum

$$I(\lambda) = \exp[-0.028 \times 10^{-46} \times 10^{14}] = \exp[-0.028 \times 10^{-32}]$$

[here $d = 10^{14}$]

B) For $d = 10^{18}$ similarly

$$I(\lambda) = \exp[-0.028 \times 10^{-46} \times 10^{18}] = \exp[-0.028 \times 10^{-28}]$$

C) For $d = 10^{21}$ similarly

$$I(\lambda) = \exp[-0.028 \times 10^{-46} \times 10^{21}] = \exp[-0.028 \times 10^{-25}]$$

2)

A) The intensity (I) of a given wavelength (λ) is given by the equation

$$I(\lambda) = \exp[-\alpha(\nu) \times d] \quad [\text{here } d = \text{thickness of slab}, \alpha(\nu) = \text{absorption co-efficient}]$$

$$n_H = 0.1, x = 0.1, \nu_0 = 2.46632 \times 10^{15}, \\ \Gamma = 6.265 \times 10^8, f = 0.4164, g_0 = 2, Z = 2.00$$

$$\nu = c/\lambda \quad \text{here } \nu_0 = 2.46632 \times 10^{15} \\ \lambda = 1/\nu_0 = 1/2.46632 \times 10^{15} = 0.405 \times 10^{-15} \\ \nu = (3 \times 10^{10}) / 0.405 \times 10^{-15} = 7.40 \times 10^{25}$$

$$\alpha(\nu) = (e^2 \times f \times n_H \times (1-x) \times g_0 \times \Gamma) / ((4 \times \pi \times m_e \times c \times Z) ((\nu - \nu_0)^2 + (\Gamma/4\pi)^2))$$

After putting all values we get $\alpha(\nu) = 0.0288 \times 10^{-46}$

Now spectrum

$$I(\lambda) = \exp[-0.0288 \times 10^{-46} \times 10^{14}] = \exp[-0.0288 \times 10^{-32}] \\ [\text{here } d = 10^{14}]$$

B) For $d = 10^{18}$ similarly

$$I(\lambda) = \exp[-0.0288 \times 10^{-46} \times 10^{18}] = \exp[-0.0288 \times 10^{-28}]$$

C) For $d = 10^{21}$ similarly

$$I(\lambda) = \exp[-0.0288 \times 10^{-46} \times 10^{21}] = \exp[-0.0288 \times 10^{-25}]$$

3)

Let's say 6 spectras

$$A = \exp[-0.028 \times 10^{-32}]$$

$$B = \exp[-0.028 \times 10^{-28}]$$

$$C = \exp[-0.028 \times 10^{-25}]$$

$$D = \exp[-0.0288 \times 10^{-32}]$$

$$E = \exp[-0.0288 \times 10^{-28}]$$

$$F = \exp[-0.0288 \times 10^{-25}]$$

INTENSITY:

Intensity of A will be slightly greater than D, Intensity of B will be slightly greater than E, Intensity of C will be slightly greater than F

Overall order **A>D>B>E>C>F**

Frequency:

Frequency of A will be slightly greater than D, Frequency of B will be slightly greater than E, Frequency of C will be slightly greater than F

Overall order **A>D>B>E>C>F**

Wavelength :

Wavelength of D will be slightly greater than A, Wavelength of E will be slightly greater than B, Wavelength of F will be slightly greater than C

Overall order **F>C>E>B>D>A**