

Interval i_1 has center c_1 and percent tolerance t_1 .

Interval i_2 has center c_2 and percent tolerance t_2 .

The upper bound of i_1 is $c_1(\frac{(100+t_1)}{100})$

The lower bound of i_1 is $c_1(\frac{(100-t_1)}{100})$

The bounds of i_2 are similarly defined in terms of c_2 and t_2 .

Let interval i_3 = the product of i_1 and i_2 .

The upper bound of $i_3 = c_3(\frac{(100+t_3)}{100})$

which is also equal to $c_1(\frac{(100+t_1)}{100})c_2(\frac{(100+t_2)}{100})$

$$\begin{aligned} c_3 &\approx c_1 c_2 \\ c_3(\frac{(100+t_3)}{100}) &\approx c_3(\frac{(100+t_1)}{100})(\frac{(100+t_2)}{100}) \\ \frac{(100+t_3)}{100} &\approx (\frac{(100+t_1)}{100})(\frac{(100+t_2)}{100}) \\ 100+t_3 &\approx (100+t_1)(\frac{(100+t_2)}{100}) \\ 100+t_3 &\approx (100+t_1)(1+\frac{t_2}{100}) \\ 100+t_3 &\approx 100+t_1+t_2+\frac{(t_1 t_2)}{100} \\ t_3 &\approx t_1+t_2+\frac{(t_1 t_2)}{100} \end{aligned}$$

newpage The lower bound of $i_3 = c_3(\frac{(100-t_3)}{100})$

which is also equal to $c_1(\frac{(100-t_1)}{100})c_2(\frac{(100-t_2)}{100})$

$$\begin{aligned} c_3 &\approx c_1 c_2 \\ c_3(\frac{(100-t_3)}{100}) &\approx c_3(\frac{(100-t_1)}{100})(\frac{(100-t_2)}{100}) \\ \frac{(100-t_3)}{100} &\approx (\frac{(100-t_1)}{100})(\frac{(100-t_2)}{100}) \\ 100-t_3 &\approx (100-t_1)(\frac{(100-t_2)}{100}) \\ 100-t_3 &\approx (100-t_1)(1-\frac{t_2}{100}) \\ 100-t_3 &\approx 100-t_1-t_2+\frac{(t_1 t_2)}{100} \\ -t_3 &\approx -t_1-t_2+\frac{(t_1 t_2)}{100} \\ t_3 &\approx t_1+t_2-\frac{(t_1 t_2)}{100} \end{aligned}$$

The percent tolerance t_3 of the product $i_3 \approx t_1+t_2 \pm \frac{(t_1 t_2)}{100}$