Challenge Problem 4

A cylindrical drum of radius R rolls down a slope without slipping. Its center has velocity v and acceleration a parallel to the slope. What are the drum's angular velocity ω and angular acceleration α in terms of v and a? Justify your answer mathematically.

Note. Angular velocity is the number of radians the drum goes around each second, and angular acceleration is the rate of change of angular velocity.