

lbfgsb3c: Using the 2011 version of L-BFGSB

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Abstract

In 2011 the authors of the L-BFGSB program published a correction and update to their 1995 code. The latter is the basis of the L-BFGS-B method of the `optim()` function in base-R. The package `lbfgsb3` wrapped the updated code using a `.Fortran` call after removing a very large number of Fortran output statements. Matthew Fidler used this Fortran code and an `Rcpp` interface to produce package `lbfgsb3c` where the function `lbfgsb3c()` returns an object similar to that of base-R `optim()` and that of `optimx::optimr()`. Subsequently, in a fine example of the collaborations that have made **R** so useful, we have merged the functionality of package `lbfgsb3` into `lbfgsb3c`, as explained in this vignette. Note that this document is intended primarily to document our efforts to check the differences in variants of the code rather than be expository.

Provenance of the R `optim::L-BFGS-B` and related solvers

The base-R code `lbfgsb.c` (at writing in R-3.5.2/src/appl/) is commented:

```
/* l-bfgs-b.f -- translated by f2c (version 19991025).
```

```
From ?optim:
```

```
The code for method "L-BFGS-B" is based on Fortran code by Zhu,  
Byrd, Lu-Chen and Nocedal obtained from Netlib (file 'opt/lbfgs_bcm.shar')
```

```
The Fortran files contained no copyright information.
```

```
Byrd, R. H., Lu, P., Nocedal, J. and Zhu, C. (1995) A limited  
memory algorithm for bound constrained optimization.  
\emph{SIAM J. Scientific Computing}, \bold{16}, 1190--1208.
```

```
*/
```

The paper R. H. Byrd, Lu, Nocedal, and Zhu (1995a) builds on Lu et al. (1994). There have been a number of other workers who have followed-up on this work, but **R** code and packages seem to have largely stayed with codes derived from these original papers. Though the date of the paper is 1995, the ideas it embodies were around for a decade and a half at least, in particular in Nocedal80 and LiuN89. The definitive Fortran code was published as Zhu et al. (1997). This is available as `toms/778.zip` on www.netlib.org. A side-by-side comparison of the main subroutines in the two downloads from Netlib unfortunately shows a lot of differences. I have not tried to determine if these affect performance or are simply cosmetic.

More seriously perhaps, there were some deficiencies in the code(s), and in 2011 Nocedal's team published a Fortran code with some corrections (Morales and Nocedal (2011)). Since the **R** code predates this, I prepared package `lbfgsb3` (Nash et al. (2015)) to wrap the Fortran code. However, I did not discover any test cases where the `optim::L-BFGS-B` and `lbfgsb3` were different, though I confess to only running some limited tests. There are, in fact, more in this vignette.

In 2016, I was at a Fields Institute optimization conference in Toronto for the 70th birthday of Andy Conn. By sheer serendipity, Nocedal did not attend the conference, but sat down next to me at the conference dinner. When I asked him about the key changes, he said that the most important one was to fix the

computation of the machine precision, which was not always correct in the 1995 code. Since **R** gets this number as `.Machine$double.eps`, the offending code is irrelevant.

Within Morales and Nocedal (2011), there is also reported an improvement in the subspace minimization that is applied in cases of bounds constraints. Since few of the tests I have applied impose such constraints, it is reasonable that I will not have observed performance differences between the base-R `optim` code and my `lbfgsb3` package. More appropriate tests are welcome, and on my agenda.

Besides the ACM TOMS code, there are two related codes from the Northwestern team on NETLIB: http://netlib.org/opt/lbfgs_um.shar is for unconstrained minimization, while http://netlib.org/opt/lbfgs_bcm.shar handles bounds constrained problems. To these are attached references Liu and Nocedal (1989) and R. H. Byrd, Lu, Nocedal, and Zhu (1995b) respectively, most likely reflecting the effort required to implement the constraints.

The unconstrained code has been converted to **C** under the leadership of Naoaki Okazaki (see <http://www.chokkan.org/software/liblbfgs/>, or the fork at <https://github.com/MIRTK/LBFGS>). This has been wrapped for **R** as Coppola, Stewart, and Okazaki (2014) as the `lbfgs` package. This can be called from `optimx::optimr()`.

Using Rcpp (see Eddelbuettel and François (2011)) and the Fortran code in package `lbfgs3`, Matthew Fidler developed package `lbfgsb3c` (Fidler et al. (2018)). As this provides a more standard call and return than `lbfgsb3` Fidler and I are unified the two packages and released them both under the same name `lbfgsb3c`.

Functions in package `lbfgsb3c`

There is really only one optimizer function in the package, but it may be called by four (4) names:

- `lbfgsb3c()` uses Rcpp (Eddelbuettel (2013), Eddelbuettel and François (2011), Eddelbuettel and Balamuta (2017)) to streamline the call to the underlying Fortran. This is the base function used.
- `lbfgsb3x()` is an alias of `lbfgsb3c()`. We were using this name for a while, and have kept the alias to avoid having to edit test scripts.
- `lbfgsb3`, which imitates a `.Fortran` call of the compiled 2011 Fortran code. The object returned by this routine is NOT equivalent to the object returned by base-R `optim()` or by `optimx::optimr()`. Instead, it includes a structure `info` which contains the detailed diagnostic information of the Fortran code. For most users, this is not of interest, and I only recommend use of this function for those needing to examine how the optimization has been carried out.
- `lbfgsb3f()` is an alias of `lbfgsb3c()`.

We recommend using the `lbfgsb3c()` call for most uses.

Comparison with `optim::L-BFGS-B`

The new Fortran package claims better performance on bounds-constrained problems. Below we present two fairly simple tests, which unfortunately do not show any advantage. We welcome examples showing differences, either better or not. Note that we use the call that returns expanded information, but we do not interpret that here. See the documentation in the source Fortran for an explanation of the data returned in object `info`.

```
# ref BT.RES in Nash and Walker-Smith (1987)
library(lbfgsb3c)
sessionInfo()
```

```
## R version 3.6.1 (2019-07-05)
## Platform: x86_64-pc-linux-gnu (64-bit)
## Running under: Linux Mint 19.1
##
```

```

## Matrix products: default
## BLAS: /usr/lib/x86_64-linux-gnu/openblas/libblas.so.3
## LAPACK: /usr/lib/x86_64-linux-gnu/libopenblas-p0.2.20.so
##
## locale:
## [1] LC_CTYPE=en_CA.UTF-8 LC_NUMERIC=C
## [3] LC_TIME=en_CA.UTF-8 LC_COLLATE=en_CA.UTF-8
## [5] LC_MONETARY=en_CA.UTF-8 LC_MESSAGES=en_CA.UTF-8
## [7] LC_PAPER=en_CA.UTF-8 LC_NAME=C
## [9] LC_ADDRESS=C LC_TELEPHONE=C
## [11] LC_MEASUREMENT=en_CA.UTF-8 LC_IDENTIFICATION=C
##
## attached base packages:
## [1] stats graphics grDevices utils datasets methods base
##
## other attached packages:
## [1] lbfgsb3c_2019-3.19-2
##
## loaded via a namespace (and not attached):
## [1] compiler_3.6.1 magrittr_1.5 tools_3.6.1 htmltools_0.3.6
## [5] yaml_2.2.0 Rcpp_1.0.1 stringi_1.4.3 rmarkdown_1.13
## [9] knitr_1.23 stringr_1.4.0 xfun_0.8 digest_0.6.20
## [13] evaluate_0.14
bt.f<-function(x){
  sum(x*x)
}

bt.g<-function(x){
  gg<-2.0*x
}

bt.badsetup<-function(n){
  x<-rep(0,n)
  lo<-rep(0,n)
  up<-lo # to get arrays set
  bmsk<-rep(1,n)
  bmsk[(trunc(n/2)+1)]<-0
  for (i in 1:n) {
    x[i]<-2.2*i-n
    lo[i]<-1.0*(i-1)*(n-1)/n
    up[i]<-1.0*i*(n+1)/n
  }
  result<-list(x=x, lower=lo, upper=up, bdmsk=bmsk)
}

bt.setup0<-function(n){
  x<-rep(0,n)
  lo<-rep(0,n)
  up<-lower # to get arrays set
  bmsk<-rep(1,n)
  bmsk[(trunc(n/2)+1)]<-0
  for (i in 1:n) {
    lo[i]<-1.0*(i-1)*(n-1)/n

```

```

    up[i]<-1.0*i*(n+1)/n
  }
  x<-0.5*(lo+up)
  result<-list(x=x, lower=lo, upper=up, bdmsk=bmsk)
}
nn <- 4
baddy <- bt.badsetup(nn)
lo <- baddy$lower
up <- baddy$upper
x0 <- baddy$x
baddy

## $x
## [1] -1.8  0.4  2.6  4.8
##
## $lower
## [1] 0.00 0.75 1.50 2.25
##
## $upper
## [1] 1.25 2.50 3.75 5.00
##
## $bdmsk
## [1] 1 1 0 1

## optim()
solbad0 <- optim(x0, bt.f, bt.g, lower=lo, upper=up, method="L-BFGS-B", control=list(trace=3))

## N = 4, M = 5 machine precision = 2.22045e-16
## The initial X is infeasible. Restart with its projection.
## At X0, 2 variables are exactly at the bounds
## At iterate    0 f=          30.363 |proj g|=          2.55
##
## iterations 1
## function evaluations 2
## segments explored during Cauchy searches 3
## BFGS updates skipped 0
## active bounds at final generalized Cauchy point 4
## norm of the final projected gradient 0
## final function value 7.875
##
## F = 7.875
## final value 7.875000
## converged
solbad0

## $par
## [1] 0.00 0.75 1.50 2.25
##
## $value
## [1] 7.875
##
## $counts
## function gradient
##          2          2

```

```

##
## $convergence
## [1] 0
##
## $message
## [1] "CONVERGENCE: NORM OF PROJECTED GRADIENT <= PGTOL"
## lbfgsb3c
solbad1 <- lbfgsb3(x0, bt.f, bt.g, lower=lo, upper=up, control=list(trace=3))

## returned from lbfgsb3
## returned itask is 21 or "FG_START"
## computing f and g at prm=
## [1] 0.00 0.75 2.60 4.80
## At iteration 0 f=30.362500 max(abs(g))=0.000000
##
## =====
## Before call f=30.362500 task number 21, or "FG_START"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.00 0.75 1.50 2.25
## At iteration 2 f=7.875000 max(abs(g))=0.000000
##
## =====
## Before call f=7.875000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=7.875000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 7 or "CONVERGENCE: NORM_OF_PROJECTED_GRADIENT_<=_PGTOL"
solbad1

## $par
## [1] 0.00 0.75 1.50 2.25
##
## $grad
## [1] 0.0 1.5 3.0 4.5
##
## $value
## [1] 7.875
##
## $counts
## [1] 2 2
##
## $convergence
## [1] 0
##
## $message
## [1] "CONVERGENCE: NORM_OF_PROJECTED_GRADIENT_<=_PGTOL"
##
## $info
## $info$task

```

```
## [1] "CONVERGENCE: NORM_OF_PROJECTED_GRADIENT_<=_PGTOL"
##
## $info$itask
## [1] 7
##
## $info$lsave
## [1] TRUE TRUE TRUE FALSE
##
## $info$icsave
## [1] 6
##
## $info$dsave
## [1] 1.000000e+00 3.036250e+01 2.220446e-09 2.777139e+00 2.220446e-16
## [6] 0.000000e+00 0.000000e+00 0.000000e+00 0.000000e+00 0.000000e+00
## [11] -1.477500e+01 1.000000e+00 0.000000e+00 1.000000e+00 -3.020000e+01
## [16] 7.712500e+00 -3.020000e+01 -3.020000e-02 -3.020000e+01 -3.020000e+01
## [21] 3.036250e+01 3.036250e+01 3.036250e+01 0.000000e+00 0.000000e+00
## [26] 0.000000e+00 5.000000e+00 1.000000e+00 2.000000e+00
##
## $info$isave
## [1] 20 25 100 1 21 41 66 91 116 216 316 320 324 328 332 336 0
## [18] 0 0 0 0 3 0 8 0 0 1 0 0 1 0 0 3 2
## [35] 0 1 -1 0 4 5 0 0 0 1

## Possible timings
## library(microbenchmark)
## tbad0 <- microbenchmark(optim(x0, bt.f, bt.g, lower=lo, upper=up, method="L-BFGS-B"))
## t3c <- microbenchmark(lbfgsb3(x0, bt.f, bt.g, lower=lo, upper=up))
## Via optimx package
## library(optimx)
## meths <- c("L-BFGS-B", "lbfgsb3") # Note: lbfgsb3c not yet in optimx on CRAN
## allbt0 <- opm(x0, bt.f, bt.g, lower=lo, upper=up, method=meths)
## summary(allbt0, order=value)

# candlestick function
# J C Nash 2011-2-3
cstick.f<-function(x,alpha=100){
  x<-as.vector(x)
  r2<-crossprod(x)
  f<-as.double(r2+alpha/r2)
  return(f)
}

cstick.g<-function(x,alpha=100){
  x<-as.vector(x)
  r2<-as.numeric(crossprod(x))
  g1<-2*x
  g2 <- (-alpha)*2*x/(r2*r2)
  g<-as.double(g1+g2)
  return(g)
}
library(lbfgsb3c)
nm <- 2
x0 <- c(10,10)
lo <- c(1, 1)
```

```

up <- c(10,10)
print(x0)

## [1] 10 10

c2o <- optim(x0, cstick.f, cstick.g, lower=lo, upper=up, method="L-BFGS-B", control=list(trace=3))

## N = 2, M = 5 machine precision = 2.22045e-16
## At X0, 2 variables are exactly at the bounds
## At iterate    0 f=      200.5 |proj g|=      9
## Nonpositive definiteness in Cholesky factorization in formk;
##   refresh the lbfgs memory and restart the iteration.
##
## iterations 8
## function evaluations 14
## segments explored during Cauchy searches 14
## BFGS updates skipped 0
## active bounds at final generalized Cauchy point 0
## norm of the final projected gradient 1.12127e-06
## final function value 20
##
## F = 20
## final value 20.000000
## converged

c2o

## $par
## [1] 2.236068 2.236068
##
## $value
## [1] 20
##
## $counts
## function gradient
##      14      14
##
## $convergence
## [1] 0
##
## $message
## [1] "CONVERGENCE: REL_REDUCTION_OF_F <= FACTR*EPSMCH"

c2l <- lbfgsb3(x0, cstick.f, cstick.g, lower=lo, upper=up, control=list(trace=3))

## returned from lbfgsb3
## returned itask is 21 or "FG_START"
## computing f and g at prm=
## [1] 10 10
## At iteration 0 f=200.500000 max(abs(g))=19.950000
##
## =====
## Before call f=200.500000 task number 21, or "FG_START"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=

```

```

## [1] 1 1
## At iteration 2 f=52.000000 max(abs(g))=48.000000
##
## =====
## Before call f=52.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 7.357616 7.357616
## At iteration 3 f=109.192649 max(abs(g))=14.589699
##
## =====
## Before call f=109.192649 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=109.192649 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1 1
## At iteration 4 f=52.000000 max(abs(g))=48.000000
##
## =====
## Before call f=52.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 5.875652 5.875652
## At iteration 5 f=70.494861 max(abs(g))=11.504812
##
## =====
## Before call f=70.494861 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=70.494861 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1 1
## At iteration 6 f=52.000000 max(abs(g))=48.000000
##
## =====
## Before call f=52.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 4.932981 4.932981
## At iteration 7 f=50.723310 max(abs(g))=9.449436
##
## =====

```



```

## Before call f=50.723310 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=50.723310 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1 1
## At iteration 8 f=52.000000 max(abs(g))=48.000000
##
## =====
## Before call f=52.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 2.727727 2.727727
## At iteration 9 f=21.600973 max(abs(g))=2.991871
##
## =====
## Before call f=21.600973 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=21.600973 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1 1
## At iteration 10 f=52.000000 max(abs(g))=48.000000
##
## =====
## Before call f=52.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 2.221436 2.221436
## At iteration 11 f=20.001724 max(abs(g))=0.118221
##
## =====
## Before call f=20.001724 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=20.001724 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 2.240681 2.240681
## At iteration 12 f=20.000170 max(abs(g))=0.036788
##

```

```

## =====
## Before call f=20.000170 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=20.000170 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 2.236113 2.236113
## At iteration 13 f=20.000000 max(abs(g))=0.000362
##
## =====
## Before call f=20.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=20.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 2.236068 2.236068
## At iteration 14 f=20.000000 max(abs(g))=0.000001
##
## =====
## Before call f=20.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=20.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 8 or "CONVERGENCE: REL_REDUCTION_OF_F_<=_FACTR*EPSMCH"
c2l
## $par
## [1] 2.236068 2.236068
##
## $grad
## [1] -1.121272e-06 -1.121272e-06
##
## $value
## [1] 20
##
## $counts
## [1] 14 14
##
## $convergence
## [1] 0
##
## $message
## [1] "CONVERGENCE: REL_REDUCTION_OF_F_<=_FACTR*EPSMCH"

```

```

##
## $info
## $info$task
## [1] "CONVERGENCE: REL_REDUCTION_OF_F_<=_FACTR*EPSMCH"
##
## $info$itask
## [1] 8
##
## $info$lsave
## [1] FALSE TRUE TRUE TRUE
##
## $info$icsave
## [1] 6
##
## $info$dsave
## [1] 7.975088e+00 2.000000e+01 2.220446e-09 6.427782e-05 2.220446e-16
## [6] 0.000000e+00 0.000000e+00 0.000000e+00 0.000000e+00 0.000000e+00
## [11] 1.019265e-10 2.719644e+04 1.121272e-06 1.000000e+00 -3.295018e-08
## [16] 4.131638e-09 -3.295018e-08 -3.295018e-11 -3.295018e-08 -3.295018e-08
## [21] 2.000000e+01 2.000000e+01 2.000000e+01 0.000000e+00 0.000000e+00
## [26] 0.000000e+00 5.000000e+00 2.719644e+04 5.439289e+04
##
## $info$isave
## [1] 10 25 100 1 11 21 46 71 96 196 296 298 300 302 304 306 0
## [18] 0 0 0 0 14 0 8 0 0 1 3 3 8 3 0 1 14
## [35] 0 1 0 2 0 3 0 0 0 2

## meths <- c("L-BFGS-B", "lbfgsb3c", "Rummin", "Rcgmin", "Rtnmin")
## require(optimx)

## cstick2a <- opm(x0, cstick.f, cstick.g, method=meths, upper=up, lower=lo, control=list(kkt=FALSE))
## print(summary(cstick2a, par.select=1:2, order=value))
lo <- c(4, 4)
c2ob <- optim(x0, cstick.f, cstick.g, lower=lo, upper=up, method="L-BFGS-B", control=list(trace=3))

## N = 2, M = 5 machine precision = 2.22045e-16
## At X0, 2 variables are exactly at the bounds
## At iterate 0 f= 200.5 |proj g|= 6
##
## iterations 1
## function evaluations 2
## segments explored during Cauchy searches 2
## BFGS updates skipped 0
## active bounds at final generalized Cauchy point 2
## norm of the final projected gradient 0
## final function value 35.125
##
## F = 35.125
## final value 35.125000
## converged
c2ob

## $par
## [1] 4 4
##

```

```

## $value
## [1] 35.125
##
## $counts
## function gradient
##      2      2
##
## $convergence
## [1] 0
##
## $message
## [1] "CONVERGENCE: NORM OF PROJECTED GRADIENT <= PGTOL"
c2lb <- lbfgsb3(x0, cstick.f, cstick.g, lower=lo, upper=up, control=list(trace=3))

## returned from lbfgsb3
## returned itask is 21 or "FG_START"
## computing f and g at prm=
## [1] 10 10
## At iteration 0 f=200.500000 max(abs(g))=19.950000
##
## =====
## Before call f=200.500000 task number 21, or "FG_START"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 4 4
## At iteration 2 f=35.125000 max(abs(g))=7.218750
##
## =====
## Before call f=35.125000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=35.125000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 7 or "CONVERGENCE: NORM_OF_PROJECTED_GRADIENT_<=_PGTOL"
c2lb

## $par
## [1] 4 4
##
## $grad
## [1] 7.21875 7.21875
##
## $value
## [1] 35.125
##
## $counts
## [1] 2 2
##
## $convergence
## [1] 0
##

```

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## $message
## [1] "CONVERGENCE: NORM_OF_PROJECTED_GRADIENT_<=_PGTOL"
##
## $info
## $info$task
## [1] "CONVERGENCE: NORM_OF_PROJECTED_GRADIENT_<=_PGTOL"
##
## $info$itask
## [1] 7
##
## $info$lsave
## [1] FALSE TRUE TRUE FALSE
##
## $info$icsave
## [1] 6
##
## $info$dsave
## [1] 1.000000e+00 2.005000e+02 2.220446e-09 8.485281e+00 2.220446e-16
## [6] 0.000000e+00 0.000000e+00 0.000000e+00 0.000000e+00 0.000000e+00
## [11] -8.662500e+01 1.000000e+00 0.000000e+00 1.000000e+00 -2.394000e+02
## [16] 7.200000e+01 -2.394000e+02 -2.394000e-01 -2.394000e+02 -2.394000e+02
## [21] 2.005000e+02 2.005000e+02 2.005000e+02 0.000000e+00 0.000000e+00
## [26] 0.000000e+00 5.000000e+00 1.000000e+00 2.000000e+00
##
## $info$isave
## [1] 10 25 100 1 11 21 46 71 96 196 296 298 300 302 304 306 0
## [18] 0 0 0 0 2 0 8 0 0 1 0 0 1 0 0 2 2
## [35] 0 1 -1 0 2 3 0 0 0 1
##
## cstick2b <- opm(x0, cstick.f, cstick.g, method=meths, upper=up, lower=lo, control=list(kkt=FALSE))
## print(summary(cstick2b, par.select=1:2, order=value))

nn <- 100
x0 <- rep(10, nn)
up <- rep(10, nn)
lo <- rep(1e-4, nn)
cco <- optim(x0, cstick.f, cstick.g, lower=lo, upper=up, method="L-BFGS-B", control=list(trace=3))

## N = 100, M = 5 machine precision = 2.22045e-16
## At X0, 100 variables are exactly at the bounds
## At iterate 0 f= 10000 |proj g|= 9.9999
## Nonpositive definiteness in Cholesky factorization in formk;
## refresh the lbfgs memory and restart the iteration.
## At iterate 10 f = 20.004 |proj g|= 0.024942
##
## iterations 13
## function evaluations 23
## segments explored during Cauchy searches 311
## BFGS updates skipped 0
## active bounds at final generalized Cauchy point 0
## norm of the final projected gradient 1.75206e-08
## final function value 20
##
## F = 20
## final value 20.000000

```

```

## converged
cco

## $par
## [1] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [8] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [15] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [22] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [29] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [36] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [43] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [50] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [57] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [64] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [71] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [78] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [85] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [92] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [99] 0.3162278 0.3162278
##
## $value
## [1] 20
##
## $counts
## function gradient
##      23      23
##
## $convergence
## [1] 0
##
## $message
## [1] "CONVERGENCE: REL_REDUCTION_OF_F <= FACTR*EPSMCH"

ccl <- lbfgsb3(x0, cstick.f, cstick.g, lower=lo, upper=up, control=list(trace=3))

## returned from lbfgsb3
## returned itask is 21 or "FG_START"
## computing f and g at prm=
## [1] 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10
## [24] 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10
## [47] 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10
## [70] 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10 10
## [93] 10 10 10 10 10 10 10 10
## At iteration 0 f=10000.010000 max(abs(g))=19.999980
##
## =====
## Before call f=10000.010000 task number 21, or "FG_START"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [12] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [23] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [34] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [45] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04

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## [56] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [67] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [78] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [89] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [100] 1e-04
## At iteration 2 f=100000000.000001 max(abs(g))=1999999999.999786
##
## =====
## Before call f=100000000.000001 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217
## [8] 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217
## [15] 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217
## [22] 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217
## [29] 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217
## [36] 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217
## [43] 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217
## [50] 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217
## [57] 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217
## [64] 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217
## [71] 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217
## [78] 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217
## [85] 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217
## [92] 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217 6.666217
## [99] 6.666217 6.666217
## At iteration 3 f=4443.867047 max(abs(g))=13.332366
##
## =====
## Before call f=4443.867047 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=4443.867047 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [12] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [23] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [34] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [45] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [56] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [67] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [78] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [89] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [100] 1e-04
## At iteration 4 f=100000000.000001 max(abs(g))=1999999999.999786
##
## =====
## Before call f=100000000.000001 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3

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## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046
## [8] 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046
## [15] 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046
## [22] 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046
## [29] 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046
## [36] 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046
## [43] 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046
## [50] 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046
## [57] 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046
## [64] 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046
## [71] 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046
## [78] 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046
## [85] 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046
## [92] 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046 4.444046
## [99] 4.444046 4.444046
## At iteration 5 f=1975.005455 max(abs(g))=8.887865
##
## =====
## Before call f=1975.005455 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=1975.005455 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [12] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [23] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [34] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [45] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [56] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [67] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [78] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [89] 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04 1e-04
## [100] 1e-04
## At iteration 6 f=100000000.000001 max(abs(g))=1999999999.999786
##
## =====
## Before call f=100000000.000001 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704
## [8] 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704
## [15] 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704
## [22] 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704
## [29] 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704
## [36] 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704
## [43] 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704
## [50] 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704

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## [57] 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704
## [64] 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704
## [71] 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704
## [78] 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704
## [85] 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704
## [92] 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704 2.962704
## [99] 2.962704 2.962704
## At iteration 7 f=877.875251 max(abs(g))=5.924638
##
## =====
## Before call f=877.875251 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=877.875251 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.0009255641 0.0009255641 0.0009255641 0.0009255641 0.0009255641
## [6] 0.0009255641 0.0009255641 0.0009255641 0.0009255641 0.0009255641
## [11] 0.0009255641 0.0009255641 0.0009255641 0.0009255641 0.0009255641
## [16] 0.0009255641 0.0009255641 0.0009255641 0.0009255641 0.0009255641
## [21] 0.0009255641 0.0009255641 0.0009255641 0.0009255641 0.0009255641
## [26] 0.0009255641 0.0009255641 0.0009255641 0.0009255641 0.0009255641
## [31] 0.0009255641 0.0009255641 0.0009255641 0.0009255641 0.0009255641
## [36] 0.0009255641 0.0009255641 0.0009255641 0.0009255641 0.0009255641
## [41] 0.0009255641 0.0009255641 0.0009255641 0.0009255641 0.0009255641
## [46] 0.0009255641 0.0009255641 0.0009255641 0.0009255641 0.0009255641
## [51] 0.0009255641 0.0009255641 0.0009255641 0.0009255641 0.0009255641
## [56] 0.0009255641 0.0009255641 0.0009255641 0.0009255641 0.0009255641
## [61] 0.0009255641 0.0009255641 0.0009255641 0.0009255641 0.0009255641
## [66] 0.0009255641 0.0009255641 0.0009255641 0.0009255641 0.0009255641
## [71] 0.0009255641 0.0009255641 0.0009255641 0.0009255641 0.0009255641
## [76] 0.0009255641 0.0009255641 0.0009255641 0.0009255641 0.0009255641
## [81] 0.0009255641 0.0009255641 0.0009255641 0.0009255641 0.0009255641
## [86] 0.0009255641 0.0009255641 0.0009255641 0.0009255641 0.0009255641
## [91] 0.0009255641 0.0009255641 0.0009255641 0.0009255641 0.0009255641
## [96] 0.0009255641 0.0009255641 0.0009255641 0.0009255641 0.0009255641
## At iteration 8 f=1167312.048755 max(abs(g))=25223796.150888
##
## =====
## Before call f=1167312.048755 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486
## [8] 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486
## [15] 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486
## [22] 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486
## [29] 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486
## [36] 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486
## [43] 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486
## [50] 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486

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## [57] 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486
## [64] 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486
## [71] 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486
## [78] 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486
## [85] 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486
## [92] 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486 1.974486
## [99] 1.974486 1.974486
## At iteration 9 f=390.116136 max(abs(g))=3.946375
##
## =====
## Before call f=390.116136 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=390.116136 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.003123492 0.003123492 0.003123492 0.003123492 0.003123492
## [6] 0.003123492 0.003123492 0.003123492 0.003123492 0.003123492
## [11] 0.003123492 0.003123492 0.003123492 0.003123492 0.003123492
## [16] 0.003123492 0.003123492 0.003123492 0.003123492 0.003123492
## [21] 0.003123492 0.003123492 0.003123492 0.003123492 0.003123492
## [26] 0.003123492 0.003123492 0.003123492 0.003123492 0.003123492
## [31] 0.003123492 0.003123492 0.003123492 0.003123492 0.003123492
## [36] 0.003123492 0.003123492 0.003123492 0.003123492 0.003123492
## [41] 0.003123492 0.003123492 0.003123492 0.003123492 0.003123492
## [46] 0.003123492 0.003123492 0.003123492 0.003123492 0.003123492
## [51] 0.003123492 0.003123492 0.003123492 0.003123492 0.003123492
## [56] 0.003123492 0.003123492 0.003123492 0.003123492 0.003123492
## [61] 0.003123492 0.003123492 0.003123492 0.003123492 0.003123492
## [66] 0.003123492 0.003123492 0.003123492 0.003123492 0.003123492
## [71] 0.003123492 0.003123492 0.003123492 0.003123492 0.003123492
## [76] 0.003123492 0.003123492 0.003123492 0.003123492 0.003123492
## [81] 0.003123492 0.003123492 0.003123492 0.003123492 0.003123492
## [86] 0.003123492 0.003123492 0.003123492 0.003123492 0.003123492
## [91] 0.003123492 0.003123492 0.003123492 0.003123492 0.003123492
## [96] 0.003123492 0.003123492 0.003123492 0.003123492 0.003123492
## At iteration 10 f=102498.874093 max(abs(g))=656309.404765
##
## =====
## Before call f=102498.874093 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159
## [8] 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159
## [15] 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159
## [22] 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159
## [29] 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159
## [36] 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159
## [43] 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159
## [50] 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159

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## [57] 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159
## [64] 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159
## [71] 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159
## [78] 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159
## [85] 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159
## [92] 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159 1.314159
## [99] 1.314159 1.314159
## At iteration 11 f=173.280478 max(abs(g))=2.619506
##
## =====
## Before call f=173.280478 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=173.280478 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003
## [7] 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003
## [13] 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003
## [19] 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003
## [25] 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003
## [31] 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003
## [37] 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003
## [43] 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003
## [49] 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003
## [55] 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003
## [61] 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003
## [67] 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003
## [73] 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003
## [79] 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003
## [85] 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003
## [91] 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003 0.01054003
## [97] 0.01054003 0.01054003 0.01054003 0.01054003
## At iteration 12 f=9001.546538 max(abs(g))=17080.648379
##
## =====
## Before call f=9001.546538 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362
## [8] 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362
## [15] 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362
## [22] 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362
## [29] 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362
## [36] 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362
## [43] 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362
## [50] 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362
## [57] 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362
## [64] 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362
## [71] 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362

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## [78] 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362
## [85] 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362
## [92] 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362 0.8692362
## [99] 0.8692362 0.8692362
## At iteration 13 f=76.880658 max(abs(g))=1.708020
##
## =====
## Before call f=76.880658 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=76.880658 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013
## [8] 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013
## [15] 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013
## [22] 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013
## [29] 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013
## [36] 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013
## [43] 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013
## [50] 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013
## [57] 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013
## [64] 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013
## [71] 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013
## [78] 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013
## [85] 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013
## [92] 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013 0.0355013
## [99] 0.0355013 0.0355013
## At iteration 14 f=793.561220 max(abs(g))=446.918351
##
## =====
## Before call f=793.561220 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149
## [8] 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149
## [15] 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149
## [22] 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149
## [29] 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149
## [36] 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149
## [43] 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149
## [50] 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149
## [57] 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149
## [64] 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149
## [71] 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149
## [78] 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149
## [85] 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149
## [92] 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149 0.5626149
## [99] 0.5626149 0.5626149
## At iteration 15 f=34.812759 max(abs(g))=1.012926

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##
## =====
## Before call f=34.812759 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=34.812759 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916
## [8] 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916
## [15] 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916
## [22] 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916
## [29] 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916
## [36] 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916
## [43] 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916
## [50] 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916
## [57] 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916
## [64] 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916
## [71] 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916
## [78] 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916
## [85] 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916
## [92] 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916 0.1157916
## [99] 0.1157916 0.1157916
## At iteration 16 f=75.924777 max(abs(g))=12.650870
##
## =====
## Before call f=75.924777 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455
## [8] 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455
## [15] 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455
## [22] 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455
## [29] 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455
## [36] 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455
## [43] 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455
## [50] 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455
## [57] 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455
## [64] 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455
## [71] 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455
## [78] 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455
## [85] 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455
## [92] 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455 0.3715455
## [99] 0.3715455 0.3715455
## At iteration 17 f=21.048563 max(abs(g))=0.353154
##
## =====
## Before call f=21.048563 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"

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##
## =====
## Before call f=21.048563 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722
## [8] 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722
## [15] 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722
## [22] 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722
## [29] 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722
## [36] 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722
## [43] 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722
## [50] 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722
## [57] 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722
## [64] 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722
## [71] 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722
## [78] 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722
## [85] 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722
## [92] 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722 0.2692722
## [99] 0.2692722 0.2692722
## At iteration 18 f=21.042426 max(abs(g))=0.485823
##
## =====
## Before call f=21.042426 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951
## [8] 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951
## [15] 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951
## [22] 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951
## [29] 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951
## [36] 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951
## [43] 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951
## [50] 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951
## [57] 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951
## [64] 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951
## [71] 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951
## [78] 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951
## [85] 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951
## [92] 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951 0.3284951
## [99] 0.3284951 0.3284951
## At iteration 19 f=20.057968 max(abs(g))=0.092777
##
## =====
## Before call f=20.057968 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=20.057968 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"

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```

## computing f and g at prm=
## [1] 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555
## [8] 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555
## [15] 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555
## [22] 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555
## [29] 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555
## [36] 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555
## [43] 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555
## [50] 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555
## [57] 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555
## [64] 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555
## [71] 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555
## [78] 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555
## [85] 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555
## [92] 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555 0.3131555
## [99] 0.3131555 0.3131555
## At iteration 20 f=20.003813 max(abs(g))=0.024942
##
## =====
## Before call f=20.003813 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=20.003813 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056
## [8] 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056
## [15] 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056
## [22] 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056
## [29] 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056
## [36] 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056
## [43] 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056
## [50] 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056
## [57] 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056
## [64] 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056
## [71] 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056
## [78] 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056
## [85] 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056
## [92] 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056 0.3164056
## [99] 0.3164056 0.3164056
## At iteration 21 f=20.000013 max(abs(g))=0.001422
##
## =====
## Before call f=20.000013 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=20.000013 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"

```

```

## computing f and g at prm=
## [1] 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304
## [8] 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304
## [15] 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304
## [22] 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304
## [29] 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304
## [36] 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304
## [43] 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304
## [50] 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304
## [57] 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304
## [64] 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304
## [71] 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304
## [78] 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304
## [85] 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304
## [92] 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304 0.3162304
## [99] 0.3162304 0.3162304
## At iteration 22 f=20.000000 max(abs(g))=0.000021
##
## =====
## Before call f=20.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=20.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [8] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [15] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [22] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [29] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [36] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [43] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [50] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [57] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [64] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [71] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [78] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [85] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [92] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [99] 0.3162278 0.3162278
## At iteration 23 f=20.000000 max(abs(g))=0.000000
##
## =====
## Before call f=20.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=20.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 8 or "CONVERGENCE: REL_REDUCTION_OF_F_<=_FACTR*EPSMCH"

```


ccl

```
## $par
## [1] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [8] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [15] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [22] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [29] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [36] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [43] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [50] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [57] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [64] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [71] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [78] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [85] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [92] 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278 0.3162278
## [99] 0.3162278 0.3162278
##
## $grad
## [1] -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08
## [6] -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08
## [11] -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08
## [16] -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08
## [21] -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08
## [26] -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08
## [31] -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08
## [36] -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08
## [41] -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08
## [46] -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08
## [51] -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08
## [56] -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08
## [61] -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08
## [66] -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08
## [71] -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08
## [76] -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08
## [81] -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08
## [86] -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08
## [91] -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08
## [96] -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08 -1.752061e-08
##
## $value
## [1] 20
##
## $counts
## [1] 23 23
##
## $convergence
## [1] 0
##
## $message
## [1] "CONVERGENCE: REL_REDUCTION_OF_F_<=_FACTR*EPSMCH"
##
## $info
```

```

## $info$task
## [1] "CONVERGENCE: REL_REDUCTION_OF_F_<=_FACTR*EPSMCH"
##
## $info$itask
## [1] 8
##
## $info$lsave
## [1] FALSE TRUE TRUE TRUE
##
## $info$icsave
## [1] 6
##
## $info$dsave
## [1] 7.993158e+00 2.000000e+01 2.220446e-09 2.598193e-05 2.220446e-16
## [6] 0.000000e+00 0.000000e+00 0.000000e+00 0.000000e+00 0.000000e+00
## [11] 4.552193e-12 1.216732e+05 1.752061e-08 1.000000e+00 -5.395867e-09
## [16] 6.750607e-10 -5.395867e-09 -5.395867e-12 -5.395867e-09 -5.395867e-09
## [21] 2.000000e+01 2.000000e+01 2.000000e+01 0.000000e+00 0.000000e+00
## [26] 0.000000e+00 5.000000e+00 1.216732e+05 2.433463e+05
##
## $info$isave
## [1] 500 25 100 1 501 1001 1026 1051 1076 1176 1276 1376 1476 1576
## [15] 1676 1776 0 0 0 0 0 311 0 8 0 0 1 5
## [29] 5 13 10 0 1 23 0 1 0 100 0 101 0 0
## [43] 0 2

## cstickc0 <- opm(x0, cstick.f, cstick.g, method=meths, upper=up, lower=lo, control=list(kkt=FALSE))
## print(summary(cstickc0, par.select=1:5, order=value))
## lo <- rep(1, nn)
## cstickca <- opm(x0, cstick.f, cstick.g, method=meths, upper=up, lower=lo, control=list(kkt=FALSE))
## print(summary(cstickca, par.select=1:5, order=value))
## lo <- rep(4, nn)
## cstickcb <- opm(x0, cstick.f, cstick.g, method=meths, upper=up, lower=lo, control=list(kkt=FALSE))
## print(summary(cstickcb, par.select=1:5, order=value))

# require(funconstrain) ## not in CRAN, so explicit inclusion of this function
# exrosen <- ex_rosen()
# exrosenf <- exrosen$f
exrosenf <- function (par) {
  n <- length(par)
  if (n%%2 != 0) {
    stop("Extended Rosenbrock: n must be even")
  }
  fsum <- 0
  for (i in 1:(n/2)) {
    p2 <- 2 * i
    p1 <- p2 - 1
    f_p1 <- 10 * (par[p2] - par[p1]^2)
    f_p2 <- 1 - par[p1]
    fsum <- fsum + f_p1 * f_p1 + f_p2 * f_p2
  }
  fsum
}
# exroseng <- exrosen$gr
exroseng <- function (par) {

```

```

n <- length(par)
if (n%%2 != 0) {
  stop("Extended Rosenbrock: n must be even")
}
grad <- rep(0, n)
for (i in 1:(n/2)) {
  p2 <- 2 * i
  p1 <- p2 - 1
  xx <- par[p1] * par[p1]
  yx <- par[p2] - xx
  f_p1 <- 10 * yx
  f_p2 <- 1 - par[p1]
  grad[p1] <- grad[p1] - 400 * par[p1] * yx - 2 * f_p2
  grad[p2] <- grad[p2] + 200 * yx
}
grad
}

exrosenx0 <- function (n = 20) {
  if (n%%2 != 0) {
    stop("Extended Rosenbrock: n must be even")
  }
  rep(c(-1.2, 1), n/2)
}

## meths <- c("L-BFGS-B", "lbfgsb3c", "Rummin", "Rcgmin", "Rtnmin")
## require(optimx)
for (n in seq(2,12, by=2)) {
  cat("ex_rosen try for n=",n,"\n")
  x0 <- exrosenx0(n)
  lo <- rep(.5, n)
  up <- rep(3, n)
  print(x0)
  eo <- optim(x0, exrosenf, exroseng, lower=lo, upper=up, method="L-BFGS-B", control=list(trace=3))
  eo
  el <- lbfgsb3(x0, exrosenf, exroseng, lower=lo, upper=up, control=list(trace=3))
  el
  ## erfg <- opm(x0, exrosenf, exroseng, method=meths, lower=lo, upper=up)
  ## print(summary(erfg, par.select=1:2, order=value))
}

## ex_rosen try for n= 2
## [1] -1.2  1.0
## N = 2, M = 5 machine precision = 2.22045e-16
## The initial X is infeasible. Restart with its projection.
## At X0, 1 variables are exactly at the bounds
## At iterate    0 f=          56.5 |proj g|=          2.5
## At iterate   10 f =    2.473e-06 |proj g|=    0.021128
##
## iterations 13
## function evaluations 19
## segments explored during Cauchy searches 14
## BFGS updates skipped 0
## active bounds at final generalized Cauchy point 0

```

```

## norm of the final projected gradient 9.85451e-06
## final function value 4.63785e-11
##
## F = 4.63785e-11
## final value 0.000000
## converged
## returned from lbfgsb3
## returned itask is 21 or "FG_START"
## computing f and g at prm=
## [1] 0.5 1.0
## At iteration 0 f=56.500000 max(abs(g))=150.000000
##
## =====
## Before call f=56.500000 task number 21, or "FG_START"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 3.0 0.5
## At iteration 2 f=7229.000000 max(abs(g))=1700.000000
##
## =====
## Before call f=7229.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.8802684 0.9239463
## At iteration 3 f=2.236637 max(abs(g))=29.814773
##
## =====
## Before call f=2.236637 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=2.236637 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1.1176910 0.9323731
## At iteration 4 f=10.053887 max(abs(g))=63.372032
##
## =====
## Before call f=10.053887 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9579399 0.9267031
## At iteration 5 f=0.009967 max(abs(g))=1.810862
##
## =====
## Before call f=0.009967 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##

```

```

## =====
## Before call f=0.009967 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.963677 0.927100
## At iteration 6 f=0.001567 max(abs(g))=0.314675
##
## =====
## Before call f=0.001567 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.001567 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9629480 0.9270802
## At iteration 7 f=0.001376 max(abs(g))=0.001478
##
## =====
## Before call f=0.001376 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.001376 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9629685 0.9271132
## At iteration 8 f=0.001375 max(abs(g))=0.001048
##
## =====
## Before call f=0.001375 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9630504 0.9272453
## At iteration 9 f=0.001370 max(abs(g))=0.011159
##
## =====
## Before call f=0.001370 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9633784 0.9277737
## At iteration 10 f=0.001352 max(abs(g))=0.051670
##
## =====
## Before call f=0.001352 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"

```

```

##
## =====
## Before call f=0.001352 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9679509 0.9358966
## At iteration 11 f=0.001134 max(abs(g))=0.206451
##
## =====
## Before call f=0.001134 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.001134 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9756907 0.9504056
## At iteration 12 f=0.000836 max(abs(g))=0.313355
##
## =====
## Before call f=0.000836 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000836 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9861682 0.9709040
## At iteration 13 f=0.000455 max(abs(g))=0.324762
##
## =====
## Before call f=0.000455 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000455 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9950881 0.9893577
## At iteration 14 f=0.000095 max(abs(g))=0.168543
##
## =====
## Before call f=0.000095 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====

```

```

## Before call f=0.000095 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9985471 0.9970361
## At iteration 15 f=0.000002 max(abs(g))=0.012034
##
## =====
## Before call f=0.000002 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000002 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9998188 0.9996336
## At iteration 16 f=0.000000 max(abs(g))=0.000800
##
## =====
## Before call f=0.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1.000009 1.000015
## At iteration 17 f=0.000000 max(abs(g))=0.000530
##
## =====
## Before call f=0.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9996797 0.9998104
## At iteration 18 f=0.000020 max(abs(g))=0.090157
##
## =====
## Before call f=0.000020 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1.000007 1.000014
## At iteration 19 f=0.000000 max(abs(g))=0.000006
##

```

```

## =====
## Before call f=0.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 8 or "CONVERGENCE: REL_REDUCTION_OF_F_<=_FACTR*EPSMCH"
## ex_rosen try for n= 4
## [1] -1.2  1.0 -1.2  1.0
## N = 4, M = 5 machine precision = 2.22045e-16
## The initial X is infeasible. Restart with its projection.
## At X0, 2 variables are exactly at the bounds
## At iterate    0 f=          113 |proj g|=          2.5
## At iterate   10 f =   4.9459e-06 |proj g|=          0.021128
##
## iterations 13
## function evaluations 19
## segments explored during Cauchy searches 16
## BFGS updates skipped 0
## active bounds at final generalized Cauchy point 0
## norm of the final projected gradient 9.85451e-06
## final function value 9.2757e-11
##
## F = 9.2757e-11
## final value 0.000000
## converged
## returned from lbfgsb3
## returned itask is 21 or "FG_START"
## computing f and g at prm=
## [1] 0.5 1.0 0.5 1.0
## At iteration 0 f=113.000000 max(abs(g))=150.000000
##
## =====
## Before call f=113.000000 task number 21, or "FG_START"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 3.0 0.5 3.0 0.5
## At iteration 2 f=14458.000000 max(abs(g))=1700.000000
##
## =====
## Before call f=14458.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.8802684 0.9239463 0.8802684 0.9239463
## At iteration 3 f=4.473275 max(abs(g))=29.814773
##
## =====
## Before call f=4.473275 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"

```



```

##
## =====
## Before call f=4.473275 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1.1176910 0.9323731 1.1176910 0.9323731
## At iteration 4 f=20.107774 max(abs(g))=63.372032
##
## =====
## Before call f=20.107774 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9579399 0.9267031 0.9579399 0.9267031
## At iteration 5 f=0.019934 max(abs(g))=1.810862
##
## =====
## Before call f=0.019934 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.019934 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.963677 0.927100 0.963677 0.927100
## At iteration 6 f=0.003134 max(abs(g))=0.314675
##
## =====
## Before call f=0.003134 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.003134 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9629480 0.9270802 0.9629480 0.9270802
## At iteration 7 f=0.002753 max(abs(g))=0.001478
##
## =====
## Before call f=0.002753 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.002753 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9629685 0.9271132 0.9629685 0.9271132

```

```

## At iteration 8 f=0.002750 max(abs(g))=0.001048
##
## =====
## Before call f=0.002750 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9630504 0.9272453 0.9630504 0.9272453
## At iteration 9 f=0.002740 max(abs(g))=0.011159
##
## =====
## Before call f=0.002740 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9633784 0.9277737 0.9633784 0.9277737
## At iteration 10 f=0.002703 max(abs(g))=0.051670
##
## =====
## Before call f=0.002703 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.002703 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9679509 0.9358966 0.9679509 0.9358966
## At iteration 11 f=0.002267 max(abs(g))=0.206451
##
## =====
## Before call f=0.002267 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.002267 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9756907 0.9504056 0.9756907 0.9504056
## At iteration 12 f=0.001673 max(abs(g))=0.313355
##
## =====
## Before call f=0.001673 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.001673 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=

```

```

## [1] 0.9861682 0.9709040 0.9861682 0.9709040
## At iteration 13 f=0.000910 max(abs(g))=0.324762
##
## =====
## Before call f=0.000910 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000910 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9950881 0.9893577 0.9950881 0.9893577
## At iteration 14 f=0.000190 max(abs(g))=0.168543
##
## =====
## Before call f=0.000190 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000190 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9985471 0.9970361 0.9985471 0.9970361
## At iteration 15 f=0.000005 max(abs(g))=0.012034
##
## =====
## Before call f=0.000005 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000005 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9998188 0.9996336 0.9998188 0.9996336
## At iteration 16 f=0.000000 max(abs(g))=0.000800
##
## =====
## Before call f=0.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1.000009 1.000015 1.000009 1.000015
## At iteration 17 f=0.000000 max(abs(g))=0.000530

```

```

##
## =====
## Before call f=0.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9996797 0.9998104 0.9996797 0.9998104
## At iteration 18 f=0.000041 max(abs(g))=0.090157
##
## =====
## Before call f=0.000041 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1.000007 1.000014 1.000007 1.000014
## At iteration 19 f=0.000000 max(abs(g))=0.000006
##
## =====
## Before call f=0.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 8 or "CONVERGENCE: REL_REDUCTION_OF_F_<=_FACTR*EPSMCH"
## ex_rosen try for n= 6
## [1] -1.2  1.0 -1.2  1.0 -1.2  1.0
## N = 6, M = 5 machine precision = 2.22045e-16
## The initial X is infeasible. Restart with its projection.
## At X0, 3 variables are exactly at the bounds
## At iterate    0 f=      169.5 |proj g|=      2.5
## At iterate   10 f =   7.4189e-06 |proj g|=    0.021128
##
## iterations 13
## function evaluations 19
## segments explored during Cauchy searches 18
## BFGS updates skipped 0
## active bounds at final generalized Cauchy point 0
## norm of the final projected gradient 9.85451e-06
## final function value 1.39136e-10
##
## F = 1.39136e-10
## final value 0.000000
## converged
## returned from lbfgsb3
## returned itask is 21 or "FG_START"
## computing f and g at prm=
## [1] 0.5 1.0 0.5 1.0 0.5 1.0

```

```

## At iteration 0 f=169.500000 max(abs(g))=150.000000
##
## =====
## Before call f=169.500000 task number 21, or "FG_START"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 3.0 0.5 3.0 0.5 3.0 0.5
## At iteration 2 f=21687.000000 max(abs(g))=1700.000000
##
## =====
## Before call f=21687.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.8802684 0.9239463 0.8802684 0.9239463 0.8802684 0.9239463
## At iteration 3 f=6.709912 max(abs(g))=29.814773
##
## =====
## Before call f=6.709912 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=6.709912 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1.1176910 0.9323731 1.1176910 0.9323731 1.1176910 0.9323731
## At iteration 4 f=30.161662 max(abs(g))=63.372032
##
## =====
## Before call f=30.161662 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9579399 0.9267031 0.9579399 0.9267031 0.9579399 0.9267031
## At iteration 5 f=0.029901 max(abs(g))=1.810862
##
## =====
## Before call f=0.029901 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.029901 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.963677 0.927100 0.963677 0.927100 0.963677 0.927100
## At iteration 6 f=0.004701 max(abs(g))=0.314675
##
## =====
## Before call f=0.004701 task number 20, or "FG_LNSRCH"

```

```

## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.004701 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9629480 0.9270802 0.9629480 0.9270802 0.9629480 0.9270802
## At iteration 7 f=0.004129 max(abs(g))=0.001478
##
## =====
## Before call f=0.004129 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.004129 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9629685 0.9271132 0.9629685 0.9271132 0.9629685 0.9271132
## At iteration 8 f=0.004125 max(abs(g))=0.001048
##
## =====
## Before call f=0.004125 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9630504 0.9272453 0.9630504 0.9272453 0.9630504 0.9272453
## At iteration 9 f=0.004110 max(abs(g))=0.011159
##
## =====
## Before call f=0.004110 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9633784 0.9277737 0.9633784 0.9277737 0.9633784 0.9277737
## At iteration 10 f=0.004055 max(abs(g))=0.051670
##
## =====
## Before call f=0.004055 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.004055 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9679509 0.9358966 0.9679509 0.9358966 0.9679509 0.9358966
## At iteration 11 f=0.003401 max(abs(g))=0.206451
##
## =====

```

```

## Before call f=0.003401 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.003401 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9756907 0.9504056 0.9756907 0.9504056 0.9756907 0.9504056
## At iteration 12 f=0.002509 max(abs(g))=0.313355
##
## =====
## Before call f=0.002509 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.002509 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9861682 0.9709040 0.9861682 0.9709040 0.9861682 0.9709040
## At iteration 13 f=0.001365 max(abs(g))=0.324762
##
## =====
## Before call f=0.001365 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.001365 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9950881 0.9893577 0.9950881 0.9893577 0.9950881 0.9893577
## At iteration 14 f=0.000285 max(abs(g))=0.168543
##
## =====
## Before call f=0.000285 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000285 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9985471 0.9970361 0.9985471 0.9970361 0.9985471 0.9970361
## At iteration 15 f=0.000007 max(abs(g))=0.012034
##
## =====
## Before call f=0.000007 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3

```

```

## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000007 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9998188 0.9996336 0.9998188 0.9996336 0.9998188 0.9996336
## At iteration 16 f=0.000000 max(abs(g))=0.000800
##
## =====
## Before call f=0.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1.000009 1.000015 1.000009 1.000015 1.000009 1.000015
## At iteration 17 f=0.000000 max(abs(g))=0.000530
##
## =====
## Before call f=0.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9996797 0.9998104 0.9996797 0.9998104 0.9996797 0.9998104
## At iteration 18 f=0.000061 max(abs(g))=0.090157
##
## =====
## Before call f=0.000061 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1.000007 1.000014 1.000007 1.000014 1.000007 1.000014
## At iteration 19 f=0.000000 max(abs(g))=0.000006
##
## =====
## Before call f=0.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 8 or "CONVERGENCE: REL_REDUCTION_OF_F_<=_FACTR*EPSMCH"
## ex_rosen try for n= 8

```



```

## [1] -1.2  1.0 -1.2  1.0 -1.2  1.0 -1.2  1.0
## N = 8, M = 5 machine precision = 2.22045e-16
## The initial X is infeasible. Restart with its projection.
## At X0, 4 variables are exactly at the bounds
## At iterate    0 f=          226 |proj g|=          2.5
## At iterate   10 f =   9.8919e-06 |proj g|=    0.021128
##
## iterations 14
## function evaluations 20
## segments explored during Cauchy searches 21
## BFGS updates skipped 0
## active bounds at final generalized Cauchy point 0
## norm of the final projected gradient 2.31162e-08
## final function value 1.60735e-16
##
## F = 1.60735e-16
## final value 0.000000
## converged
## returned from lbfgsb3
## returned itask is 21 or "FG_START"
## computing f and g at prm=
## [1] 0.5 1.0 0.5 1.0 0.5 1.0 0.5 1.0
## At iteration 0 f=226.000000 max(abs(g))=150.000000
##
## =====
## Before call f=226.000000 task number 21, or "FG_START"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 3.0 0.5 3.0 0.5 3.0 0.5 3.0 0.5
## At iteration 2 f=28916.000000 max(abs(g))=1700.000000
##
## =====
## Before call f=28916.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.8802684 0.9239463 0.8802684 0.9239463 0.8802684 0.9239463 0.8802684
## [8] 0.9239463
## At iteration 3 f=8.946550 max(abs(g))=29.814773
##
## =====
## Before call f=8.946550 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=8.946550 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1.1176910 0.9323731 1.1176910 0.9323731 1.1176910 0.9323731 1.1176910
## [8] 0.9323731
## At iteration 4 f=40.215549 max(abs(g))=63.372032

```

```

##
## =====
## Before call f=40.215549 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9579399 0.9267031 0.9579399 0.9267031 0.9579399 0.9267031 0.9579399
## [8] 0.9267031
## At iteration 5 f=0.039868 max(abs(g))=1.810862
##
## =====
## Before call f=0.039868 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.039868 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.963677 0.927100 0.963677 0.927100 0.963677 0.927100 0.963677 0.927100
## At iteration 6 f=0.006268 max(abs(g))=0.314675
##
## =====
## Before call f=0.006268 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.006268 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9629480 0.9270802 0.9629480 0.9270802 0.9629480 0.9270802 0.9629480
## [8] 0.9270802
## At iteration 7 f=0.005506 max(abs(g))=0.001478
##
## =====
## Before call f=0.005506 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.005506 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9629685 0.9271132 0.9629685 0.9271132 0.9629685 0.9271132 0.9629685
## [8] 0.9271132
## At iteration 8 f=0.005501 max(abs(g))=0.001048
##
## =====
## Before call f=0.005501 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3

```

```

## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9630504 0.9272453 0.9630504 0.9272453 0.9630504 0.9272453 0.9630504
## [8] 0.9272453
## At iteration 9 f=0.005481 max(abs(g))=0.011159
##
## =====
## Before call f=0.005481 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9633784 0.9277737 0.9633784 0.9277737 0.9633784 0.9277737 0.9633784
## [8] 0.9277737
## At iteration 10 f=0.005407 max(abs(g))=0.051670
##
## =====
## Before call f=0.005407 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.005407 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9679509 0.9358966 0.9679509 0.9358966 0.9679509 0.9358966 0.9679509
## [8] 0.9358966
## At iteration 11 f=0.004535 max(abs(g))=0.206451
##
## =====
## Before call f=0.004535 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.004535 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9756907 0.9504056 0.9756907 0.9504056 0.9756907 0.9504056 0.9756907
## [8] 0.9504056
## At iteration 12 f=0.003346 max(abs(g))=0.313355
##
## =====
## Before call f=0.003346 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.003346 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9861682 0.9709040 0.9861682 0.9709040 0.9861682 0.9709040 0.9861682

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## [8] 0.9709040
## At iteration 13 f=0.001820 max(abs(g))=0.324762
##
## =====
## Before call f=0.001820 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.001820 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9950881 0.9893577 0.9950881 0.9893577 0.9950881 0.9893577 0.9950881
## [8] 0.9893577
## At iteration 14 f=0.000381 max(abs(g))=0.168543
##
## =====
## Before call f=0.000381 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000381 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9985471 0.9970361 0.9985471 0.9970361 0.9985471 0.9970361 0.9985471
## [8] 0.9970361
## At iteration 15 f=0.000010 max(abs(g))=0.012034
##
## =====
## Before call f=0.000010 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000010 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9998188 0.9996336 0.9998188 0.9996336 0.9998188 0.9996336 0.9998188
## [8] 0.9996336
## At iteration 16 f=0.000000 max(abs(g))=0.000800
##
## =====
## Before call f=0.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"

```

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## computing f and g at prm=
## [1] 1.000009 1.000015 1.000009 1.000015 1.000009 1.000015 1.000009 1.000015
## At iteration 17 f=0.000000 max(abs(g))=0.000530
##
## =====
## Before call f=0.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9996797 0.9998104 0.9996797 0.9998104 0.9996797 0.9998104 0.9996797
## [8] 0.9998104
## At iteration 18 f=0.000082 max(abs(g))=0.090157
##
## =====
## Before call f=0.000082 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1.000007 1.000014 1.000007 1.000014 1.000007 1.000014 1.000007 1.000014
## At iteration 19 f=0.000000 max(abs(g))=0.000006
##
## =====
## Before call f=0.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1 1 1 1 1 1 1 1
## At iteration 20 f=0.000000 max(abs(g))=0.000000
##
## =====
## Before call f=0.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 8 or "CONVERGENCE: REL_REDUCTION_OF_F_<=_FACTR*EPSMCH"
## ex_rosen try for n= 10
## [1] -1.2 1.0 -1.2 1.0 -1.2 1.0 -1.2 1.0 -1.2 1.0
## N = 10, M = 5 machine precision = 2.22045e-16
## The initial X is infeasible. Restart with its projection.
## At X0, 5 variables are exactly at the bounds
## At iterate      0 f=          282.5 |proj g|=          2.5

```

```

## At iterate    10  f =   1.2365e-05  |proj g|=      0.021128
##
## iterations 14
## function evaluations 20
## segments explored during Cauchy searches 23
## BFGS updates skipped 0
## active bounds at final generalized Cauchy point 0
## norm of the final projected gradient 2.31163e-08
## final function value 2.00919e-16
##
## F = 2.00919e-16
## final  value 0.000000
## converged
## returned from lbfgsb3
## returned itask is 21 or "FG_START"
## computing f and g at prm=
## [1] 0.5 1.0 0.5 1.0 0.5 1.0 0.5 1.0 0.5 1.0
## At iteration 0 f=282.500000 max(abs(g))=150.000000
##
## =====
## Before call f=282.500000 task number 21, or "FG_START"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 3.0 0.5 3.0 0.5 3.0 0.5 3.0 0.5 3.0 0.5
## At iteration 2 f=36145.000000 max(abs(g))=1700.000000
##
## =====
## Before call f=36145.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.8802684 0.9239463 0.8802684 0.9239463 0.8802684 0.9239463 0.8802684
## [8] 0.9239463 0.8802684 0.9239463
## At iteration 3 f=11.183187 max(abs(g))=29.814773
##
## =====
## Before call f=11.183187 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=11.183187 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1.1176910 0.9323731 1.1176910 0.9323731 1.1176910 0.9323731 1.1176910
## [8] 0.9323731 1.1176910 0.9323731
## At iteration 4 f=50.269436 max(abs(g))=63.372032
##
## =====
## Before call f=50.269436 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"

```

```

## computing f and g at prm=
## [1] 0.9579399 0.9267031 0.9579399 0.9267031 0.9579399 0.9267031 0.9579399
## [8] 0.9267031 0.9579399 0.9267031
## At iteration 5 f=0.049836 max(abs(g))=1.810862
##
## =====
## Before call f=0.049836 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.049836 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.963677 0.927100 0.963677 0.927100 0.963677 0.927100 0.963677
## [8] 0.927100 0.963677 0.927100
## At iteration 6 f=0.007835 max(abs(g))=0.314675
##
## =====
## Before call f=0.007835 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.007835 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9629480 0.9270802 0.9629480 0.9270802 0.9629480 0.9270802 0.9629480
## [8] 0.9270802 0.9629480 0.9270802
## At iteration 7 f=0.006882 max(abs(g))=0.001478
##
## =====
## Before call f=0.006882 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.006882 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9629685 0.9271132 0.9629685 0.9271132 0.9629685 0.9271132 0.9629685
## [8] 0.9271132 0.9629685 0.9271132
## At iteration 8 f=0.006876 max(abs(g))=0.001048
##
## =====
## Before call f=0.006876 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9630504 0.9272453 0.9630504 0.9272453 0.9630504 0.9272453 0.9630504
## [8] 0.9272453 0.9630504 0.9272453

```

```

## At iteration 9 f=0.006851 max(abs(g))=0.011159
##
## =====
## Before call f=0.006851 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9633784 0.9277737 0.9633784 0.9277737 0.9633784 0.9277737 0.9633784
## [8] 0.9277737 0.9633784 0.9277737
## At iteration 10 f=0.006758 max(abs(g))=0.051670
##
## =====
## Before call f=0.006758 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.006758 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9679509 0.9358966 0.9679509 0.9358966 0.9679509 0.9358966 0.9679509
## [8] 0.9358966 0.9679509 0.9358966
## At iteration 11 f=0.005669 max(abs(g))=0.206451
##
## =====
## Before call f=0.005669 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.005669 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9756907 0.9504056 0.9756907 0.9504056 0.9756907 0.9504056 0.9756907
## [8] 0.9504056 0.9756907 0.9504056
## At iteration 12 f=0.004182 max(abs(g))=0.313355
##
## =====
## Before call f=0.004182 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.004182 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9861682 0.9709040 0.9861682 0.9709040 0.9861682 0.9709040 0.9861682
## [8] 0.9709040 0.9861682 0.9709040
## At iteration 13 f=0.002275 max(abs(g))=0.324762
##
## =====

```



```

## Before call f=0.002275 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.002275 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9950881 0.9893577 0.9950881 0.9893577 0.9950881 0.9893577 0.9950881
## [8] 0.9893577 0.9950881 0.9893577
## At iteration 14 f=0.000476 max(abs(g))=0.168543
##
## =====
## Before call f=0.000476 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000476 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9985471 0.9970361 0.9985471 0.9970361 0.9985471 0.9970361 0.9985471
## [8] 0.9970361 0.9985471 0.9970361
## At iteration 15 f=0.000012 max(abs(g))=0.012034
##
## =====
## Before call f=0.000012 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000012 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9998188 0.9996336 0.9998188 0.9996336 0.9998188 0.9996336 0.9998188
## [8] 0.9996336 0.9998188 0.9996336
## At iteration 16 f=0.000000 max(abs(g))=0.000800
##
## =====
## Before call f=0.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1.0000009 1.000015 1.0000009 1.000015 1.0000009 1.000015 1.0000009
## [8] 1.000015 1.0000009 1.000015
## At iteration 17 f=0.000000 max(abs(g))=0.000530

```

```

##
## =====
## Before call f=0.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9996797 0.9998104 0.9996797 0.9998104 0.9996797 0.9998104 0.9996797
## [8] 0.9998104 0.9996797 0.9998104
## At iteration 18 f=0.000102 max(abs(g))=0.090157
##
## =====
## Before call f=0.000102 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1.000007 1.000014 1.000007 1.000014 1.000007 1.000014 1.000007
## [8] 1.000014 1.000007 1.000014
## At iteration 19 f=0.000000 max(abs(g))=0.000006
##
## =====
## Before call f=0.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1 1 1 1 1 1 1 1 1
## At iteration 20 f=0.000000 max(abs(g))=0.000000
##
## =====
## Before call f=0.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 8 or "CONVERGENCE: REL_REDUCTION_OF_F_<=_FACTR*EPSMCH"
## ex_rosen try for n= 12
## [1] -1.2 1.0 -1.2 1.0 -1.2 1.0 -1.2 1.0 -1.2 1.0 -1.2 1.0
## N = 12, M = 5 machine precision = 2.22045e-16
## The initial X is infeasible. Restart with its projection.
## At X0, 6 variables are exactly at the bounds
## At iterate 0 f= 339 |proj g|= 2.5
## At iterate 10 f = 1.4838e-05 |proj g|= 0.021128
##

```

```

## iterations 14
## function evaluations 20
## segments explored during Cauchy searches 25
## BFGS updates skipped 0
## active bounds at final generalized Cauchy point 0
## norm of the final projected gradient 2.31162e-08
## final function value 2.41099e-16
##
## F = 2.41099e-16
## final value 0.000000
## converged
## returned from lbfgsb3
## returned itask is 21 or "FG_START"
## computing f and g at prm=
## [1] 0.5 1.0 0.5 1.0 0.5 1.0 0.5 1.0 0.5 1.0 0.5 1.0
## At iteration 0 f=339.000000 max(abs(g))=150.000000
##
## =====
## Before call f=339.000000 task number 21, or "FG_START"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 3.0 0.5 3.0 0.5 3.0 0.5 3.0 0.5 3.0 0.5 3.0 0.5
## At iteration 2 f=43374.000000 max(abs(g))=1700.000000
##
## =====
## Before call f=43374.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.8802684 0.9239463 0.8802684 0.9239463 0.8802684 0.9239463 0.8802684
## [8] 0.9239463 0.8802684 0.9239463 0.8802684 0.9239463
## At iteration 3 f=13.419825 max(abs(g))=29.814773
##
## =====
## Before call f=13.419825 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=13.419825 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1.1176910 0.9323731 1.1176910 0.9323731 1.1176910 0.9323731 1.1176910
## [8] 0.9323731 1.1176910 0.9323731 1.1176910 0.9323731
## At iteration 4 f=60.323323 max(abs(g))=63.372032
##
## =====
## Before call f=60.323323 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9579399 0.9267031 0.9579399 0.9267031 0.9579399 0.9267031 0.9579399

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```

## [8] 0.9267031 0.9579399 0.9267031 0.9579399 0.9267031
## At iteration 5 f=0.059803 max(abs(g))=1.810862
##
## =====
## Before call f=0.059803 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.059803 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.963677 0.927100 0.963677 0.927100 0.963677 0.927100 0.963677
## [8] 0.927100 0.963677 0.927100 0.963677 0.927100
## At iteration 6 f=0.009401 max(abs(g))=0.314675
##
## =====
## Before call f=0.009401 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.009401 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9629480 0.9270802 0.9629480 0.9270802 0.9629480 0.9270802 0.9629480
## [8] 0.9270802 0.9629480 0.9270802 0.9629480 0.9270802
## At iteration 7 f=0.008258 max(abs(g))=0.001478
##
## =====
## Before call f=0.008258 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.008258 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9629685 0.9271132 0.9629685 0.9271132 0.9629685 0.9271132 0.9629685
## [8] 0.9271132 0.9629685 0.9271132 0.9629685 0.9271132
## At iteration 8 f=0.008251 max(abs(g))=0.001048
##
## =====
## Before call f=0.008251 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9630504 0.9272453 0.9630504 0.9272453 0.9630504 0.9272453 0.9630504
## [8] 0.9272453 0.9630504 0.9272453 0.9630504 0.9272453
## At iteration 9 f=0.008221 max(abs(g))=0.011159
##

```

```

## =====
## Before call f=0.008221 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9633784 0.9277737 0.9633784 0.9277737 0.9633784 0.9277737 0.9633784
## [8] 0.9277737 0.9633784 0.9277737 0.9633784 0.9277737
## At iteration 10 f=0.008110 max(abs(g))=0.051670
##
## =====
## Before call f=0.008110 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.008110 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9679509 0.9358966 0.9679509 0.9358966 0.9679509 0.9358966 0.9679509
## [8] 0.9358966 0.9679509 0.9358966 0.9679509 0.9358966
## At iteration 11 f=0.006802 max(abs(g))=0.206451
##
## =====
## Before call f=0.006802 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.006802 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9756907 0.9504056 0.9756907 0.9504056 0.9756907 0.9504056 0.9756907
## [8] 0.9504056 0.9756907 0.9504056 0.9756907 0.9504056
## At iteration 12 f=0.005019 max(abs(g))=0.313355
##
## =====
## Before call f=0.005019 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.005019 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9861682 0.9709040 0.9861682 0.9709040 0.9861682 0.9709040 0.9861682
## [8] 0.9709040 0.9861682 0.9709040 0.9861682 0.9709040
## At iteration 13 f=0.002730 max(abs(g))=0.324762
##
## =====
## Before call f=0.002730 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3

```

```

## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.002730 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9950881 0.9893577 0.9950881 0.9893577 0.9950881 0.9893577 0.9950881
## [8] 0.9893577 0.9950881 0.9893577 0.9950881 0.9893577
## At iteration 14 f=0.000571 max(abs(g))=0.168543
##
## =====
## Before call f=0.000571 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000571 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9985471 0.9970361 0.9985471 0.9970361 0.9985471 0.9970361 0.9985471
## [8] 0.9970361 0.9985471 0.9970361 0.9985471 0.9970361
## At iteration 15 f=0.000015 max(abs(g))=0.012034
##
## =====
## Before call f=0.000015 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000015 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9998188 0.9996336 0.9998188 0.9996336 0.9998188 0.9996336 0.9998188
## [8] 0.9996336 0.9998188 0.9996336 0.9998188 0.9996336
## At iteration 16 f=0.000000 max(abs(g))=0.000800
##
## =====
## Before call f=0.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1.0000009 1.000015 1.0000009 1.000015 1.0000009 1.000015 1.0000009
## [8] 1.000015 1.0000009 1.000015 1.0000009 1.000015
## At iteration 17 f=0.000000 max(abs(g))=0.000530
##
## =====

```

```

## Before call f=0.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 0.9996797 0.9998104 0.9996797 0.9998104 0.9996797 0.9998104 0.9996797
## [8] 0.9998104 0.9996797 0.9998104 0.9996797 0.9998104
## At iteration 18 f=0.000123 max(abs(g))=0.090157
##
## =====
## Before call f=0.000123 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1.000007 1.000014 1.000007 1.000014 1.000007 1.000014 1.000007
## [8] 1.000014 1.000007 1.000014 1.000007 1.000014
## At iteration 19 f=0.000000 max(abs(g))=0.000006
##
## =====
## Before call f=0.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 20 or "FG_LNSRCH"
## computing f and g at prm=
## [1] 1 1 1 1 1 1 1 1 1 1 1 1
## At iteration 20 f=0.000000 max(abs(g))=0.000000
##
## =====
## Before call f=0.000000 task number 20, or "FG_LNSRCH"
## returned from lbfgsb3
## returned itask is 1 or "NEW_X"
##
## =====
## Before call f=0.000000 task number 1, or "NEW_X"
## returned from lbfgsb3
## returned itask is 8 or "CONVERGENCE: REL_REDUCTION_OF_F_<=_FACTR*EPSMCH"

```

Using compiled function code

While you may use the same interface as described in the writing R extensions to interface compiled code with this function, see L-BFGS-B, it is sometimes more convenient to use your own compiled code.

The following example shows how this is done using the file `jrosen.f`

```

subroutine rosen(n, x, fval)
double precision x(n), fval, dx

```

```

integer n, i
fval = 0.0D0
do 10 i=1,(n-1)
  dx = x(i + 1) - x(i) * x(i)
  fval = fval + 100.0 * dx * dx
  dx = 1.0 - x(i)
  fval = fval + dx * dx
10  continue
return
end

```

Here is the example script, which is run OUTSIDE the vignette builder in a temporary directory.

```

system("cd ~/temp")
system("R CMD SHLIB jrosen.f")
dyn.load("jrosen.so")
is.loaded("rosen")
x0 <- as.double(c(-1.2,1))
fv <- as.double(-999)
n <- as.double(2)
testf <- .Fortran("rosen", n=as.integer(n), x=as.double(x0), fval=as.double(fv))
testf

rrosen <- function(x) {
  fval <- 0.0
  for (i in 1:(n-1)) {
    dx <- x[i + 1] - x[i] * x[i]
    fval <- fval + 100.0 * dx * dx
    dx <- 1.0 - x[i]
    fval <- fval + dx * dx
  }
  fval
}

(rrosen(x0))

frosen <- function(x){
  nn <- length(x)
  if (nn > 100) { stop("max number of parameters is 100")}
  fv <- -999.0
  val <- .Fortran("rosen", n=as.integer(nn), x=as.double(x), fval=as.double(fv))
  val$fval # NOTE--need ONLY function value returned
}

# Test the funcion
tval <- frosen(x0)
str(tval)

mynm <- optim(x0, rrosen, control=list(trace=1))
mynm
mynmf <- optim(x0, frosen, control=list(trace=1))
mynmf

library(lbfgsb3c)
cat("try min")
myopR <- lbfgsb3c(x0, rrosen, gr=NULL, control=list(trace=3))

```



```

myopR
myop <- lbfgsb3c(x0, frosen, gr=NULL, control=list(trace=3))
myop

```

The output is as follows.

```

> system("cd ~/temp")

> system("R CMD SHLIB jrosen.f")

> dyn.load("jrosen.so")

> is.loaded("rosen")
[1] TRUE

> x0 <- as.double(c(-1.2,1))

> fv <- as.double(-999)

> n <- as.double(2)

> testf <- .Fortran("rosen", n=as.integer(n), x=as.double(x0), fval=as.double(fv))

> testf
$n
[1] 2

$x
[1] -1.2  1.0

$fval
[1] 24.2

> rrosen <- function(x) {
+   fval <- 0.0
+   for (i in 1:(n-1)) {
+     dx <- x[i + 1] - x[i] * x[i]
+     fval <- fval + 100.0 * dx * dx
+     dx <- .... [TRUNCATED]
+   }

> tt <-rrosen(x0)

> str(tt)
  num 24.2

> frosen <- function(x){
+   nn <- length(x)
+   if (nn > 100) { stop("max number of parameters is 100")}
+   fv <- -999.0
+   val <- .Fortran .... [TRUNCATED]

> tval <- frosen(x0)

```

```

> str(tval)
num 24.2

> mynm <- optim(x0, rrosen, control=list(trace=1))
Nelder-Mead direct search function minimizer
function value for initial parameters = 24.200000
Scaled convergence tolerance is 3.60608e-07
Stepsize computed as 0.120000
BUILD          3 24.200000 7.095296
REFLECTION     5 15.080000 4.541696
REFLECTION     7 7.095296 4.456256
HI-REDUCTION   9 4.728125 4.456256
HI-REDUCTION  11 4.541696 4.210000
LO-REDUCTION  13 4.456256 4.178989
LO-REDUCTION  15 4.210000 4.070813
HI-REDUCTION  17 4.178989 4.039810
HI-REDUCTION  19 4.070813 4.009379
HI-REDUCTION  21 4.039810 4.009379
REFLECTION    23 4.020798 3.993600
HI-REDUCTION  25 4.009379 3.993115
EXTENSION     27 3.993600 3.971089
HI-REDUCTION  29 3.993115 3.971089
EXTENSION     31 3.980807 3.932179
LO-REDUCTION  33 3.971089 3.932179
EXTENSION     35 3.935345 3.849794
LO-REDUCTION  37 3.932179 3.849794
EXTENSION     39 3.855730 3.684292
LO-REDUCTION  41 3.849794 3.684292
EXTENSION     43 3.699672 3.413447
EXTENSION     45 3.684292 3.229015
LO-REDUCTION  47 3.413447 3.229015
REFLECTION    49 3.230691 3.103710
EXTENSION     51 3.229015 3.003490
REFLECTION    53 3.103710 2.942017
EXTENSION     55 3.003490 2.708997
LO-REDUCTION  57 2.942017 2.708997
EXTENSION     59 2.713454 2.299507
HI-REDUCTION  61 2.708997 2.299507
REFLECTION    63 2.531644 2.205440
EXTENSION     65 2.299507 1.918698
HI-REDUCTION  67 2.205440 1.918698
EXTENSION     69 2.090865 1.646608
HI-REDUCTION  71 1.918698 1.646608
REFLECTION    73 1.846675 1.599128
REFLECTION    75 1.646608 1.512003
REFLECTION    77 1.599128 1.398251
LO-REDUCTION  79 1.512003 1.396387
REFLECTION    81 1.398251 1.343582
REFLECTION    83 1.396387 1.300594
LO-REDUCTION  85 1.343582 1.257303
HI-REDUCTION  87 1.300594 1.257303
HI-REDUCTION  89 1.269330 1.242346
EXTENSION     91 1.257303 1.199712

```

HI-REDUCTION	93	1.242346	1.199712
EXTENSION	95	1.226601	1.157795
EXTENSION	97	1.199712	1.100429
EXTENSION	99	1.157795	0.980250
LO-REDUCTION	101	1.100429	0.980250
EXTENSION	103	0.998877	0.807009
LO-REDUCTION	105	0.980250	0.807009
EXTENSION	107	0.853222	0.586726
LO-REDUCTION	109	0.807009	0.586726
HI-REDUCTION	111	0.689741	0.586726
LO-REDUCTION	113	0.656247	0.586726
EXTENSION	115	0.622985	0.558089
EXTENSION	117	0.586726	0.448731
LO-REDUCTION	119	0.558089	0.448731
EXTENSION	121	0.499381	0.340534
LO-REDUCTION	123	0.448731	0.340534
EXTENSION	125	0.377625	0.243089
REFLECTION	127	0.340534	0.226575
REFLECTION	129	0.243089	0.180213
HI-REDUCTION	131	0.226575	0.180213
EXTENSION	133	0.204666	0.123935
HI-REDUCTION	135	0.180213	0.123935
LO-REDUCTION	137	0.164902	0.123935
REFLECTION	139	0.126595	0.088760
HI-REDUCTION	141	0.123935	0.088760
EXTENSION	143	0.109726	0.075099
EXTENSION	145	0.088760	0.050955
EXTENSION	147	0.075099	0.022726
HI-REDUCTION	149	0.050955	0.022726
LO-REDUCTION	151	0.038467	0.017697
HI-REDUCTION	153	0.022726	0.017697
HI-REDUCTION	155	0.022600	0.013923
REFLECTION	157	0.017697	0.008524
HI-REDUCTION	159	0.013923	0.008524
EXTENSION	161	0.012718	0.008024
EXTENSION	163	0.008524	0.002530
EXTENSION	165	0.008024	0.000463
HI-REDUCTION	167	0.002530	0.000463
HI-REDUCTION	169	0.002405	0.000351
HI-REDUCTION	171	0.000710	0.000351
HI-REDUCTION	173	0.000463	0.000183
HI-REDUCTION	175	0.000351	0.000044
HI-REDUCTION	177	0.000183	0.000044
LO-REDUCTION	179	0.000082	0.000002
HI-REDUCTION	181	0.000044	0.000002
HI-REDUCTION	183	0.000012	0.000002
HI-REDUCTION	185	0.000009	0.000002
HI-REDUCTION	187	0.000002	0.000002
HI-REDUCTION	189	0.000002	0.000000
HI-REDUCTION	191	0.000002	0.000000
LO-REDUCTION	193	0.000001	0.000000

Exiting from Nelder Mead minimizer

195 function evaluations used

```

> mynm
$par
[1] 1.000260 1.000506

$value
[1] 8.825241e-08

$counts
function gradient
      195      NA

$convergence
[1] 0

$message
NULL

> mynmf <- optim(x0, frozen, control=list(trace=1))
  Nelder-Mead direct search function minimizer
function value for initial parameters = 24.200000
  Scaled convergence tolerance is 3.60608e-07
Stepsize computed as 0.120000
BUILD           3 24.200000 7.095296
REFLECTION      5 15.080000 4.541696
REFLECTION      7 7.095296 4.456256
HI-REDUCTION    9 4.728125 4.456256
HI-REDUCTION   11 4.541696 4.210000
LO-REDUCTION   13 4.456256 4.178989
LO-REDUCTION   15 4.210000 4.070813
HI-REDUCTION   17 4.178989 4.039810
HI-REDUCTION   19 4.070813 4.009379
HI-REDUCTION   21 4.039810 4.009379
REFLECTION     23 4.020798 3.993600
HI-REDUCTION   25 4.009379 3.993115
EXTENSION      27 3.993600 3.971089
HI-REDUCTION   29 3.993115 3.971089
EXTENSION      31 3.980807 3.932179
LO-REDUCTION   33 3.971089 3.932179
EXTENSION      35 3.935345 3.849794
LO-REDUCTION   37 3.932179 3.849794
EXTENSION      39 3.855730 3.684292
LO-REDUCTION   41 3.849794 3.684292
EXTENSION      43 3.699672 3.413447
EXTENSION      45 3.684292 3.229015
LO-REDUCTION   47 3.413447 3.229015
REFLECTION     49 3.230691 3.103710
EXTENSION      51 3.229015 3.003490
REFLECTION     53 3.103710 2.942017
EXTENSION      55 3.003490 2.708997
LO-REDUCTION   57 2.942017 2.708997
EXTENSION      59 2.713454 2.299507
HI-REDUCTION   61 2.708997 2.299507
REFLECTION     63 2.531644 2.205440

```

EXTENSION	65	2.299507	1.918698
HI-REDUCTION	67	2.205440	1.918698
EXTENSION	69	2.090865	1.646608
HI-REDUCTION	71	1.918698	1.646608
REFLECTION	73	1.846675	1.599128
REFLECTION	75	1.646608	1.512003
REFLECTION	77	1.599128	1.398251
LO-REDUCTION	79	1.512003	1.396387
REFLECTION	81	1.398251	1.343582
REFLECTION	83	1.396387	1.300594
LO-REDUCTION	85	1.343582	1.257303
HI-REDUCTION	87	1.300594	1.257303
HI-REDUCTION	89	1.269330	1.242346
EXTENSION	91	1.257303	1.199712
HI-REDUCTION	93	1.242346	1.199712
EXTENSION	95	1.226601	1.157795
EXTENSION	97	1.199712	1.100429
EXTENSION	99	1.157795	0.980250
LO-REDUCTION	101	1.100429	0.980250
EXTENSION	103	0.998877	0.807009
LO-REDUCTION	105	0.980250	0.807009
EXTENSION	107	0.853222	0.586726
LO-REDUCTION	109	0.807009	0.586726
HI-REDUCTION	111	0.689741	0.586726
LO-REDUCTION	113	0.656247	0.586726
EXTENSION	115	0.622985	0.558089
EXTENSION	117	0.586726	0.448731
LO-REDUCTION	119	0.558089	0.448731
EXTENSION	121	0.499381	0.340534
LO-REDUCTION	123	0.448731	0.340534
EXTENSION	125	0.377625	0.243089
REFLECTION	127	0.340534	0.226575
REFLECTION	129	0.243089	0.180213
HI-REDUCTION	131	0.226575	0.180213
EXTENSION	133	0.204666	0.123935
HI-REDUCTION	135	0.180213	0.123935
LO-REDUCTION	137	0.164902	0.123935
REFLECTION	139	0.126595	0.088760
HI-REDUCTION	141	0.123935	0.088760
EXTENSION	143	0.109726	0.075099
EXTENSION	145	0.088760	0.050955
EXTENSION	147	0.075099	0.022726
HI-REDUCTION	149	0.050955	0.022726
LO-REDUCTION	151	0.038467	0.017697
HI-REDUCTION	153	0.022726	0.017697
HI-REDUCTION	155	0.022600	0.013923
REFLECTION	157	0.017697	0.008524
HI-REDUCTION	159	0.013923	0.008524
EXTENSION	161	0.012718	0.008024
EXTENSION	163	0.008524	0.002530
EXTENSION	165	0.008024	0.000463
HI-REDUCTION	167	0.002530	0.000463
HI-REDUCTION	169	0.002405	0.000351
HI-REDUCTION	171	0.000710	0.000351

```

HI-REDUCTION      173 0.000463 0.000183
HI-REDUCTION      175 0.000351 0.000044
HI-REDUCTION      177 0.000183 0.000044
LO-REDUCTION      179 0.000082 0.000002
HI-REDUCTION      181 0.000044 0.000002
HI-REDUCTION      183 0.000012 0.000002
HI-REDUCTION      185 0.000009 0.000002
HI-REDUCTION      187 0.000002 0.000002
HI-REDUCTION      189 0.000002 0.000000
HI-REDUCTION      191 0.000002 0.000000
LO-REDUCTION      193 0.000001 0.000000
Exiting from Nelder Mead minimizer
      195 function evaluations used

```

```

> mynmf
$par
[1] 1.000260 1.000506

```

```

$value
[1] 8.825241e-08

```

```

$counts
function gradient
      195      NA

```

```

$convergence
[1] 0

```

```

$message
NULL

```

```

> library(lbfgsb3c)

```

```

> cat("try min")
try min
> myopR <- lbfgsb3c(x0, rrosen, gr=NULL, control=list(trace=1))
At iteration 0 f=24.200000
At iteration 2 f=171.335959
At iteration 3 f=4.225209
At iteration 4 f=4.127276
At iteration 5 f=4.120517
At iteration 6 f=4.115575
At iteration 7 f=4.087545
At iteration 8 f=4.032007
At iteration 9 f=3.917829
At iteration 10 f=3.775253
At iteration 11 f=3.451302
At iteration 12 f=2.743645
At iteration 13 f=7.136647
At iteration 14 f=2.314771
At iteration 15 f=4.974153
At iteration 16 f=2.206918
At iteration 17 f=2.093263

```

```

At iteration 18 f=1.834870
At iteration 19 f=1.457101
At iteration 20 f=1.332676
At iteration 21 f=1.303252
At iteration 22 f=0.958191
At iteration 23 f=0.874145
At iteration 24 f=0.635020
At iteration 25 f=0.610113
At iteration 26 f=105.549878
At iteration 27 f=0.546422
At iteration 28 f=0.517374
At iteration 29 f=0.498255
At iteration 30 f=0.468898
At iteration 31 f=0.405481
At iteration 32 f=0.290616
At iteration 33 f=0.566440
At iteration 34 f=0.229204
At iteration 35 f=0.172410
At iteration 36 f=0.101578
At iteration 37 f=0.066809
At iteration 38 f=0.047129
At iteration 39 f=0.022114
At iteration 40 f=0.010238
At iteration 41 f=0.006164
At iteration 42 f=0.001247
At iteration 43 f=0.000193
At iteration 44 f=0.000044
At iteration 45 f=0.000001
At iteration 46 f=0.000000
At iteration 47 f=0.000000

> myopR
$par
[1] 0.9999997 0.9999995

$grad
[1] -3.276165e-05 1.607110e-05

$value
[1] 7.416322e-13

$counts
[1] 47 47

$convergence
[1] 0

$message
[1] "CONVERGENCE: REL_REDUCTION_OF_F_<=_FACTR*EPSMCH"

> myop <- lbfgsb3c(x0, frosen, gr=NULL, control=list(trace=1))
At iteration 0 f=24.200000
At iteration 2 f=171.335959

```

```
At iteration 3 f=4.225209
At iteration 4 f=4.127276
At iteration 5 f=4.120517
At iteration 6 f=4.115575
At iteration 7 f=4.087545
At iteration 8 f=4.032007
At iteration 9 f=3.917829
At iteration 10 f=3.775253
At iteration 11 f=3.451302
At iteration 12 f=2.743645
At iteration 13 f=7.136647
At iteration 14 f=2.314771
At iteration 15 f=4.974153
At iteration 16 f=2.206918
At iteration 17 f=2.093263
At iteration 18 f=1.834870
At iteration 19 f=1.457101
At iteration 20 f=1.332676
At iteration 21 f=1.303252
At iteration 22 f=0.958191
At iteration 23 f=0.874145
At iteration 24 f=0.635020
At iteration 25 f=0.610113
At iteration 26 f=105.549878
At iteration 27 f=0.546422
At iteration 28 f=0.517374
At iteration 29 f=0.498255
At iteration 30 f=0.468898
At iteration 31 f=0.405481
At iteration 32 f=0.290616
At iteration 33 f=0.566440
At iteration 34 f=0.229204
At iteration 35 f=0.172410
At iteration 36 f=0.101578
At iteration 37 f=0.066809
At iteration 38 f=0.047129
At iteration 39 f=0.022114
At iteration 40 f=0.010238
At iteration 41 f=0.006164
At iteration 42 f=0.001247
At iteration 43 f=0.000193
At iteration 44 f=0.000044
At iteration 45 f=0.000001
At iteration 46 f=0.000000
At iteration 47 f=0.000000
```

```
> myop
```

```
$par
```

```
[1] 0.9999997 0.9999995
```

```
$grad
```

```
[1] -3.276165e-05 1.607110e-05
```

```
$value
```


[1] 7.416322e-13

\$counts

[1] 47 47

\$convergence

[1] 0

\$message

[1] "CONVERGENCE: REL_REDUCTION_OF_F_<=_FACTR*EPSMCH"

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