

AHSANULLAH UNIVERSITY OF SCIENCE &
TECHNOLOGY

CSE 4129

FORMAL LANGUAGES & COMPILERS LAB

Assignment 6 on Predictive Parsing

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Given,

The following grammar:

$$\begin{array}{l} S \rightarrow axd \\ x \rightarrow yz \\ y \rightarrow b \\ y \rightarrow \epsilon \\ z \rightarrow cx \\ z \rightarrow \epsilon \end{array}$$

The input string = abcd

1. Find the FIRST and FOLLOW sets of each of the non-terminals.

Soln:

$$\text{FIRST}(S) = \{a\}$$

$$\text{FIRST}(x) = \{b, c, \epsilon\}$$

$$\text{FIRST}(y) = \{b, \epsilon\}$$

$$\text{FIRST}(z) = \{c, \epsilon\}$$

$$\text{FOLLOW}(S) = \{\$ \}$$

$$\text{FOLLOW}(x) = \{d\}$$

$$\text{FOLLOW}(y) = \{c, d\}$$

$$\text{FOLLOW}(z) = \{d\}$$

2. Construct the predictive parsing table for LL(1) method.

Soln:

Non-terminal	Input Symbol				
	a	b	c	d	\$
S	$S \rightarrow axd$				
X		$X \rightarrow Yz$	$X \rightarrow Yz$	$X \rightarrow Yz$	
Y		$Y \rightarrow b$	$Y \rightarrow \epsilon$	$Y \rightarrow \epsilon$	
Z			$Z \rightarrow cx$	$Z \rightarrow \epsilon$	

3. Demonstrate the moves of the LL(1) parser on the given input = abcd

Stack	Input	Action
\$	abcd	$s \rightarrow axd$
axd	abcd	match a
x	cd	$x \rightarrow yz$
xyz	cd	$y \rightarrow b$
xyzd	cd	match b
z	cd	$z \rightarrow cx$
xcd	cd	match c
x	d	$x \rightarrow yz$
xyz	d	$y \rightarrow e$
xyzd	d	$z \rightarrow f$
xyzd	d	match d

4. Construct the LR(0) automaton for the grammar. We can derive an augmented grammar \bar{G} from the given grammar.

Augmented \bar{G} :

$$\begin{aligned}
 S' &\rightarrow S \\
 S &\rightarrow axd \\
 x &\rightarrow yz \\
 y &\rightarrow b \\
 y &\rightarrow \epsilon \\
 z &\rightarrow cx \\
 z &\rightarrow \epsilon
 \end{aligned}$$

Now, we've to find out the LR(0) automaton for the given grammar.

01 Initial state, I_0 :

$$\text{closure}(I_0, S) = \{S' \rightarrow S, S \rightarrow a \cdot x d\} = I_0$$

02

state I_1 :

$$\text{GOTO}(I_0, S) = \{S' \rightarrow S \cdot\} = I_1$$

$$\# \text{GOTO}(I_1, \$) = \text{accepted}$$

03

04

state I_3 :

$$\text{GOTO}(I_2, x) = \{s \rightarrow a \cdot x \cdot d\} = I_3$$

05

state I_4 :

$$\text{GOTO}(I_2, y) = \{x \rightarrow y \cdot z, z \rightarrow c \cdot x, z \rightarrow \cdot\} = I_4$$

Now, we've to find out the LR(0) automaton

for the given grammar.

01

Initial state, I_0 :

$$\text{CLOSURE}(\{s' \rightarrow \cdot s\}) = \{s' \rightarrow \cdot s, s \rightarrow \cdot a \cdot x \cdot d\} = I_0$$

02

state I_1 :

$$\text{GOTO}(I_0, s) = \{s' \rightarrow s \cdot\} = I_1$$

$$\# \text{GOTO}(I_1, \$) = \text{accepted}$$

03

state I_2 :

$$\text{GOTO}(I_0, a) = \{s \rightarrow a \cdot x \cdot d, x \rightarrow \cdot y \cdot z, y \rightarrow \cdot b,$$

$$y \rightarrow \cdot\} = I_2$$

04

state I_3 :

$$\text{GOTO}(I_2, x) = \{s \rightarrow a \cdot x \cdot d\} = I_3$$

05

state I_4 :

06 state I_5 :

$$\text{GOTO}(I_2, b) = \{Y \rightarrow b \cdot\} = I_5$$

07 state I_6 :

$$\text{GOTO}(I_3, d) = \{axd \cdot\} = I_6$$

08 state I_7 :

$$\text{GOTO}(I_4, z) = \{x \rightarrow yz \cdot\} = I_7$$

09 state I_8 :

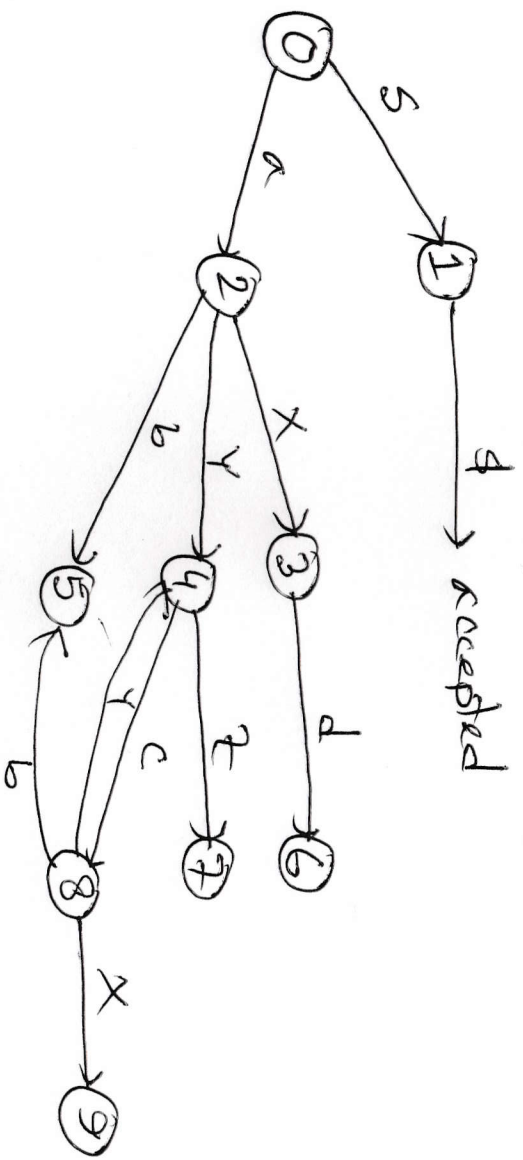
$$\begin{aligned} \text{GOTO}(I_4, c) &= \{z \rightarrow c \cdot x, x \rightarrow \cdot yz, y \rightarrow \cdot b, y \rightarrow \cdot\} \\ &= I_8 \end{aligned}$$

10 state I_9 :

$$\text{GOTO}(I_8, x) = \{z \rightarrow cx \cdot\} = I_9$$

$$\underline{\underline{11}} \quad \text{GOTO}(I_8, y) = \{x \rightarrow y \cdot z, z \rightarrow \cdot cx, z \rightarrow \cdot\} = I_4$$

$$\underline{\underline{12}} \quad \text{GOTO}(I_8, b) = \{Y \rightarrow b \cdot\} = I_5$$



Q5 Construct the parsing table for LR(1) parsing with the grammar.

state	Action					GOTO			
	a	b	c	d	\$	s	x	y	z
0	s2					1			
1		s5	r4	r4	accepted				
2		s5	r4	r4			3	4	
3				s6					
4			s8	r6					7
5			r3	r3					
6				r2	r1				
7			r2	r2					
8		s5	r4	r4			9	4	
9				r5					

6 Demonstrate the moves of the LR(1) parse on the given input

	Stack Symbol	Stack State	Input	Action
0	\$	0	abcd\$	s2
1	\$ab	02 3	bcd\$	s5
2	\$ab	025	cd\$	r3($Y \rightarrow b$)
3	\$aY	024	cd\$	s8
4	\$aYc	0248	d\$	r4($Y \rightarrow c$)
5	\$aYcY	02484	d\$	r6($Z \rightarrow c$)
6	\$aYcYz	024847	d\$	r2($X \rightarrow Yz$)
7	\$aYcx	02489	d\$	r5($Z \rightarrow cx$)
8	\$aYz	0247	d\$	r2($X \rightarrow Yz$)
9	\$ax	023	d\$	s6
10	\$axd	0236	\$	r1($S \rightarrow axd$)
11	\$	01		accepted