

Tokenization: How do language models see text?

Jan 27, 2025

CSE 447/517: NLP

Guest lecture from Alisa Liu

Inspiration taken from lectures of Yejin Choi, Andrej Karpathy, Sachin Kumar, Oreva Ahia

Tokenization :(

Tokenization is at the heart of much weirdness of LLMs. Do not brush it off.

- Why can't LLM spell words? **Tokenization**.
- Why can't LLM do super simple string processing tasks like reversing a string? **Tokenization**.
- Why is LLM worse at non-English languages (e.g. Japanese)? **Tokenization**.
- Why is LLM bad at simple arithmetic? **Tokenization**.
- Why did GPT-2 have more than necessary trouble coding in Python? **Tokenization**.
- Why did my LLM abruptly halt when it sees the string "<|endoftext|>"? **Tokenization**.
- What is this weird warning I get about a "trailing whitespace"? **Tokenization**.
- Why does the LLM break if I ask it about "SolidGoldMagikarp"? **Tokenization**.
- Why should I prefer to use YAML over JSON with LLMs? **Tokenization**.
- Why is LLM not actually end-to-end language modeling? **Tokenization**.
- What is the real root of suffering? **Tokenization**.



Let's build the GPT Tokenizer

 Andrej Karpathy
609K subscribers

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 **Mark Dredze**
@mdredze

There are no days without tokenization accidents. There are only:
- days when you know about them
- days when you do not

 **Luca Soldaini**   @soldni · Aug 21, 2024
x.com/magikarp_token...



imgflip.com

7:35 AM · Aug 21, 2024 · 1,643 Views

Outline

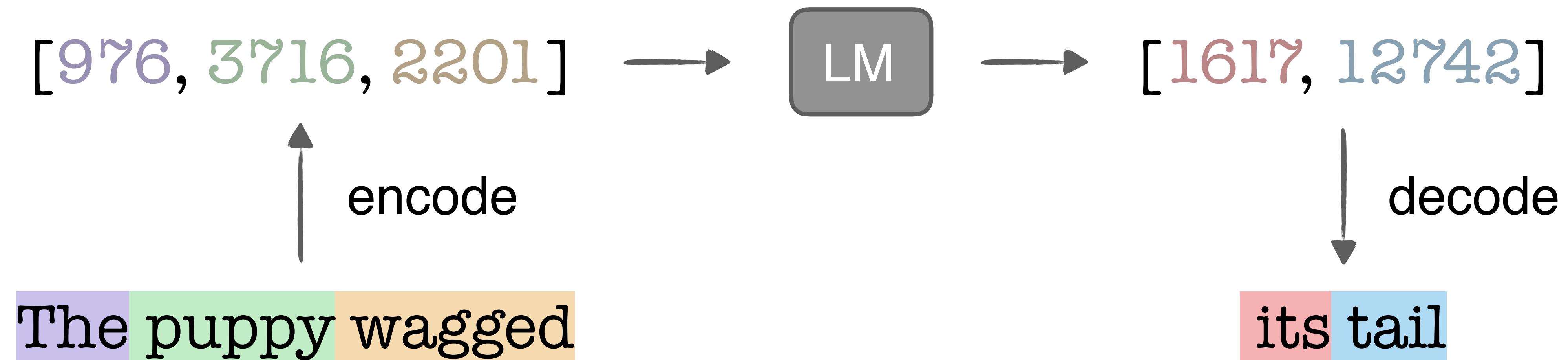
1. What is tokenization?
2. Word-level and character-level tokenizers
3. Subword-level tokenizers
4. BPE: Byte Pair Encoding
5. Variations on BPE

What is tokenization?

Token = a “word” unit with its own embedding representation

A **tokenizer** translates between text and a sequence of **tokens** that a language model (LM) learns representations over

The **vocabulary** V is the set of known tokens

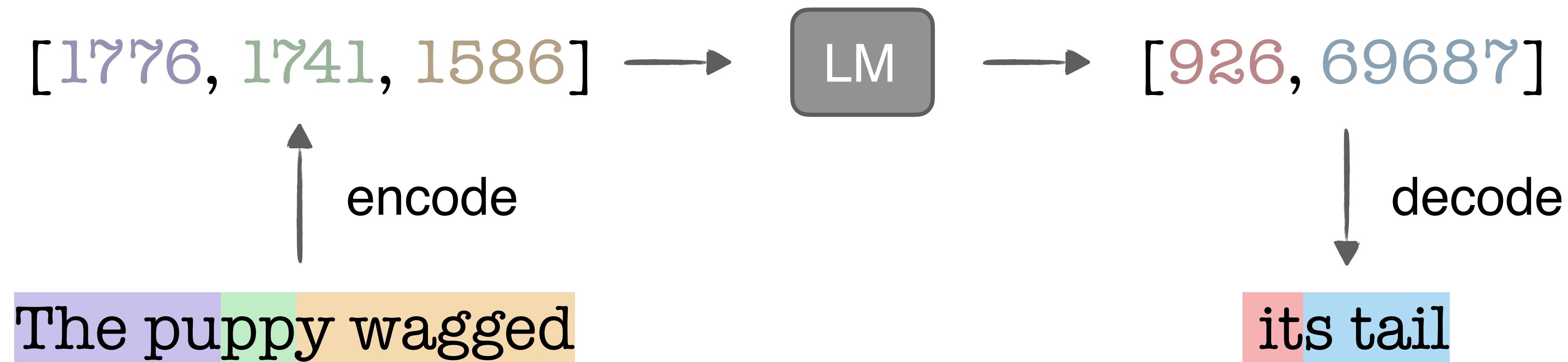


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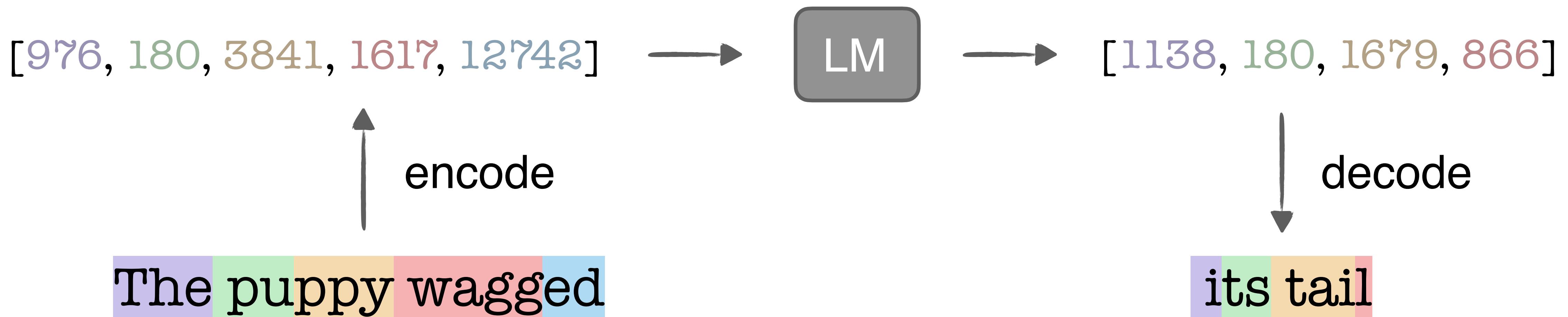


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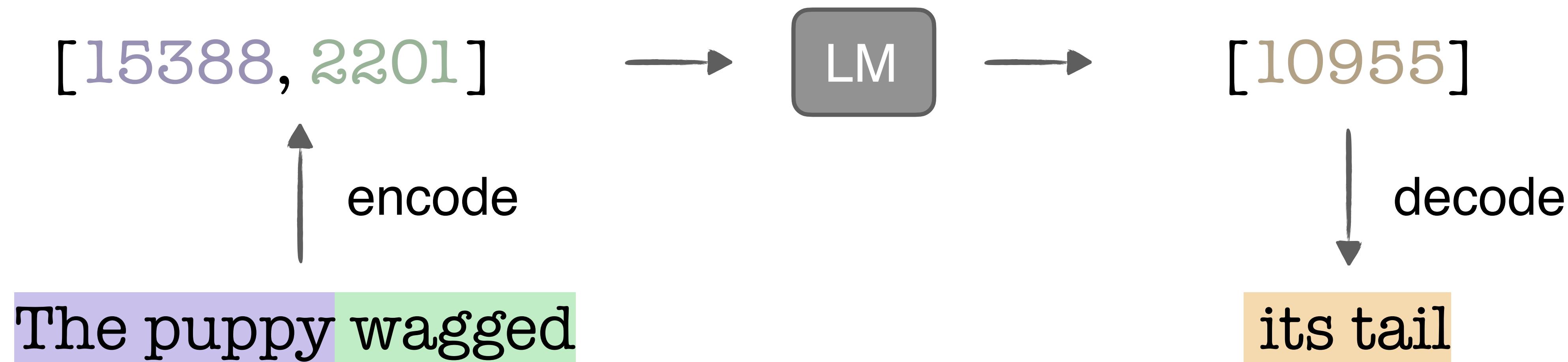


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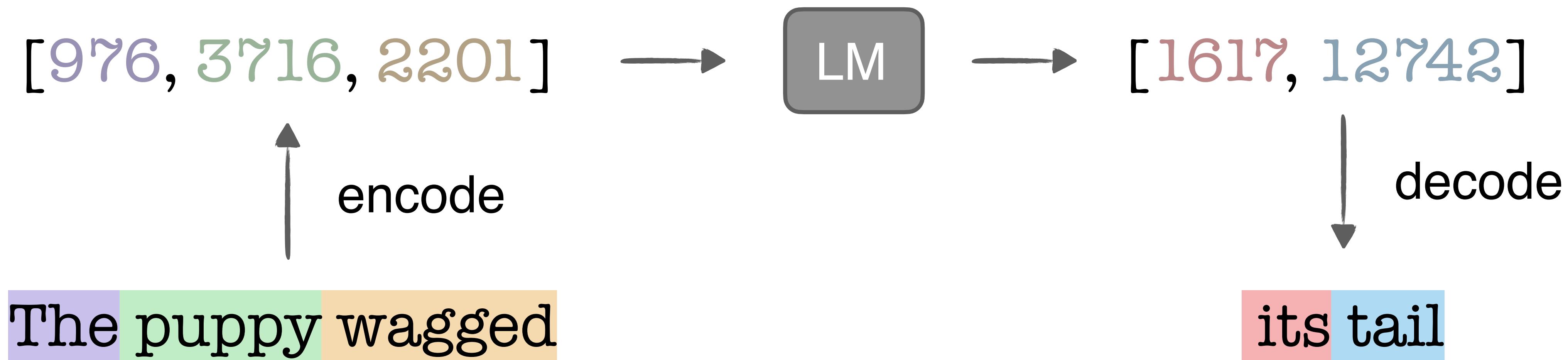
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Word-level tokenization

V = set of all words in the English language



Word-level tokenization

Word-level tokenization

✗ Cons

Word-level tokenization

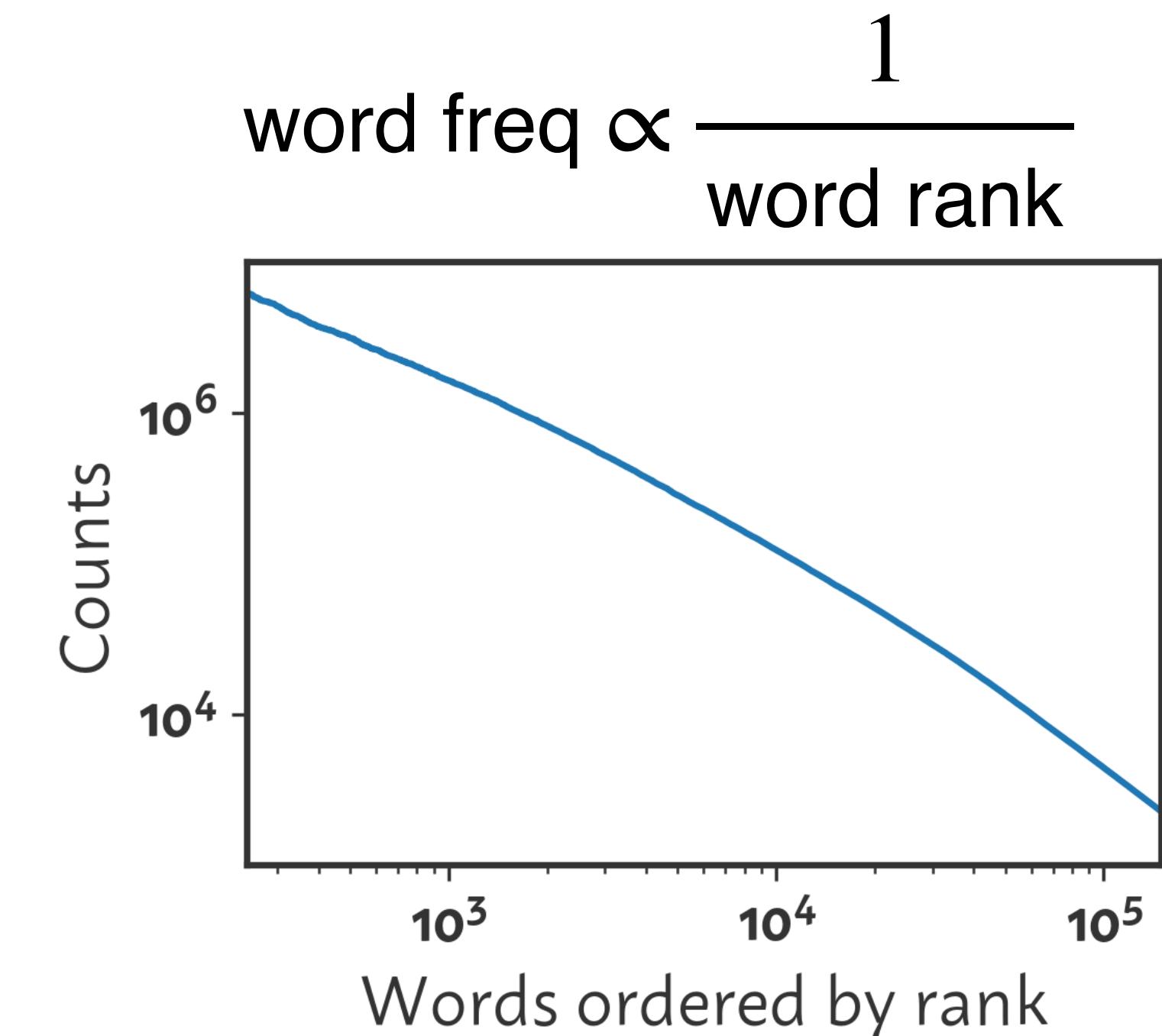
✗ Cons

- $|V|$ can be quite large
 - Webster's English dictionary has ~470,000 words!

Word-level tokenization

✗ Cons

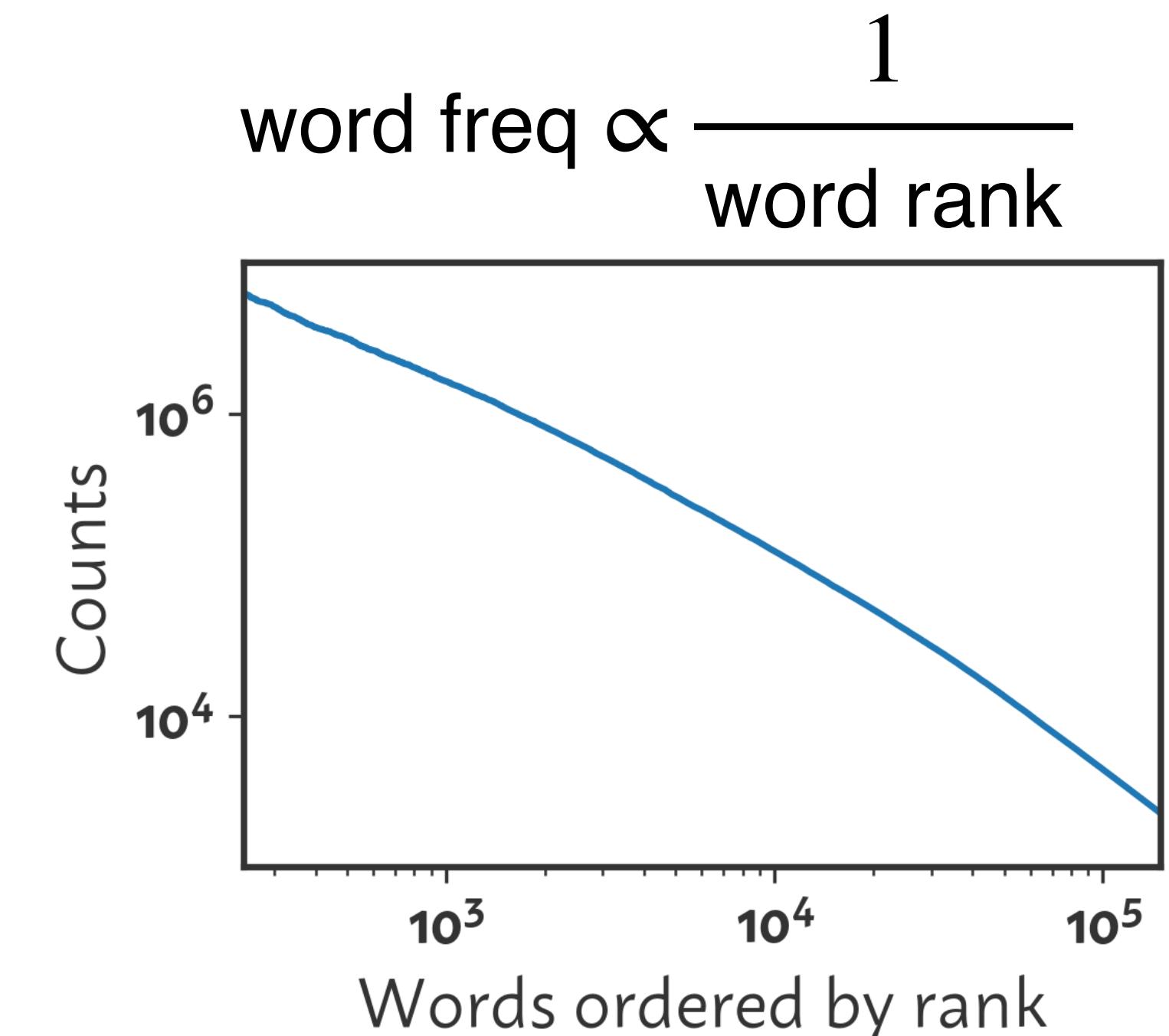
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- Long tail of infrequent words
- **Zipf's law:** word freq. is inversely prop. to rank



Word-level tokenization

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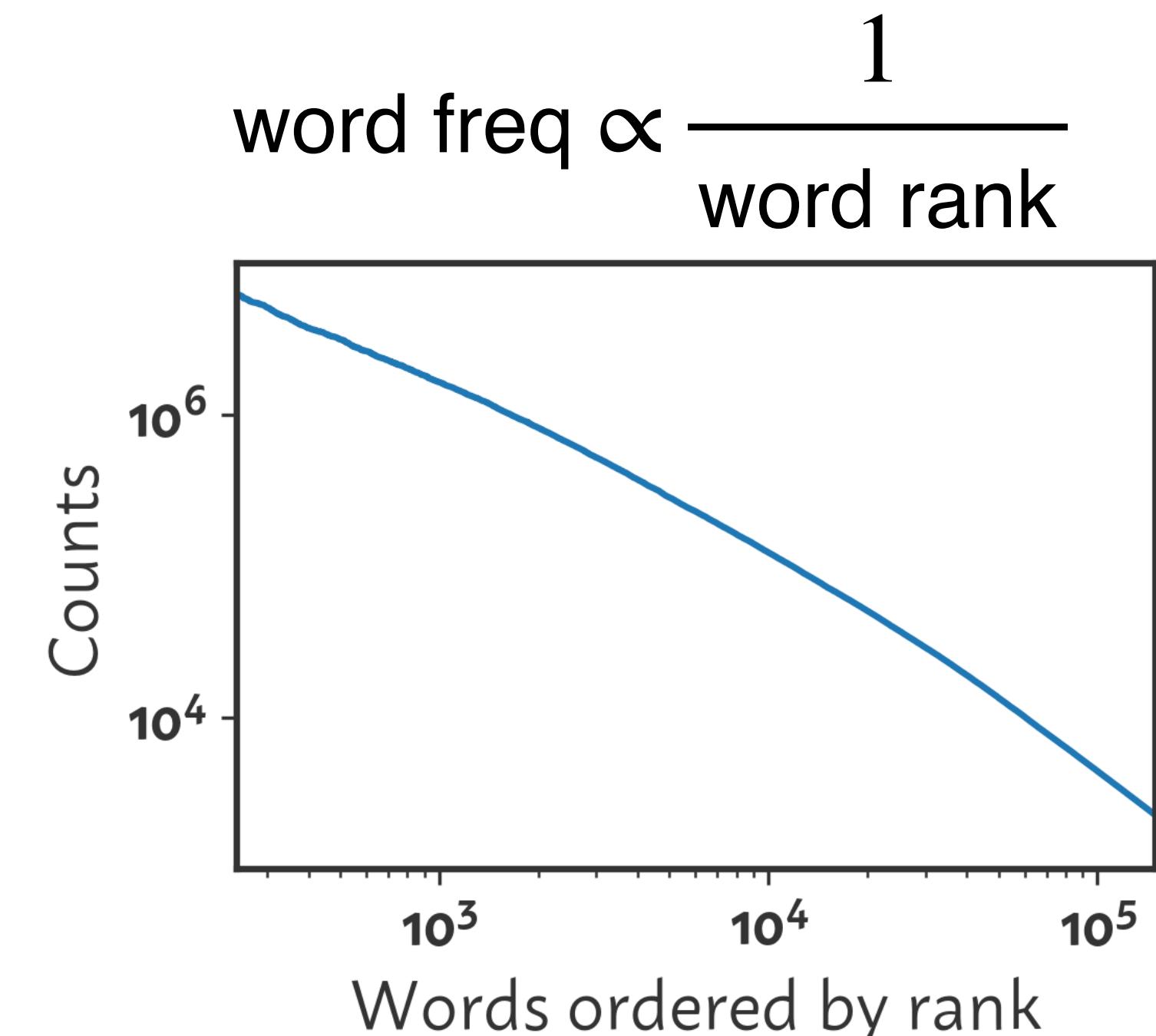
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Word-level tokenization

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 - Webster's English dictionary has ~470,000 words!
- Long tail of infrequent words
 - **Zipf's law:** word freq. is inversely prop. to rank
- Language is changing all the time
 - 690 new words [added in Sep 2023](#): "rizz," "goated," "bussin'," "mid"
- Still need a way to deal with unknown words



What does "breakfastish" mean?

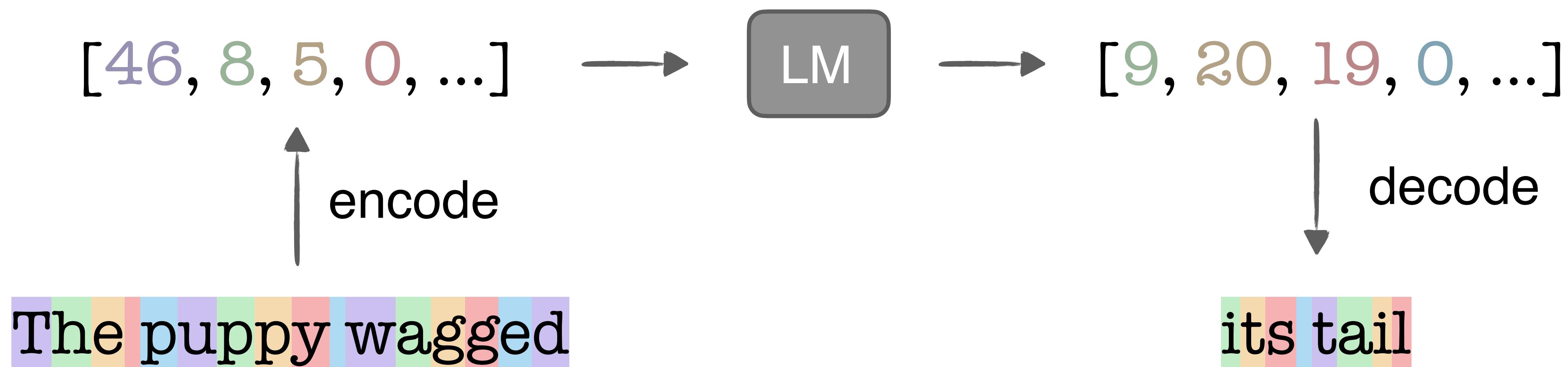


"Breakfastish" is an informal and playful term that means "resembling or characteristic of breakfast." It's used to describe something that has qualities typically associated with breakfast, such as food items, timing, or atmosphere.

Character-level tokenization

$$V = \{a, b, c, \dots, z, A, B, C, \dots, Z\}$$

(plus spaces + punctuation?)



Character-level tokenization



Character-level tokenization



Pros



Cons

Character-level tokenization



Pros

- Small vocabulary size



Cons

Character-level tokenization



Pros

- Small vocabulary size
- Complete coverage of input



Cons

Character-level tokenization



Pros

- Small vocabulary size
- Complete coverage of input
- Direct observation of spelling



Cons

Character-level tokenization



Pros

- Small vocabulary size
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- Direct observation of spelling



Cons

- Super long sequences

Character-level tokenization



Pros

- Small vocabulary size
- Complete coverage of input
- Direct observation of spelling



Cons

- Super long sequences
- Difficult to learn over

Subword tokenization

Subword tokenization

How can we combine the high coverage of character-level representation with the efficiency of word-level representation?

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Tokens are **subwords**, i.e., *parts* of words

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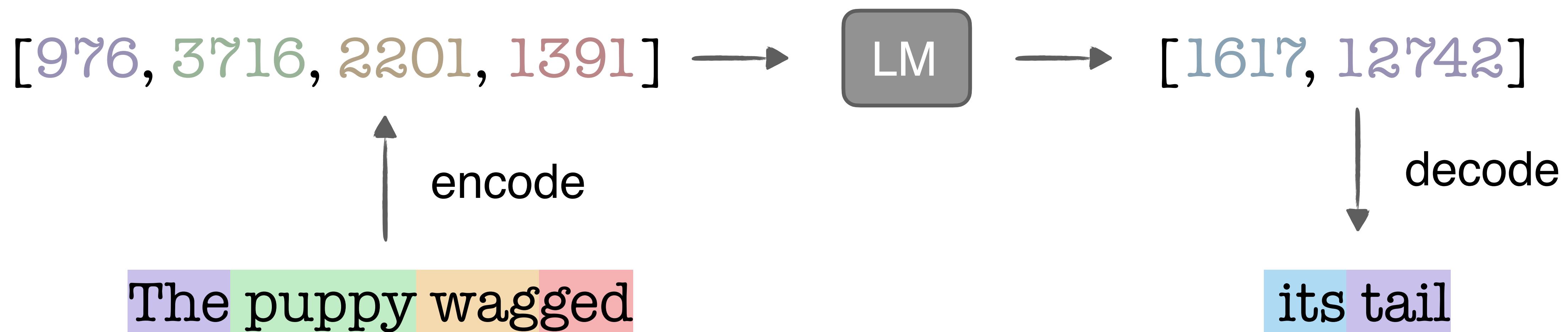
Instead of defining the vocabulary a-priori, use *data* to tell us what our vocabulary should be

Subword tokenization

How can we combine the high coverage of character-level representation with the efficiency of word-level representation?

Tokens are **subwords**, i.e., *parts* of words

Instead of defining the vocabulary a-priori, use *data* to tell us what our vocabulary should be



BPE: Byte Pair Encoding

Universal method today for learning subword tokenizers

Intuition: build the vocabulary bottom-up by repeatedly merging common token sequences into new tokens

Introduced by [Sennrich et al., 2016](#) & popularized by [GPT-2 \(2019\)](#)

BPE Algorithm

Required:

Training data D

Desired vocab size N

Algorithm:

1. Pretokenize D by splitting on whitespace
2. Initialize V as characters in D
3. Convert D into sequence of tokens (i.e., characters)
4. While $|V| < N$:
 - a. Get counts of all bigrams (v_i, v_j) in D
 - b. Merge most frequent pair into new token $v_n = v_i v_j$ where $n = |V| + 1$
 - c. Replace all instances of $v_i v_j$ in D with v_n

BPE Algorithm

Given: Training data D

tweetle_beetles_battle



BPE Algorithm

1. Pretokenize D by splitting on whitespace

tweetle

_beetles

_battle

BPE Algorithm

1. Pretokenize D by splitting on whitespace

tweetle

_beetles

_battle

BPE Algorithm

2. Initialize V as characters in D

tweetle

_beetles

_battle

BPE Algorithm

3. Convert D into sequence of tokens (i.e., characters)

t w e e t l e
_ b e e t l e s
_ b a t t l e

BPE Algorithm

4a. Get counts of all bigrams (v_i, v_j) in
 D

tweetle
_beetles
_battle

BPE Algorithm

4a. Get counts of all bigrams (v_i, v_j) in D

 t w e e t l e	 t w	1
 _ b e e t l e s		
 _ b a t t l e		

BPE Algorithm

4a. Get counts of all bigrams (v_i, v_j) in D

t w eeetle	tw	1
_beetles	we	1
_battle		

BPE Algorithm

4a. Get counts of all bigrams (v_i, v_j) in D

tweetle	tw	1
_beetles	we	1
_battle	ee	1

BPE Algorithm

4a. Get counts of all bigrams (v_i, v_j) in D

tweetle	tw	1
_beetles	we	1
_battle	ee	1
	et	1

BPE Algorithm

4a. Get counts of all bigrams (v_i, v_j) in D

tweetle	tw	1
_beetles	we	1
_battle	ee	1
	et	1
	tl	1

BPE Algorithm

4a. Get counts of all bigrams (v_i, v_j) in D

tweetle	tw	1
_beetles	we	1
_battle	ee	1
	et	1
	tl	1
	le	1

BPE Algorithm

4a. Get counts of all bigrams (v_i, v_j) in D

tweetle	tw	1	_b	1
_beetles	we	1		
_battle	ee	1		
	et	1		
	tl	1		
	le	1		

BPE Algorithm

4a. Get counts of all bigrams (v_i, v_j) in D

tweetle	tw	1	_b	1
_beetles	we	1	be	1
_battle	ee	1		
	et	1		
	tl	1		
	le	1		

BPE Algorithm

4a. Get counts of all bigrams (v_i, v_j) in D

tweetle	tw	1	_b	1
_beetles	we	1	be	1
_battle	ee	2		
	et	1		
	tl	1		
	le	1		

BPE Algorithm

4a. Get counts of all bigrams (v_i, v_j) in D

tweetle	tw	1	_b	1
_beetles	we	1	be	1
_battle	ee	2		
	et	2		
	tl	1		
	le	1		

BPE Algorithm

4a. Get counts of all bigrams (v_i, v_j) in D

tweetle	tw	1	_b	1
_beetles	we	1	be	1
_battle	ee	2		
	et	2		
	tl	2		
	le	1		

BPE Algorithm

4a. Get counts of all bigrams (v_i, v_j) in D

tweetle	tw	1	_b	1
_beetles	we	1	be	1
_battle	ee	2		
	et	2		
	tl	2		
	le	2		

BPE Algorithm

4a. Get counts of all bigrams (v_i, v_j) in D

tweetle	tw	1	_b	1
_beetles	we	1	be	1
_battle	ee	2	es	1
	et	2		
	tl	2		
	le	2		

BPE Algorithm

4a. Get counts of all bigrams (v_i, v_j) in D

tweetle	tw	1	_b	2
_beetles	we	1	be	1
_battle	ee	2	es	1
	et	2		
	tl	2		
	le	2		

BPE Algorithm

4a. Get counts of all bigrams (v_i, v_j) in D

tweetle	tw	1	_b	2
_beetles	we	1	be	1
_battle	ee	2	es	1
	et	2	ba	1
	tl	2		
	le	2		

BPE Algorithm

4a. Get counts of all bigrams (v_i, v_j) in D

tweetle	tw	1	_b	2
_beetles	we	1	be	1
_bat t le	ee	2	es	1
	et	2	ba	1
	tl	2	at	1
	le	2		

BPE Algorithm

4a. Get counts of all bigrams (v_i, v_j) in D

tweetle	tw	1	_b	2
_beetles	we	1	be	1
_battle	ee	2	es	1
	et	2	ba	1
	tl	2	at	1
	le	2	tt	1

BPE Algorithm

4a. Get counts of all bigrams (v_i, v_j) in D

tweetle	tw	1	_b	2
_beetles	we	1	be	1
_battle	ee	2	es	1
	et	2	ba	1
	tl	3	at	1
	le	2	tt	1

BPE Algorithm

4a. Get counts of all bigrams (v_i, v_j) in D

tweetle	tw	1	_b	2
_beetles	we	1	be	1
_battle	ee	2	es	1
	et	2	ba	1
	tl	3	at	1
	le	3	tt	1

BPE Algorithm

Merge List

	Text	Pair Frequencies			
1					
2	tweetle	tw	1	_b	2
3	_beetles	we	1	be	1
4	_battle	ee	2	es	1
:		et	2	ba	1
		tl	3	at	1
		le	3	tt	1

BPE Algorithm

Merge List

	Text	Pair Frequencies		
1				
2	tweetle	tw	1	_b
3	_beetles	we	1	be
4	_battle	ee	2	es
		et	2	ba
		tl	3	at
		le	3	tt
	4b. Find most frequent pair (v_i, v_j)			

BPE Algorithm

Merge List

	Text	Pair Frequencies		
1				
2	tweetle	tw	1	_b
3	_beetles	we	1	be
4	_battle	ee	2	es
		et	2	ba
		tl	3	at
		le	3	tt
	4b. Find most frequent pair (v_i, v_j)			

BPE Algorithm

Merge List

	Merge List	Text	Pair Frequencies
1	1 e		
2		tweetle	tw 1 _b 2
3	add to merge list	_beetles	we 1 be 1
4		_battle	ee 2 es 1
			et 2 ba 1
			tl 3 at 1
			le 3 tt 1
	4b. Find most frequent pair (v_i, v_j)		

BPE Algorithm

Merge List

	Merge List	Text	Pair Frequencies
1	1 e		
2		tweetle	tw 1 _b 2
3		_beetles	we 1 be 1
4		_battle	ee 2 es 1
:			et 2 ba 1
			tl 3 at 1
			le 3 tt 1

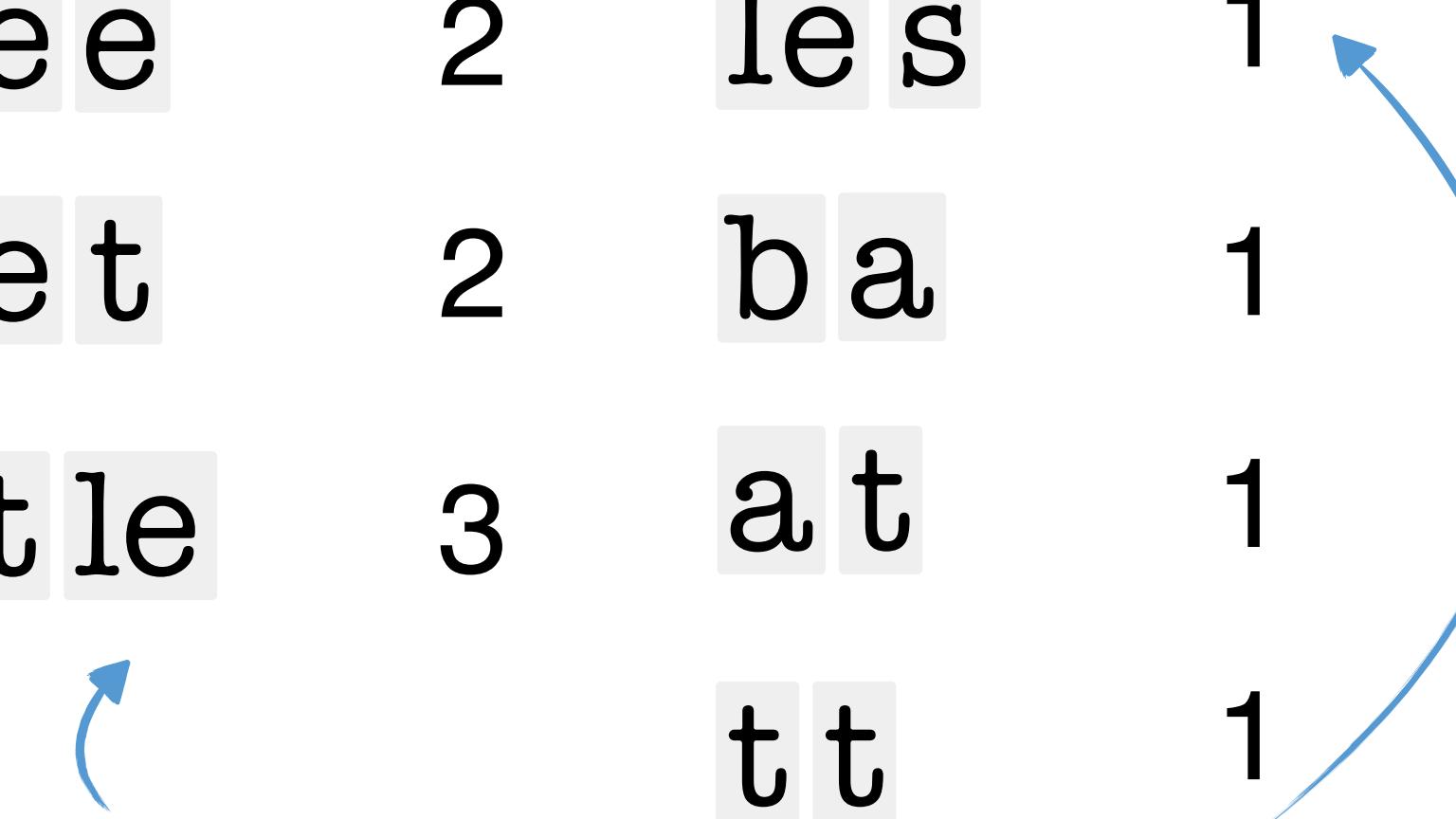
4c. Replace all instances of $v_i v_j$ in D with v_n

BPE Algorithm

Merge List

	Merge List	Text	Pair Frequencies
1	1 e		
2		tweetle	tw 1 _b 2
3		_beetles	we 1 be 1
4		_battle	ee 2 le s 1
			et 2 ba 1
			tle 3 at 1
			tt 1

4a. Update pair frequencies



BPE Algorithm

Merge List

	Merge List	Text	Pair Frequencies			
1	l e					
2		tweettle	t w	1	_ b	2
3		_ beetles	w e	1	be	1
4		_ battle	ee	2	le s	1
	:		et	2	ba	1
			tle	3	at	1
			tt			1

BPE Algorithm

Merge List

	Merge List	Text	Pair Frequencies
1	l e		
2		tweettle	tw 1 _b 2
3		_beetles	we 1 be 1
4		_battle	ee 2 le s 1
			et 2 ba 1
			tle 3 at 1
			tt 1

4b. Find most frequent pair

BPE Algorithm

Merge List

	Merge List	Text	Pair Frequencies
1	l e		
2		tweettle	tw 1 _b 2
3		_beetles	we 1 be 1
4		_battle	ee 2 le s 1
			et 2 ba 1
			tle 3 at 1
			tt 1

4b. Find most frequent pair

BPE Algorithm

Merge List

1	l e
2	t le
3	
4	
	add to merge list
	⋮

	Text	Pair Frequencies		
1	tweettle	tw	1	_b
2	_beetles	we	1	be
3	_battle	ee	2	le s
4		et	2	ba
		t le	3	at
		tt		

4b. Find most frequent pair

BPE Algorithm

Merge List

	Merge List	Text	Pair Frequencies
1	l e		tw 1 _b 2
2	t le	tweeble	we 1 be 1
3		_beetles	ee 2 les 1
4		_battle	et 2 ba 1
			tle 3 at 1
			tt 1

4c. Apply merge to text

BPE Algorithm

Merge List

	Merge List	Text	Pair Frequencies
1	l e		t w 1 _b 2
2	t le	tweeble	w e 1 b e 1
3		_beetles	e e 2 tles 1
4		_battle	e tle 2 ba 1
			a t 1
			t tle 1

4a. Update pair frequencies

The diagram shows two blue curved arrows. One arrow originates from the 'ttle' entry in the 'Merge List' at row 4 and points to the 'ttle' entry in the 'Pair Frequencies' table at row 6. Another arrow originates from the 'ttle' entry in the 'Merge List' at row 5 and points to the same 'ttle' entry in the 'Pair Frequencies' table at row 6.

BPE Algorithm

Merge List

	Merge List	Text	Pair Frequencies
1	l e		
2	t le	tweetle	tw 1 _b 2
3		_beetles	we 1 be 1
4		_battle	ee 2 tles 1
			etle 2 ba 1
			at 1
			tle 1

BPE Algorithm

Merge List

	Merge List	Text	Pair Frequencies
1	l e		t w 1 _b 2
2	t le	tweeble	w e 1 be 1
3		_beetles	ee 2 tles 1
4		_battle	etle 2 ba 1
			at 1
			ttle 1

BPE Algorithm

Merge List

	Merge List	Text	Pair Frequencies
1	l e		t w 1 _ b 2
2	t le	tweeble	w e 1 be 1
3		_beetles	ee 2 tles 1
4		_battle	etle 2 ba 1
			at 1
			ttle 1

BPE Algorithm

Merge List

	Merge List	Text	Pair Frequencies
1	l e		t w 1 _ b 2
2	t le	tweeble	w e 1 be 1
3	e tle	_beetles	ee 2 tles 1
4		_battle	etle 2 ba 1
			at 1
			ttle 1

BPE Algorithm

Merge List

	Text		Pair Frequencies		
1	l	e	tw	w	b
2	t	le	we	e	be
3	e	tle	_beetles	ee	tes
4			_battle	etle	ba
⋮	⋮	⋮			at
					t tle

BPE Algorithm

Merge List

	Merge List	Text	Pair Frequencies
1	l e		
2	t le	tweetle	tw 1 _b 2
3	e tle	_beetles	we 1 be 1
4		_battle	eetle 2 etles 1
	⋮		ba 1
			at 1
			ttle 1

BPE Algorithm

Merge List

	Merge List	Text	Pair Frequencies
1	l e		
2	t le	tweetle	tw 1 _b 2
3	e tle	_beetles	we 1 be 1
4		_battle	eetle 2 etles 1
	⋮		ba 1
			at 1
			ttle 1

BPE Algorithm

Merge List

	Merge List	Text	Pair Frequencies
1	l e		t w 1 _ b 2
2	t le	tweetle	we 1 be 1
3	e tle	_beetles	eetle 2 etles 1
4		_battle	ba 1 at 1 ttle 1

BPE Algorithm

Merge List

	Merge List	Text	Pair Frequencies
1	l e		t w 1 _ b 2
2	t le	tweetle	we 1 be 1
3	e tle	_beetles	eetle 2 etles 1
4		_battle	ba 1 at 1 ttle 1

BPE Algorithm

Merge List

	Merge List	Text	Pair Frequencies
1	l e		t w 1 _ b 2
2	t le	t we etle	w e 1 be 1
3	e tle	_ beetles	e etle 2 etles 1
4	e etle	_ batte	b a 1 at 1 t tle 1
	⋮		

BPE Algorithm

Merge List

	Merge List	Text	Pair Frequencies
1	l e	t w e e t t l e	t w 1 _ b 2
2	t le	_ b e e t t l e s	w e 1 b e 1
3	e tle	_ b a t t l e	e e t t l e 2 et t l e s 1
4	e etle		b a 1
	:		a t 1
			t t l e 1

BPE Algorithm

Merge List

	Merge List	Text	Pair Frequencies
1	l e		
2	t le	tw ee ettle	t w 1 _ b 2
3	e tle	_beetles	w e 1 be 1
4	e etle	_battle	eetles 1
	⋮		ba 1
			at 1
			ttle 1

... until we reach the desired vocabulary size, $|V| = N$

BPE Algorithm

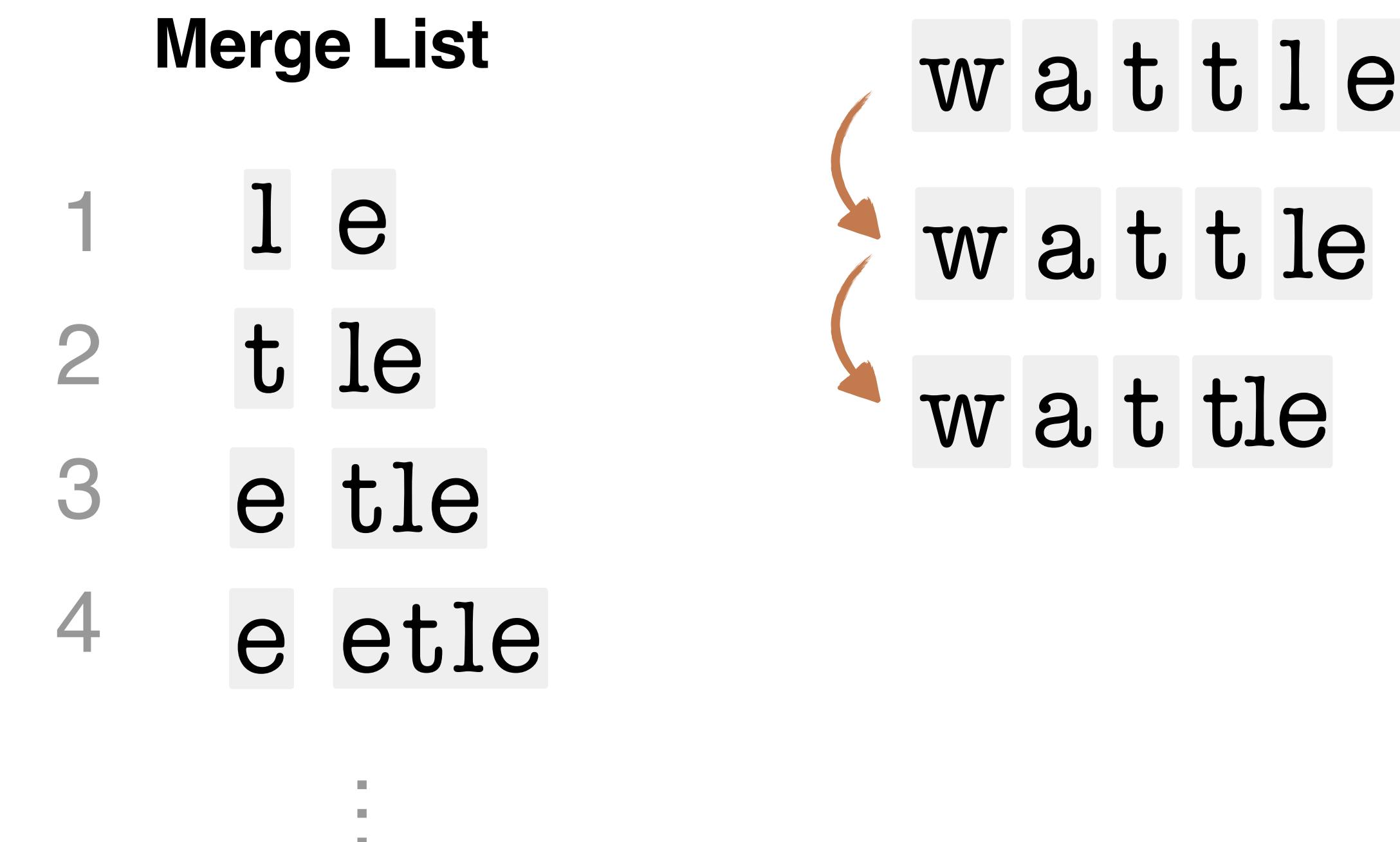
To tokenize new text at test time, we split it into the characters and apply merge rules in order.

Merge List

1	l	e
2	t	le
3	e	tle
4	e	etle
⋮		

BPE Algorithm

To tokenize new text at test time, we split it into the characters and apply merge rules in order.



BPE: Examples

Given this BPE tokenizer, how would _the be tokenized?

Vocab

t

h

e

Merge List

_t

_ t

_th

_t h

he

h e

BPE: Examples

Given this BPE tokenizer, how would _the be tokenized?

Vocab

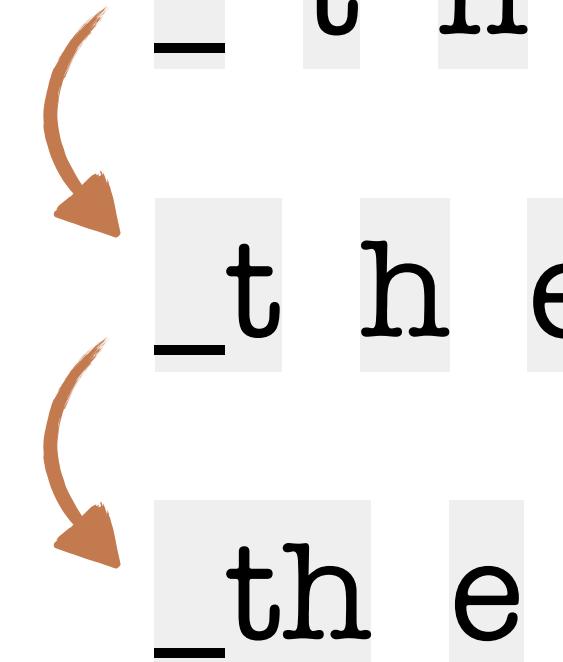
t
h
e

Merge List

_t	_t
_th	_t h
he	h e

Answer:

_ t h e
_t h e
_th e



BPE: Examples

Given this BPE tokenizer, how would _the be tokenized?

Vocab

t

h

e

Merge List

_t

_ t

he

h e

_th

_t h

BPE: Examples

Given this BPE tokenizer, how would _the be tokenized?

Vocab

t

h

e

Merge List

_t

_ t

he

h e

_th

_t h

Answer:

_ t h e
_ t he
_t he

ChatGPT's tokenizer

Tokenizers are one of the core components of the NLP pipeline. They serve one purpose: to translate text into data that can be processed by the model. Models can only process numbers, so tokenizers need to convert our text inputs to numerical data. In this section, we'll explore exactly what happens in the tokenization pipeline.

<https://platform.openai.com/tokenizer>

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Subword tokenizers

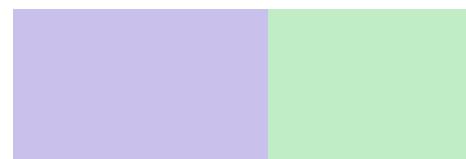
Subword tokenizers



Pros



Cons

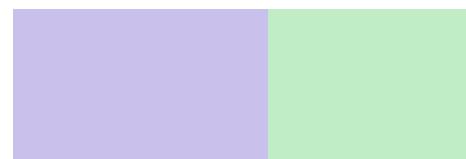


Subword tokenizers



Pros

Everything can be represented with the vocabulary



Cons



Subword tokenizers



Pros

Everything can be represented with the vocabulary

Some shared representations

wagged



Cons



Subword tokenizers



Pros

Everything can be represented with the vocabulary

Some shared representations

wagged

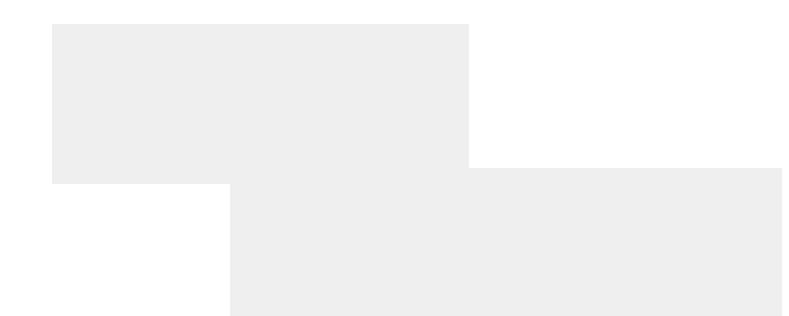
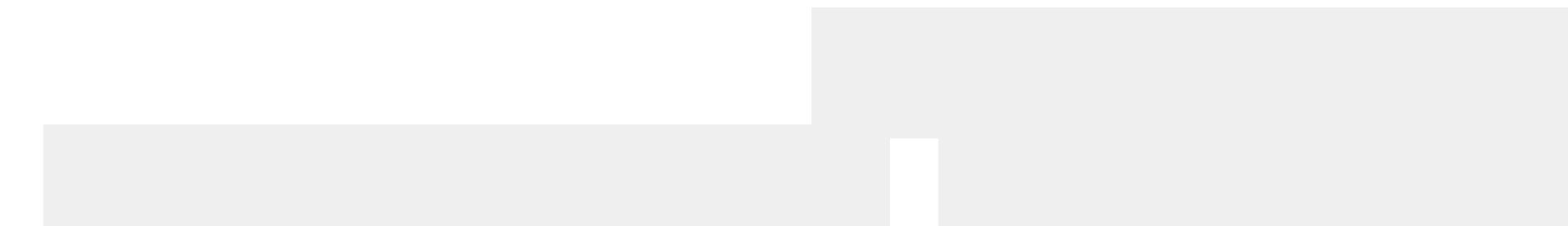


Cons

No association between related words

Run ≠ run ≠ RUN

_Hello ≠ Hello



Subword tokenizers



Pros

Everything can be represented with the vocabulary

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GPT-2 tokens¹: _RandomRedditor,
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No direct observation of spelling

“Intermediate” tokens can be useless

entucky token is completely subsumed by _Kentucky

What could we do differently?

Variant: how to treat whitespace

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Instead of merging spaces into the beginning of words, use special “continue word” character

With whitespace:[_Token, ization, _is, _cool]

W/o whitespace: [Token, ##ization, is, cool]

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✗ Cons

Loses whitespace information
(especially problematic for code!)

```
from transformers import AutoTokenizer
tokenizer = AutoTokenizer.from_pretrained("openai-gpt")
```

✓ 0.4s

```
token_ids = tokenizer.encode("Tokenization is cool.")
print(token_ids)
print(tokenizer.decode(token_ids))
```

✓ 0.0s

```
[571, 2987, 26922, 544, 2548, 239]
tokenization is cool .
```

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But there are *many* characters if you want to support...

- Character-based languages (e.g., עברית, 學ひ한국)
 - Non-alphanumeric characters (e.g., 💀 😊 😍)

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Instead, use UTF-8 to map all characters in Unicode to byte strings (of 1-4 bytes)

Initialize base vocab as the set of 256 bytes, instead of the English characters

A	Ω	語	三	UTF-8
41	CE A9	E8 AA 9E	F0 90 8E 84	

Variants: pretokenization decisions

Recall: pretokenization sets limits on what boundaries our tokens can cross

How should we pretokenize...

Digits? Consider: 10 vs. 1000000 vs. 5493747

Consecutive spaces? Consider:

```
loop {  
    // Stop as soon as we have a big enough vocabulary  
    if word_to_id.len() >= self.vocab_size {  
        break;  
    }  
  
    let mut top: Merge = queue.pop().unwrap();
```

Punctuation? Consider: yay!, !=, get., .get

Newlines? Consider: ;\n

Whitespace? Consider: thank you, New York