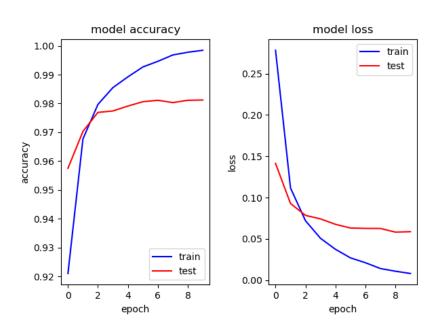
Multi-layer Perceptron

I began by running the mnist_mlp_baseline.py to see what prediction error it reported. I found that without any modifications, the base model produced the following results:

Baseline Error: 1.88%



I started by modifying the batch size to see how that impacted the model:

Batch_size=500 Baseline Error: 1.82%
Batch_size=32 Baseline Error: 2.36%

I reset the batch_size to see how the number of epochs affected the error.

nb_epoch=5 Baseline Error: 2.14%
nb_epoch=30 Baseline Error: 1.63%

A larger number of epochs increases performance, so the rest of my testing uses 30 epochs. The next thing I tried was increasing the number of layers. I found that adding layers of 1000, 256, and 128 worked well.

```
model.add(Dense(1000, input_dim=num_pixels, init='normal',
activation='relu'))
model.add(Dense(num_pixels, init='normal', activation='relu'))
model.add(Dense(256, init='normal', activation='relu'))
model.add(Dense(128, init='normal', activation='relu'))
model.add(Dense(num_classes, init='normal', activation='softmax'))

Baseliner Error: 1.49%
```

I then added drop out layers and batch normalization layers to stabilize the training process and prevent overfitting.

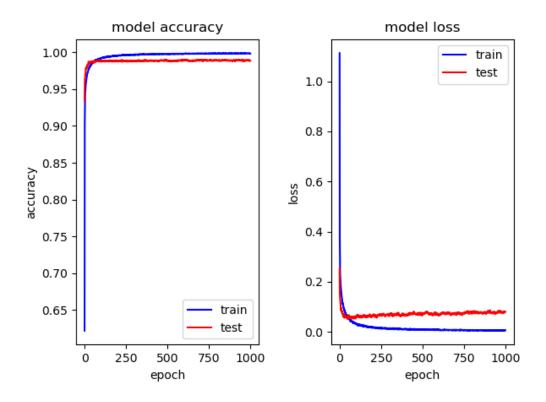
```
model.add(Dense(1000, input_dim=num_pixels, init='normal',
    activation='relu'))
model.add(BatchNormalization())
model.add(Dropout(.5))
model.add(Dense(num_pixels, init='normal', activation='relu'))
model.add(BatchNormalization())
model.add(Dropout(.5))
model.add(Dense(256, init='normal', activation='relu'))
model.add(BatchNormalization())
model.add(Dropout(.5))
model.add(Dense(128, init='normal', activation='relu'))
model.add(BatchNormalization())
model.add(Dropout(.5))
model.add(Dropout(.5))
model.add(Dropout(.5))
model.add(Dense(num_classes, init='normal', activation='softmax'))

Baseliner Error: 1.35%
```

I continued to add layers and modify the batch_size through a trial-and-error process to improve the model. I had a hard time improving the model past an average error of 1.10%. I continued to modify batch_size and drop out rates until I saw it reach 1.07%. This occurred with a **batch_size of 104** and I let it run for **1000 epochs** overnight. The final model and results were as follows:

```
model.add(Dense(1000, input dim=num pixels, init='normal',
activation='relu'))
model.add(BatchNormalization())
model.add(Dropout(.57))
model.add(Dense(num pixels, init='normal', activation='relu'))
model.add(BatchNormalization())
model.add(Dropout(.3))
model.add(Dense(num pixels, init='normal', activation='relu'))
model.add(BatchNormalization())
model.add(Dropout(.57))
model.add(Dense(256, init='normal', activation='relu'))
model.add(BatchNormalization())
model.add(Dropout(.56))
model.add(Dense(256, init='normal', activation='relu'))
model.add(BatchNormalization())
model.add(Dropout(.15))
model.add(Dense(256, init='normal', activation='relu'))
model.add(BatchNormalization())
model.add(Dropout(.72))
model.add(Dense(256, init='normal', activation='relu'))
model.add(BatchNormalization())
model.add(Dropout(.35))
model.add(Dense(128, init='normal', activation='relu'))
model.add(BatchNormalization())
model.add(Dropout(.6))
model.add(Dense(num classes, init='normal', activation='softmax'))
```

Baseliner Error: 0.99%



The final baseline error was **0.99%**, which completes the assignment. I found the lowest error occurred at epoch 608 which was an error of **0.97%**. While these errors are good, they are not consistent and didn't appear on every run of the model.

```
Epoch 608/1000

- 10s - loss: 0.0084 - accuracy: 0.9982 - val_loss: 0.0668 - val_accuracy: 0.9903

Epoch 609/1000

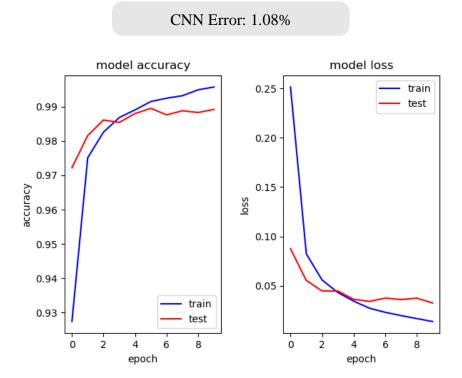
- 10s - loss: 0.0055 - accuracy: 0.9988 - val_loss: 0.0734 - val_accuracy: 0.9897

Epoch 610/1000

- 10s - loss: 0.0065 - accuracy: 0.9983 - val_loss: 0.0724 - val_accuracy: 0.9901
```

Convolutional Neural Network

I began by running the mnist_cnn.py to see what prediction error it reported. I found that without any modifications, the base model produced the following results:



I began by modifying the batch size and found the following:

Batch_Size = 300 CNN Error: 1.05%

Batch_Size = 128 CNN Error: 1.31%

While it looks like a larger batch size is better, I know from experience that increasing the number of epochs will change these results. I increased the number of epochs to 50 and found the following results:

nb_epoch = 50

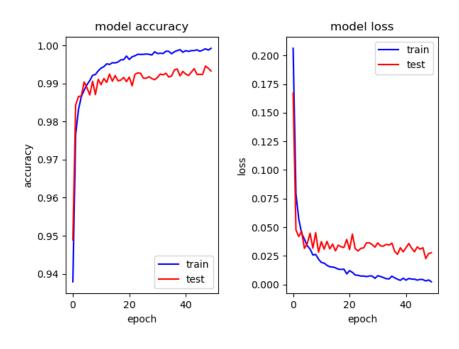
Batch_Size = 300 CNN Error: 1.02%

Batch_Size = 128 CNN Error: 0.97%

While this completed the assignment, I knew I could improve the model. I added a convolution layer and two dense layers. I modified the drop out value and found that 0.45 worked the best. The next thing I added was batch normalization to stabilize the training process. I chose 500, 250, 100 for the neurons in the dense layer because I have used thes values for past discussion board problems and found they had good performance. Putting it all together and running the model for 50 epochs with a batch_size of 128 produced the following results:

```
model = Sequential()
model.add(Convolution2D(32, 5, 5, border mode='valid', input shape=(1, 28, 28),
activation='relu', dim ordering ='th'))
model.add(Convolution2D(32, 5, 5, activation='relu', border mode='valid'))
model.add(BatchNormalization())
model.add(MaxPooling2D(pool size=(2, 2)))
model.add(Dropout(.45))
model.add(Flatten())
model.add(Dense(500, activation='relu'))
model.add(BatchNormalization())
model.add(Dense(250, activation='relu'))
model.add(BatchNormalization())
model.add(Dense(100, activation='relu'))
model.add(BatchNormalization())
model.add(Dropout(.45))
model.add(Dense(num classes, activation='softmax'))
```

CNN Error: 0.67%



A CNN error of 0.67 is very good. Below is a screenshot of the last few epochs. We can see that the model's best performance was on epoch 48 where it had a **cnn_error of 0.054%**

```
Epoch 48/50
- 14s - loss: 0.0030 - accuracy: 0.9991 - val_loss: 0.0226 - val_accuracy: 0.9946

Epoch 49/50
- 14s - loss: 0.0039 - accuracy: 0.9988 - val_loss: 0.0269 - val_accuracy: 0.9940

Epoch 50/50
- 14s - loss: 0.0023 - accuracy: 0.9992 - val_loss: 0.0278 - val_accuracy: 0.9933

CNN Error: 0.67%
```